Interpretable Deep Learning for Marble Tiles Sorting

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Keywords: Machine Vision, Deep Learning, Dolomite Tile Sorting, Interpretable Machine Learning.

Abstract: One of the main problems in the final stage of the production line of ornamental stone tiles is the process of quality control and product classification. Successful classification of natural stone tiles based on their aesthetical value can raise profitability. Machine learning is a technology with the capability to fulfil this task with a higher speed than conventional human expert based methods. This paper examines the performance of 15 convolutional neural networks in sorting dolomitic stone tiles as far as models' accuracy and interpretability are concerned. For the first time, these two performance indices of deep learning models are studied massively for the industrial application of machine vision based marbles sorting. The experiments revealed that the examined convolutional neural networks are able to predict the quality of the marble tiles in an industrial environment accurately in an interpretable way. Furthermore, the DenseNet201 model showed the best accuracy of 83.24%, a performance, which is supported by the consideration of the appropriate quality patterns from the marble tiles' surface.

1 INTRODUCTION

Natural stones, like granites, sandstones, marbles and basalts were used for centuries as the main building materials. Apart from the endurance of a rock type, the aesthetic was also an important factor for choosing a rock over the other. Although modern building materials and technology have replaced natural stones they are still used mainly for decoration, and their market share is rising. These ornamental rocks are quarried in blocks, cut into slabs from which the final tiles are manufactured. The last step of the tile production line, before shipping, is the classification of the tiles, which is still done mainly manually by experts. The main factor that needs to be considered, when classifying natural rock tiles is the number of visible cracks and impurities, which change the overall look of the product. The absence

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of cracks and impurities is usually adding value to the quality, and therefore its market price, but is not always the rule. This delicate part of the production line is time consuming and very subjective. This results in misclassification of the final product and thus raising the production cost. Moreover, the number of experts that can efficiently sort the marble tiles is decreased constantly. The use of machine learning (ML) and computer/machine vision (CV/MV) can automate the process of quality control and classification, leading to the reduction of production cost.

One of the first attempts to classify marble slabs by using Neural Networks (NN) was made in 1995, when a multilayer perceptron (MLP) with Backpropagation (BP) was used (Hernandez et al., 1995). In 1999 the Learning Vector Quantization (LVQ) NN was used for the clustering and classification of marble slabs according to their

DOI: 10.5220/0010517001010108

In Proceedings of the 2nd International Conference on Deep Learning Theory and Applications (DeLTA 2021), pages 101-108 ISBN: 978-989-758-526-5

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Ouzounis, A., Sidiropoulos, G., Papakostas, G., Sarafis, I., Stamkos, A. and Solakis, G. Interpretable Deep Learning for Marble Tiles Sorting.

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information (Martínez-Cabeza-de-Vacatexture Alajarín & Tomás-Balibrea, 1999). In 2005 a classification rate of 98.9% was achieved for classifying the "Crema Marfil Sierra de la Puerta" marble slabs into three categories by using MLP and BP (Martínez-Alajarín et al., 2005). In 2010 functional neural networks were tested in order to classify granite tiles (Lopez et al., 2010). Convolutional Neural Network (CNN) approaches were first applied on granite tile classification in 2017. In this approach, small patches of images taken from granites were used in order to augment the dataset and a majority voting procedure was taken into account (Ferreira & Giraldi, 2017). In 2020, the VISUAL Geometry Group 16 (VGG16) (Simonyan & Zisserman, 2015) CNN was used to identify images of peridotite, basalt, marble, gneiss, conglomerate, limestone, granite and magnetite quartzite with a recognition probability greater than 96%. In the case of multi-type hybrid images the recognition probability was greater than 80% (Liu et al., 2020). In 2021, machine learning algorithms (Sidiropoulos et al., 2021) were tested on the same dataset used in the current study. Original RGB images and images produced by 18 texture descriptors on a dataset provided by Solakis Marble S.A. were used. This former research is extended in this study, by examining the performance of CNN models on the same dataset in terms of accuracy and interpretation of their decisions. For this purpose, 15 CNNs were tested on RGB digital images acquired in an industrial environment in order to find the best performing model.

The main contribution of this study can be summarized as follows:

1. A massive comparison of 15 CNN models was made on real world data originating from the production line of natural stone tile production.

2. By using heatmaps the results of the tiles' classifications were interpreted for the first time.

This paper is organized as follows: In section 2, the dataset and the methodology used are described. Section 3 presents the experiments and the corresponding results. Finally, section 4, discusses the results and delineates the future research.

2 MATERIALS AND METHODS

2.1 The Dataset

The stone tiles, sized 30x60 cm (Figure 1), which were used to compile the dataset, were delivered by Solakis Antonios Marble S.A. (*Solakis*, n.d.). This

decorative material is cut from slabs exclusively quarried in the village of Kokkinoghia, in Drama, in North-east Greece. According to the EN 12440 (Laskaridis et al., 2015) this ornamental stone is known as Kokkonoghia Grey but is usually referred to with the name Grey Lais. This ornamental stone is a carbonate metamorphic rock known as dolostone or dolomite with a chemical composition consisting of 94% of the mineral dolomite CaMg(CO₃)₂ and 6% of the mineral calcite CaCO₃ (Laskaridis et al., 2015). Dolomites are often referred to as marbles in the industry. The term marble tile will also be used throughout this study. The digital images of the tiles were acquired by using a low cost experimental setup in an industrial environment described briefly in section 2. This setup delivered 986 digital images from the polished side of the tiles with a resolution of 1500x725 pixels compressed in the jpg format.



Figure 1: Representative tiles of (a) Class A: Lais G Extra, (b) Class B: Lais GA and (c) Class C: Lais GM.

Specialised workers classified the samples into three classes based on their decorations. Cracks and impurities are unwanted structures for this type of marble. Class A included 697 samples, class B was comprised of 133 samples and in class C 156 samples were available. Class A, B and C have specific market names, which are Lais G Extra, Lais GA and Lais GM respectively (*Solakis*, n.d.). Because of the dataset been imbalanced, class A was reduced to 200 images randomly. This resulted in the final dataset size of 489 (class A: 200 samples, class B: 133 samples and class C: 156 samples).

2.2 Methodology

This study was completed in six steps. The pipeline is depicted in Figure 2.



Figure 2: Pipeline of the methodology applied. Step 4 does not depict a specific CNN. The example tile is classified as class B.

2.2.1 Digital Image Acquisition

The original RGB digital images, from which the dataset was compiled, were acquired by a device consisting of a mechanical roller table, a digital camera and a lighting setup. The roller table was fed manually with the labelled marble tiles which were photographed on the move by a MV_CA050-10GM/GC digital camera equipped with a MVL-MF0824M-5MP lens at a 90 cm distance. L.E.D. arrays were used as a light source inside a diffusion box.

2.2.2 Dataset Preprocessing

In order to feed the CNNs under examination, the original RGB digital images, had to be preprocessed. In the second step (Figure 2), noise from the surrounding environment was removed, the tile was extracted and the image was downsized. This was achieved by converting the color space from RGB to HSV followed by a Gaussian blur. Next, a threshold was applied using a specific range of values followed by the application of a contour detection algorithm filtering out the vertical and horizontal lines. The resulting four lines were used to determine the corners of the rectangle tile. Finally, a perspective

transform was applied to align and to resize the tiles to a 400x700 pixel vector.

CNNs have their own specific requirements for the size of the inputs that they can handle. Therefore the digital images had to be downsized to meet these specifications. This was done in step 3 where the preprocessed images were downsized to 224x224 pixels.

2.2.3 Convolutional Neural Networks

CNNs are essentially deep neural networks (DNNs) specially developed for image classification. The extensive use of DNNs in real world problems was delayed for many years because high computational power needed was not available. The progress in computer hardware and especially in Graphical Process Units (GPUs) of the recent years allowed the usage of complex DNNs for numerous real world problems encountered in the industry. In step 4 of the proposed methodology, 15 pretrained CNNs using the ImageNet database, available from the Keras library (Chollet, 2015), were used to build the models using the dataset of the 489 digital images of the dolomite tiles. The pretrained models based on 15 CNNs were used, namely, DenseNet121 (DN121), DenseNet169 (DN169), DenseNet201 (DN201) (Huang et al., 2018)., InceptionResNetV2 (IRNV2) (Szegedy et al., 2016), MobileNet (MN) (Howard et al., 2017), MobileNetV2 (MNV2) (Sandler et al., 2019), ResNet101 (RN101), ResNet152 (RN152), ResNet50 (RN50), (He et al., 2015), ResNet101V2 (RN101V2), ResNet152V2 (RN152V2), ResNet50V2 (RN50V2), VGG16, VGG19 (Simonyan & Zisserman, 2015) and Xception (XC) (Chollet, 2017).

These aforementioned pretrained models were fine-tuned applying the following modifications:

1. The original output layer of the NN was removed.

2. The model's weights were frozen.

3. A Global AveragePooling2D was added, followed by a Dropout layer with a 20% frequency rate to avoid overfitting.

4. A Dense output layer using the softmax activation function for the three quality classes was added

5. The output layer was trained with the training and validation set of the current fold

6. The weights for only a part of the network's layers were unfrozen.

7. The unfrozen weights were trained again, with the training and validation sets

It should be noted that the Adam optimizer was used with a learning rate of 1e-5 and the categorical crossentropy function as the loss. Moreover, the backbone of all the models was kept the same, without any changes to the model itself, keeping the original input shape of three channel images with a size of 224x224. Additionally, the modifications 6 and 7 are part of the fine-tuning of the transfer learning. These modifications were applied in order to find the number of trained layers that yielded the best performance for the model. Moreover, the fine-tuning was done for each additional quarter of the network's layers, meaning that we tested the network's performance by training 25% of the layers, 50%, 75% and 100%. All models were trained with default parameters and the number of layers used are summarized in Table 1.

Table 1: Layers used to train each model.

Model	DN121	DN169	DN201	IRNV2	MN
layers	199	595	707	572	63
Model	MNV2	RN101	RN101V2	RN152	RN152V2
layers	71	345	377	103	413
Model	RN50	RN50V2	VGG16	VGG19	XC
layers	175	88	19	16	132

A 10-fold cross validation technique was applied for the evaluation of the CNNs, which were trained for 50 epochs. The dataset was split initially to 90% for training and 10% for testing, where the training set was split again by 90% for training and 10% for validation. The python programing language was used to implement the code by using the Tensorflow library (Abadi et al., 2015), for training the models, and the machine learning library sklearn (Pedregosa et al., 2018) for the evaluation. For the evaluation of the models' performance, the following metrics were used: accuracy, precision, recall and f1-score.

2.2.4 Gradient-weighted Class Activation Mapping

Until recently, Neural Networks were handled as black boxes. The results from classification and regression tasks were impossible to interpret. Gradient-weighted Class Activation Mapping (Grad-CAM) (Selvaraju et al., 2017) is an algorithm, which outputs heatmaps of the images used for the training of the CNNs. Heatmaps highlight, using colors, the areas where the model is focusing on for extracting the decisions, thus allowing the interpretation of the results. Warm colors indicate important, whereas colder colors indicate less important areas for the model's decisions. Areas not marked by any color were not taken into account during the prediction process. In the fifth step of this study, Grad-CAM is applied for the interpretation of the results. In the sixth step, the heatmaps' output was interpreted in order to validate the classification's reliability

3 EXPERIMENTS

3.1 Results and Metrics

An overview of each metric versus the fine-tuned model used can be examined in the boxplots of



Figure 6: F1 for the 15 CNNs.

Figures 3-6. Each model's metrics are summarized in Table 2.

Model	accuracy	precision	recall	f1
DenseNet121	79.98%	80.11%	79.14%	79.09%
DenseNet169	82.84%	83.97%	81.56%	81.83%
DenseNet201	83.24%	82.98%	82%	82.04%
InceptionResNetV2	79.77%	79.87%	79.31%	79.05%
MobileNet	82.23%	82.27%	81.40%	81.36%
MobileNetV2	80.79%	80.90%	80.37%	80.20%
ResNet101	81.80%	81.80%	80.97%	80.86%
ResNet101V2	80.59%	80.75%	79.93%	79.85%
ResNet152	82.63%	82.59%	81.39%	81.46%
ResNet152V2	81.60%	80.59%	80.42%	80.25%
ResNet50	79.96%	79.96%	78.97%	78.83%
ResNet50V2	80.57%	80.23%	79.05%	79.12%
VGG16	79.76%	80.25%	79.10%	78.96%
VGG19	80.38%	80.59%	79.47%	79.43%
Xception	78.73%	79.14%	77.88%	77.98%

Table 2: Results of the experiments.

DN201 had the best overall performance: accuracy =83.24%, precision=82.98, recall=82.00% and f1-score=82.04%. DN169 achieved better precision with a value of 83.97%, almost 1% better than the DN201, but had an outlier. XC performed worst with accuracy=78.73%, precision=79.14, recall = 77.88% and f1-score = 77.98%. The boxplots show that the DN201 is the most robust as it has the highest median

for all metrics excluding the precision. Also the dispersion is comparable low. Other models like MNV2 and RN101 have a lower dispersion but outliers are present. All models have many outliers except DN201, IRNV2, MN, RN101V2, RN152, RN152V2 and RN50V2.

3.2 Interpretation of the Heatmaps

Heatmaps of all models, classifying successfully three different sample tiles belonging to class A, B and C are depicted in Figure 7, 8 and 9 respectively. As it can be observed each model is not focusing on the exact same area in order to classify each tile.

This confirms that each CNN is working in a different way.

The probability of the correct classifications is >99% in all than five cases: RN101V2 classified sample 1 to class A (Figure 7) with a probability of 93.7%. DN121 classified sample 2 to class B (Figure 8) with a probability of 80.32%. MN, RN101 and RN50 classified sample 3 to class C (Figure 9) with a probability of 97.44%, 98.9% and 74.31% respectively.





Figure 8: Heatmaps for the same marble tile (sample 2) successfully classified by all CNNs as class B.



Figure 9: Heatmaps for the same marble tile (sample 3) successfully classified by all CNNs as class C.

By comparing the heatmaps (Figure 10) of the three models representing the best (DN201, f1=82.04%), the mean (RN101, f1=80.86%) and the worst (XC, f1=77.98%) f1-score, the following qualitative interpretation for the classification can be made: In sample 1, DN201, RN101 and XC successfully spotted the areas with alternating dark and light colored lineation, which define class A. The best classification metrics of DN201 can be attributed to that it is not focusing on a specific structure of the tile but rather draws conclusions from the whole tile in class A. In sample 2, light colored intruding veins and intersecting cracks were focused on, which define class B. In sample 3, DN201 focused on the dark inclusions, which characterizes class C. RN101 and XC only focus partially (light blue color) on these areas leading to lower metrics.



Figure 10: Heatmaps of the three representative CNNs, correctly classifying three different marble tiles (sample 1-3).

In Figure 11 the heatmaps of DN201, RN101 and XC are compared on tiles that were not successfully classified by all models. In this comparison, the first

column represents the heatmaps of the DN201, which successfully classified the samples, whereas the second and the third column shows the heatmaps of the models, RN101 and XC, which misclassified the same samples. Table 3 lists the probability of each classification

Table 3: Model's classifying probability of samples.



Figure 11: Heatmaps of the three representative CNNs classifying four different marble tiles (samples 4-7) with correct and incorrect classification results.

Sample 1 was correctly classified by DN201 to class A with a probability of 97.15% by focusing on a broader area where the alternating dark and light colored lines are present. RN101 and XC incorrectly classified the samples to class C with a lower probability, 78.86% and 51.29% respectively, focusing on discreet areas of dark lines and misinterpreting them as spots.

Sample 2 was classified successfully as class A by DN201 with a probability of 97.33%. RN101 incorrectly classified the sample as class B with a probability of 56.41%, focusing on the light colored intruding veins and XC classified it incorrectly as class C, with a probability of 97.44%, by focusing on the dark colored intruding veins.

Sample 3 was classified correctly as class B by DN201 with a probability of 96.37%. RN101 and XC models classified incorrectly the sample as class C by focusing on the dark lines misinterpreting them as dark spots with probabilities 79.09% and 89.22% respectively.

Sample 4 was classified correctly as class C by DN201 with a probability of 79.81%. Both RN101 and XC incorrectly classifies sample 4 as class A with a probability of 84.16% and 100% by failing to focus on the dark spots.

4 DISCUSSION

This paper tested the effectiveness of using pretrained CNNs in order to classify natural dolomite rock tiles. The results showed that this type of NN performs better than conventional classifiers like Support Vector Machine (SVM) (Cortes & Vapnik, 1995), K-Nearest Neighbors (KNN) (Altman, 1992), Random Forest (RF) (Breiman, 2001), Multilayer Perceptron (MLP) (Popescu et al., 2009), Logistic Regressor (Webb et al., 2011), Stochastic Gradient Descent Classifier (SGD) (Ruder, 2017) and XGBoost Classifier (XGB) (Chen & Guestrin, 2016) when trained to discriminate dolomite tiles based on their texture (Sidiropoulos et al., 2020).

Model DN201, using 707 layers, performed with f1-score 82.04% trained with RGB images, whereas the the XGBoost classifier trained by XCS-LBP texture descriptors, achieved a performance of f1-score 65.06% (Sidiropoulos et al., 2020).

By using Grad-CAM, it was possible to track the areas on the surface of the tiles, which the model focused on, in order to classify the tiles. This added reliability to the results. The model build, focused on the alternating light and dark colored banding for identifying class A. Class B was recognized by the model focusing on the light colored veins cutting the banding in different angles. Class C was classified by focusing on the dark spots.

In the next step of this research the best performing model (DN201) will be reevaluated using an augmented dataset using new techniques such as MixUp (Zhang et al., 2018) and CutMix (Yun et al., 2019). Furthermore the possibility of using a combination of the CNNs studied in this paper to compile an ensemble (Zhou, 2009) will be studied.

In the final stage of this project the resulting model will be integrated into an automation system at the facilities of Intermek Industrial & Trading Ltd. This integration will permit the real-time performance analysis of the proposed tiles sorting model under industrial conditions.

ACKNOWLEDGEMENTS

This research has been co-financed by the European Union and Greek national funds through the Operational Program Competitiveness, Entrepreneurship and Innovation, under the call RESEARCH – CREATE – INNOVATE (project code: T1EDK-00706).

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