Breathing Life into Models: The Next Generation of Enterprise Modeling

Peter Fettke\textsuperscript{1,2}\textsuperscript{a} and Wolfgang Reisig\textsuperscript{3}\textsuperscript{b}

\textsuperscript{1}German Research Center for Artificial Intelligence (DFKI), Saarbrücken, Germany
\textsuperscript{2}Saarland University, Saarbrücken, Germany
\textsuperscript{3}Humboldt-Universität zu Berlin, Berlin, Germany

Keywords: Systems Composition, Data Modeling, Behaviour Modeling, Process Modeling, Composition Calculus, Algebraic Specification, Systems Mining.

Abstract: Edsger W. Dijkstra has frequently suggested building a “firewall” between the technology- and application-side of computer science. His justification: The methods to attack the computer scientists’ formal, mathematical “correctness problem” differ fundamentally from the methods to attack the applicants’ informal “pleasantness problem”. In this setting, a model is always confined to one side or the other of this wall. This keynote shows that a seamless transition between both sides can be achieved by a framework with \textit{architecture}, \textit{statics}, and \textit{dynamics} as the three pillars of modeling computer-integrated systems. Selected examples justify this framework. It allows to “breathe life” into (static) models, and it implies a new understanding of the “pleasantness” of computer-integrated systems, which is well-needed in the age of “digital first”.

1 INTRODUCTION: THE TWO FACES OF COMPUTER SCIENCE

Computer-integrated systems exhibit two faces: the technological and the applied face. Edsger W. Dijkstra has frequently suggested to strictly separate both sides and to build a “firewall” between them (Dijkstra, 1989). His justification: The methods to attack the computer scientists’ formal, mathematical “correctness problem” differ fundamentally from the methods to attack the applicants’ informal “pleasantness problem”. In this setting, a model is always confined to one side or the other of this wall.

In contrast to Dijkstra, we understand modeling as an activity that should allow a seamless transition between formally and informally given or asserted facts of a computer-integrated system. Technology and applications must be interlocked by shared models, based on the same foundations.

This keynote shows that our goal can be achieved by the H\textsc{ERAKLIT} framework with \textit{architecture}, \textit{statics}, and \textit{dynamics} as the three pillars of modeling computer-integrated systems (Fettke and Reisig, 2021\textsubscript{a}; Fettke and Reisig, 2021\textsubscript{b}). Selected examples justify this framework. It allows to “breathe life” into previous static, logic-based models, and it implies a new understanding of the “pleasantness” of computer-integrated systems. This is a key to understanding systems in the age of “digital first”.

This contribution consists of five sections. After this introduction, Section 2 explains what is needed for the foundations of computer-integrated systems from the application perspective. Section 3 presents our approach to digital modeling through a plain case study. Main characteristics of H\textsc{ERAKLIT} and related work are discussed in Section 4 and 5, respectively. The paper concludes with Section 6.

2 TOWARDS FOUNDATIONS FOR THE APPLICATION SIDE OF COMPUTER SCIENCE

In the last decades, computing-oriented disciplines have developed several strong ideas for the foundations of computer science. Typically, foundations of computer science stem from technical foundations such as abstractions of hardware, physical devices, sensors, actuators, etc. Another approach stems from theoretical computer science, starting with alphabets, formal languages, computable functions, etc.
But what are the foundations from the application-side of computer science? In this contribution, we argue that such foundations must cope with three fundamental phenomena:

- **Architecture**: Computer-integrated systems in the real or an imagined world are not monolithic, amorphous, or unstructured, but can best be described and understood as the composition of different sub-systems. Hence, composing a system is inevitable for the proper understanding of a complex system. In one sentence: **composition matters**!

- **Statics**: Computer-integrated systems process data. However, the world we live in consists not only of symbolic data objects but of many more relevant objects, e.g. invoices, customers, agreements, orders, and products. These objects need to be understood and represented adequately. Again, in one sentence: **objects matter**!

- **Dynamics**: The world is not static, but continuously evolving. Events happen all over the world in time and space. A system’s progress in time induces an order of events; however, this order is irrelevant for a proper understanding of the event flow. On the contrary, it spoils the causal order of events, which orders two events \( a \) and \( b \) by \( a < b \) if and only if \( a \) is a prerequisite for \( b \). Of course, \( a < b \) implies each potential clock to timestamp \( a \) before \( b \). But \( a \) timestamped before \( b \) only implies that \( b \) is not a prerequisite for \( a \). Again, in one sentence: **causality matters**!

To sum up, composition, objects, and causality are important for understanding the application side of computer science. In other words, the world we are living in matters. In our contribution, we show that HERAKLIT, an integrated modeling framework to formally describe the aspects mentioned before, is indeed feasible.

### 3 A PLAIN EXAMPLE

The following subsections illustrate the three HERAKLIT’s pillars by the plain example of a digital stamp, a stamp that is augmented with a matrix code. Fig. 1 depicts one exemplar of a digital stamp; each digital stamp carries a unique matrix code for individual identification.

#### 3.1 Architecture

The basic concept of architecture is modules. Inside a module, HERAKLIT typically uses Petri nets in various forms. In general, a module \( M \) has two interfaces, the left interface \( *M \), and the right interface \( M^* \). An interface can contain Petri net places as well as transitions. Graphically, a module is represented as a rectangle, with the elements of the left interface on the left or top edge of the rectangle and the elements of the right interface on the right or bottom edge.

Fig. 2 shows a typical model for the transportation of conventional letters. There are three modules: the sender, the postal service, and the receiver. The left interface of the sender is empty, its right interface contains a Petri net transition. The label of this transition, post, matches the labels of the transition of the left interface of the postal service; transitions with the same labels are merged later on when the two modules will be composed. Likewise, the right interface of the postal service and the left interface of the receiver contain equally labeled transitions.

The labels of the interface elements indicate the behavior and functionality of the modules: the sender posts each letter to the postal service. The postal service delivers each letter to the receiver. The receiver finds the letter in its inbox.

Fig. 3 shows the composition of the three modules, namely:

\[
\text{sender} \bullet \text{postal service} \bullet \text{receiver} \tag{1}
\]

with \( \bullet \) being the universal composition operator. This bracket free notation is possible since the composition operator is associative, i.e. for any three models \( R, S, T \) holds (Reisig, 2019):

\[
(R \bullet S) \bullet T = R \bullet (S \bullet T). \tag{2}
\]

The greatest possible abstraction of the modules is depicted in Fig. 4. Two activities of a postal service are modeled: post and deliver a letter; technically as Petri net transitions in "postal service and postal service" with the labels post and deliver, respectively.

#### 3.2 Statics

In each postal service, three sets of items play a central role: letters, stamps, and matrix codes. In a postal service, these quantities consists of different elements: each postal service has different sets of letters, stamps, and matrix codes.
Nevertheless, to formulate the processes for all postal services in the same way, we use a signature, $\Sigma_0$, shown in Fig. 5, a technique to model a schema. This technique allows to characterize concrete objects from the real and imagined world as instantiations of such a schema. Here, we adopt notions such as structures, signatures, and instantiations of signatures, that are well-known from first-order logic (Suppes, 1957). Technically, a signature is just a set of sorted symbols for \textit{sets}, \textit{constants}, and \textit{functions}. An instantiation interprets these symbols consistently. We extend signatures by requirements to exclude “unwanted” instantiations.

In the example, the signature contains the three symbols \textit{letters}, \textit{stamps}, and \textit{matrix codes} for the three sets described above, plus two symbols ($f$ and $g$) for functions. The symbol $f$ stands for a function that assigns to each letter its stamp; $g$ for a function that assigns to each stamp its matrix code. Both functions are injective. The function symbol $g$ stands for a function that is only partially defined since some stamps do not carry a matrix code.

The signature $\Sigma_0$ can be instantiated in many ways. Each concrete postal service is characterized by such an instantiation of the signature. In the case study, we discuss the instantiation $S_0$ of Fig. 6. This instantiation consists of three letters $(a,b,c)$, four stamps $(l,m,n,o)$, three matrix codes $(1,2,3)$, and a particular assignment between letters, stamps, and matrix codes. For example, letter $a$ is assigned to stamp $m$; stamp $m$ is assigned to matrix code 1.

### 3.3 The Behavior of the Three Modules at the Schema Level

Signatures and their instantiations can naturally be transferred to define Petri net schemata. Such a schema can be instantiated in different ways; each instantiation results in a concrete Petri net.

We model the behavior of each of the three modules from Fig. 2. Fig. 3 shows the behavior of each module at the schema level, i.e. based on the signature $\Sigma_0$, rather than a single instantiation. As a mathematical concept, a place represents a predicate that applies to a set of objects. This set can grow and shrink through the entry of transitions.

The sender module in Fig. 2 describes the letters to be sent. The question of an appropriate initial marking arises: for a given instantiation, i.e. a concrete
Postal service, the place `outbox` initially contains all letters as tokens. In the example of the structure \( S_0 \) from Fig. 6, these are the three tokens \( a, b, \) and \( c \). On the schematic level, we only know the symbol `letters`, for which each instantiation can freely choose an assignment with a set of letters. However, the intuitively obvious idea of labeling the place `outbox` with the symbol "letters" falls short: when instantiating the symbol `letters` with a set, for example \( \{a, b, c\} \), initially this set would emerge as a single token. However, we want the three elements of this set as individual tokens. This is noted as "elm(letters)".

Mathematically, the idea behind this is that a place represents a predicate that currently applies to the tokens on the place. The place `outbox` with the inscription `elm(letters)` thus stands for the logical expression:

\[
\forall x \in \text{letters} : \text{outbox}(x). \tag{3}
\]

The instantiation \( S_0 \) thus generates in the initial marking the logical expression \( \forall x \in \{a, b, c\} : \text{outbox}(x) \). Thus, initially, the three tokens \( a, b, c \) lie on the place `outbox`.

In a given instantiation \( S_0 \), the transition `post` can occur in the sender or postal service module as soon as a token is present on the place `outbox`. The assignment of the variable \( x \) can freely be chosen from the set with which the instantiation \( S_0 \) instantiates the set `symbol letters`. In analogy, the postal service module forwards one letter from the postbox to the delivery box. Finally, the letter is delivered to the receiver.

### 3.4 The Instantiation \( S_0 \) and its Behavior

Fig. 7 shows three instantiated modules; Fig. 8 shows the module system \( S_0 \), which is created from the modules of Fig. 2 in two steps: first, the three modules from Fig. 2 are composed into a single module, and second, the signature \( \Sigma_0 \) of Fig. 5 is instantiated with the structure \( S_0 \) of Fig. 6. In particular, the place `outbox` now contains three tokens.

In the instantiation \( S_0 \), one can now document the processing of individual postal services. In the initial state, for example, the transition `post` is activated. After that, the letter can be posted by the sender, forwarded to the delivery box, and be delivered to the receiver.

**HERAKLIT** models a behavior as a distributed run; formally conceived as a module. This makes it easy to compose distributed runs. The current example also shows that distributed runs show details of behavior much more explicitly than is possible with sequential runs. In particular, relationships between objects and causality is explicitly modeled.

Fig. 9 shows what happens with the letter \( a \): The letter moves from the sender's outbox to the postbox, then to the delivery box and finally to the receiver's inbox. Technically, this is the run of letter \( a \) in the system \( S_0 \). Fig. 8 depicts two more letters, \( b \) and \( c \), yielding corresponding runs. Together, the three runs of \( a, b, \) and \( c \) define the overall run of the system \( S_0 \), shown in Fig. 10. In the run of each single letter, the events `post`, `forward` and `deliver` occur strictly ordered. As the letters proceed independently of each other, the events of different letters occur independently, namely their occurrences are not ordered in the overall run of the system \( S_0 \).

Fig. 10 exemplifies that events are not ordered along a time axis; instead, order represents causality. For example, the event `forward` for letter \( a \) occurs causally after the event `post` for letter \( a \), but is causally independent from all events of the letters \( b \) and \( c \). The run of Fig. 10 is the only run of the system \( S_0 \) in Fig. 8. System \( S_0 \) is deterministic, as there is never a decision to be taken; and \( S_0 \) is concurrent, as some events occur unordered. One may nevertheless introduce global views into the run of Fig. 10. A global view is a maximal set of unordered places. Each of the three letters can be in exactly one of the four boxes. In technical terms, each such set corresponds to one of the \( 64 = 4 \times 4 \times 4 \) reachable markings of the system in Fig. 8.

### 4 MAIN CHARACTERISTICS OF HERAKLIT

The main characteristics of the HERAKLIT framework were introduced by means of a plain example. From a conceptual point of view, the HERAKLIT framework is based on three pillars (Fettke and Reisig, 2021a; Fettke and Reisig, 2021b). Each pillar focuses on different but integrated aspects of modeling (Fig. 11):

- **Architecture**: A HERAKLIT model consists of modules. Each module has an arbitrarily designed interior; in particular, the level of abstraction of the representation is freely selectable. The interface of a module contains labeled elements. The composition of modules is technically simple and always associative. The formal basis of this architectural principle is the composition calculus (Reisig, 2019).
- **Statics**: For dealing with data and data structures, HERAKLIT employs abstract data types and algebraic specifications, as they have turned out to be useful in computer science from the begin-
ning and have long been used in specification languages such as VDM, Z, etc. (Sanella and Tarlecki, 2012). Symbolic representations (in terms of a signature) are used as in predicate logic. Each module has a signature, i.e. a set of symbols for sets, constants, and functions, from which, together with variables, terms are then formed. A signature, and thus its terms, can be instantiated in quite different ways.

- **Dynamics:** A module for describing behavior contains a Petri net inside of it. Here, each place of the Petri net is a logical predicate, each arrow is labeled with a term of the module’s signature, and each transition with a condition. For a given instantiation of the signature, the set of objects to which the predicate applies can grow or shrink due to the occurrence of an event. In detail, this is described by terms at the arrows of the Petri net. This allows behavior to be represented abstractly on a schematic level, but also concretely for a “meant” instantiation.

![Figure 7: Three instantiated modules.](image1)

![Figure 8: System S0.](image2)

![Figure 9: The run of letter a.](image3)

![Figure 10: The run of S0.](image4)

![Figure 11: The three pillars of HERAKLIT.](image5)
5 RELATED WORK

In the last decades, a plethora of modeling frameworks emerged (Frank et al., 2014; Sandkuhl et al., 2018; Vernadate, 2020; Wand and Weber, 2002). In 1992 already, some colleagues coined the term “methodology jungle” for characterizing the variety and diversity of the research field (ter Hofstede and van der Heide, 1992). Nowadays, this field is still evolving and maturing. Relevant work can be approached from different angles, e.g. the problem addressed or the solution purported.

In the field of business informatics, typical frameworks used are Architecture for Integrated Information Systems (ARIS) (Scheer, 1999), Business Process Model and Notation (BPMN) (Object Management Group, 2014), Event-Driven Process Chains (EPC) (Keller et al., 1992), MEMO (Frank, 2014), the St. Gallen Approach to Business Engineering (Österle, 1995; Winter, 2001), and Unified Modeling Language (UML) (Object Management Group, 2017). Most of them offer graphical representations to describe behavior (e.g. BPMN, EPC), some have expressive means for data structures (e.g. ARIS, MEMO), and in some cases also for schemas (MEMO). Some known frameworks use more or less formally defined composition operations. None of the frameworks are fully formally defined but describe many aspects only intuitively. Thus, no other framework reaches the scope of expressive means of HERAKLIT. This characterization is also true for frameworks stemming from the information systems discipline, e.g. Bunge’s ontological model (Wand and Weber, 1990) or work system theory (Alter, 2013).

From a computer science perspective, several modeling frameworks were proposed, e.g. Abstract State Machines (ASM) (Gurevich, 2000), Aloy (Jackson, 1987), High-level Petri Nets (Genrich and Lautenbach, 1981; Jensen and Kristensen, 2009), event-B (Abrial, 2005), FOCUS (Broy, 1997; Broy and Stolen, 2001), Statecharts (Harel, 1987), TLA (Lamport, 2002), and Z (Spivey, 1992). The central ideas and concepts of HERAKLIT combine three well-proven, intuitively easy to understand, and mathematically sound concepts that have been used for the specification of systems in the past:

- Architecture: The composition calculus for structuring large systems. This calculus with its widely applicable associative composition operator is the most recent contribution to the foundations of HERAKLIT. The obvious idea, often discussed in literature, of modeling composition as fusion of equally labeled interface elements of modules is supplemented by the distinction of left and right interface elements, and composition \( A \bullet B \) as fusion of right interface elements of \( A \) with left interface elements of \( B \). According to (Reisig, 2019), this composition is associative (as opposed to the naïve fusion of interface elements); it also has several other useful properties. In particular, the composition is compatible with refinement and with single (distributed) runs.

- Statics: Abstract data types and algebraic specifications for the formulation of concrete and abstract data: since the 1970s such specifications have been utilized, built into specification languages, and often used for (domain-specific) modeling. (Sanella and Tarlecki, 2012) presents systematically the theoretical foundations and some applications of algebraic specifications.

- Dynamics: Petri nets for formulating dynamic behavior: HERAKLIT uses the central ideas of Petri nets (Petri, 1962; Reisig, 2013). A step of a system, especially of a large system, has locally limited causes and effects (Petri, 1977). This allows processes to be described without having to use global states and globally effective steps. The connection with algebraic specifications is established by (Reisig, 1991).

These three theoretical principles harmonize together and generate further best-practice concepts that contribute to a methodical approach of modeling with HERAKLIT and which could only be touched upon in this keynote. On the downside, industrially mature tools for HERAKLIT are still under development.

6 CONCLUSIONS

The fundamental focus of our approach becomes clear in comparison with the firewall propagated by Dijkstra: HERAKLIT follows the tradition of logic, integrating formal arguments as part of the scientific penetration of real-life facts. Logic has successfully been doing this for 2000 years. HERAKLIT extends formal logic by including dynamic aspects, and shapes a connection between informal and formal concepts.

Like no other framework, HERAKLIT combines the three pillars of architecture, statics, and dynamics for modeling computer-integrated systems. Formulated in buzzword form on a technical level:

\[
\text{HERAKLIT} = \text{modules} \oplus \text{relational structures} \oplus \text{local steps},
\]

and on the level of calculi:

\[
\text{HERAKLIT} = \text{composition calculus} \oplus \text{logic} \oplus \text{Petri nets}.
\]
With HERAKLIT, both sides of Dijsktra’s wall can be grounded on the same foundations. It is obvious that this approach has decisive advantages and will achieve tremendous gains: It is seamlessly possible to capture the main ideas of a natural and intuitive understanding of the world we live in, enrich this understanding with formal concepts, and use the description as a foundation for (forthcoming) supporting software.

The technical HERAKLIT concepts described can be used to model aspects of discrete systems in a way that no other modeling technique can:

- Modules of different hierarchical levels can be composed, e.g. a module may represent the behavior of a component at the finest, operational level. At the same time, its neighboring modules are given only by their names and their interface.
- Real-world and abstract objects are coequal elements of formal reasoning. HERAKLIT follows predicate logic and conceives both, real-world and formal objects, as interpretations of terms of a signature (an alphabet with typed symbols).
- Behavioral models can be parameterized. Each interpretation of the symbolic labels of a schematic HERAKLIT module generates a separate system model. For example, a schematic module describes the principles of business processes of all branches of a commercial bank; each interpretation describes a concrete branch.
- The size of models grows linearly with the size of systems. This is especially true for modeling dynamic behavior. To achieve this, HERAKLIT works without globally effective constructs, in particular without global states. The notion of single runs, as well as the composition operator for modules, are likewise locally confined.
- HERAKLIT adopts verification techniques. Petri nets provide a variety of efficient computational verification techniques. The most important ones, in particular place- and transition invariants, also work at the symbolic (signature) level and – more expressively – for individual interpretations of a signature. Verification based on model checking is only possible for individual interpretations of a signature; efficient procedures exist for this. A large, still open research area is compositional verification: properties of a composed system are derived from properties of the composed modules.
- A single run can be distributed. In a run of a system, events often occur independently. For example, in a bank branch, employees interact with individual customers largely independently; they are only occasionally synchronized when accessing scarce resources, such as meeting rooms. Many modeling frameworks model this kind of independent events as "occurrence in any order". This leads to exponentially many supposedly different "sequential" processes. HERAKLIT explicitly models independence of events, not only in sequences but any other partial order. This yields a clear notion of non-determinism and a theorem according to which the runs of a composed system are derivable from the runs of its components.

- HERAKLIT uses intuitively simple basic concepts: predicate logic is familiar to many users from other contexts anyway. Petri nets are also widely used in computer science and its application areas. The composition calculus is immediately conceivable from small examples. The graphical means of expression of Petri nets and the composition calculus complement each other harmoniously.

It is plausible that HERAKLIT will help to harmonize the plethora of different phenomena associated with computer-integrated systems. In other words, it will be possible to describe the essence of different application types, and system structures of applications, including real-time systems, reactive systems, data-intensive systems, cyber-physical systems, service-based systems, integrated business systems for enterprise resource planning ("ERP systems"), supply chain management ("SCM systems"), customer relationship ("CRM systems", "ticket systems"), product lifecycle management ("PLM systems"), and many more system types in the "digital world".

In the future, more work is needed to develop the HERAKLIT framework into a universal modeling infrastructure:

1. More case studies and industrial applications are required, to identify special classes of models, shorthands, best practices, etc.
2. HERAKLIT specific analysis methods have to be developed, respecting and employing the local character of events and modules, to formulate and to prove decisive properties of models.
3. Powerful software tools have to be created, supporting the construction of models, their analysis, the integration of databases, etc.

So far, HERAKLIT provides fundamental pillars for systematically developed, theory-based models, covering a broader spectrum of aspects than any other modeling infrastructure. It is now time to “breathe life” into models with HERAKLIT.
REFERENCES


