# Dynamic Assignment Vehicle Routing Problem with Generalised Capacity and Unknown Workload

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Abstract: In this paper we present a modification to the Dynamic Assignment Vehicle Routing Problem. This problem arises in parcel to vehicle assignment where the destination of the parcels is not known up to the assignment of the parcel to a delivering route. The assignment has to be done immediately without the possibility of re-assignment afterwards. We extend the original problem with a generalisation of the definition of capacity, with an unknown workload, unknown number of parcels per day, and a generalisation of the objective function. This new problem is defined and various methods are proposed to come to an efficient solution method.

## **1 INTRODUCTION**

In city logistics, the efficient and effective transportation of goods in urban areas is important. For the community as a whole however, taking into account the negative effects on congestion, safety, and environment (Savelsbergh and Van Woensel, 2016) is important. These aspects come together in consolidation and transshipment on satellite locations with cross docking, redistributing the incoming freight into other, possibly smaller vehicles to serve customers. This results in a 2-echelon distribution and vehicle routing problem (2E-VRP), which are described in the survey of (Cuda et al., 2015). The authors of this survey consider strategic planning decisions, including decisions concerning the infrastructure of the network, and tactical planning decisions, including the routing of freight through the network and the allocation of customers to the intermediate facilities. At the tactical level, the customer locations are considered known. This is not the case in most situations in practice. There, a considerable part of the customer locations is revealed late in the process. This brings us in the field of dynamic vehicle routing problems.

The review of Pillac et al. (Pillac et al., 2013) gives an overview of dynamic vehicle routing problems. They make a separation of those problems between 'static and dynamic' on one axis and 'deterministic and stochastic' on the other axis. This gives four fields of research. In field (1) 'static and deterministic problems', all input is known beforehand and vehicle routes do not change once they are in execution, see for an overview of these classic vehicle routing problems (VRPs) (Baldacci et al., 2007). In field (2), 'Static and stochastic', problems are characterised by input partially known as random variables, which realisations are only revealed during the execution of the routes, see for example (Bertsimas and Simchi-Levi, 1996). Here also clustering techniques for stochastic data can be used (Ngai et al., 2006).

In field (3) 'dynamic and deterministic' problems, part or all of the input is unknown and revealed dynamically during the design or execution of the routes. These problems are also called online VRP problems (Bjelde et al., 2017; Jaillet and Wagner, 2008). Similarly, in the problems of field (4), 'dynamic and stochastic' problems, a part or all of their input unknown. The unknown information is revealed dynamically during the execution of the routes, but in contrast with the latter category, exploitable stochastic knowledge is available on the dynamically revealed information. See for a survey (Ritzinger et al., 2016). In addition, methods based on anticipation can be used (Ulmer et al., 2015).

In (Phillipson and De Koff, 2020) the Dynamic Assignment Vehicle Routing Problem (DA-VRP) is introduced. This is a field (3) 'dynamic deterministic' VRP, however, the assignment of the parcels is done at the same time the destination is revealed. This means that the planning is done dynamically, but in contrast

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to the common dynamic case, it is done in upfront, where the route is not being executed yet, giving the possibility to change the order per route, but not to interchange between the routes. This problem relates directly to the practice in parcel distribution. Often, a satellite location where the incoming parcels have to be distributed over a number of vehicles to deliver them to the customers, has no, or a rather small, space for storage. This means that the parcels have to be assigned directly, after unloading and scanning, to an outgoing vehicle. There is no possibility to reassign on a later moment in time. The parcels are delivered to the assigned vehicle instantaneously. The destination of the parcels is not known on beforehand and is revealed only at arrival at the satellite location.

In (Phillipson and De Koff, 2020) an approach is presented to solve this problem. However, some assumptions are made there that will be generalised in this work. This generalisation will be on:

- the *capacity* of the routes: this is now not only driven by the number of parcels, but also by the (time) length of the tour. The tour cannot be longer than a specific time *t*.
- the *forecast*: we do not longer know the exact number of parcels to be distributed per day. In some cases we assume we have some approximate forecast using a seasonal or weekly pattern.
- the *objective*: the objective to be minimised is no longer only the total distance of the tours in kilometres, but a combination of this total distance (monetised by multiplying it with a priceper-kilometre) and the costs (salary cost per hour) of the driver. For this we will round the number of hours per driver to a certain amount (7 or 8 hours) to illustrate what happens when a driver can only be hired for (almost) a whole day.

The remaining of this paper is organised as follows. First, in Section 2, we present the general approach to come to a dynamic assignment of the parcels to the routes. In Section 3, we elaborate on the cases we use to show the performance of the various approaches. Conclusions can be found in Section 4.

### 2 METHOD

In this section we present an approach that can be used to assign the parcels to the routes. In (Phillipson and De Koff, 2020) two steps were distinguished:

- 1. Initial assignment of direction to routes;
- 2. Dynamic assignment of arriving parcels;

The first step gives a potential direction to each of the routes, or none if empty vehicles are used, by assigning a base load, a certain region or some initial direction. The second step assigns directly the incoming parcels to the routes. The uncertainty about the number of parcels per day will lead to two extra steps in our approach:

- 1. Initial assignment of direction to routes;
- 2. Dynamic decision of daily fleet size;
- 3. Dynamic assignment of arriving parcels;
- 4. Post-processing.

All steps will be discussed in more detail in the next sections. In Section 2.3 solution techniques that are used, are presented in more detail. After those steps the load assigned to all routes is known and for each route a regular TSP can be solved.

#### 2.1 Assumptions and Notation

In a Dynamic Assignment Vehicle Routing Problem (DA-VRP) k parcels arrive at a location in a specific order. In that specific order, each of the parcels reveal their destination and have to be assigned immediately to one of the m (identical) vehicles, that will deliver the parcel to its destination. Each parcel requires one capacity unit of the vehicles and all vehicles have capacity C. When assigning the jth parcel, vehicle i can only be regarded iff  $n_i < C$ , where  $n_i$  equals the load of vehicle i at that current moment. No information is known or used about the geographical location of the client. Only a estimation of the total volume is assumed, based on a similar day in the past.

#### 2.2 Detailed Steps

We go into more detail on each of the four steps.

*Step 1: Initial assignment of direction to vehicles.* It is helpful to give an initial direction or assignment of a certain area to each of the routes. This is done in Step 1 of the approach, the initial assignment. We consider two possible approaches:

- 1. Separation by dummy location We perform a k-Means clustering over all potential customers and assign a dummy parcel, having as location one of the cluster means, to each route. K-means clustering (James et al., 2013) aims to partition observations into k clusters, in which each observation belongs to the cluster with the nearest mean.
- 2. Total geographical separation Again we perform a (k-Means) clustering over all potential customer locations (postal codes) and assign each of those (postal codes) clusters to a route.

Step 2: Dynamic decision of daily fleet size. In (Phillipson and De Koff, 2020) the (exact) number of parcels is known in advance and from that we can compute the number of routes we need, given only a capacity constraint on the number of parcels. However, now we don't know the number of required vehicles for two reasons. Firstly we don't (exactly) know the number of parcels per day and, secondly, we don't know the location of the parcels and thus we don't know the (time) lengths of the resulting routes. This means that we have to decide on the number of routes, somewhere before, during or after the assignment of arriving parcels. We actually do all three: we start with a certain number, add extra routes during the sorting process and finally, we combine, where possible, routes into one route after sorting. This also means that Step 2 and Step 3 are happening somewhat in parallel: the number of tours are not defined beforehand but during the assignment. For the sake of clarity, we will use the term tour for the first three steps. The result of the third step will then be a number of tours with parcels assigned to it. In Step 4 the tours will be assigned to routes, that can be executed by vehicles.

In Step 2 we decide on the number of tours to start with, and on the procedure and conditions to add an extra tour to the problem. We looked at two possible approaches for this step. For both approaches we assume a (rough) estimation of the number of arriving parcels, coming from a seasonal or weekly pattern. We estimate the number of tours to distribute these parcels and call this number N for a certain day. The two approaches are now:

- 1. 'Overall capacity based' Start with nN < N(0% < n < 100%) tours. When the *overall tour load* gets higher than a certain value c (0% < c < 100%) during the assignment phase, we add an extra tour.
- 2. 'Tour capacity based' Start with nN < N (0% < n < 100%) tours. When the tour load of a *specific tour* is higher than a certain value c (0% < c < 100%) when trying to assign a parcel to it, we add an extra tour and assign this parcel to it.

We found in prior analyses that approach 2 performs better than approach 1 and that approach 2 performed best with parameters n = 75% and c = 99%. Note that these parameters are case specific.

*Step 3: Dynamic assignment of arriving parcels.* Next, three methods for the third step, the dynamic assignment of arriving parcels, are proposed:

1. Based on minimal insertion costs – for all tours we calculate the minimal cost of inserting the arriving parcel destination to the tour. Details of this approach are in the next section. We assume that the assigned parcels are ordered in the routing of the tour, so we can calculate the cost by trying to insert the parcel between each pair of consecutive parcels in the tour. The insertion that is cheapest is selected.

- 2. Based on minimal insertion costs with penalty for all tours we calculate the minimal cost of inserting the arriving parcel destination to the tour. Again, as we assume that the assigned parcels are ordered in the routing of the tour, we can calculate the cost by trying to insert the parcel between each pair of consecutive parcels in the tour. The cost is multiplied by a penalty factor, depending on the load of the tour. The insertion that is cheapest will be selected. The calculation of the penalty is explained in the next sub-section.
- 3. Based on fixed clusters here the parcel is simply assigned to the tour it belongs to, using the total geographical separation of the initial stage, based on customer or postal code of the customer.

When, by one of these methods, the assignment is determined, the parcel is inserted on the right place in the route of the selected vehicle, meeting the assumption of ordering.

*Step 4: Post-processing.* In the post-processing step we assign tours to vehicles. Due to the fact that we do not know the exact number of parcels and the driving times, and due to the heuristic character of Step 2, we can end with tours that are small and can be combined (together) to one vehicle. Again we consider two flavours.

- 1. Combining: Assume that the tours start and end at the depot, such that any two tours can be combined, as long as the time restriction, the maximum driving time of the driver, is met. The restriction on the number of parcels is not important, due to the extra stop at the depot. It also is not important which two tours are combined, where we assume that there is no gain to obtain by combining two (near) tours smartly. In this post-processing step we just try to minimise the number of vehicles, given the tours. We do so in a greedy way, start with the longest tour and try to add the longest tour as possible that fits the requirements.
- 2. Integrating: Optimise further by integrating combined tours, such that they do not have to go to the depot in between. For this we use a greedy heuristic as shown below:
  - (a) Sort the tours on available capacity;

- (b) Take the tour with the smallest available capacity (but not zero);
- (c) Take a number (max 20) of the largest tours that can be combined with this tour, within the capacity constraints;
- (d) Calculate the costs of the integrated routes of those combined tours and select the best. Combine those tours into one;
- (e) Go back to step (b) until no combinations can be made.

Integrating tours, in the second option, means that two tours are combined by removing the extra stop at the depot (D). For example, if we have two routes, visiting customers with ID 1-10:

route 1: D - 1 - 2 - 3 - 4 - D,

route 2: D-5-6-7-8-9-10-D. Those can be combined to each of the following two: D-1-2-3-4-5-6-7-8-9-10-D, D-5-6-7-8-9-10-1-2-3-4-D.

#### 2.3 Solution Techniques

We use two mathematical solution techniques within our approaches: k-Means clustering method, and the Insertion method (with penalty).

For the k-Means clustering method in the Separation methods we use the basic Matlab implementation, 'kmeans(X,k)'

The Insertion method works as follows. We assume that already each tour *i* has a sorted route indicated by the (x, y) coordinates of the destination of the parcels, starting and ending at the satellite location with coordinates  $(x_{i,0}, y_{i,0}) = (x_0, y_0)$ :

 $(x_{i,0}, y_{i,0}), (x_{i,1}, y_{i,1}), \dots, (x_{i,n_i}, y_{i,n_i}), (x_{i,0}, y_{i,0}).$ 

Now, a parcel with coordinates (x, y) has to be assigned to a cluster. For each tour *i*, determine the pair of consecutive points k, l such that

$$d_{i} = \min_{k,l} d((x_{i,k}, y_{i,k}), (x, y)) + d((x, y), (x_{i,l}, y_{i,l}))$$

$$-d((x_{i,k}, y_{i,k}), (x_{i,l}, y_{i,l}))$$

is minimal for all pairs k, l, where  $d((x_1, y_1), (x_2, y_2))$ denotes the distance between two destinations, noted by their (x, y) coordinates. The parcel will now be inserted, on the spot between  $k_i^*$  and  $l_i^*$ , in the tour *i* that minimises  $d_i$  for all *i*. In case of the Insertion method with penalty, this distance is multiplied by a penalty factor  $(1 + p_i)$  where

$$p_i = P \cdot \max(n_i/C, t_i/T),$$

where *P* is the chosen penalty value,  $n_i$  the current load of tour *i*, *C* the capacity of the tour,  $t_i$  the timelength of tour *i* and *T* the maximum length of the tour. The value of *P* is case dependent. A part of the data can be used to calculate the best value of *P*.

### **3 RESULTS**

In this section we show the performance of the approach in practice. The use case is based on real data from a Dutch satellite location, of November 2018. Here, every day, on average 12,000 parcels are handled. We disregard the pick-up orders, where a parcel has to be collected. This satellite location serves a geographical area of approximately 80x100 kilometres.

The first analysis compares two approaches, each of which is a different implementation of the four steps, as presented in Section 2. In the second analysis we will look if we can say something about the optimal number of tours. The last analysis looks at the performance of the alternative method of step 4, which is harder to implement in practice.

For the first analysis, we compare two approaches, we will call approach 1 'Base' and approach 2 'Alternative'. The idea of 'Base' is that there is a fixed assignment of an area (postal code based) to (a set of) routes. This approach is used often in practice. We will present approach 'Alternative' as an alternative approach. The approaches are explained in detail in Table 1. We looked at the best penalty parameter for approach 2. We found that a low penalty (or even zero) performs best. This means we actually use the 'filled by insertion approach' in Step 3. It was beneficial to keep some slack in the routes when the number of routes was known (but fixed during assignment), to have the possibility to assign some very well fitting parcels to a tour. However, in this problem we want to assign the parcel to the best route possible. If that route is fully loaded, we just add a new route. Assuming the (fictional) costs per kilometre of 0.6 euro and cost per driver hour of 15 euro, for the data of November 2018, the 'Alternative' approach performs 9.5% better in total cost, as is shown in Table 2. The table shows the costs of the tours, based on distance (in euro), the costs of the drivers (in euro) and the total costs (all averages per day). In addition in the table are displayed the number of tours, after Step 3, and the number of vehicles after the post-processing Step 4, resulting from combining tours.

We see that the process results in a certain number of tours after Step 1-3 and a certain number of vehicles resulting from the post-processing step. The question of the second analysis is whether we can say something about the optimum number of tours and the optimum number of routes. For this we run the algorithms (without Step 2) for a fixed number of tours and derive the number routes and the costs for that solution. We do that for a specific day (having 11,100 parcels). A theoretical minimum of routes needed equals 61, when the capacity is only based on the

	'Base'	'Alternative'
Step 1	Total geographical separation	Separation by dummy location
Step 2	Tour capacity based	Tour capacity based
Step 3	Fixed Clusters	Minimal insertion (with penalty)
Step 4	Combining	Combining

Table 1: Overview of two approaches.

Table 2: Result for first analysis.

	'Base'	'Alternative'
Distance (euro)	10,472	9,012
Driver hours (euro)	14,577	13,633
Total costs (euro)	25,049	22,645
Tours (Step 1-3)	142	130
Vehicles (after Step 4)	116	112

number of parcels per route, which is assumed 180, or 90, when the capacity is time based, assuming an average of 150 km per route per day. We vary the number of tours between 160 and 110. The algorithm does not find solutions having less than 117 tours. For a low number of tours, all parcels are forced in tours that can be one-on-one translated into routes. However, when filling the tours, some tours may become full and the parcels have to be assigned to 'less optimal' tours. Choosing a high number of tours, we might end up with a number of (very) small tours, that cause a lot of empty capacity in the routes. Note that we restrict ourselves to combining a maximum number of two tours. The results for this analysis can be found in Figure 1. We see (using a polynomial trend line) that there actually is an optimal number of tours, around 144 for 'Base' and 140 for 'Alternative' (ALT in the figure). Resulting in a minimum number of vehicles of 105 for 'Alternative'.

If we now change the method in step 4 to 'integrating' instead of 'combining', we get even better results. The results are displayed in Figure 2. There is shown that using 'integrating', a further increase in the number of tours leads to lower costs, which appeared to be at a resulting number of vehicles of 91. This is already close to the theoretically estimated optimum.

# 4 CONCLUSIONS

In this study we looked at the Dynamic Assignment Vehicle Routing Problem. In contrast to earlier research, we now assumed the capacity of the routes based on both the number of parcels and the driving time, we assumed the number of parcels per day to be unknown and we optimised the total costs. The two main conclusions for this problem are:

- 1. Using the 4-step approach with a variable number of routes can be beneficial, leading to lower costs of around 9%.
- 2. Assigning parcels to a higher number of tours, and combining them to routes afterwards gives another gain of around 15%.

These gains are calculated against the 'Base' approach, which serves as an approximation for the approach used in practice.

A few remarks on these conclusions. The improvement in performance by using a larger number of tours, and then combining those to real routes driven by vehicles, is obvious. Theoretically, a number of tours equal to the number of parcels and then combining those tours, thus consisting of exactly one delivery, is optimal. However, this is obviously equal to solving the underlying VRP problem, which is hard for those number of deliveries. Also, clustering the deliveries in a smart way and conducting the VRP on those clusters is a smart heuristic in some way. The question now is how big those clusters should be, or, how many clusters you should have. We see in the example that at a small number of clusters (relative to the number of parcels) 160 clusters vs 11,000 parcels leads to a number of vehicles that is already close to the theoretical minimum number. An even bigger number of clusters and a higher number of routes to be combined is not expected to give a huge increase in performance. Note that the presented approach can be seen as an example of multi-tier territory clustering and multi-plane meshed hub within the Physical Internet approach (Tu and Montreuil, 2019). They introduce flexibility to assign resources (depots, vehicles) to delivery-addresses.

The 'BASE' approach leads in practice to a situation in which drivers have a largely fixed delivery area. The practical question now is whether drivers are willing to change their way of working. In the new setting they might have a combination of multiple delivery areas that might change every day. Note that this could be solved by assigning (tactically) a number of tours to drivers, where they will only serve a subset of those tours per day, increasing their operating area. Here a bigger number of tours could be beneficial. Also, one would have to check whether the combining of tours to the vehicles is workable



Figure 2: Costs as function of tours, after integrating tours.

in practice in the distribution centre. Here a smaller number could be better feasible, what limits the number needed by the previous point in this list. Also, the combining of tours leads to a more dynamic demand on the number of vehicles. In practice vehicles (and drivers) are contracted some time in advance. A new process will have to be devised to cope with a more dynamic usage of vehicles.

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