Analysing Clustering Algorithms Performance in CRM Systems

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Abstract: Customer Relationship Management technology plays an important role in business performance. The main problem is the extraction of valuable and accurate information from large customers' transactional data sets. In data mining, clustering techniques group customers based on their transaction’s details. Grouping is a quantifiable way to analyse the customers’ data and distinguish customers based on their purchases. Number of clusters plays an important role in business intelligence. It is an important parameter for business analysts. In this paper the performance of K-means and K-medoids algorithm will be analysed based on the impact of the number of clusters, number of dimensions and distance function. The Elbow method combined with K-means algorithm will be implemented to find the optimal number of clusters for a real data set from retail stores. Results show that the proposed algorithm is very effective when customers need to be grouped based on numerical and nominal attributes.

1 INTRODUCTION

Customer Relationship Management (CRM) technology is a mediator between customer management activities and business performance (Mohammed et al, 2014). Customer Segmentation gives a quantifiable way to analyse the customer data and distinguish the customers based on their purchase transactions (Sarvari et al, 2016). Customers can be grouped into different categories for which the marketing people can employ targeted marketing and thus retain the customers increasing the business performance. Once the customers are clustered, rules can be generated to increase business performance. Data mining is the process of extracting useful information from large volumes of data. Different techniques use statistical, mathematical, artificial intelligence and machine learning as analysing techniques (Palmer et al,2011). Its predictive power comes from unique design by combining techniques from machine learning, pattern recognition, and statistics to automatically extract concepts, and to determine the targeted interrelations and patterns from large databases. Organizations get help to use their current reporting capabilities to discover and identify the hidden patterns in databases. The extracted patterns from the database are then used to build data mining models and can be used to predict performance and behaviour with high accuracy.

Descriptive and Predictive data mining are the most important approaches that are used to discover hidden information (Coenen, 2004; Sondwale, 2015). Clustering is one of the most important techniques of the descriptive model. It finds a useful application in CRM where large amount of customer data is dealt (Ngai et al, 2009). Clustering technique in data mining produces clusters for the given input data where data in one cluster is more similar when compared to data in other clusters. The similarity is measured in terms of the distance between the data (Madhulatha, 2012). The different ways in which clustering methods can be compared are partitioning criteria, separation of clusters, similarity measures and clustering space. Clustering algorithms can be categorized into partition-based algorithms, hierarchical-based algorithms, density-based algorithms and grid-based algorithms. These methods vary in: (a) the procedures used for measuring the similarity (within and between clusters), (b) the use of thresholds in creating clusters, (c) the way of clustering, that is, whether they allow objects to belong to strictly to one cluster or can belong to more clusters in different degrees and the structure of the algorithm (Shah et al, 2015), (Lico, 2017). Widely used partitioning clustering methods are K-Medoids and K-Means.
Table 1: Clustering Algorithms.

<table>
<thead>
<tr>
<th>Partition-based algorithms</th>
<th>Hierarchic al-based algorithms</th>
<th>Density-based algorithms</th>
<th>Grid-based algorithms</th>
</tr>
</thead>
<tbody>
<tr>
<td>K-Means</td>
<td>Agglomerative (BIRCH, CHAMAL, EON)</td>
<td>DBSCAN</td>
<td>STING</td>
</tr>
<tr>
<td>K-Medoids (PAM, CLARA)</td>
<td>Divisive</td>
<td>DENCLUE</td>
<td>CLIQUE</td>
</tr>
</tbody>
</table>

In the paper K-Means algorithm is used for clustering. The basic requirement of K-Means clustering is that taking the number of cluster as ‘k’ from the user initially. A mean value as a representation of the cluster is based on similarity of the data items in a cluster. The mean or centre point of the cluster is known as ‘centroid’. Centroid is a value which can be find out through the mean of related points. K-means algorithms simple and have high speed access to databases on very large scales (Kalra et al, 2018).

K-medoids clustering is a variant of K-means that is more robust to noises and outliers. Instead of using the mean point as the centre of a cluster, K-medoids use an actual point in the cluster to represent it. Medoid is the most centrally located object of the cluster, with minimum sum of distances to other points (Han, 2011).

Several methods exist to identify the optimal number of clusters for a given dataset, but only some of them provide reliable and accurate results, such as Elbow method, Average Silhouette method and Gap Statistic method (Tripathi et al. 2018) (Babić et al, 2019) (Yan et al, 2007).

For a well-distributed data set, it is observed that the mean cluster density decreases with the increase number of clusters in a non-linear fashion. The resulting graph looks similar to that of the graph obtained in Elbow method wherein the decrease in mean cluster density is rapid when K is less than the optimal value and gradually decreases as it nears the optimum number of clusters, after which the gradient becomes almost constant or the graph changes direction. This region is known as the “Elbow” region. Amongst the points in the elbow region lies the optimum number of clusters. Sometimes, the elbow region contains a high range of values. In this scenario, coupling this algorithm with pre-existing methods such as the Average Silhouette method or any of the available methods will provide the required output (Nanjundan et al, 2019).

Cluster variation, execution time and number of iterations are evaluated based on number of clusters for 2 and 5 attributes for Euclidian and Manhattan distances. Elbow method combined with K-means is used for finding optimal number of clients’ clusters. The main issue of the paper is to find the most appropriate number of clients groups of a retail department store based on their annual purchases and quantities. Weka and Python are used as data analytics tools.

The rest of the paper is organized in the following: in Section 2 we describe the customer grouping process and clustering algorithms. In section 3 we implement clustering algorithms on a real dataset and their performance is analysed. In Section 4 we compare the clustering results obtained by clustering algorithms. Finally, conclusions and future works are described in sections 5 and 6.

2 CLUSTERING

Clustering is an unsupervised classification where there are no predefined classes. The data in the data set are assigned to one of the output class depending upon its distance to other data. The data within each class form a cluster. The number of clusters is equal to the number of output classes. The clustering technique produces clusters in which the data inside a cluster has high intra class similarity and low inter class similarity. Clustering is mainly classified into hierarchical and partitioning algorithms. The hierarchical algorithms are further sub divided into agglomerative and divisive. Agglomerative clustering treats each data point as a singleton cluster and then successively merges clusters until all points have been merged into a single cluster. Divisive clustering treats all data points in a single cluster and successively breaks the clusters till one data point remains in each cluster. Partitioning algorithms partition the data set into predefined k number of clusters (Datanovia, 2021).

Clustering is used to group the clients based on transaction data. K-Means and K-Medoids are still the most used algorithms for clustering because of
their simplicity. Anyway, many challenges raise in the use of these algorithms such as: a) identifying the right number of clusters, b) the metrics to be used, c) the performance for high-dimension data, d) the local nature of the algorithms. This issues need to be addressed to improve the performance of these algorithms.

### 2.1 K-means Algorithm

The K-means algorithm defines the centroid of a cluster as the mean value of the points within the cluster. First, it randomly selects k objects in D, each of which initially represents a cluster mean or centre. Remaining objects are assigned to the clusters to which they are the most similar, based on the Euclidean distance between the object and the cluster mean. Then the K-means algorithm iteratively improves the within-cluster variation. For each cluster, a new mean is computed using the objects assigned to the cluster in the previous iteration. All the objects are then reassigned using the updated means as the new cluster centres. The iterations continue until the assignment is stable, that is, the clusters formed in the current round are the same as those formed in the previous round (Han et al, 2011). The within-cluster variation can be calculated from the formula below:

$$E = \sum_{i=1}^{k} \sum_{p \in C_i} \text{dist}(p, c_i)^2$$ (1)

In this formula, k is the number of clusters, p are the objects in the cluster Ci and ci is the centroid of cluster Ci. The aim is to lower the variation E and to make the clusters as separate as possible (Sondwale, 2015).

The steps in K-means algorithm are as follows:

1. Initialize centres for k clusters randomly
2. Calculate distance between each object to k-cluster centres using the formula given by Eq. 1
3. Assign objects to the nearest cluster centre
4. Calculate the centre for each cluster as the mean value of the objects assigned to it
5. Repeat steps 2 to 4 until the objects assigned to the clusters do not change.

In this the assignment of objects to k clusters depends on the initial centres of the clusters. The output differs if the initial centres of the clusters are varied. It is not suitable to discover clusters with non-elliptical shapes because the objects are scattered around the centre of the clusters.

### 2.2 K-medoids Algorithm

Instead of taking the mean value of the objects in a cluster as a reference point, we can pick actual objects to represent the clusters, using one representative object per cluster. Remaining objects are assigned to the clusters where the representative objects are the most similar. The partitioning method is then performed based on the principle of minimizing the sum of the dissimilarities between each object p and its corresponding representative object. The absolute-error criterion is defined as:

$$E = \sum_{i=1}^{k} \sum_{p \in C_i} \text{dist}(p, o_i)$$ (2)

where E is the sum of the absolute error for all objects p in the data set, and oi is the representative object of Ci. This is the basis for the k-medoids method, which groups n objects into k clusters by minimizing the absolute error (Sondwale, 2015).

Steps of K-Medoids algorithm are:

1. Initialize: randomly select k of the n data points as the medoids
2. Assignment step: Associate each data point to the closest medoid.
3. Update step: For each medoid m and each data point o associated to m swap m and o and compute the total cost of the configuration (that is, the average dissimilarity of o to all the data points associated to m). Select the medoid o with the lowest cost of the configuration.

Repeat alternating steps 2 and 3 until there is no change in the assignments.

### 2.3 The Elbow Method

The Elbow method is based on the observation that the increased number of clusters trend to reduce the sum of within-cluster variance of each cluster. More clusters allow one to capture finer groups of data objects that are more similar to each other. However, the marginal effect of reducing the sum of within-cluster variances may drop if too many clusters are formed, because splitting a cohesive cluster into two
gives only a small reduction. Consequently, the right number of clusters is the turning point in the curve of the sum of within-cluster variances regarding the number of clusters.

Technically, for a given positive number $k > 0$, $k$ clusters are formed on the data set using a clustering algorithm and the sum of within-cluster variances is calculated. The curve of variances based on $k$ is plotted. The first (or most significant) turning point of the curve suggests the “right” number of clusters (Sondwale, 2015).

Steps of Elbow algorithms are:
1. Compute clustering algorithm for different values of $k$.
2. For each $k$, calculate the total within-cluster sum of square (wss).
3. Plot the curve of wss according to the number of clusters $k$.
4. The location of a bend (knee) in the plot is generally considered as an indicator of the appropriate number of clusters.

### 3 IMPLEMENTATION OF K-MEANS AND K-MEDOIDS IN A REAL DATASET

#### 3.1 Analyses of K-means and K-medoids

A real dataset with the annual sales of 13,260 clients were used. Annual sales and quantities were filtered and grouped. Before applying clustering algorithms, the data were normalized because if different components of data (features) have different scales, then derivatives tend to align along directions with higher variance, which leads to poorer/slower convergence. In our case we want our features to be treated equally. Both algorithms were applied in different scenarios. First K-Means algorithm was applied on dataset using Weka tool. It was executed for different number of clusters. Euclidian and Manhattan distances are analysed. Three other nominal attributes were added to the data (city, age and gender of the client). K-means was executed again with new dimensions. The values of within-cluster cluster variation, number of iterations and the time of the execution were measured depending of number of clusters.
It can be seen from the results that K-Means performs really good with two numerical values and Euclidian distance but the performance deteriorates when Manhattan distance is used. With the additions of nominal attributes and the increased number of dimensions the performance for both Euclidean and Manhattan distances measures is not very different from one another. It yields that K-means is very good when continuous numerical values attributes and Euclidian Distance are used. With the addition of categorical or nominal attributes K-means performance deteriorates and there is little impact from the distance of the measure used.

It is observed that when Manhattan distance is used, the number of iterations and execution time is decreased. It is argued from the fact that K-means algorithm uses the median and not the mean as a centroid when Manhattan distance is used.

### 3.2 Finding the Optimal Number of Clusters

The aim of the study is to categorize clients based on their purchases and quantities. Only these two attributes will be used for clustering. From section 3.1 it was concluded that K-means with the Euclidian distance performs well in this case. The challenge remains in finding the optimal number of clusters. The Elbow method was used to find the optimal number of clusters. This number represents the best within cluster variance and clusters are the far from each other. Python language was used to calculate this value as below:

From the plot, it can be seen that the optimal number of cluster is 4. K-Means and K-Medoids will be run with the predefined 4 number of cluster. For K-
Means, Weka is used as an analytics tool. For implementing K-Medoids, Python will be used.

4 COMPARISON OF ALGORITHMS

For the predefined number of clusters equal to 4, the results from K-medoids algorithm are shown in table 2 and results from K-means algorithm are shown in table 3. Different results are produced by running K-means algorithm using the Euclidian distance and the means and K-Medoids ones using Manhattan distance and the medoids. In section 3.1 resulted that Euclidian distance is better when 2 continuous numeric values were used. From the analyses of the clustered data by both algorithms, it was noticed that the segmentation done by K-means is more efficient for our retail dataset.

Interesting data were obtained by the analysis. It was observed that 10% of the clients make 43.33% of the purchases. There is a big amount of clients (87%) that make only 35% of the total purchases. Another interesting information that need to be exploited is that quantities for 10% of the clients are very similar to quantities for 87% of the clients although total purchases are different.

5 CONCLUSIONS

The usage of Clustering in CRM systems is a very interesting and effective technique for customer grouping and can produce very interesting information. It was shown that K-means is very effective when customers need to be segmented based on their purchase and quantity values. The algorithm shows great performance when used for continuous numerical values. Usage K-means combined elbow method together can be very useful in this type of applications.

6 FUTURE WORK

The study will be carried on in cases when the analyses need to be done with multiple dimensions of the data. Another interesting future work will be the usage of data mining classification techniques in CRM systems in order to be able not only to analyse customer behaviour but also to predict it. The final step would be to integrate Clustering and Classification algorithms in BI systems in order to make it simpler for marketing and sales team to use them.

<table>
<thead>
<tr>
<th>Row Labels</th>
<th>Sum of Purchases</th>
<th>Sum of quantities</th>
<th>Purchase Percentage on Total</th>
<th>Number of Clients</th>
<th>Number of Clients Percentage on the Total</th>
</tr>
</thead>
<tbody>
<tr>
<td>0</td>
<td>487373059</td>
<td>56301</td>
<td>30.93%</td>
<td>320</td>
<td>2%</td>
</tr>
<tr>
<td>1</td>
<td>386956118</td>
<td>54723</td>
<td>24.56%</td>
<td>3043</td>
<td>23%</td>
</tr>
<tr>
<td>2</td>
<td>517144745</td>
<td>63574</td>
<td>32.82%</td>
<td>1215</td>
<td>9%</td>
</tr>
<tr>
<td>3</td>
<td>184132724</td>
<td>41907</td>
<td>11.69%</td>
<td>8682</td>
<td>65%</td>
</tr>
<tr>
<td>Grand Total</td>
<td>1575606646</td>
<td>216505</td>
<td></td>
<td>13260</td>
<td></td>
</tr>
</tbody>
</table>

Table 2: Results from K-Medoids algorithm for 4 clusters.

<table>
<thead>
<tr>
<th>Row Labels</th>
<th>Sum of Purchases</th>
<th>Sum of quantities</th>
<th>Purchase Percentage on Total</th>
<th>Number of Clients</th>
<th>Number of Clients Percentage on the Total</th>
</tr>
</thead>
<tbody>
<tr>
<td>cluster0</td>
<td>552876375</td>
<td>72781</td>
<td>35.09%</td>
<td>1386</td>
<td>10%</td>
</tr>
<tr>
<td>cluster1</td>
<td>336678950</td>
<td>45240</td>
<td>21.37%</td>
<td>269</td>
<td>2%</td>
</tr>
<tr>
<td>cluster2</td>
<td>556281399</td>
<td>81934</td>
<td>35.31%</td>
<td>11561</td>
<td>87%</td>
</tr>
<tr>
<td>cluster3</td>
<td>129769922</td>
<td>16550</td>
<td>8.24%</td>
<td>44</td>
<td>0%</td>
</tr>
<tr>
<td>Grand Total</td>
<td>1575606646</td>
<td>216505</td>
<td></td>
<td>13260</td>
<td></td>
</tr>
</tbody>
</table>

Table 3: Results from K-Means algorithm for 4 clusters.
REFERENCES


