

Single-shot Acquisition of Cylindrical Mesostructure Normals using Diffuse Illumination

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Abstract: Capturing high-quality surface normals is critical to acquire the surface geometry of mesostructures, such as hair and metal wires with high resolution. Existing image-based acquisition methods have assumed a specific type of surface reflectance. The shape-from-shading approach, a.k.a. photometric stereo, makes use of the shading information by a point light, assuming that surfaces are perfectly diffuse. The shape-from-specularity approach captures specular reflection densely, assuming that surfaces are overly smooth. These existing methods often fail, however, due to the difference between the presumed and the actual reflectance of real-world objects. Also, these existing methods require multiple images with different light vectors. In this work, we present a single-shot normal acquisition method, designed especially for cylindrical mesostructures on a near-flat geometry. We leverage diffuse illumination to eliminate the reflectance assumption. We then propose a local shape-from-intensity approach combined with local orientation detection. We conducted several experiments with synthetic and real objects. Quantitative and qualitative results validate that our method can capture surface normals of cylindrical mesostructures with high accuracy.

1 INTRODUCTION

Capturing the surface geometry of mesoscale objects, such as textiles, brush hair, and metal wires, is demanding, and is often limited by the optical resolving power of 3D scanning systems; i.e., the spatial resolution of many 3D scanning systems is limited by the spatial resolution of the active illumination module. To overcome the limitation of 3D scanning resolution, a hybrid approach that combines the low-resolution geometry and the high-resolution surface normals has been proposed and commonly used (Nehab et al., 2005). For instance, we can obtain high-frequency geometric details as surface normals using a high-resolution camera. These normals are then transferred into low-frequency 3D geometry through the backprojection of the normals, yielding a high-resolution 3D model.

To this end, capturing high-quality surface normals is critical to achieving high-resolution 3D scanning. Existing image-based acquisition methods rely on some assumptions. More specifically, they assume that the target object has a specific type of surface reflectance. For instance, the shape-from-shading approach, a.k.a. photometric stereo imaging (Woodham, 1980), estimates surface normals by means of

the shading information. It captures multiple images with a point light of known positions and decomposes shading to light vectors and surface normals by assuming that the surface reflectance is perfectly diffuse. Another popular approach is the shape-from-specularity approach that captures specular reflections very densely (Sanderson et al., 1988; Oren and Nayar, 1997). The surface normals are then estimated by decomposing the specular reflections into the half-way vectors and surface normals, assuming that surfaces are overly smooth. However, these existing methods to capture surface normals often fail due to the difference between the presumed and the actual surface reflectance of real-world objects.

In this work, we present a single-shot normal acquisition method that can capture high-quality surface geometry of mesostructures. In particular, we target cylindrical mesostructures on a flat geometry, such as threads, brush hair, wires, etc. We first built an experimental setup for diffuse illumination, where 156 lights illuminate the target object. The diffuse illumination setup removes the long-employed assumption on the type of surface reflectance in our method. We then propose a novel, local shape-from-intensity method, combined with local orientation detection to enhance robustness against noise. We derive the re-

lation between the unit variance of the input image and the local height under diffuse illumination by formulating a cylindrical model for orientation cues. Finally, we calculate normals from the orientation cues through the local orientations of cylindrical shapes.

Our method does not assume any specific surface reflectance and can robustly capture surface normals of any diffuse and specular surfaces of various objects. The input of our method is a single-shot image under diffuse illumination. This allows us to capture normals efficiently.

2 RELATED WORK

Photometric Stereo. The shading information contains incident light direction and surface normals. It has been used to estimate surface normals by formulating a linear equation of the cosine law, so-called photometric stereo (Woodham, 1980). However, this method is valid only with perfect diffuse reflectance. Specular reflection often breaks the cosine law.

Several advanced photometric stereo methods have been proposed to overcome the limitation by specular reflection. Barsky and Petrou use four images to perform photometric stereo (Barsky and Petrou, 2003). Mallick et al. extract the pure diffuse component in the color space, which is perpendicular to incident light color (Mallick et al., 2005). Ma et al. separate diffuse and specular reflection using the different polarization properties of both reflections (Ma et al., 2007). However, their method has limitations as perfect diffuse specular separation is impossible.

Shape from Specularity. Instead of relying on shading information, many shape-from-specularity methods have been proposed to capture surface normals. Chen et al. exploit specular highlights from densely captured images in different illumination (Chen et al., 2006). In their method, if a pixel is a specular highlight, then the surface normal of the point is calculated from light and view vectors. However, this method requires a set of many input images with a condition that the entire surfaces should show specular highlights more than one time. Specular reflection is supposed to be observed in a narrower angle range than diffuse reflection; therefore, the methods that exploit specular reflection require many input images.

Shape Acquisition from a Single Image. There have been several attempts to obtain shape from a single image using strong assumptions. Langer et al. pro-

posed the so-called dark-means-deep model (Langer and Bülthoff, 2000). Dong et al. obtain spatial varying reflectance properties and a normal map from a single image using user interaction (Dong et al., 2011). Barron et al. calculate shape, reflectance, and illumination from a single image (Barron and Malik, 2015). However, the shape calculation of these methods assumes that specific reflection cases to solve a severely ill-posed problem. Recently, the methods to calculate SVBRDF from a single image have been developed (Aittala et al., 2016; Li et al., 2017; Deschaintre et al., 2018; Li et al., 2018). They exploit deep learning techniques. Existing single-shot normal acquisition methods require strong prior information, such as user interaction, diffuse surface, or training data. In contrast, our method requires only a single shot under uniform illumination, measuring surface normals directly without any prior or inference.

3 CAPTURING CYLINDRICAL MESOSTRUCTURES

Overview. Our method employs a single image taken under diffuse illumination as input. We then standardize the input image with local mean and variance to make the input illumination-invariant. Next, we detect the radius of the cylindrical shapes of mesostructures using the scale-invariant Laplacian detector. Furthermore, we detect the per-pixel orientation of local geometry in the screen space. Lastly, we compute surface normals using the cross product after projecting image gradients to the local orientation. Figure 1 provides an overview.

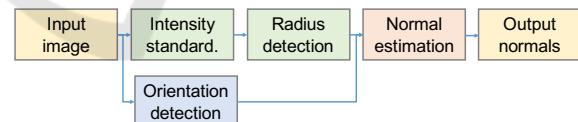


Figure 1: Normal estimation pipeline of our algorithm. We calculate normal orientation using the Gabor filter and a unit-variance intensity map from intensity statistics. The final normal output comes from combining orientation and a unit-variance intensity map.

3.1 Cylindric Image Formation

The target objects of our method are a set of cylindrical mesostructures that spread on a nearly flat plane. In our research scope, we ignore the property of surface colors, assuming that the surface albedo is monochromatic. Our main objective is to capture high-frequency surface normals of cylindrical mesostructures from an intensity image taken under diffuse illumination.

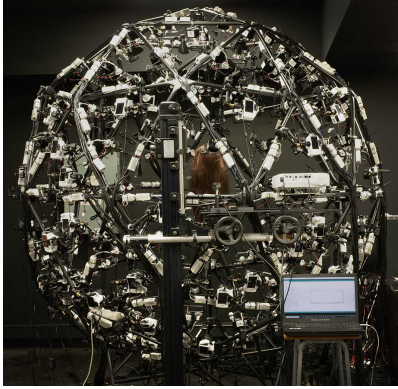


Figure 2: The light-stage system that we built to capture the input image. The light stage consists of uniformly distributed 156 LED lights.

Input. Our method takes a single intensity image as input. The image is taken under diffuse illumination, implemented by building a light stage. The light stage includes 156 LED lights, which are uniformly distributed over the sphere. Figure 2 presents our capture system. We then take a monochromatic intensity image as input.

Image Formation Model. We first begin with the traditional formulation of a cylinder shape (Glencross et al., 2008). Suppose a cylinder of radius R exists along the vertical y -axis. The height of the cylinder comes out along the z -axis on the right-hand basis, assuming an orthographic camera model. It can be parameterized by the x -coordinates as follows:

$$h(x) = (R^2 - x^2)^{\frac{1}{2}}. \quad (1)$$

The basic image formulation of our method follows the existing methods of the shape-from-intensity approaches (Glencross et al., 2008; Beeler et al., 2010). They assume that the locally lower points, such as pores or wrinkles, are darker, and higher points are lighter on the human face. Local heights correspond to the high-pass filtered image in their method. However, the high-pass filtered values are intensity-variant; i.e., the heights estimated in the bright region will be elongated relative to those estimated in the dark region. To achieve intensity-invariant estimation, we propose a local adaptation method of image intensity.

Under diffuse illumination, the image intensity can be determined by the local height of the point. Since a cylinder is symmetric, the points on the half side of the cylinder have their correspondences in the opposite side. Also, any points on the same latitude level are assumed to have the same level of illumination. For half of the cylinder, the height increases

monotonically for each level of pixel positions. The relation of the set of points that have the same intensity to the height level is a bijective function. Now the domain of the intensity function can change from the position to the height:

$$I(x) = f(h(x)), \quad (2)$$

where I is the intensity of the position x , h is the height of the position x , and $f(\cdot)$ is the unknown mapping function from height to intensity (see Section 4.2 for validation).

Since we use the linear camera signals without applying gamma correction, we assume that the above mapping function f is linear as follows:

$$I(x) = c_1 \cdot h(x) + c_0, \quad (3)$$

where c_0 and c_1 are unknown constants. The constants c_0 and c_1 include all information of image formation, such as surface albedo, incident light intensity, camera exposure, linear camera response function, etc. To eliminate the constants c_0 and c_1 , we standardize the image intensity as unit variance, a.k.a. the z-score value, using a function $z(\cdot)$:

$$z(I(x)) = \frac{(c_1 \cdot h(x) + c_0) - (c_1 \cdot \mu + c_0)}{c_1 \cdot \sigma} = \frac{h(x) - \mu}{\sigma}, \quad (4)$$

where μ is the mean of height h and σ is the standard deviation of height h . With the assumption of cylindrical shapes of objects, the height function is symmetric and thus the mean and variance can be calculated for only a half period as follows:

$$\mu = \frac{1}{R} \int_0^R h(x) dx = \frac{\pi}{4} R. \quad (5)$$

This integral can be solved as an area of a quarter of a circle. The variance is

$$\sigma^2 = \frac{1}{R} \int_0^R h(x)^2 dx - \mu^2 = \frac{2}{3} R^2 - \frac{\pi^2}{16} R^2. \quad (6)$$

Finally, the height function of the z-score of image and the cylinder radius can be written as follows:

$$h(x) = \sqrt{\frac{2}{3} - \frac{\pi^2}{16}} R z(I(x)) + \frac{\pi}{4} R. \quad (7)$$

3.2 Estimating Mesostructures

Intensity Standardization. As mentioned earlier, z-score maps can be converted to height maps using Equation (7). However, the simple and global formulation does not hold in a real scene; for instance, the real-world object might not be a perfect plane and might not be perfectly parallel to the sensor space due to its shape geometry. In addition, even our experimental setup is not perfect diffuse illumination due to the sparsity of the lights.

To mitigate these issues, we use the *local* z-score map. First, the mean calculation in Equation (4) is replaced with the Gaussian-weighted local mean μ_I :

$$\mu_I(x, y) = (G_\sigma * I)(x, y), \quad (8)$$

where G is the Gaussian kernel, σ is the standard deviation of the Gaussian kernel, and $*$ is the convolution operator. Similarly, the local standard deviation σ_I is

$$\sigma_I(x, y) = \sqrt{(G_\sigma * I^2)(x, y) - ((G_\sigma * I)(x, y))^2}. \quad (9)$$

The local unit-variance value can then be expressed as

$$\tilde{I}(x, y) = \frac{I(x, y) - \mu_I(x, y)}{\sigma_I(x, y)}. \quad (10)$$

The local unit-variance value is invariant to low-frequency change of local intensity and irregular light conditions. The smaller sigma makes the local unit-variance more independent of local illumination difference, but an overly small value can lose local statistics. We select a sigma level that has a larger value than the diameters of the cylindrical objects in the image.

Radius Detection. The radius of the cylinder is required to calculate the height map from the local unit-variance map. Assuming that the same cylindrical shapes exist in the scene, only a radius value in the screen coordinates is required to calculate the surface normal. We obtain the radius of the cylinder from the blob size using the Laplacian of Gaussian (LoG) blob detection (Lindeberg, 1998) based on the hills and valleys model of (Langer and Bülthoff, 2000). A hill means a high area in the cylinder, which is a bright area in the image. Valleys are the opposite of hills. The LoG blob detection algorithm detects both areas, and thus we use both blob scale results.

In detail, we apply the LoG blob detection first to the local unit-variance map. Owing to the maximum response of the LoG operation, the blob size is multiplied by $\sqrt{2}$. The detected position and blob size cannot be used directly as the numbers of blobs in hills and valley are different. A blob is identified as either a hill or a valley by the z-score of the blob position in the local unit-variance map. If the z-score is larger than a threshold, the blob is in the hill. Otherwise, the blob is in the valley.

Orientation Detection. In our cylinder model, the gradient of the image is perpendicular to the cylinder orientation (the height axis of the cylinder). However, the gradient is not perfectly perpendicular to the orientation in the real scene. The derivation operation to calculate gradients is sensitive to noise in nature.

Since we are targeting small-scale objects of a small radius, our method is very sensitive to noise in gradients. To mitigate the noise problem, we exploit directional derivatives using the cylinder orientation from the larger-scale operation.

We first employ the Gabor filter to find the orientation of the cylinders. The Gabor filter has been commonly used in the orientation estimation of objects with a small cylindrical geometry, such as hair (Paris et al., 2004; Jakob et al., 2009; Nam et al., 2019). We estimate the orientations of cylinders by detecting the maximum amplitude of the Gabor filter.

$$\theta^*(x, y) = \arg \max_{\theta} |(F_\theta * I)(x, y)|, \quad (11)$$

where F_θ is the Gabor filter that is tilted at the θ angle from the x -axis and θ^* is the calculated orientation map.

We compute the orientation map by convolving the input image with predefined angle candidates in a certain angle resolution. We apply the Gabor filters of different angles in 5-degree intervals. We then apply a median filter of 3×3 to suppress noise. However, the angle values have a period; the median filter cannot be used directly. Therefore, we first apply the median filters to three different angle ranges as follows:

$$m_n(x, y) = \text{mod} \left(\text{median}_{(s,t) \in S_{xy}} (\theta_n^*(s, t)), \pi \right), \quad (12)$$

where m_n is the median filter result where the range shifted $\frac{n\pi}{3}$ radians, n is 0, 1 or 2, S_{xy} is a 3×3 window of the median filter, and the shifted angle values as

$$\theta_n^*(x, y) = \text{mod} \left(\theta^*(x, y) - \frac{n\pi}{3}, \pi \right) + \frac{n\pi}{3}. \quad (13)$$

We obtain the cosine value of the angle difference to derive the angle pair with high confidence that has the smallest difference:

$$C_{ij}(x, y) = \cos(m_i(x, y) - m_j(x, y)). \quad (14)$$

where $i \neq j$.

We choose the pair that has the largest absolute cosine value, not the signed cosine value, as the direction, and the opposite direction is the same for the cylinder orientation:

$$(i^*(x, y), j^*(x, y)) = \arg \max_{i, j} |C_{ij}(x, y)| \text{ s.t. } i \neq j. \quad (15)$$

We use the mean angle of the pair of the median value. When the mean angle is calculated, the direction and the opposite direction yield different values. We compute the mean angle that has a smaller difference with the median value.

$$\theta_{ij}(x, y) = \begin{cases} \frac{m_i(x, y) + m_j(x, y)}{2} & \text{if } C_{ij}(x, y) \geq 0 \\ \frac{m_i(x, y) + m_j(x, y) + \pi}{2} & \text{otherwise} \end{cases} \quad (16)$$

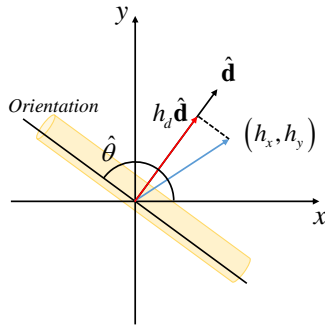


Figure 3: The image gradients are projected to the direction perpendicular to the cylinder orientation, suppressing noise in the calculated gradients.

Finally, the median angle estimated by the Gabor filter is given as follows:

$$\theta_{med}(x, y) = \theta_{i^*(x, y), j^*(x, y)}(x, y). \quad (17)$$

Normal Estimation. The final step is to calculate normals from the unit-variance intensity map and the orientation map. First, we obtain the local height map from the local z-score map.

$$h(x, y) = \sqrt{\frac{2}{3} - \frac{\pi^2}{16}} R\bar{I}(x, y) \quad (18)$$

The coefficients of the local z-score values are inherited from Equation (7). The constant term in Equation (7) is not necessary as we use the derivation of the local height map to compute the normal map.

Next, we obtain the directional derivatives that are perpendicular to the cylinder orientations. We calculate partial derivatives of the x - and y -axis using the Sobel filter:

$$h_x(x, y) = \frac{\partial h(x, y)}{\partial x}, \quad h_y(x, y) = \frac{\partial h(x, y)}{\partial y}. \quad (19)$$

The gradients are then projected to the lines that are perpendicular to the cylinder orientations by the dot product:

$$h_d(x, y) = \begin{bmatrix} h_x(x, y) \\ h_y(x, y) \end{bmatrix} \cdot \hat{\mathbf{d}}(x, y), \quad (20)$$

where $\hat{\mathbf{d}}(x, y) = [\sin \theta^*(x, y) \quad -\cos \theta^*(x, y)]^T$ is the direction that is perpendicular to the cylinder orientation, and θ^* is the angle of the cylinder orientation from the x -axis. The projection mechanism is depicted in Figure 3.

Finally, we obtain the surface normals from the cylinder directions and the derivatives. The tangent vector $\hat{\mathbf{t}}$ of the normal vector is

$$\hat{\mathbf{t}}(x, y) = \frac{\mathbf{t}(x, y)}{\|\mathbf{t}(x, y)\|}, \quad (21)$$

where

$$\mathbf{t}(x, y) = [\sin \theta^*(x, y) \quad -\cos \theta^*(x, y) \quad h_d(x, y)]^T. \quad (22)$$

And its bitangent vector $\hat{\mathbf{b}}$ is

$$\hat{\mathbf{b}}(x, y) = [\cos \theta^*(x, y) \quad \sin \theta^*(x, y) \quad 0]^T. \quad (23)$$

The bitangent vector is the orientation that makes the normal orientation to the camera placement. Finally, the normal map $\hat{\mathbf{n}}$ can be calculated as follows:

$$\hat{\mathbf{n}}(x, y) = \hat{\mathbf{t}}(x, y) \times \hat{\mathbf{b}}(x, y). \quad (24)$$

4 RESULTS

In this section, we validate our normal estimation algorithm by providing quantitative and qualitative analyses of experiment results with synthetic ground truth and real data. We implemented our algorithm in MATLAB without code optimization and computed in Intel i7-7700K CPU and 32GB memory. For an image with a resolution of 256×256 , our algorithm took approximately 0.63 seconds in total.

4.1 Evaluation on Real Data

Experimental Details. For real scene experiments, we built a light stage with 156 LED lights uniformly distributed over the sphere to capture an object. The LED lights (CXA1512-0000-000N00N20E1) have a flux of 1650lm, a power 12.6W, and a correlated color temperature of 6500K. The lights are located at the edge and vertex of the subdivision of an icosahedron. The diameter of a sphere is 2.6m. We use a machine-vision camera (GS3-U3-123S6C-C) with a resolution of 4096×3000 and a pixel pitch size of $3.45 \mu\text{m}$. To achieve the orthographic camera assumption of our image formation, we employ a lens with a focal length of 35mm and crop the 256×256 center region of the captured image, of which the field of view is 1.45° .

Qualitative Comparison. We compared our results with four existing methods: photometric stereo, mesostructure from specularly (Chen et al., 2006), and two deep learning-based single image normal acquisition methods (Ye et al., 2018; Deschaintre et al., 2018). For photometric stereo and mesostructure from specularly, we captured 60 images with different light positions and calibrated them using a mirror sphere. As Deschaintre's method requires a captured image under a flashlight, we captured an image with a single light. We experimented with various surfaces for our model. They include diffuse surfaces (flower

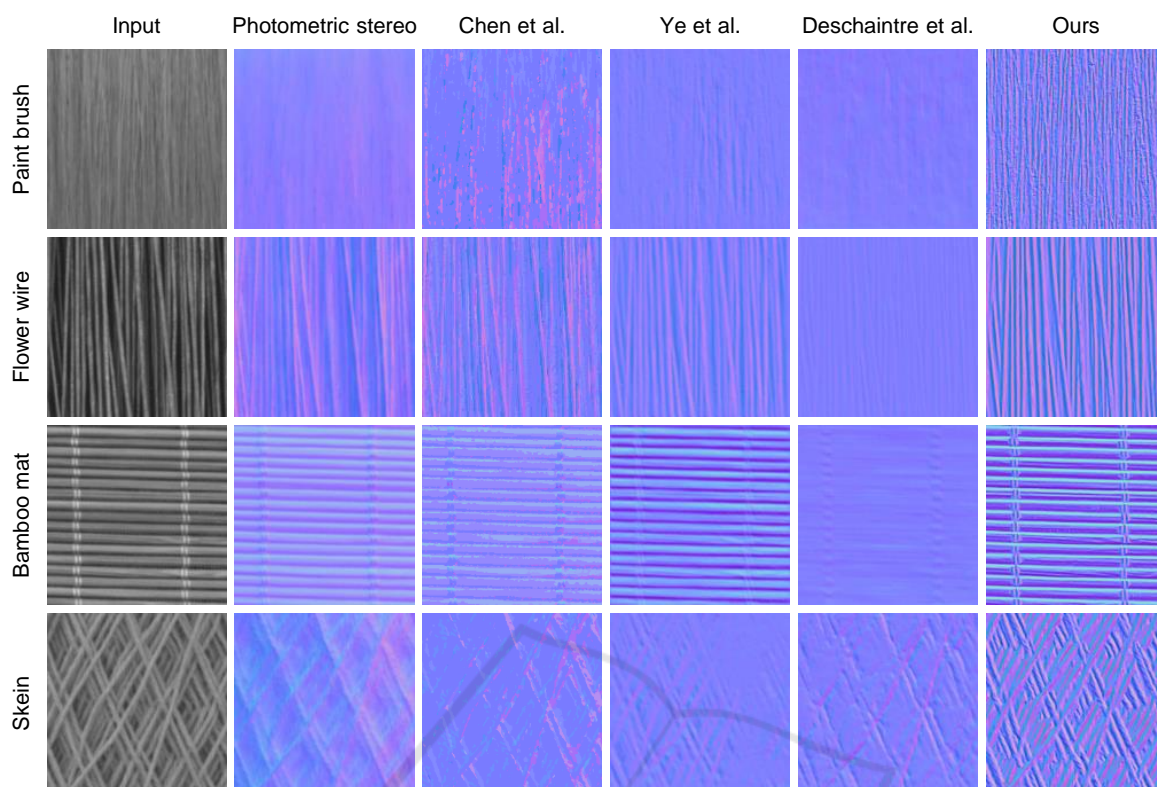


Figure 4: We compare the results of our normal estimation method with other existing methods. Other methods fail to estimate thin cylindrical structures of surfaces.

wire, bamboo mat), thin specular structures (brush), and complex structures (skein).

Figure 4 shows the captured images and reconstructed normal maps. Photometric stereo measures the overall normal map well but fails in capturing high-frequency surface orientation. Deep learning-based methods show low-quality normal map results for thin cylindrical structures. These methods require a single input image with specular reflection under a point light. For transparent surfaces and thin cylindrical shapes, these methods fail to capture high-frequency details because specular reflection occurs in arbitrary directions by refraction and occlusion. This phenomenon reduces the surface orientation cues of the light direction. Compared with other existing methods, our method shows the best quality, achieving fine-level details of surface orientations of mesostructures.

4.2 Quantitative Evaluation with Simulation

Here we validate our cylinder model by comparing the ground truth normals and reconstructed normals from synthetic images. We rendered an array of cylin-

ders in a uniform illumination using the Mitsuba renderer. The GGX microfacet distribution (Walter et al., 2007) was used for a specular reflectance model. All cylinders have the same radius and reflection parameters, including albedo and specular roughness, by changing α parameter of the GGX model. We evaluate our algorithm with various roughness to validate the performance of our algorithm.

Figures 5(a) and (b) present rendered synthetic input images and the ground truth normal maps of the same geometry. Figures 5(c) and (d) show the normal maps yielded by our method and the angle difference between our results and the ground-truth normal maps. Almost every position over the mesostructures presents smaller differences than 20 degrees. However, we found that there are large angle differences in the deepest points in the valley. These points are not differentiable and thus the finite differences lead to suboptimal results.

Figure 5(e) shows the relation between the ground-truth height and the unit variance intensity values. It shows that the height and the unit-variance intensity have a linear relation for a wide range of roughness. When the surface is a mirror, the surface makes only two values that are the high intensity from the specular reflection and the low intensity

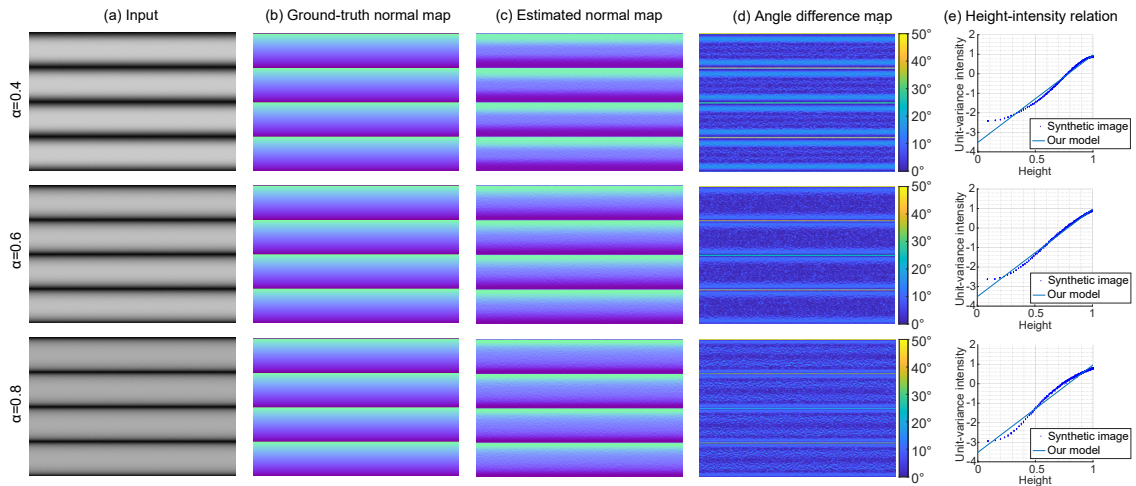


Figure 5: Quantitative evaluation with the synthetic ground-truth dataset. (a) Input image of cylinders (without gaps) rendered with the Mitsuba renderer. (b) Ground-truth normals of the same geometry (c) Estimated normals. (d) The angle difference between our results and the ground truth. (e) The comparison between the intensities and the estimated height levels.

from the occlusion around cylinders. If the surface becomes rougher, the relation of the height and the unit-variance intensity become closer to the linear relation. However, the intensity of the top of the cylinder is weaker than near points where the surface is diffuse because the top of the cylinder does not have interreflection. Table 1 shows the average angle difference in each image. The average angle difference is smaller than 15 degrees in the tested roughness range. The average differences decrease when the roughness becomes larger, but they increase again when the surface is highly diffuse. Figure 6 includes the results for different alignment of cylinders, such as varying on the inter-cylinder distance and crossing. All cylinders have the fixed roughness ($\alpha=0.4$). The intervals among cylinders are set to half of a cylinder and a cylinder. The background shown in the intervals is

set to the infinite distance, yielding no value of rendering. Therefore, we exclude the values at the infinite distance from the calculation. The results of the inter-cylinder gap and crossing also show small differences, compared with the ground truth.

Table 1: Average angle errors of our method with different surface roughness parameters.

Roughness (α)	0.4	0.5	0.6	0.7	0.8
Mean error (deg)	10.64	9.49	8.57	8.26	8.91
Std. dev (deg)	8.49	8.23	7.88	7.51	7.15

5 LIMITATIONS

Our method is not free from limitations. First, our method presents a suboptimal performance in capturing normals for highly specular objects such as a mirror or highly diffuse objects. As shown in our synthetic experiments, the perfect mirror surfaces present only two intensity levels: light existing and light occluded. For perfect diffuse surfaces, the interreflection becomes larger where the height is smaller, while our relation conversion is valid on the top of cylinders. This breaks our assumption. These surfaces of extreme reflectances require a roughness estimation or interreflection calculation. Second, the processing of string crossing areas of our method could be developed further. If the texture has many cross-sections, the ambiguity in detecting surface orientations might become severely ill-posed when applying for the Gabor filter. Third, diffuse illumination is hard to acquire. We used a large light stage to obtain diffuse illumination. Single-shot acquisition of cylindrical

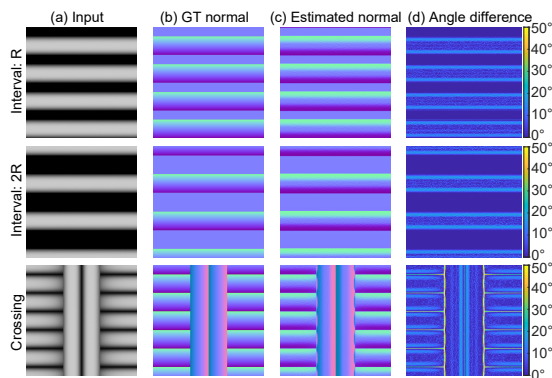


Figure 6: Quantitative evaluation with the synthetic ground-truth dataset which have inter-cylinder distance and crossing. The intervals among cylinders are set to half of a cylinder and a cylinder. (a) Input image. (b) Ground-truth normals. (c) Estimated normals. (d) The angle difference between our results and the ground truth.

mesostructure normals with a point light or without any light condition are possible areas of future work.

6 CONCLUSIONS

We have presented a normal map acquisition method primarily designed for mesoscale cylindrical objects using a single input image. We have discovered that mesoscale geometry can provide local intensity statistics to solve practical issues in the existing shape-from-intensity approach. We showed that the relation of the local height and unit-variance intensity under diffuse illumination of the light stage. We calculated the normal maps from the local unit-variance values and the detected cylindrical orientations from a single image. We validated that our method consistently outperforms existing methods for capturing high-frequency details of the surface orientation of both specular and diffuse objects in the real world.

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