







In Vitro Quantification of Cellular Spheroids in Patterned Petri Dishes

Jonas Schurr^{1,2}^a, Andreas Haghofer^{1,2}^b, Marian Fürsatz^{3,4}^c, Hannah Janout^{1,2}^d,
Sylvia Nürnberger^{3,4,5}^e and Stephan Winkler^{1,2}^f

¹Bioinformatics Research Group, University of Applied Sciences Upper Austria, Softwarepark 11–13, Hagenberg, Austria

²Department of Computer Science, Johannes Kepler University, Altenberger Straße 69, Linz, Austria

³Department of Orthopedics and Trauma-Surgery, Division of Trauma-Surgery, Medical University of Vienna, Austria

⁴Ludwig Boltzmann Institute for Traumatology, The Research Center in Cooperation with the AUVA, Vienna, Austria

⁵Austrian Cluster for Tissue Regeneration, Vienna, Austria

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Abstract: Cell Spheroids are of high interest for clinical cell applications and cell screening. To allow the extraction of early readout parameters a high amount of image data of petri dishes is created. To support automated analyses of spheroids in petri dish images we present a method for analysing and quantification of spheroids in its development stages. The algorithm is based on multiple image processing algorithms and neural networks. With an evolutionary strategy, engraved grid cells on petri dish are extracted and on top a Unet is used for the segmentation and quantification of different cell compartment states. The measured f1-scores for the different states are 0.77 for monolayer grid cells, 0.86 for starting formation grid cells and 0.85 for spheroids. As we describe in this study we can provide thorough analyses of cell spheroid in petri dishes, by automating the quantification process.


1 INTRODUCTION


Cell spheroids are an important 3D model for in vitro testing and are gaining interest for their use in clinical applications. Especially for chondrogenic differentiation, this is the golden standard model system (Zhang et al., 2010; Johnstone et al., 1998). However, its drawbacks encompass a large consumption of time and reagents in addition to lacking early readout parameters, limiting its usefulness as a screening system. To remedy this, a petri dish system was created, allowing for the creation of many spheroids within one vessel while reducing media consumption via self-assembly from cell monolayers (Fürsatz et al., 2021). This was achieved by subdividing the growth surface of standard cell culture treated petri dishes using CNC-guided CO₂ laser engraving. The engraved surface yielded anti-adhesive properties confining cell attachment only to the compartments and leading to self-assembly over time. This self-assembling pro-


cess can be monitored over time using macroscopic and microscopic imaging, and the resulting formation kinetics can be used to assess the effect of treatments (e.g. anti-inflammatory compounds) due to treatment depending change in formation behavior. However, due to the amount of image data and spheroids per well, automated detection of formation state is necessary to allow for efficient use of data. While the detection of fully formed spheroids would already give a good measurement of the formation progress, the detection of starting and not fully completed formation refine this data further. To achieve this, macroscopic images of petri dish plates seeded with adipose-derived stem cells (1×10^6 cell/plate) were obtained over the time course of the spheroid formation using an Olympus OM-D E-M1 digital camera with an Olympus M.Zuiko Digital ED 60mm 1:2.8 46 makro objective, fixed to a macrostrand at a distance of ~ 230 mm. The formation process was separated into four separate classes to describe the current state of self-assembly:


- (1) Monolayer describes a compartment with a completely attached cell layer.
- (2) starting formation describes a compartment where $>50\%$ of the cell layer remains attached.
- (3) late-stage formation describes a compartment


^a <https://orcid.org/0000-0001-8536-8354>

^b <https://orcid.org/0000-0001-6649-5374>

^c <https://orcid.org/0000-0003-4990-3326>

^d <https://orcid.org/0000-0002-0294-3585>

^e <https://orcid.org/0000-0002-5175-5118>

^f <https://orcid.org/0000-0002-5196-4294>

where $<50\%$ of the cell layer remains attached.

- (4) fully formed describes a completely detached and condensed spheroid. Due to the detachment, this class can also translocate to other compartments.

The differentiation between these groups is important as it allows a closer insight into the current formation state and, therefore a better characterization and possible earlier read-out of treatment effects compared to solely detecting fully formed spheroids.

Improvements in cell spheroid in vitro testing setups and screening systems with petri dishes causes new challenges for subsequent data analysis and fast data extraction. Improvements in technology enable a faster generation of image data due to simpler setups and a higher experiment frequency. To analyse a large amount of images An algorithm that provides automatic extraction allows more efficient data analyses, a faster overall experiment execution and increases objectivity, reproducibility and comparability. Many essential steps like localization and quantification are performed manually or with the help of multiple algorithms carried out in different software like ones of microscope manufacturers or ImageJ. While these often deliver a wide range of algorithm, many subsequent steps still need to be carried out manually or require expert knowledge. To allow faster and simple experiment analyses and information extraction, an easy-to-use end-to-end workflow for automated analyses are of high interest.

In this work, we show a robust method for the automatic extraction of the grid structure in petri dishes and the applicability of automated segmentation for the classification and subsequent quantification of different types of cell compartments in petri dish images. Multiple steps are needed to enable automatic information extraction and subsequent quantification. The cell compartments are segmented and classified for the extraction of the classes described above. For the quantification of monolayer (type 1) and formation (types 2 and 3), each grid cell of the petri dish is assigned to cell compartment type. Therefore, an automated grid extraction to extract single grid cells is crucial in addition to the segmentation step.

1.1 Data

As shown in Figure 1, the datasets consist of petri dish images from a digital single-lens reflex camera using a 60mm F2.8 macro lens. All images provide a color depth of 24 bits and a dimension of 4608×3456 pixels. All shown annotations are created using the slide runner labeling tool (Aubreville et al., 2018)

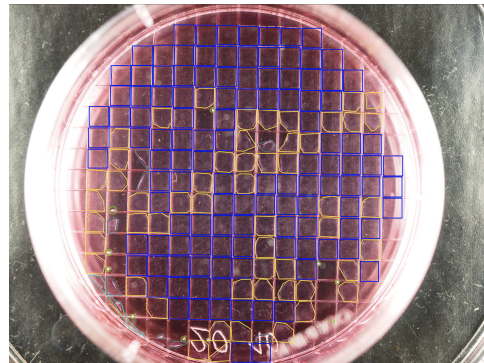


Figure 1: Representation of an example image out of the used dataset, including the manually labeled objects to be segmented and classified. The blue marks represent the initial monolayer class. The yellow and gray marks are used for the early and late formation of future spheroids. The green color indicate the final spheroids.

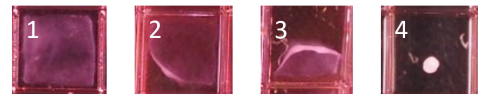


Figure 2: Example of the four stages from the initial monolayer (1) to the formation stages of early (2) and late (3) formations until the final spheroid form (4).

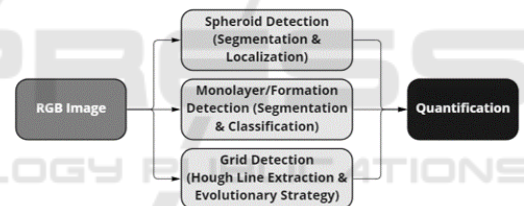


Figure 3: Simplified representation of the quantification workflow, including the three independent detection steps.

As shown by the individual cells in Figure 2, initially a monolayer (1) forms within each compartment of the petri dish. During the ongoing formation process, this monolayer transforms into the final spheroid form (4). The states in between are separated into early (2) and late (3) formations, which are combined into one formation class for the workflow in this paper. The whole image dataset contains 20 images which are divided into three separate sets for training the segmentation models (12 images), validation (2 images) and testing (6 images).

2 METHODS

Our presented workflow has a modular design and is based on three detection steps as shown in Figure 3. This design decision allows future adjustments of the used image processing algorithms as well as replace-

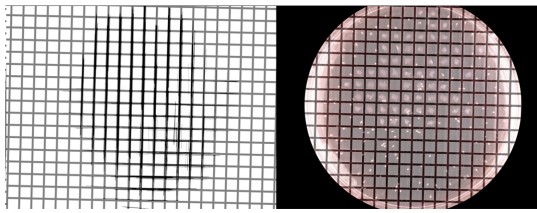


Figure 4: Examples of the grid identification with the mapped grid in binary (left) used for the fitness function and the mapped grid in the RGB image (right).

ments of the current segmentation neural networks.

2.1 Heuristic Grid Identification

Grid mapping is performed to analyse single grid cells in the image of a petri dish. A generated grid mask maps the underlying grid. This grid mask defines single grid cells and is used to extract the single grids correctly. The grid is optimized with image processing algorithms and an evolutionary strategy.

2.1.1 Preprocessing

Multiple preprocessing steps are performed before the final grid optimization can be executed. To avoid possible noise outside of the petri dish and to further on enable the identification of grid cells within it, the petri dish itself is extracted. This is achieved by hough circles (Barabas et al., 2013; Forero et al., 2020; Duda and Hart, 1972). The parameters for blurring, canny edge detection, and the accumulator threshold of the hough transformation were identified manually on 14 images. It is presumed that the center of the petri dish is within a window of 30% image length in the middle of the image. As fitness function of the evolutionary strategy, a binary mask is extracted automatically from the original RGB image. This processed binary mask is used as a ground truth image in the fitness function, which is defined by the inverted Dice coefficient, whereas the prediction is the solution candidate representing a mask counting a predicted grid (as shown in 5). To extract the binary mask, after CLAHE, to increase the contrast, borders are extracted with hough lines representing the grid on the petri dish image (Zuiderveld, 1994; Duda and Hart, 1972; Hansard et al., 2014). To allow the extraction of hough lines, a binary image with Roberts edge detection is created based on the equalized RGB image (Roberts et al., 1965; Bhardwaj and Mittal, 2012). The connection of multiple extracted hough lines for one line, is realized by morphological filtering especially closing. Kernel size is reflected by the size of the border and is extracted in relation to the image size. The final extracted mask, consists of white

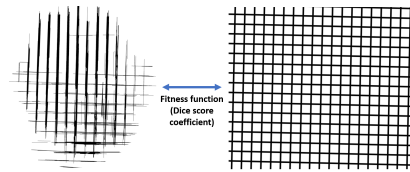


Figure 5: Representative images for Dice coefficient between preprocessing image used as ground truth (left) and predicted grid (right).

background and black lines. A too-low minimum line length increases the amount of noise within the image, whereas a too high number of minimum line length misses too many lines. In our evaluations, a minimum length given with 10% of the image height provides robust results. In the experimental setup, light is coming from the sides of the images, which increases the contrast of vertical borders and allows an easier extraction. Therefore, a lower threshold can be used optionally for horizontal lines to avoid overlooking them. With the described steps, a sufficient amount of horizontal and vertical borders are extracted within the petri dish, which is important as ground truth for a proper evaluation of the solution candidates.

2.1.2 Grid Optimization by Evolution strategy

Due to low contrast, shadows and disturbing effects, not all borders in the image are visible or can be extracted from the image. Therefore, an evolution strategy is used for the approximation of the full grid and the prediction of missing borders in the petri dish (Borgmann et al., 2012). The goal is to use the extracted lines in the preprocessing step as ground truth and fit a predicted full grid onto the extracted ground truth image based on the fitness function. The error of the fitness function is defined by the Dice coefficient between the extracted binary images of the preprocessing step containing the extracted lines and a predicted grid image represented by a solution candidate, as shown in equation 1.

$$DiceCoefficient = \frac{2 * TP}{2 * TP + FP + FN} \quad (1)$$

Defined by: true positive (TP), false positive (FP) and false negative (FN). Each solution candidate defines a grid (see 6). Four adjustable parameters leaned on affine transformation parameters are used to represent a grid:

- Rotation: Rotation of the grid lines to the origin.
- Scaling: Width of a single grid cell.
- Horizontal and Vertical offset: Position and translation of the grid.

For each solution candidate, an image containing the grid using the parameters is created to evaluate the fitness of the solution candidate. An applicable amount

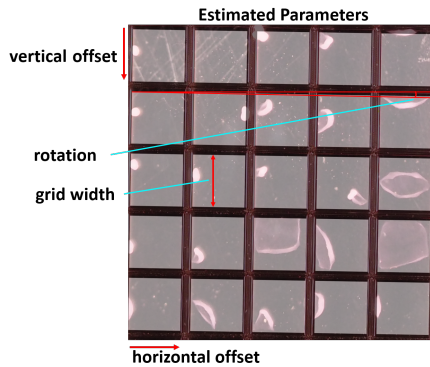


Figure 6: Explanation of solution candidate parameters.

for the population and starting sigma of the evolutionary strategy to allow a robust convergence was evaluated. Elitism was used for the creation of new generations to keep the best candidate until this point. Moreover, the initial search space is reduced by problem-specific constraints. The maximum width of a grid cell also defines the maximum offset. Additionally, the grid cells can not exceed 10% of the image's height. The rotation is limited to a maximum of 5 degrees. The evolutionary strategy is used for the optimization of the grid prediction and, therefore, the accurate extraction of every single grid cell.

2.2 Object Detection

2.2.1 Segmentation Models

Descendent from the Unet architecture (Ronneberger et al., 2015) which represents a specialized artificial neural network for image segmentation, the used Unet ++ (Zhou et al., 2018) represents the base architecture for our segmentation models. Provided by the segmentation models package (Iakubovskii, 2019) for the used Pytorch framework these models were trained with the support of the Pytorch-lightning framework (Falcon et al., 2019). Out of the several provided backbones for the Unet ++, our segmentation models are built with the regnety_120 backbone (Radosavovic et al., 2020) which delivered the best results for our use case. Due to limitations of the available sample images, our modelling process also included the use of data augmentation techniques (Shorten and Khoshgoftaar, 2019) which represents a commonly used approach for artificially extending the available amount of image data. In our case, it was necessary to use image cropping, which was realised by randomly selecting small parts of the images instead of using the whole image for the input of the neural network. This technique was used on the training as well as the validation data. For the training

data, color and contrast adjustments combined with image distortion, transposing, scaling, and rotation added some variation in the available image properties. All in all, it was possible to extend our training and validation data by a factor of 30. The separated test data was not changed using any of the mentioned algorithms. The original dataset without augmentation included 12 training images, 2 validation images and 6 test images with a resolution of 4608x3456 pixel. The concept of using two models instead of one is built up on the idea that the first stages of a forming spheroid can not move within the petri dish.

2.2.2 Monolayer and Forming Spheroids Classification

As Figure 7 shows, our segmentation model separates the monolayers (blue) as well as the currently forming spheroids (green) from the background represented by the rest of the petri dish. This segmentation neural network classifies the corresponding stage for each pixel without the possibility for the same pixel to be part of more than one class. This design decision was made due to the property that these objects can not overlay each other, which led to the use of a softmax activation within the final layer.

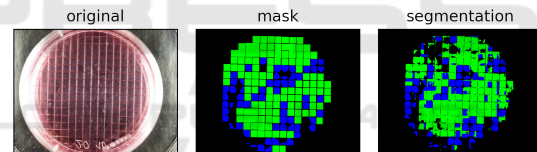


Figure 7: Example image of the segmentation result (right) based on the raw RGB image (left) in comparison to the mask (middle) representing the to be achieved separation of the two classes. Green represents the already forming spheroids out of the blue monolayer.

To further improve the accuracy of the prediction used for a final quantification of monolayer cells and currently forming spheroid cells, a prediction for every single grid cell is performed. The prediction is based on the segmentation results. Since a prediction of both classes can be within a single grid cell of the grid a final decision to correctly classify such a grid cell has to be made. The quantification of each cell type is allowed by the assignment of the class to each valid grid cell. Only grid cells within the petri dish are considered. Therefore, grid cells that are not fully within the petri dish and grid cells with a high percentage of background are removed for the evaluation since they cannot contain any cell or the cell is cut and not fully in the image. The estimated grid defines each grid cell. For each grid cell, a prediction of either one class is performed. If a grid cell

contains a prediction for a monolayer, it is assigned as a monolayer and vice versa for the second class of forming spheroids. A prediction within a grid cell is extracted by connected components. If both classes are predicted within a single grid cell, the monolayer class is taken if the predicted overall area is larger or if the confidence of the model is higher in comparison to the second class. This is suitable since monolayers are larger by definition.

2.2.3 Spheroid Localization

In contrast to the monolayer and forming spheroid stages, the final spheroid objects can move around and overlay other objects. This property could lead to a pixel with more than one class, which is possible by using a second model specifically for this class. Normally, this would be realized by a multiclass segmentation model for all stages at once, but this decision would inhibit the ability of the workflow to only allow spheroid objects to overlap other classes. As shown in

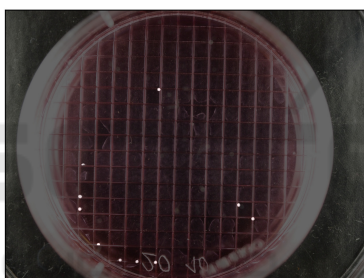


Figure 8: Example of the test dataset with an overlay of the segmentation on the original RGB image. All detected spheroids are represented by the white dots.

Figure 8 this second neural network only separates the possible spheroid objects from the background without any knowledge of the other stages. Therefore, all the other stages are considered as background. Based on this segmentation result, the actual localization of the individual objects is realized using the connected components algorithm from the Open CV Python framework (OpenCV, 2015). After a filtering step that removes every object smaller than 70 percent of the average object size, the resulting objects are located by their center pixel as assigned to the spheroid class for the final quantification step. This size filtering has to be done individually for each image to be segmented by the fact that the object size also relies on the camera parameters and the used lens. Therefore, it would not be possible to set a specific size limit for all now-arriving objects. This 70 percent of the average size limit was set based on the current dataset. It still allows some wrong detected objects, but it in-

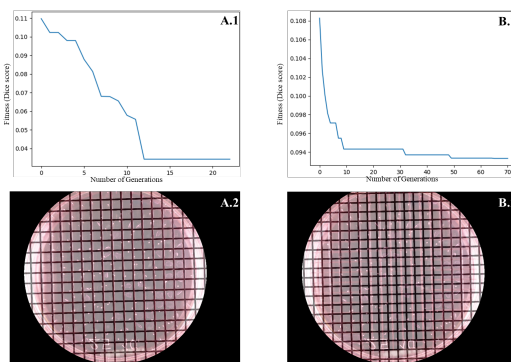


Figure 9: Comparison of a sufficient and insufficient result for grid alignment on an image of a petri dish.

hibits nearly all artifacts that are smaller than all valid spheroids, like wrongly as spheroids detected reflections or air bubbles. Based on the used imaging setup, this limit can be adjusted by the user for future applications. Due to the possibility of the final spheroid stage merging together with other spheroids, an upper size limit is not considered to have any positive impact on the segmentation quality.

3 RESULTS

3.1 Monolayer & Forming Spheroid Quantification

3.1.1 Parameter evaluation of Grid Estimation

In Figure 9 the applicability of the evolutionary strategy and its used fitness function is shown. Two different results on the same image with its corresponding fitness score histories can be seen. In the first results (A.1 and A.2) the fitness is improved over multiple generations down to a value of 0.034. The low value is also connected to a good result (as shown in sub-image A.2). Whereas in the second result (B.1 and B.2) the error (fitness score) can be reduced slightly in the first generations but there is no further improvement also after multiple generations. This states a false optimization in a local optimum and is reflected in a higher value of 0.093. The higher error is also reflected in the corresponding sub-image (B.2), as it can clearly be seen that the grid is not aligned and even divides the actual grid cells on the petri dish into two parts. The second result was generated by an ES with an insufficient size for the population. The aligned grid and the converging error over multiple generations in sub-images A.1 and A.2 show the applicability of the used fitness function and also the overall approach.

Table 1: Fitness comparison of multiple runs with different settings for the evolutionary strategy.

Population	sigma	mean \pm std [min - max]
1,50	0.05	0.086 \pm 0.003 [0.063 - 0.229]
10,50	0.05	0.063 \pm 0.005 [0.052 - 0.229]
20,100	0.05	0.061 \pm 0.005 [0.05 - 0.231]
20,100	0.1	0.062 \pm 0.01 [0.048 - 0.229]
20,100	0.001	0.125 \pm 0.048 [0.044 - 0.25]

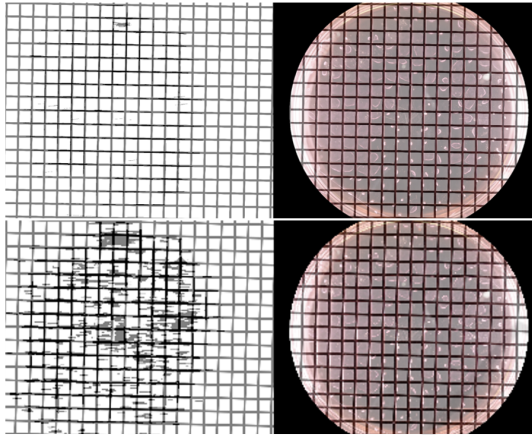


Figure 10: Example results of the mapped grid on an image with different resolutions (row 1: factor 1.25, row 3: Factor 0.25). On the left the overlap of the grid and the binary image can be seen. on the right the fitted grid on the rgb image is shown.

As shown in Table 1, multiple runs for a different setting for the population of the ES and the initial sigma were performed. In it, the average error over 20 images is shown. The used setting with 20 parents and 100 children and an initial sigma of 0.05 provides the best and most robust results with the lowest average error of 0.061 and a standard deviation of 0.005. Whereas other runs with a higher starting sigma (0.01) and a lower amount for the population (10,50) provide similar results, lower values for the population, especially with only one parent or a lower starting value of sigma for faster convergence is insufficient and provides clearly worse results reflected in a higher error of 0.086 and 0.125.

As it is important that the grid detection also works size independently, example images of different sizes can be seen in Figure 10. The shown resolutions are factor 1.25 and 0.25. In a both results (rows) the grid is aligned correctly. For resize factor 1.25 in all tested images, the grid was identified correctly. The grid lies perfectly on the preprocessed image. The preprocessed image also contains a very low amount of noise and a large amount of extracted hough lines. With smaller images, the amount of noise increases. The result in row 2 shows a worst

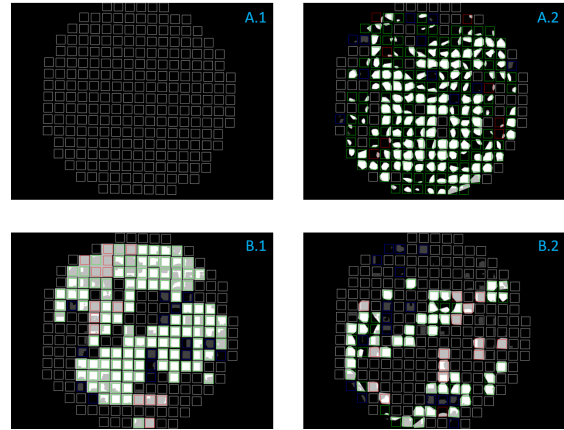


Figure 11: Final grid cell prediction based on two example images (A and B) for the prediction results of both classes (monolayer and starting formation). The Figure shows the final evaluation of the algorithm with its assignments per grid cell (white: true negative, green: true positive, blue: false positive, red: false negative).

case scenario with a high amount of noise, but still shows a correct grid. In almost all cases, the evolutionary strategy is robust enough to allow a correct alignment also in smaller images or images with higher noise.

3.1.2 Segmentation of Monolayer & Starting Formation

Table 2: Monolayer and forming spheroids segmentation quality measurements on the test dataset.

Class	Jaccard	F1
Empty	0.8739	0.9671
Monolayer	0.5995	0.3674
Forming spheroid	0.7969	0.7754

As shown in Table 2, our segmentation neural network can identify empty cells and already forming spheroids with an F1 score of over 0.9671 for the empty ones and a slightly lower score of 0.7754 for the forming spheroid class. The main struggle for our network is the identification of the monolayer class, which led us to the presented post-processing steps for an increase of the initial F1 score as low as 0.3674.

3.1.3 Classification Monolayer and Starting Formation

In the final object detection step the quantification for each relevant type of cell is fulfilled. In Figure 11 the classification and quantification of monolayers (class 1) and starting formation cells (class 2) can be shown. In the figure the results for both classes on two example images are shown (Image A, and Image B). Image

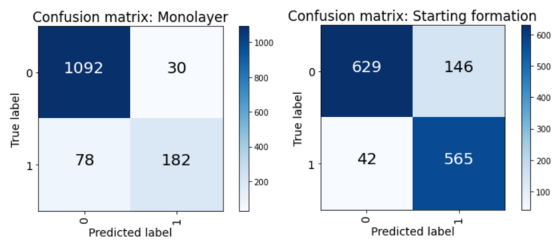


Figure 12: Confusion matrix of grid cell classification for the classes monolayer & starting formation).

A shows a result without any monolayer cells in the ground truth. The predictions for the monolayer class in sub-image A.1 are all correctly true negative. The model can therefore predict correctly even if there is no cell in that class. In the prediction of the monolayers (image B.1) in image B a high amount of monolayers can be seen. It can be seen that the models' prediction and the subsequent class assignment to a grid cell do indicate good results. Despite some false positives (blue colored grid cells) and false negatives (red colored grid cells) the prediction result can be considered as good. Most errors in class 1 appear in monolayer cells that span the whole grid cell with bad lighting or starting formations cells that just started and are still covering almost a full grid cell. Another problem is the mentioned division of a single cell into two different classes, which can lead to false negatives in one class and false positives in the other cells. These problems can also be seen in sub-images B.1 and B2, where most false negatives are starting formation cells with almost full coverage of the grid cell. In sub-image A.2 these problems appear much less therefore, a higher performance can be reached. All in all, the approach shows minor problems with border cases but a good overall performance.

Table 3: Metrics of grid cell classification for the classes monolayer and starting formation.

class	accuracy	precision	recall	f1-score
monolayer	0.92	0.86	0.70	0.77
formation	0.86	0.80	0.93	0.86

The general performance on all test images is shown in Table 3 and Figure 12. The result shows a high accuracy of 0.92 for class 1 and 0.86 for class 2. Especially the predictions for the monolayer cells do have high accuracy. This is in comparison to the class with cells that started the formation due to a very good prediction of true negatives (also shown in sub-image A.1 in Figure 11). Overall, the prediction of cells with starting formation provides slightly better results, as shown in the f1-score. With scores of 0.77 and 0.86 the error, especially for cells of the starting formation class, is low. The lower f1-score in the first class

can be explained by a lower recall resulting in more missed cells, whereas the precision is higher. For the class of starting formations, most cells are detected with slightly lower precision. Both have a considerably high performance. With a f1-score of 0.77 and 0.86, the final quantification was increased in comparison to the performance of the segmentation itself and subsequently allows a good automatized quantification.

3.2 Spheroid localisation

As shown in Table 4, the raw segmentation mask can not provide the demanded quality for accurate quantification of the spheroids within an image.

Table 4: Spheroids segmentation quality measured on the test dataset.

Class	Jaccard	F1
Spheroid	0.7642	0.6889

The exceptionally low F1/Dice Score is significantly increased during the post-processing, including the actual location of the floating objects, as shown in Table 5. As explained in section 2.2.3, the localization of each spheroid is represented by its center pixel. Based on these coordinates, the quality measures of Table 5 where realized by the comparison with the label masks. The mentioned filtering, as well as the added localisation workflow increased the final F1 Score from 0.6889 to 0.8457.

Table 5: Spheroids localisation quality measured on the test dataset.

Class	Accuracy	Precision	Recall	F1
Spheroid	0.7327	0.8962	0.8007	0.8457

As shown in the confusion matrix of Figure 13, most of the actual spheroid objects are segmented and classified correctly. Despite the high amount of falsely as background detected objects, the number of false positives could be kept on a significantly lower level, which is realized by the mentioned size filter. Without this filter, the number of false positives would increase significantly by a factor of 6.5 due to the increased amount of noise detected as objects.

4 DISCUSSION AND OUTLOOK

Regarding the presented results, our workflow already provides the functionality for the automated quantification of cell compartments on petri dishes by forming spheroids based on RGB images. Simply imaged using a normal DSLR camera, these images are

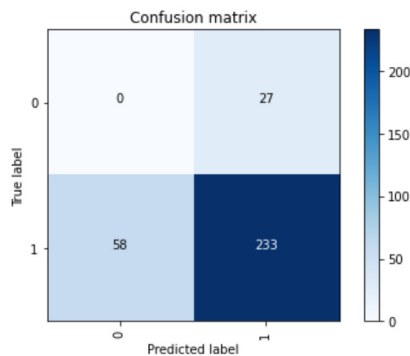


Figure 13: Confusion matrix of the spheroid localisation showing result measures on the test dataset.

processed using a combination of machine learning algorithms, heuristic optimization, and computer vision. This combination of state-of-the-art algorithms allows our workflow to quantify different stages of forming spheroids which will be used for statistical analysis in future work, including the influence of different drugs measured over a period of time. Despite the low initial segmentation quality, our presented post-processing and quantification algorithms increases the classification performance of our workflow significantly, which still allows reliable quantification of the different stages. In future different segmentation methods will be further evaluated to increase the overall performance. Regarding these first results, the amount of data used for the modeling steps will be increased significantly in future work, which should further increase the final quality of the quantification.

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