

Ultra-Low Power Electronic Circuits Inspired by Biological Genetic Processes

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Abstract: Neuromorphic engineering, inspired by principles and architecture of neuronal circuitries, enabled the design of Artificial Neural networks (ANNs) for Intelligent systems. These systems perform very complex computation tasks, yet they consume significant power. Thus, using artificial intelligence (AI) for applications where only a small power source is available is very limited. While the neuronal networks in the brain can recognize complex patterns and memorize enormous elements, molecular and protein networks can perform other complex tasks such as adaptive immunity and cell differentiation at high energy efficiency. Here, we claim that a bio-inspired computing platform mimicking molecular protein networks can lead to ultra-low power emergent computation. Previously, we proposed a molecular-inspired computing model named Perceptgene that has the attributes of learning and adaptivity as the neural network (Rizik et al., 2022). Similarities were found between equations describing biochemical reactions and transistor operation at subthreshold (Sarpeshkar, 2011) enabling the design of Perceptgene with subthreshold electrical circuits. Thus, the subthreshold Perceptgene circuits are expected to allow computing and learning capabilities at ultra-low power consumption.

1 INTRODUCTION

Biological neural systems are comprised of remarkable parallel and distributed computing networks with adaptive, self-repairing, and replicative capacities in the performance of real-world tasks. Scientists and engineers have been inspired to mimic these features when designing artificial intelligence systems. Neuromorphic computing (Mead, 1990) applies abstract models of neural systems, such as the perceptron (Haykin, 2004), and uses microelectronics to build artificial intelligent machines. Today, the world is increasingly dependent upon this artificial intelligence (AI) and machine learning (ML) systems in several fields. Among these fields are health and finance, face and object recognition, command of autonomous vehicles, speech recognition, and natural language processing. However, the power consumption of current deep-learning machines and ‘layered neural networks’ is one of the most challenging limitations of these systems. The steep increase in their energy consumption and the computing power required for training them, which has grown 300,000-fold between 2012-18, are both unsustainable, putting substantial applications beyond the reach of all but well-resourced organizations. While the brain can perform

sophisticated information processing by employing complex neuronal circuit topologies with highly interconnected nodes, molecular biological systems contain extensively noisy parts that collectively interact to solve parallel tasks online with high energy efficiency. A single cell in the body, for example, performs 10 million energy-consuming biochemical operations per second on its noisy molecular inputs at 1pW of average power (Sarpeshkar, 2010). **In this study, we propose ultra-low power electronic circuits inspired by gene networks to demonstrate the computational abilities of neuronal networks. This approach relies on insights we have gained that map neuronal networks to molecular biological systems (biomorphic (Rizik et al., 2022) (Daniel et al., 2013)) and then to electronic circuits (cytomorphic (Sarpeshkar, 2011) (Hanna et al., 2020)), as shown in Fig. 1.** The proposed computational approach is realized by building subthreshold electronic circuits mimicking molecular networks based on the Perceptgene model [1]. We anticipate that subthreshold Perceptgene circuits will enable the implementation of an adaptive system with ultra-low power computation abilities.

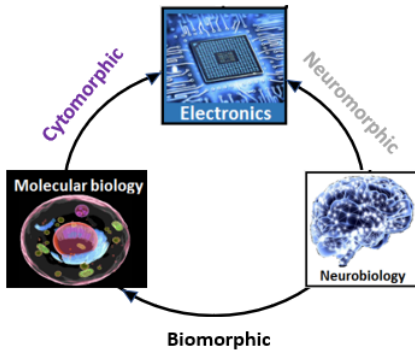


Figure 1: From Biomorphic to cytomorphic. **Biomorphic:** implementation of neural networks into synthetic molecular networks. **Cytomorphic:** implementation of molecular networks into electronics. **Neuromorphic:** implementation of the neural network into electronics.

2 BIO-MOLECULAR "NEURON"

Our neural model was inspired by combinatorial gene regulation kinetics of promoter activation (Fig. 2). A combinatorial promoter is regulated by multiple transcription factors x_i , each transcription factor binds to its designated region and afterward participates in recruiting the RNA polymerase to form the activation complex. In our model, several biological parameters are involved, such as the biological cooperativity of proteins, the number of binding sites in the promoter, the protein quaternary structure, and the binding affinities of protein-protein/protein-DNA reactions. In this process, multiple transcription factors participate and bind upstream to a gene sequence. Together they facilitate the binding of RNA polymerase to the promoter region forming the activation complex which initiates gene transcription.

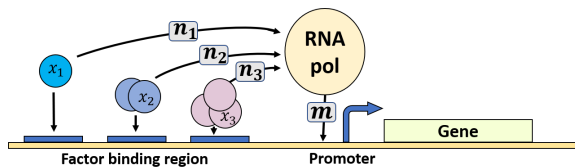


Figure 2: Anatomy structure of operating principles of gene regulatory network.

For a combinatorial activation, the relation between the transcription factors concentration and the promoter transcription rate, under certain conditions (Bintu, 2005), can be simplified and modeled as follows:

$$P = \frac{(\prod_i^N x_i^{n_i})^m}{(\prod_i^N x_i^{n_i})^m + kd^m} \quad (1)$$

Where P is the activation rate, x_i is the transcrip-

tion factor concentration, n_i is the Hill coefficient of transcription factor i associated with the activation complex formation, m is the Hill coefficient for the binding of the activation complex with the promoter and kd is the dissociation constant for the complex binding with the promoter.

By applying a logarithmic transform to Eq. 1, we obtain a new abstract model analogous to the perceptron model that is used in artificial neural networks (Fig. 3a). Similar to other artificial neuron models that operate as binary classifiers, this model achieves classification via a weighted input integration followed by a threshold activation for the output. However, three notable differences exist. First, the weighing of the inputs is done here according to a power law and not multiplication. Second, the inputs are integrated via a product rather than a summation. And third, the activation function used for this model is the Hill equation instead of the standard logistic function. Interestingly the perceptgene model can be viewed as a perceptron (Fig. 3) with a log transform over its input dynamic range, the proof is straightforward from the following equality:

$$P = \frac{(\prod_i^N x_i^{n_i})^m}{(\prod_i^N x_i^{n_i})^m + kd^m} = \frac{e^{m \sum_i^N n_i \text{Ln}(x_i)}}{e^{m \sum_i^N n_i \text{Ln}(x_i)} + e^{m \text{Ln}(kd)}} \quad (2)$$

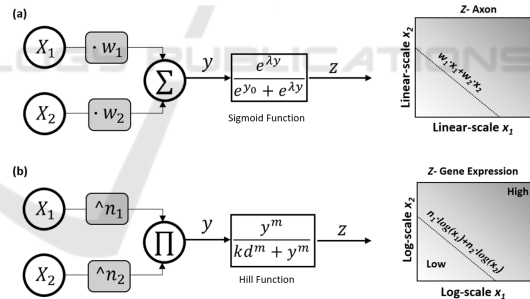


Figure 3: Abstract artificial intelligence models for (a) perceptron inspired by neural networks: x_i are the inputs, w_i are multiplicative weights, input integration is done via summation, and the activation function is the sigmoid function. Depicted on the right is the resulting linear separable classification of the analog inputs x_1 and x_2 (b) perceptgene inspired by genetic networks: x_i are the inputs, n_i are power weights, input integration is done via a product, and the activation function is the Hill equation. Depicted on the right is the resulting logarithmically separable classification of the analog inputs x_1 and x_2 .

3 PERCEPTGENE CIRCUIT CONCEPT

Analogous to perceptron implementation using analog linear circuits (e.g., resistors), we implement the Perceptgene using analog logarithmic circuits. Specifically, we use translinear analog circuits (Gilbert, 1975) with MOSFET transistors operating at the subthreshold region. The circuits implement power-law and multiplication functions for the input signals, while a nonlinear activation function circuit generates the output result. The proposed analog circuit for implementing the Perceptgene model as can be seen in Fig. 3b includes three subcircuits: 1. Power circuit – to implement the power (n_1 , n_2) function over X_1 , X_2 inputs 2. Multiplication circuit – to multiply the output of the power circuits 3. Activation function – a decision-making circuit based on the Hill equation

The analog subcircuits are translinear circuit that operates at the subthreshold region. The operation at the subthreshold region ensures that the current of the transistors depends exponentially on the voltage between the gate and the source of the transistor (Eq. 3). The translinear circuits follow the Trans Linear Principle (TLP) which refers to the summation of voltages with exponential dependency over closed loops. On these circuits, the product of the currents through the clockwise Translinear Elements (TEs) equals the product of the currents through the counter-clockwise TEs (Eq. 4). The usage of translinear subthreshold circuits enables us to implement the arithmetic function needed for Perceptgene at ultra-low power.

$$I_{ds} = I_0 \cdot \text{Exp}^{\frac{(V_{GS} - V_{th})}{U_T}} \quad (3)$$

$$Cw\{\pi(I_n)\} = CCw\{\pi(I_n)\} \quad (4)$$

3.1 Multiplication Circuit

The purpose of the multiplication circuit is to implement the multiplication function between the outputs of the power circuits. An illustration of the proposed translinear subthreshold analog circuit for implementing the multiplication can be viewed in Fig. 4. Since all the transistors operate in the subthreshold region, the current through them is exponentially influenced by their gate-source voltage. According to KVL, the voltages of the transistors sums up over a closed loop. The log summation of the voltages over a closed-loop turns into a multiplication of currents (Eq.5) as expected according to the TLP. Thus, for input currents I_1, I_2 , and a constant current I_3 we get the required functionality.

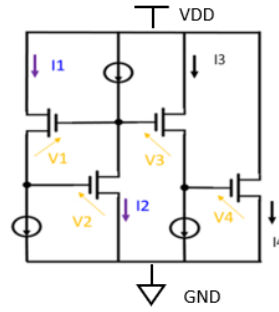


Figure 4: Multiplication subthreshold translinear circuit.

$$V_1 + V_2 - V_3 - V_4 = 0$$

$$\ln(I_1) + \ln(I_2) - \ln(I_3) - \ln(I_4) = 0$$

$$I_4 = \frac{I_1 \cdot I_2}{I_3} \quad (5)$$

Spice sweep simulations (Fig. 5) with $I_3=100\text{pA}$ and a I_1, I_2 varying from 100pA to 500pA resulted in the expected behavior of multiplication between I_1 and I_2 .

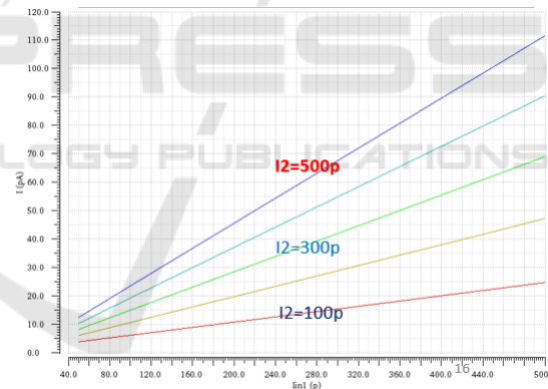


Figure 5: Multiplication circuit simulations.

3.2 Power Circuit

The goal of the power circuit is to implement the power (n_1 , n_2) function over the input signals X_1 and X_2 . An illustration of the proposed translinear subthreshold analog circuit which implements the power function can be viewed in Fig. 6.

The power circuit is similar to the multiplication circuit except for the resistors (R_1, R_2) which are connected to the device's gates. These resistors are connected as voltage dividers and thus define the V_{gs} of the transistors (Eq. 6). The relation between these resistors will be used to define the power constant n_1, n_2 (Eq. 7)

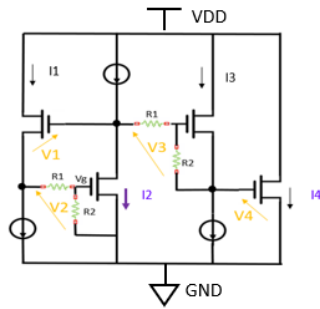


Figure 6: Power subthreshold translinear circuit.

$$V_{gs} = V * \frac{R2}{R1 + R2} \quad (6)$$

$$n = \frac{R1 + R2}{R2} \quad (7)$$

Due to the operation in the subthreshold region, the current is an exponential function of the V_{gs} voltage which is set by the ratio of the resistors. Thus we get a voltage that is a function of the power (n) of the current (Eq. 8)

$$V = \ln(I d s^n) \quad (8)$$

Summation of the voltages over a closed loop and a constant reference current ($I1, I3$) will then give the power (n) dependency between the input ($I2$) and the output ($I4$) currents (Eq. 9) as required.

$$I4 = I1 * \left(\frac{I2}{I3}\right)^n$$

$$I4 = \left(\frac{I2^n}{K}\right) \quad (9)$$

Spice sweep simulations (Fig. 7) with $I3=200\text{pA}$, $I1=100\text{pA}$ and I_{in} varying from 50pA to 500pA resulted in the expected behavior of a power function for different n values.

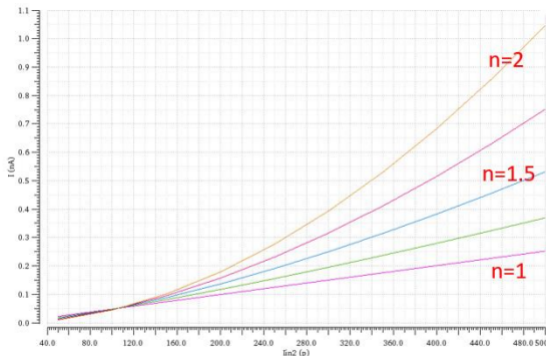


Figure 7: Power circuit simulations.

To insure minor currents through the voltage dividers the value of the resistors ($R1, R2$) should be

extremely high. The ability to design Giga ohms pseudo-resistors using transistors was already demonstrated ((Kassiri et al., 2013), (Puddu et al., 2016)). Our implementation of the voltage dividers might also include transistors or capacitors instead of resistors as can be viewed in Fig. 8 and Fig. 9 below.

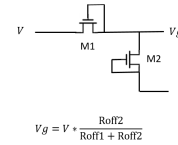


Figure 8: Transistors Voltage dividers.

The transistors implementation of the voltage divider (Fig. 8) includes transistors that operate at a subthreshold region and thus demonstrate huge resistivity. For deep subthreshold or cut-off connectivity where $V_{gs}=0$ the resistance can get to hundreds of Giga Ohms. The sizes of these transistors which are connected in series will define the exact amount of voltage divider which is implemented. The main challenge of this implementation is its sensitivity due to the exponential dependency of the current and thus the resistance in threshold voltage V_t .

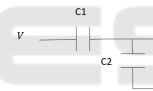


Figure 9: Capacitors Voltage dividers.

The capacitors implementation of the voltage divider (Fig. 9) includes capacitors that are connected in series. The capacitors are charged to different voltage values based on their capacitance thus creating a voltage divider with 0 dc current as required. The main challenge of this implementation is the need to deal with the dynamic behavior of the divider which might require extra switches for discharging the capacitors. On both implementations of the voltage divider, the n power coefficient of the circuit will be tuned by changing the capacitor or transistor sizes.

3.3 Activation Function Circuit

The Activation Function (AF) Circuit is a decision-making circuit implementing the Hill function (Eq. 1) and it generates the result based on multiplication circuit output. The nonlinear activation function circuit previously suggested in (Daniel et al., 2011) is based on a differential amplifier and 2 current mirrors as illustrated in Fig. 10.

Due to the symmetry of the circuit and the current

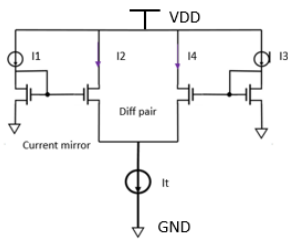


Figure 10: Activation function circuit.

mirrors, the ratio of the currents can be defined by (Eq. 10) The total current (It) of the differential pair is the summation of the currents on its branches and thus we get an output current (Eq. 11) which follow the Hill equation.

$$\frac{I2}{I1} = \frac{I4}{I3} \tag{10}$$

$$It = I2 + I4$$

$$I2 = It * \frac{I1}{I1 + I3} \tag{11}$$

The output current I2 is a nonlinear function of input current I1. When operated on the log scale we get the sigmoid activation function described in Eq. 12 below.

$$I2 = It * \frac{e^{Ln(I1)}}{e^{Ln(I1)} + e^{Ln(I3)}} \tag{12}$$

Fig. 11 shows the spice simulation results of the circuit. In that simulation, I1 varying from 10pA to 1nA (while It=500pA, I3=100pA) and the result in the log domain shows the expected sigmoid behavior.

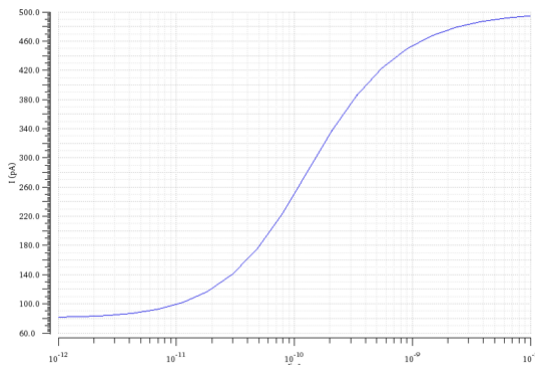


Figure 11: Activation circuit simulations.

3.4 Full Perceptgene Circuit

The circuits described in the previous sections were integrated into the full Perceptgene circuit as can be seen in Fig. 12 below. The full Perceptgene circuit

includes 2 power function circuits a multiplier and an AF circuit. The 2 input currents Iin1 and Iin2 are being processed by the circuit to generate the output current Iout. The Weights of the Perceptgene can be configured by changing the voltage dividers values and the Bias can be configured by changing the Iref current of the multiplier.

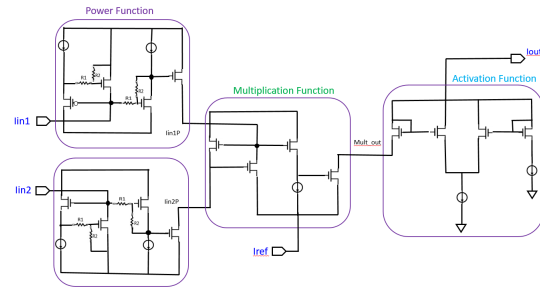


Figure 12: Full Perceptgene circuit.

As expected, due to its subthreshold operation, simulations of the circuit resulted in ultra-low power consumption ranging from a few to hundred nano Watts depending on the inputs and usage.

4 BASIC CLASSIFIER AND ANN IMPLEMENTATION

To build an ANN network, the perceptgene circuit needs to demonstrate its classification capabilities. Thus basic classifiers were implemented using a single neuron ANN realized by perceptgene circuit (Fig. 13).

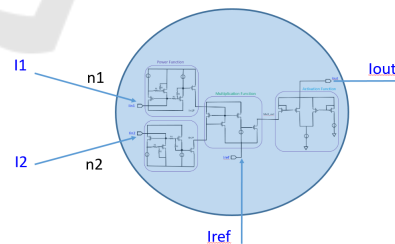


Figure 13: Single neuron classifier.

The first single perceptgene classifiers implemented two inputs OR/AND logic functions. Those functions were created by configuring the weights (R1, R2) and the bias (Irefm) of the perceptgene circuit. The following simulation results in Fig. 14 show that the circuit function as AND classifier when using the correct weights.

Spice simulation results of a perceptgene circuit in which the weights and bias were set to create an OR

I1[μ A]	I2[μ A]	I1*n1	I2*n2	Mult_Out	AF_out[μ A]
50	50	23	11	1.85	82 → 0
50	500	21	1040	13	109 → 0
500	50	1800	13	14	109 → 0
500	500	1680	1180	960	451 → 1

Figure 14: Two inputs AND simulations.

function can be viewed in Fig. 15 below.

I1[μ A]	I2[μ A]	I1*n1	I2*n2	Mult_Out	AF_out[μ A]
50	50	23	11	15	113 → 0
50	500	21	1040	1040	454 → 1
500	50	1800	13	1070	455 → 1
500	500	1680	1180	54000	498 → 1

Figure 15: Two inputs OR simulations.

From a single perceptgene classifier we move to a multi-layer ANN implementation. An example of such ANN can be viewed in Fig. 16. The three inputs ANN includes three perceptgene cells organized in two layers to implement the majority function when the correct weights ($n1$ - $n8$) are set. The majority function is a logic function in which its output is high when the majority of its inputs are high. Finding the weights ($n1$ - $n8$) which will enable the ANN to execute the majority function required the use of a Back-Propagation Gradient-Descend (BPGD) algorithm. Due to differences between the perceptron and the perceptgene a special version of the BPGD algorithm was developed.

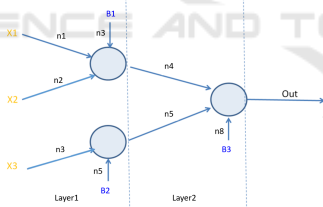


Figure 16: Three inputs Majority ANN.

In the Back-Propagation Gradient-Descend algorithm, the inputs are fed to the ANN and the weights are tuned based on the difference between the actual result at its output vs. the expected result. The algorithm search for the required weights of the ANN which provide the minimum error as can be viewed in Fig. 17.

The BPGD algorithm was tuned to operate in the log domain to fit the perceptgene operation. Thus the LOG of the error is calculated as can be viewed in Eq. 13.

$$Error = 1/2 * \text{Log}\left(\frac{Output_{Actual}}{Output_{Expected}}\right)^2 \quad (13)$$

The tuned BPGD algorithm was used successfully

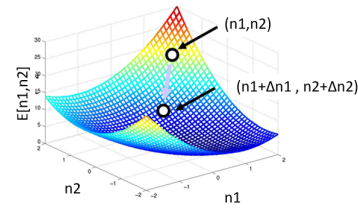


Figure 17: Gradient descends algorithm.

to build a few other multi-layer ANN which implements logic functions such as Muxes and full-adders.

5 CONCLUSION

We propose ultra-low power electronic circuits inspired by gene networks to demonstrate the computational abilities of neural networks. These circuits were implemented using MOSFET devices operating at the sub-threshold region. Basic training abilities for two and three inputs perceptgene networks were demonstrated. This study presents an energy-efficient bio-inspired platform that allows ANN computing with learning capabilities

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