

Analysis of the Relationship between Subjective Difficulty of a Task and the Efforts Put into It using Biometric Information

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Abstract: This paper proposes a novel method for analyzing the relationships between the difficulty of tasks and the effort of learners to accomplish them using biometric information. The biometric information we adopted was as follows: 1) pupil diameter variation for estimating subjective task difficulty, and 2) eye movements indicative of answer selection times for assessing subjective efforts and strategies to solve the problems. The data used in this study are eye movement data obtained in a different study for studying brain activities during arithmetic calculations in terms of electroencephalography (EEG) data (Suzuki et al., 2021). This study reanalyzed the eye movement data by introducing the following two variables: 1) the duration times in the characteristic areas for solving the tasks to understand how the participants strategically retrieved the task information, and 2) the changes in the sizes of pupil diameter to understand the levels of engagement of the participants while solving the tasks. This study suggests that the relationships found in these variables should characterize the participants' learning attitudes and could be related to confidence and satisfaction in the attention-relevance-confidence-satisfaction (ARCS) model, indicating the possibility of applying the results to educational systems.

1 INTRODUCTION

Since the onset of the Coronavirus-2019 pandemic, opportunities for online learning centered on e-learning have increased from the perspectives of social distance and avoidance of crowds. This is also the case in the context of higher education institutions. Additionally, issues related to learning attitudes such as *the quality of learning* and *the level on motivation* have emerged. The intensive e-learning that is currently practiced, makes it difficult to motivate students to learn and keep the quality of learning at high levels by the timely and appropriate interventions of the teachers.

One of the reasons for the difficulty might be the discrepancy between the difficulty level of the tasks given to the learner and the learner's learning ability. In order for a learner to stay motivated to learn a subject, it is crucial to have the learner engage in the task, which has to be at the right level of difficulty for the learner. In other words, the subjective task difficulty should be at the right level; when it is

too easy, the learner would consider the time spent for solving the task wasteful. On the other hand, if it is too hard, the learner would give up without gaining any knowledge from the learning. Learning through the right task would provide the learner with the satisfaction of task-accomplishment. Even if the learner fails to solve the problem, s/he would gain useful information after understanding the correct answer by gaining knowledge on solving the problem correctly.

In this paper, as a method to solve this discrepancy, we examine the possibility of estimating the appropriateness of the difficulty level of the presented task from the degree of cognitive load at the time of task execution, using the task of mental arithmetic addition and multiplication as an example task. In order to estimate the degree of matching of the difficulty level of a given task with the ability of participants, this paper examines the utility of biometric information such as eye movement and pupil diameter during calculation.

This paper is organized as follows. Section 2 describes the model of assessment of task difficulty and efforts in solving tasks via biometric information. Section 3 outlines the previous experiment whose data we use for this paper. Section 4 describes the

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method for analyzing biometric information. Section 5 describes the results of the analysis. Section 6 discusses the obtained results from the perspective of applying them for effective education.

2 SUBJECTIVE TASK DIFFICULTY AND EFFORTS IN SOLVING TASKS

This section commences with a description of the method for estimating the degree of subjective difficulty of tasks by using biometric information in Section 2.1. It is assumed that the reaction of the learner at the very moment when s/he observes the task should be critical to estimating his/her motivation to engage in the task, and not after s/he spends some amount of time solving the task. The biometric information should reflect his/her unconscious reaction to the task, which should be dependent on his/her personal experience and moment by moment situation.

The second topic of this section described in Section 2.2 is the amount of effort expended in solving the task. This is again estimated by using biometric information, more specifically using the eye movement patterns that should characterize when the learner confirms that the problem has been solved. Directly observable behavior such as completion of entering the answer by using a keyboard could be used for estimating the above, but the biometric information should be more accurate than the latter for estimating it.

2.1 Pupil Diameter: Estimating Subjective Task Difficulty

There are two types of changes concerning the pupil; *mydriasis* (dilation of the pupil) and *miosis* (contraction of the pupil of the eye) depending on the amount of light entering the eye and the mental state. It has been reported that the relationship between the pupil diameter and the mental state of a person shows a large mydriasis with the passage of time when a mental stress load is applied, but shows different changes depending on the type of stress (Taba et al., 1996). In addition, it has been reported that when the subject was shown a video in which the object gradually appeared, mydriasis had already occurred before the inspiration or new perception was reported (Suzuki et al., 2018).

These findings could be used for deriving relationships between the states of efforts and the degree of task difficulties; the amount of mydriasis is propor-

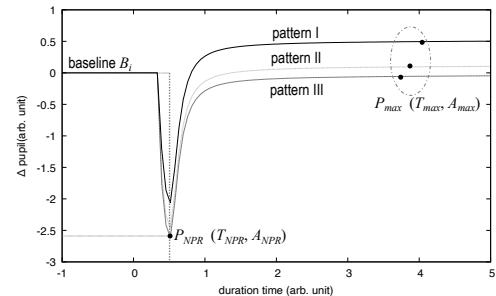


Figure 1: The relation between duration time and Δ pupil diameter.

tional to the degree of task difficulty, i.e., the more difficult the task becomes, the larger the mydriasis becomes due to increased cognitive processing.

Figure 1 schematically shows the relationships between the changes in pupil diameter and the duration times. The vertical axis represents the variation of the pupil diameter denoted as A with reference to the baseline B_i where i denotes the index of the participant of the experiment. The horizontal axis represents the duration time t where $t = 0$ corresponds to the time when the stimulus was provided. The points P_{NPR} and P_{max} characterize the pupil reaction to the input stimuli; P_{NPR} corresponds to so-called “near pupil response,” and P_{max} is the point where the answer to the problem is confirmed.

Figure 1 illustrates three patterns that are differentiated by the task solving situations depending on the values of A_{max} relative to B_i . The respective participant’s states would be estimated as follows:

- (I) $A_{max} > B_i$ (top); severely unexpected discovery of solution with intensive thinking.
- (II) $A_{max} \sim B_i$ (middle); weak unexpected discovery of solution with moderate thinking.
- (III) $A_{max} < B_i$ (bottom); no unexpected discovery of solution or idle. Gives up to find the candidate answer.

2.2 Answer Selection Time for Assessing Subjective Task Efforts and Strategies

In arithmetic calculation tasks, there are numerous steps to select the answer. For example, Lebier (Lebriere, 1999) suggested that there are two basic strategies to confirm the answer: simple retrieving and calculation answer. After choosing strategy, participants execute the task. The termination condition of the arithmetic calculation task is divided into the case where answer confirmation is possible and not possible. If answer confirmation is possible, the

task is completed by selecting either the correct or incorrect answer. If answer confirmation is not possible, the task ends due to giving up on the task.

In the experiment referred in this paper, the arithmetic calculation task is performed within a fixed time of t_{task} seconds in order to induce the partial strategy selection time to be performed in a short time or to give up. The difficulty level L_t of the task presented to the partial is set to the following three types in light of the arithmetic teaching guidelines in Japan:

1. Those that can be solved almost easily within t_{task} seconds,
2. Those that are thought to be multi-decomposable in about t_{task} seconds, and
3. Those that are almost unlikely to be solved in t_{task} seconds.

For retrieving strategy, the process of selecting answers basically matches the pattern of perception information and memory information. In this sense, the answer selection time for the arithmetic calculation task is dependent on whether the participants' finish the pattern matching. If the participant is accustomed to doing calculations on a regular basis, the pattern matching will take less time. However, participants may find it uninteresting because it is a dry task. If not, since it is difficult for participants to perform pattern matching on the task, they will continue matching for a long time or give up matching. In any case, the participant needs to change the strategy from retrieving to calculation, in order to select the right answer.

With regard to calculation strategy, there are multiple steps for answer confirmation. Since the calculation strategy is a procedural task, it will take more time for a participant than a simple search, but it will feel like an intellectual task.

On the other hand, it is also assumed that the partial cannot answer confirmation by retrieving or calculation for the arithmetic calculation task. The existence of inference, which is a third strategy, is conceivable so as not to give up answer confirmation easily. In other words, when answer confirmation is possible for some digits, answer confirmation is performed from the candidate presented based on that information. In the case of answer confirmation by inference, answer confirmation needs to be performed only for some digits, and thus can be completed quickly compared to retrieving and calculation. From the above, the answer selection time T_c can be an index of how the partial selection was performed.

Figure 2 shows the relation between duration time and eye movement which is represented by AOI. The participants' eye movement will be 3 steps:

- watch the given task (Zone A in Figure 2),

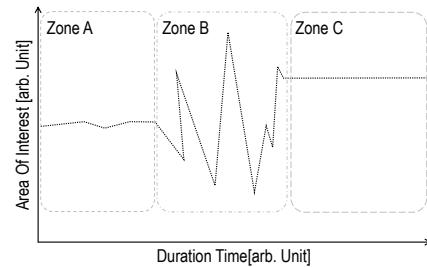


Figure 2: The relation between duration time and eye movement which represented AOI.

- Work on the task and select the answer (Zone B in Figure 2),
- stare at the answer (Zone C in Figure 2).

In this paper, T_c is defined by the boundary Zones A and B. When participants are watching the given task, they concentrate on performing the task; this means that they cannot afford to look away. In a sense, participants' eye movements are for engaging in the specific area. At the time of finishing the given task, they prepare to select the answer candidate. The reason why we set T_c as the boundary Zones of A and B is that we save time with regard to participants who finished the task and began to select the answer candidate. The relationships between the strategy which participants selected and T_c are as follows:

- Pattern D: short time T_c , Zone B area, and long time Zone C. Selected retrieving strategy with high confidential of answer.
- Pattern E: long time T_c , middle time of Zone B, and short time Zone C. There are two possibilities. (1) selected calculation strategy with high confidential of answer, and (2) selected inference strategy.
- Pattern F: short time T_c , long time of Zone B, and no show of Zone C. Gave up to find answer.

Through these consideration, we analyze the relation between ΔA and T_c , which indicate the participants' condition, and whether they perceive the task as dry/intellectual issue.

3 SUZUKI ET AL.'S EXPERIMENT (Suzuki et al., 2021)

The purpose of this study was to conduct a basic analysis to estimate the difficulty level of a task for learners by designing calculation tasks with three difficulty levels and measuring biometric data of learners while

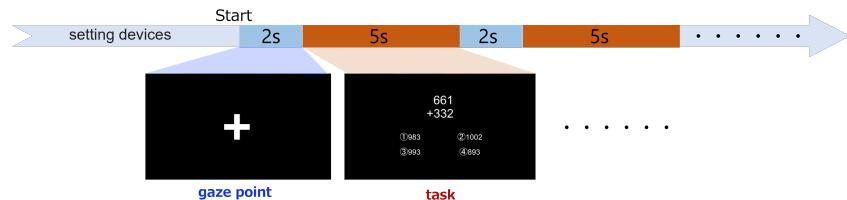


Figure 3: Flow of the experiment.

they were working on the task. This section reviews the method of the experiment and the main results concerning the EEG data, which motivated us to conduct re-analysis of the pupillary dilation in conjunction with the times necessary for the participants to confirm their answers.

3.1 Overview of the Experiment

3.1.1 Equipment

EPOC+ was used for measuring EEG data of the participants while engaging in the arithmetic tasks with the sampling rate of 128 Hz. Tobii Pro Nano was used for gaze measurement. The sampling rate was 60 Hz. The monitor used in this experiment was 21.5 inches with a resolution of 1920×1080 pixels. It was set up so that the distance between the monitor and the subject was about 57.3 cm. Tobii Pro Lab was used to conduct the task.

3.1.2 Participants

18 undergraduate and graduate students in their teens and twenties participated in the experiment. This experiment was approved by the Ergonomic Experiment Ethics Committee of Nagaoka University of Technology.

3.1.3 Procedure

The experimental flow is shown in Figure 3. This experiment was conducted in a cycle in which the gazing point was displayed at the center of the monitor for 2,000 msec, followed by the computation task and answer choices for 5,000 msec.

Three task levels were set for the arithmetic problems as shown in Table 1 with the following expected times to solve the problems:

- Normal tasks were expected to be answered in 0.5 sec,
- Easy tasks, less than 0.5 sec, and
- Hard tasks, more than 0.5 sec.

Table 1: Level of calculation task.

Level	Contents
Easy	Addition of two numbers of three digits <i>without</i> carry-overs
Normal	Addition of two numbers of three digits <i>with</i> carry-overs
Hard	Multiplication of 3-digit and 2-digit numbers

The participants were instructed to press a key once to start the experiment. During the experiment, they were required to solve arithmetic problems one by one, and to gaze at one which matched with what they thought was the answer for the problem, among the four alternatives.

3.2 Overview of the Main Results

The EEG data for the period of 1500 msec before and 4500 msec after the presentation of the task were analyzed by using EEGLAB version 2019.0 and EEGLAB version 2019.1. The baseline was used for analysis. Suzuki et al. (Suzuki et al., 2021) specifically focused on the EEG data known as Fmθ (Yamaguchi, 2008) expressed at 67 Hz from the midline of the frontal lobe. They obtained the frequency spectra of F3 and F4 channels closest to the midline of the frontal lobe.

In this experiment, participants responded not by pressing buttons but by gazing in order to reduce the effect on the EEG as much as possible. Therefore, their answer status was analyzed from their gaze data. The participant calculates the question, then looks for the number that matches the answer, and stares at the one with the correct number. The sum of the time spent gazing at the correct number and the time spent gazing at the wrong number was calculated.

In the Easy and Normal conditions, the correct and wrong numbers were clear and the distribution characteristics were similar. The total time spent looking at the wrong number in one trial was often less than 0.5 seconds, and the task was viewed within 4.5 seconds after presentation. In Hard condition, the distribution of gazing at the wrong number and the correct number was similar, and it was difficult to determine the answer chosen by the participant from the gaze

data. These results indicate that the correct answer was given when the gaze was on the correct number for more than 0.5 sec, a feature observed in the Easy and Normal. A reading of 0.5 sec or less, but after 4.5 sec, was also considered a correct answer.

4 ANSWER SELECTION AND PUPILLARY DILATION

4.1 Answer Selection Time

The participant's task was to mentally calculate the answer to a given arithmetic problem. The problem was displayed in the upper center of the screen. The answer to that question was one of the four choices given in two rows and two columns at the bottom of the screen. It was assumed that after seeing the problem, the participant would complete this task by deriving an answer using mental arithmetic, finding a match among the four options, and staring at it. Based on this task achievement process, we devised a method to derive the answer selected by the participant from the recorded eye movement data.

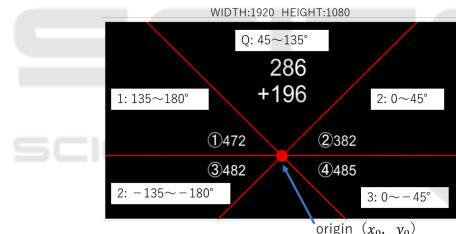


Figure 4: Angle from the center of the answer numbers.

Among the eye tracking data measured by the eye tracker, we analyzed those wherein the type of eye movement was "Fixation." The gaze data, which were recorded as two-dimensional data using the coordinates of the monitor (x, y), were converted to one-dimensional data as shown in Figure 4; a gaze point was represented as its angle θ from the center of the four answers denoted as (x_0, y_0) as follows:

$$\theta = \tan^{-1} \frac{y_0 - y}{x - x_0} \quad (-180^\circ \leq \theta \leq 180^\circ) \quad (1)$$

A participant's gaze was initially directed to the question and then on one of the answers s/he chose. It then directed participants to the area where the choices for the correct answer were presented. When the participant's gaze stayed on the answer area longer than 100 msec, the entry time was recorded as the answer selection time.

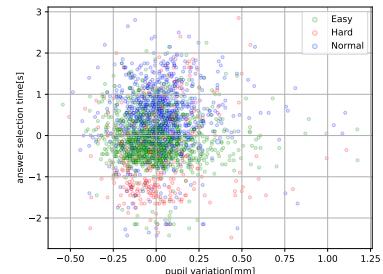


Figure 5: Difference from the median.

4.2 Pupil Diameter Variation

The pupil diameter data measured by the eye tracker was analyzed by linear interpolation using the eye movement type of Fixation. The baseline was defined as the average pupil diameter during the 500 ms immediately preceding the presentation of the tasks, and the pupil diameter data were calculated as the variation from the baseline (Tobii-AB, 2021).

The pupil diameter tended to contract significantly immediately after the task was presented (between 1~2 sec). This is thought to be a convergence reaction caused by near vision effect. Therefore, the pupil diameter variation was defined as the range from the minimum value during the 1~2 sec, when the congestion reaction was considered to have occurred, to the maximum value thereafter.

5 RESULT

The answer selection time and the pupil diameter variation were calculated for tasks of all participants that were judged to be correct. The median value for each participant was then calculated, and the difference between the answer selection time and the pupil diameter variation for each task and the median value for each participant was calculated. The results are shown in Figure 5. Five areas are identified in Figure 5 as follows:

- Area 1. Pupil diameter variation is more than average and answer selection time is above average.
- Area 2. Pupil diameter variation is below average and answer selection time is later than average.
- Area 3. Pupil diameter variation is less than average and answer selection time is below average.
- Area 4. Pupil diameter variation is above average and answer selection time is earlier than average.
- Area 5. Belonging to the ellipse with four points as vertices, where the pupil diameter variation is ± 0.1 mm, and the answer selection time is ± 0.6 sec.

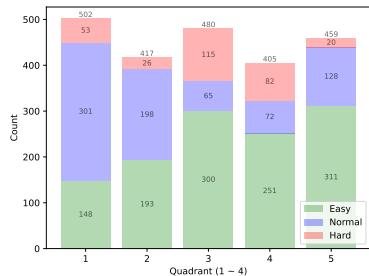


Figure 6: Quantity for each area.

The results of the count are shown in Figure 6. The number of trials for each condition estimated to be correct was 1203 for Easy, 764 for Normal, and 296 for Hard. The average values divided by the number of areas 5 were 240.6 for Easy, 152.8 for Normal, and 59.2 for Hard. In the Easy condition, Area 5 was the most common area, and Areas 3 and 4 were more common than average. The Easy condition exists mostly near the median of the participants. The difficulty level of the problems should have been higher than that of the Easy condition, so it can be said that this was the correct attitude to take. In addition, the change in pupil diameter tended to be larger, suggesting that the students were concentrating more on solving the problem than in the other conditions. In the Hard condition, Area 3 had the most trials and Area 4 had more trials than the average. Trials judged to be correct in the Hard condition, moved pupils' eyes to the answer numbers more quickly than in the other conditions, suggesting that they were not taking the task seriously. The degree of change in pupil diameter tended to be less than the average, suggesting that the participants were not taking the calculation seriously.

As shown in Figure 7, the results of Suzuki et al.'s analysis showed high amplitudes in the range of 6 to 7 Hz in the Normal condition, suggesting that Fmθ could be detected without problems. Pupil diameter variation was also higher in the Normal condition, suggesting that these two indicators are related.

6 TOWARD APPLICATION TO EFFECTIVE EDUCATION: RELATIONSHIP BETWEEN ARCS MODEL

In this section, we discuss how to apply these results towards effective education. One of the famous motivation models is the ARCS model which was proposed by Keller (Keller, 1983; Keller, 1987). According to ARCS model, learner's motivation is enhanced

by four categories of variables synthesis (Keller, 1987): 1) Attention, 2) Relevance, 3) Confidence, and 4) Satisfaction. Due to its high practicality, the ARCS model is used in a wide range of fields such as training design and teaching material development in companies, including educational places such as universities.

Based on the ARCS model, we focus on the category of confidence and satisfaction. In procedural tasks, the learners' behavior can be represented as below. Before the learner cannot learn the procedure, when the learner is presented a task, firstly they try to candidate the difficulty of the task. If the task expects the task to be easy, the learner will think that the task can be performed without difficulty. If not, the learner will think that it can be performed with difficulty. We regard this as the process of "candidate". On the other hand, the degree of agreement between the difficulty level felt when the task is actually completed and the expected difficulty level is directly related to the satisfaction level felt by the learner. We regard this as the process of "assessment".

Candidates and assessments can be associated with conflicts and satisfactions in the ARCS model. "*Candidates*" predict whether the learner will have the expectation that he or she will be able to do it, and as a result, the probability that the task will be successful. The success of a task is equivalent to the learner's successful experience. If the learner's successful experience leads to a psychological reward of "good to do", it will in turn lead to the learner's "*satisfaction*".

Table 2 represents the criterion of confidence or satisfaction. The table represents classification the participants' condition according to the match/mismatch between the L_t candidate when the task is presented and the L_t assessment after the task is executed. Let the candidate L_t be $L_{t,c}$ and the assessed L_t be $L_{t,a}$. Pattern A and pattern C are cases where the $L_{t,c}$ and $L_{t,a}$ do not match. Pattern A is $L_{t,c} < L_{t,a}$, though the candidate wrongly estimates the task-ease assessment. This is an opportunity to deny one's ability, so satisfaction is expected to be low. Pattern C is $L_{t,c} > L_{t,a}$, though the candidate wrongly estimated the ease of the task. This is an opportunity to feel the improvement of one's own ability, and as a result, satisfaction is expected to increase. Pattern B and pattern D are cases where the $L_{t,c}$ and $L_{t,a}$ match. Pattern B shows a successful experience with almost no motivation. Therefore, participants will only attain low satisfaction for high confidence, which means it is no surprise that the task is finished. Pattern D shows the failure experience that difficult tasks could not be executed after all. Therefore, although the confidence

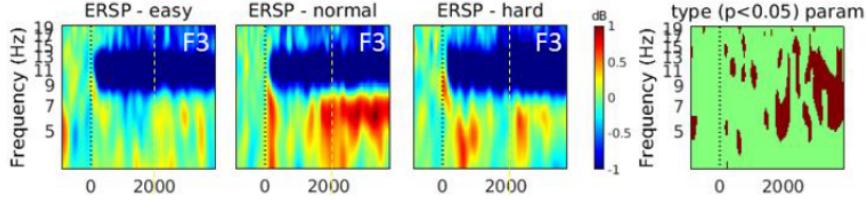


Figure 7: The results of EEG analysis by Suzuki et al. The results of the time-frequency analysis for each condition are shown, as well as the intervals where a significant difference (without multiple comparison correction) was obtained at the 5% level between the conditions. The color of the figure means that the higher the power compared to the baseline, the redder the color, and the lower the color, the bluer the color. The horizontal axis of the figure is time (msec) and the vertical axis is frequency (Hz).

Table 2: Categorization of candidate/assessment difficulty Level and participants' condition.

		assessment	
		high	low
candidate	high	Pattern D: feel difficult, give up to solve	Pattern C: feel difficult, can solve with ease
	low	Pattern A: not motivated, feel difficult to solve	Pattern B: not motivated, can solve with ease

is low, there will be no decrease in satisfaction due to the experience of failure.

One of the similar tasks is the score reading process. As shown by Nakahira and Kitajima (Nakahira and Kitajima, 2017), the reading recognizes and reproduces the pitch, interval, note value, and motif after perceiving the representation. Of these, for pitch, interval, and note value, musical information is acquired while selecting one of the following two strategies. (1) Matching of memorized representation and perceptual information, (2) Judgment of note type and note value according to procedure based on partially memorized reference note.

Participants who are accustomed to score reading, memorize almost all musical note representations and use them on a regular basis. Therefore, it is faster to read the note type and pitch by adopting the strategy (1). In the case of a complicated score or participants who are not accustomed to reading notes, it is necessary to adopt strategy (2) to read the pitch, interval, and note value. If the participants adopt strategy (1), they can understand the score structure in a short time. From the viewpoint of playing an instrument, they will think that the score is easy to play. However, it will often be considered a dry task. When adopting strategy (2), it takes a long time to understand the structure of the score. But from the viewpoint of playing an instrument, it may be difficult to play. In that case, participants will give up playing the music or practice playing with the knowledge that it will take time. In particular, in the case of (2), there is a possibility that the partial completion can be used to judge the difficulty level in order to provide music at a level that does not cause participants to quit.

7 CONCLUSION

In this study, we analyzed the relationship between the difficulty of arithmetic using pupil diameter data and eye movement data and the state of work. We designed a plane view centered on the answer confirmation time estimated from the eye movement and ΔA . On the plain, we plotted biometric information to categorize the condition of the participants corresponding to the 5 areas which set the vicinity of the origin and the four quadrants for the two axes.

As a result, both T_c and ΔA were characterized by the difference in labeled L_t . The values of both T_c and ΔA increased in the order of Hard, Easy, and Normal modes. From the scatter plot, we found that the data for the low difficulty tasks were most concentrated in the Areas 3 and 5, the data for standard difficulty tasks were concentrated in the Areas 1 and 2, and the data for high difficulty tasks were mostly concentrated in the Areas 3 and 4. These suggested that both T_c and ΔA , as biometric information, were suitable quantities for estimating the states of the participants' confidence and satisfaction. Based on these results, our future tasks would be to improve the accuracy of estimation of participants' conditions for any given tasks.

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