On-Board Estimation of Vehicle Speed and the Need of Braking Using Convolutional Neural Networks

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- Keywords: Autonomous Vehicles, Self-Driving Vehicles, Convolutional Neural Network, Velocity Prediction, Vehicle Speed, Recurrent Neural Network, Long Short-Term Memory, Vehicle State Estimation, Visual Odometry.
- Abstract: Detecting the ego-vehicle state is a challenging problem in the context of autonomous vehicles. Perceptionbased methods leverage information from on-board cameras and sensors to determine the surrounding traffic scene and vehicle state. Monocular based approaches are becoming more popular for driver assistance, and accurate vehicle speed prediction plays an important role for improving road safety. This research paper presents an implementation of a Convolutional Neural Network (CNN) model for vehicle velocity prediction using sequential image input, as well as an extended model that also features sensorial data as input. The CNN model is trained on a dataset featuring sets of 20 sequential images, captured from a moving car in a road traffic scene. The aim of the model is to predict the current vehicle speed based on the information encoded in the previous 20 frames. The model architecture consists of convolutional layers followed by fully connected layers, having a linear output layer for the ego-vehicle velocity prediction. We evaluate our proposed models and compare them using existing published work that features Recurrent Neural Networks (RNNs). We also examine the prediction of the brake pedal pressure required while driving.

1 INTRODUCTION

The field of autonomous driving has become a thriving area of research for scientists and leading manufacturers such as Tesla, Waymo, and Baidu. This increased interest is driven by the remarkable progress made in computer vision, particularly in deep learning. These recent advancements have paved the way for significant breakthroughs for autonomous driving technologies.

Developing perception-based policies to facilitate complex autonomous behaviours, such as driving, remains an ongoing challenge in the fields of computer vision and machine learning. The recent advancements in deep learning techniques for visual perception tasks have sparked considerable interest in exploring their effectiveness for learning driver intentions and actions to provide better road traffic safety.

Accurate vehicle speed prediction plays a crucial role for various applications in autonomous driving,

traffic monitoring, and driver assistance systems. The main factor for road accidents is still represented by the human error, according to the National Highway Traffic Safety Administration (NHTSA). They also claim that speeding represents one of the main problems for road accidents with fatalities (NHTSA, 2023). Determining the vehicle speed from on-board images can be used for video forensics, especially when using uncalibrated video data. Accurate prediction models enables us to gain a deeper understanding of the underlying factors and motivations driving the decision-making process of drivers.

This research focuses on developing a CNNbased model that leverages sequential image input to predict the current vehicle velocity (speed) and the need for braking during driving. By analysing a sequence of images, captured from a moving car in a road traffic scene, the model aims to estimate the velocity based on the temporal information encoded in the previous frames. We use only the front image

600

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input from the ego-vehicle, as it provides the most accurate representation of the visual input that the driver also has of the scene. We then extend our model to feature sensorial input (velocity data expressed in km/h) as well. We compare our approach with a method based on recurrent neural networks (RNNs), more specifically Long Short-Term Memories (LSTMs) that features multiple inputs in order to produce a prediction. We have also tested a model to estimate the brake pedal pressure needed in road traffic scenarios and the results are promising.

2 RELATED WORK

We analyse the related work that features visual input (images captured from the scene) and sensorial input or measurements for self-driving vehicles related tasks.

The authors of (Xue, 2018), propose an approach that combines a Convolutional Neural Network (CNN) and Long Short Term Memory (Hochreiter, 1997) to predict the future positions of pedestrians in video sequences captured by static cameras. The method utilizes an occupancy grid, along with image inputs and observed trajectory (x, y pedestrian coordinates), to predict the forthcoming pedestrian position data in the image frame or scene.

The work (Xu, 2017), proposes an approach that leverages a Fully Convolutional Network (FCN) to extract road scene image data and combines it with a LSTM to encode the current sensorial data of the egovehicle, including speed and angular velocity. The objective is to predict the next action that the egovehicle should undertake. The network's output represents the recommended current action, which can be one of the following: go straight, stop, turn left, or turn right.

The work of (Codevilla, 2018) also presents an approach to predict the appropriate action for the driver using both scene image and sensorial data. The network takes as input the image from the road traffic scene, along with measurement data such as egovehicle speed, and command data including egovehicle steering angle and acceleration. The neural network's objective is to predict the recommended action for the ego-vehicle, which can be one of the following: continue (follow the road), left (turn left at intersection), straight (go straight at intersection), or right (turn right at intersection). This paper makes use of CARLA (Dosovitskiy, 2017), an open-source urban driving simulator that can provide a realistic environment for training and evaluating autonomous driving related algorithms.

In (Gu, 2020), the authors present an LSTM-based solution for predicting future driver behaviour. The approach incorporates a CNN to represent the image frames and a recurrent neural network (LSTM) to encode twelve features extracted from the frames, including ego-vehicle velocity on three axes, distance from the ego-vehicle to the front car (dx, dy), front car velocity (three axes), front car acceleration (three axes), and the number of existing front vehicles. The input video sequence consists of ten frames (ten images), and the model predicts the future values of ego-vehicle acceleration on three axes. The approach employs a pretrained ResNet (He, 2016) for feature extraction from the input frames.

In (Ding, 2022), the authors focus on speedcontrol forecasting for autonomous or self-driving vehicles. The approach utilizes positional data of objects in the scene, which are processed through a CNN and LSTM to extract the ego-vehicle speed. The network incorporates Mask R-CNN (He, 2017) with a pretrained ResNet-50 backbone to extract object information, including bounding box coordinates. The proposed method constructs object-related graphs based on object proximity, where graph edges connect pairs of objects in the scene. Subsequently, graph convolution is applied to extract local spatial relations. The results are then fed into an LSTM and a multi-layer perceptron to obtain the ego-vehicle speed control data.

Most related work features imagery data from the scene, together with sensorial data that is then combined to extract current or future predictions, usually with recurrent neural networks (mostly using LSTM's). Usually, these methods feature complex deep learning architectures that require a lot of training data, pre-processing this data, and also the additional sensorial data as input. These neural networks are difficult to implement on hardware systems with limited resources (with the aim of being integrated in the vehicle).

In this paper, we propose making use of only imagery data in order to predict the current state of the vehicle (in this case the ego-vehicle velocity), based on previous "N" frames (image sequence). We choose N = 20 to represent the image input sequence. We then extend our initial solution to include the velocity as input along with the image data. Our work is similar to (Bojarski, 2016), where the authors make use of an end-to-end learning approach for a selfdriving car using artificial neural networks. The previous published paper explores using CNNs to learn driving behaviours directly from visual input and predicts the ego-vehicle steering angle from an image from the road traffic scene. We extend this to make use of sensorial data as input using CNN only models.

Our approach uses a publicly available large-scale video dataset that can be extended to also use different input data sources as presented in the results section.

3 SOLUTION OVERVIEW

We implement 2 CNN models to predict ego-vehicle speed. The first model features a sequence of images as input, whereas the second one features also the associated vehicle speed for each image as input into the network. We have also tested a Recurrent Neural Network based solution, that we implemented in order to compare our results. The third model features images and associated vehicle speed as input.

3.1 Proposed CNN Model: Image Input (V1)

The initial CNN model architecture proposed in this paper features several convolutional layers, followed by fully connected layers. This model is able to predict the current velocity, using only the extracted relevant features from the pixel data. An overview of the solution is presented in figure 1.



Figure 1: The proposed CNN model (V1) to predict the current vehicle speed based on an input sequence of 20 past frames (front-view images of the road traffic scene).

The model takes as input a sequence of 20 sequential images, each with a dimension of 300x300 pixels. The convolutional layers use different filter sizes and strides to extract spatial features from the images, progressively increasing the number of feature maps. Rectified Linear Unit (ReLU) activation functions are used to introduce non-linearity and enhance the model's ability to learn complex patterns. A Dropout layer is incorporated to mitigate overfitting. The output of the convolutional layers is flattened and fed into a stack of fully connected layers, which further capture higher-level representations of the input data. The final layer is a linear activation function that predicts the current vehicle speed. The model features a total of ~5.9 million trainable parameters, meaning

that it is easily trainable and also portable on other hardware (such as Nvidia Jetson platform).

3.2 Extended CNN Model: Image and Velocity Input (V2)

The initially proposed model (V1) was trained with the dataset presented in the next section. Then, we freeze the convolutional layers and the flatten layer wights, and the next step is to extend the CNN to also feature a measurement input, in this case the past 20 velocity values along with the 20 images.

Therefore, the extended network (V2) has the following structure (figure 2).



Figure 2: The extended CNN model (V2) that uses pairs of 20 images and 20 velocity measurements as input to predict the current velocity.

The flatten layer is then concatenated with the sensorial data input (reshaped to feature the same data ordering/dimensionality), followed by the same 4 Dense layers as the initially proposed model. Finally, we retrained the extended CNN (V2) and evaluate it.

3.3 Recurrent Neural Network Based Model (V3)

Based on previous published work, we have implemented our own version of a CNN+LSTM model based on the work of (Xue, 2018). Our implementation features a sequence of 20 images of the scene, as well as 20 corresponding ego-vehicle speed data as input. An overview of this approach is depicted in figure 3.

The layer architecture of this model is similar to the one published by the authors of (Xue, 2018). We change the input to use 20 images as input and predict one measurement.



Figure 3: An implementation of a CNN+LSTM network to predict the velocity data using pairs of images and velocities as input.

3.4 Dataset

We trained using the Honda Research Institute Driving Dataset - HDD (Ramanishka, 2018) that consists of 104 hours of driving data in road traffic scenes from the San Francisco area. The provided dataset introduces supplementary annotations that feature various driver behaviours observed in driving scenes, surpassing the limited focus on turn, go straight, and lane change present in existing datasets. Additionally, the dataset captures Controller Area Network (CAN) signals to depict driver behaviours in diverse scenarios, particularly interactions with other participants in traffic.

The dataset features the following sensor types: camera, Lidar, GPS, IMU and CAN bus signals, in various scenarios such as: suburban, urban and highway. The imagery data is encoded as colour images with the size of 1280x720 pixels, captured at 30 Hz. On the data we received, we actually found that some frames are missing and therefore not all sequences feature 30 fps. The dataset contains 137 trips, out of which we selected 7 random trips to be excluded from the training process (to be used for evaluation). The remaining 130 trips are split into training and testing/validation sets (80/20% split).

The 137 individual trips from the dataset feature various road traffic scenes, captured at different moments of the day and in various weather conditions. From these trips we have extracted sequences of N = 20 images, along with the provided ego-vehicle speed for each image, using a sliding window with an overlap of 5. We were able to obtain a total of over 14.000 continuous sequences of 20 images and 20 velocity data pairs ([T_{-21} : T_{-1}]), as well the current velocity data (T_0).

3.5 Implementation

The experimental setup features a desktop computer, equipped with an Intel i7 CPU and two Nvidia 1080

Ti GPUs that have a total of 22 GB VRAM that are used during the training process of the neural network. The software development is based on TensorFlow and Keras (Chollet, 2015) for the neural network, and OpenCV and Matplotlib for visualisation and video generation of the results.

4 EXPERIMENTAL RESULTS

4.1 Training the CNNs

All of the proposed CNN models for predicting vehicle velocity are trained using the Mean Squared Error (MSE) loss function and optimized using the Adam optimizer featuring an initial learning rate of 0.001 that is decreased if the loss function doesn't improve. The training process aims to minimize the difference between the predicted and ground truth vehicle speeds that are expressed in km/h.



Figure 4: The loss function values over 50 epochs for V1.

We make use of loss monitorization to early stop the model if the loss doesn't improve after 10 epochs, therefore we got a fully trained model after 53 epochs. Each epoch takes around ~18 minutes to train, resulting in a total training time of ~16 hours using our hardware setup. The extended model (V2) features a similar number of trainable parameters (5.909 million versus 5.907 for the initial), and the training times are almost identical. The CNN+LSTM based model (V3) features a total of ~26 million parameters, and using the same dataset means that the total training time is mostly similar.

4.2 Initial Evaluation and Optimization

The accuracy for all of the proposed models is evaluated using standard regression performance metrics, including R-squared, Mean Absolute Error (MAE), Root Mean Squared Error (RMSE).

We tried to determine the impact of selecting different regions of interest within an image on the

performance of a CNN-based regression model. The selected regions include the centre, left, and right portions of the input image, with the normal-sized input image serving as the baseline. Figure 5 illustrates the selected regions of interest (ROIs).



Figure 5: Selecting the regions of interest from the original input image.

Table 1 represents the evaluation results from the initial proposed model (V1), compared with the results obtained from the regions of interest models. We first trained on a small subset of 25 trips out of the entire 137 trips available in the HDD dataset, to determine the best performing input image (Normal or ROI). Then, we retrained the network (V1) with the entire train set (130 trips) using the most optimal input image type.

Table 1: Evaluation of the initial proposed CNN model (V1) for predicting the velocity (km/h).

Model image	R-squared	MAE	RMSE
input	(km/h)	(km/h)	(km/h)
Normal	0.825	4.334	6.085
(fully trained)		-	
Normal	0.448	8.335	10.831
ROI Centre	0.333	8.672	11.91
ROI Left	0.335	9.011	11.888
ROI Right	0.243	9.302	12.689

The analysis revealed that the normal-sized input image (no ROI applied) provided the best overall performance in terms of R-squared, MAE, and RMSE. Moreover, the centre region demonstrated relatively better performance compared to the left and right regions, indicating that the model relied heavily on the central information for accurate predictions.

Figure 6 contains the prediction versus ground truth of the ego-vehicle speed on a subset of frames from trip with the id "201703081617" from the HDD dataset.



Figure 6: Ground truth and prediction visual representation on a trip from the validation set for model V1.

Figure 7 represents some of our results on the evaluation test set, where the ground truth is displayed with blue, whereas the prediction is coloured red.



Figure 7: Ground truth and prediction visual representation on a trip from the validation set for model V1.

A video of the velocity prediction results, from the initial model (V1) using only images as input, is available here: https://vimeo.com/832355875.

The results from the extended model (V2) can be seen here: https://vimeo.com/832353512, whereas the V3 model (CNN+LSTM) predictions video is here: https://vimeo.com/832438597.

4.3 Evaluation of the Proposed Models

We have compared our proposed models (V1 - initial and V2 - extended) with the CNN+LSTM based method (V3). The results are presented in table 2.

Having the velocity as input and using it into a Recurrent Neural Network, combined with the extracted road scene data, means that the model is able to predict more accurately the current ego-vehicle velocity (speed). The downside is that existing published models (V3) feature more trainable parameters, therefore directly affecting negatively the prediction time (as can be seen in table 2).

CNN Model	R-squared (km/h)	MAE (km/h)	RMSE (km/h)	Prediction time (ms)	Model parameters
SS-LSTM based implement ation (Xue, 2018) - (V3)	0.99	0.52	0.76	18.64	~26 million
Proposed model (V1)	0.82	4.33	6.08	3.1	~5.9 million
Proposed extended model (V2)	0.96	1.93	2.66	3.1	~5.9 million

Table 2: Comparison between CNN+LSTM and CNN (initial and extended model) for velocity prediction (km/h).

From our experiments, we have found that the LSTM-based implementation (V3), although produces more accurate evaluation results, is actually heavily dependent on the past velocity input data. This can be proven simply by using random vehicular speed inputs to the network, as can be seen in the below figure:



Figure 8: Wrong ego-vehicle speed predictions (from the CNN+LSTM model) when the ego-vehicle data is corrupt/erroneous.

If we provide a constant past ego-vehicle speed as input along with the images, the predicted output of the CNN+LSTM model (V3) is also constant:



Figure 9: Wrong ego-vehicle speed predictions (from the CNN+LSTM model) when the ego-vehicle data is constant throughout the entire sequence/trip.

Our initial model (V1), even though not so accurate on the standard evaluation metrics, is proven

to be more robust because it is capable of correctly extracting the relevant features from the visual image sequence to predict the current speed:



Figure 10: Prediction of ego-vehicle current speed from our proposed model (V1 - using only image sequence input).

Furthermore, in order to compare our extended model (V2) with the same test scenario, we have simulated a sensor failure, meaning that we feed the CNN with "-1" values for the velocity as input into the model. Figure 11 illustrates the result of this test scenario.



Figure 11: Prediction of the ego-vehicle speed from the extended model (V2 - using image and past velocity input) with sensor failure simulated (0km/h past velocity fed as input into the model).

In order to validate the robustness of our solution, we have performed multiple tests with simulated sensor failure. The results are presented in table 3.

Table 3: Velocity (km/h) prediction evaluation of V2 model using different simulated sensor failures.

Sensor failure	R-squared	MAE	RMSE
rate	(km/h)	(km/h)	(km/h)
0%	0.966	1.93	2.66
10%	0.843	2.87	5.77
20%	0.770	3.51	6.98
30%	0.764	3.79	7.07
50%	0.765	4.24	7.06
80%	0.694	4.90	8.06
100%	0.796	4.67	6.57

The extended model (V2) is able to rely on pixel data in order to extract the relevant features to predict accurately the ego-vehicle velocity even in simulated velocity input failure (80% and 100% of the input

data is -1km/h). A video with the prediction results on the 80% fail rate can be seen here: https://vimeo.com/832352987.

We have also tested our models on a different dataset (Nedevschi, 2004), with images and data acquired using a different hardware setup. The data is acquired using a stereo-camera setup from which we use only the images from the left camera. The sensorial data is acquired using the CAN Bus from the vehicle, from which we use the velocity.

We have found that the image-based model (V1) is able to generalize and predict the ego-vehicle velocity accurately in most situations, especially when braking in intersections or decelerating during driving. Some of the results are presented in figure 12.



Figure 12: Predicting velocity on a different dataset using only images as input (V1).

We tested the extended model (V2) on the same dataset, and figure 13 presents examples of the prediction results.



Figure 13: Prediction of the ego-vehicle speed from the extended model (V2 - using image and past velocity input) with sensor failure simulated (0km/h past velocity fed as input into the model).

Given the fact that the new dataset uses a different hardware setup for the image acquisition process, we can reason that the image-based input only model (V1) is able to detect properly the velocity acceleration and deceleration when needed. This is effective in the situations where accidents can occur (intersections, pedestrian crossings, forward collision warning, etc.). When moving at a constant speed, the V1 model predicts an inaccurate speed due to difference in the frame rates from the training set and the new evaluation set (Nedevschi, 2004). The V2 model, that also features velocity as input, is proven to be more robust, and the evaluation of both versions on the new dataset is presented in table 4.

Table 4: Velocity (km/h) prediction evaluation of the proposed CNN models on the new dataset (Nedevschi, 2004).

CNN Model	R-squared	MAE	RMSE
	(km/h)	(km/h)	(km/h)
V1	-0.507	15.25	19.17
V2	0.871	4.04	5.59

4.4 Brake Pedal Sensor Evaluation

We have also trained the image-only based CNN (V1) to predict the brake pedal pressure that needs to be applied, as it was available in the additional sensorial data from the dataset. Figure 14 represents some results we have obtained on a small evaluation set.



Figure 14: Evaluation of the brake predictions versus ground truth from the dataset.

The evaluation results are based on the brake pedal pressure sensor from the dataset, which is expressed in kPa, meaning that no brake pedal pressed will give low values (close to 0), whereas full brake pedal pressed will represent a larger value (usually 2-3000 kPa. Evaluating the brake pedal pressure gives the following results: a MAE of 245.95, R-squared 0.52 and the RMSE is 422.15 on the V1 model that uses only images as input into the neural network. An example is presented in figure 15.

We found that the brake pedal pressure prediction is robust even on different datasets than the ones that were used during training, as can be seen in figure 15. The figure shows a case when the model is able to predict correctly that the brake pedal needs to be pressed when the vehicle is stationary.



Figure 15: Visualisation of the brake predictions and the ground truth velocity from a different dataset.

5 CONCLUSIONS

The implementation of a CNN model for vehicle speed prediction using sequential image input demonstrates the potential of leveraging temporal information captured in sequential frames. The model architecture, effectively extracts relevant spatial features and captures high-level representations of the input data. The model is evaluated using several evaluation metrics, providing insights into its accuracy and reliability. We extend our model to provide sensorial data as input and we compare both models with existing published work that uses additional sensorial input. We found that our approaches are more robust compared to other methods that leverage additional data while using recurrent neural networks, if the additional input sensorial data is corrupt or erroneous. We have also tested and evaluated our image based model to predict brake pedal pressure given the same sequence of input images, and the results are promising even on un-seen data from different datasets. Further experiments can enhance the understanding of the model's capabilities and potentially lead to improvements in vehicle speed prediction for realworld applications, such as video forensics.

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