Lane-changing Decision-making using Single-step Deep Q Network

Yizhou Song^{1, a}, Kaisheng Huang^{1, b, *} and Wei Zhong^{1, 2, c}

¹The Joint Laboratory for Internet of Vehicles, Ministry of Education - China Mobile Communications Corporation, State Key Laboratory of Automotive Safety and Energy, School of Vehicle and Mobility, Tsinghua University, Beijing 100084, China

China

²China North Vehicle Institute, Science and Technology on Vehicle Transmission Laboratory, Beijing 100072, China

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Abstract: The lane-changing decision-making is a great challenge in autonomous driving system, especially to judge the feasibility of lane-changing due to the randomness and complexity of surrounding traffic participants. Reinforcement learning has been shown to outperform many rule-based algorithm for some complex systems. In this paper, the single-step deep Q network algorithm is proposed by combining single-step reinforcement learning and deep Q network, and it is applied to judge the feasibility of lane-changing for autonomous vehicle. In a real-world-like and random traffic environment built in Carmaker, the trained agent can make correct judgment about the feasibility of lane-changing. Comparing the single-step deep Q network with the general deep Q network, although the general deep Q network can converge, there are still collisions, and the agent trained by single-step deep Q network is absolutely safe.

1 INTRODUCTION

The data shows that in the transportation system, 90% of the total number of traffic accidents are caused by driver improper operations (Aufrère, R, et.al, 2003). Autonomous vehicles are developed to eliminate driver errors to improve traffic safety. Typically, an autonomous vehicle consists of a perception module, a decision-making module and a control module (Li, D, et.al, 2018). The decision-making module makes correct decisions based on the information of sensors of the perception module. Making correct decision is challenging because of the influence of surrounding traffic participants. The lane-changing decision is particularly important because collision is more likely to happen when changing lane compared with driving in a single lane. In recent years, the lane-changing decision has gradually become one of the research focuses in the field of autonomous vehicles.

The methods of lane-changing decision of autonomous vehicle can be divided into two categories: rule-based and machine learning-based. Currently, rule-based methods have been widely used. And machine learning-based methods have also proven to perform better in many scenarios in recent years.

The main method of the rule-based lane change decision system is the finite state machine method. This method requires determining multiple states that an autonomous vehicle may execute, and then determining the switching conditions between the states (Schwarting, W, et.al, 2018). Representative works of this method are the 'Stanley' developed by Stanford University Thrun, S., et.al, 2006) and the 'Boss' developed by Carnegie Mellon University (Urmson, C, et.al, 2008). They decide to execute a lane-change decision based on some pre-set rules and thresholds. However, the rule-based method relies too much on the experience of engineers, and the pre-set states and thresholds have poor adaptability to complex traffic conditions. The developers of 'Junior' from Stanford University acknowledged that although the junior was able to complete the DARPA Challenge, it was unable to cope with real urban traffic (Chen, J, et.al, 2014).

In recent years, machine learning-based methods have become the focus of research in the field of decision-making. Researchers from NVIDIA (Bojarski, M, et.al, 2016), Intel (Codevilla, F., et.al, 2018) and Comma.ai (Santana, E., & Hotz, G, 2016) used an end-to-end supervised learning approach to train decision-making systems for autonomous vehicles. They used a car equipped with various sensors to collect data from all on-board sensors when the driver was driving the car. By training a convolutional neural network, the mapping of the camera's original image to the vehicle control parameters is completed. This method has a certain ability to adapt to complex traffic, but it requires a large amount of data collected in advance, which is difficult to manipulate in practice.

In addition to end-to-end supervised learning, reinforcement learning is also widely used in decision-making systems for autonomous vehicles. Reinforcement learning is an algorithm that teaches an agent so that it can perform correct actions in a random environment to get the maximum reward. Different from supervised learning, there is no fixed label for reinforcement learning. Trial and error methods are used to simulate the learning process. It is usually implemented in the fields of robot control (Gu, S., et.al, 2017), autonomous driving (Alizadeh, A., et.al, 2019), and gaming (Kamaldinov, I., & Makarov, 2019).

Desjardins et al. (Desjardins, C., & Chaib-Draa, B, 2011) used reinforcement learning to study adaptive cruise control system. They used policy gradient reinforcement learning to teach autonomous vehicle to follow the car in front. Ure et al. (Ure, N. K, 2019) introduced reinforcement learning based on the model predictive control adaptive cruise control system. Reinforcement learning is used to train model predictive control weights so that autonomous vehicles can perform better when facing more complex scenarios.

This paper introduces a single-step deep Q network algorithm. This algorithm combines single-step reinforcement learning with deep Q network algorithm. And it is used to train an autonomous vehicle to judge the feasibility of lane-change. In this way, the autonomous vehicle can make correct decision under different conditions, and ensure the safety of the lane-changing process.

2 REINFORCEMENT LEARNING

2.1 Deep Reinforcement Learning

In reinforcement learning, agent performs action according to a policy π . There are two ways to represent a policy. The first is expressed in the form of a function $a = \pi(s)$, which is a mapping of state space S to action space A. The second is expressed in the form of probability $\pi(s, a)$, so that $\sum_a \pi(s, a) =$ 1. In this paper, the policy is expressed as a function. The quality of a policy can be evaluated using a state-action value function $Q_{\pi}(s, a)$. The state-action value function is defined as the expected value of the cumulative reward from state s_t to state s_{∞} , when perform an action a_t at the state s_t and keep interacting with the environment according to the policy π , i.e.,

$$Q_{\pi}(s, a) = E_{\pi}(R_t | s_t = s, a_t = a)$$
 (1)

 R_t in (1) is the cumulative reward, and can be calculated as follows:

$$R_t = \sum_{k=0}^{\infty} \gamma^k r_{t+k} \tag{2}$$

Where r_{t+k} is the reward obtained by performing the action a_t in state s_t , and γ is the discount factor. Combining (1) and (2):

$$Q_{\pi}(s, a) = E_{\pi} \left(\sum_{k=0}^{\infty} \gamma^{k} r_{t+k} \, | s_{t} = s, a_{t} = a \right) \quad (3)$$

The basis of reinforcement learning is the Markov Decision Process (MDP), which means, the future state $\{s_t, ..., s_{\infty}\}$ of the agent is only related to the current state s_t , and not to the past state $\{s_1, ..., s_{t-1}\}$. Therefore, the Bellman equation of the state action value function can be derived by combining (3), i.e.,

$$Q_{\pi}(s,a) = \sum_{s'} P^{a}_{ss'} \left(R^{a}_{ss'} + \gamma Q_{\pi}(s',a') \right)$$
(4)

Where $P_{ss'}^a$ is the state transition probability, $R_{ss'}^a$ is the reward obtained when action a is taken and the state transfers from s to s'. And a' = $\pi(s')$.

The purpose of reinforcement learning is to obtain the optimum policy π_* to maximize the cumulative reward obtained by the agent, i.e.,

$$Q_{\pi_*}(s,a) = \max_{\pi} Q_{\pi}(s,a) \tag{5}$$

Combining (4) and (5) can get the optimal Bellman equation, i.e.,

$$Q_{\pi_*}(s, a) = \sum_{s'} P^a_{ss'} \left(R^a_{ss'} + \gamma max_{a'} Q_{\pi_*}(s', a') \right)$$
(6)

Reinforcement learning to find the optimal policy is to find the only solution for (6). Traditional reinforcement learning methods, such as Q learning, build a Q table to find the optimal solution. The columns of the Q table represent all states in the state space, and the rows represent all actions in the action space. The values in the table are Q values and they are updated according to (7).

$$Q(s,a) \leftarrow Q(s,a) + \alpha[r + \gamma \max_{a'}Q(s',a') - Q(s,a)]$$
(7)

Where α is learning rate.

This method has very good results when solving simple problems. But when the problem becomes more complicated, especially when the state variable is continuous, the curse of dimensionality will occur.

Deep Q Network (DQN) can solve the above problems well. DQN combines deep learning and reinforcement learning. It utilizes a neural network to get approximate Q values. Since the neural network can fit any function, DQN can successfully approximate the Q value, even if the state space is multidimensional and continuous.

The input of the neural network in DQN is state, and the output is the Q value of different actions. At each training step, DQN saves the current state s_t , action a_t , reward r_t and next state s_{t+1} to the replay memory, and samples a mini-batch of tuples (s_t, a_t, r_t, s_{t+1}) to train the neural network. The parameter of neural network θ is updated to minimize the loss function (8).

$$L = \frac{1}{m} \sum_{m} (r_{t} + \gamma \max_{a'} Q_{\theta'}(s_{t+1}, a') - Q_{\theta}(s_{t}, a_{t}))^{2}$$
(8)

 θ' is the parameter of target neural network, which has the same structure as θ , but is updated more slowly than θ .

2.2 K-armed Bandit Problem

K-armed bandit problem is a single-step reinforcement learning task, which maximizes the single-step reward. It is a mathematical model extracted from the scene of a multi-arm gambling machine in a casino. The k-armed bandit has k arms. After placing a coin, a gambler can choose to press one of the arms. Each arm spit out coins with a certain probability. The goal is to maximize the reward through a certain policy, that is, to get the most coins.

Similar to general reinforcement learning problem, the state-action value function is used to evaluate the quality of the policy. Since the K-armed bandit problem is a one-step reinforcement learning problem, the state of each execution is the same, and only the action is different, so it can be simplified into an action value function Q(a). Q(a) represents the expected reward obtained after executing action a. And after the n-th attempt of action a, Q(a) is updated as:

$$Q_{n}(a) = \frac{1}{n} [(n-1) \times Q_{n-1}(a) + r_{n}]$$
(9)

3 SCENE STATEMENT

The driver's decision to change lane usually consists of three steps: making a lane-changing plan, judging the feasibility of lane-changing, and executing lanechanging (Hidas, P, 2005). In this paper, we focus on the step of judging the feasibility of lane-changing. Generally speaking, the lane-changing plan is made by the higher-level path-planning module. It may be a free lane-changing due to obstacles ahead or a forced lane-changing to reach the destination. In this paper, we use a random number to simulate the lanechanging plan made by the driver. An LQR-based path tracking method is used to execute lanechanging with the goal of minimizing distance and deviation angle to the path at previewed point.

The research scenario of this paper is shown in Fig. 1. The autonomous vehicle expects to change from the current lane to the target lane, and there may be a leading vehicle and a following vehicle on the target lane.

 v_e , v_l and v_f are velocity of ego vehicle, leading vehicle and following vehicle respectively. d_l is the distance between the ego vehicle and the leading vehicle, and d_f is the distance between the ego vehicle and the following vehicle.

This paper aims to use reinforcement learning to teach autonomous vehicle to judge if it is proper to change lane, with the goal to start lane-changing as early as possible to improve traffic efficiency and avoid collisions during lane-changing.



Figure 1: Lane-Changing Scenario.

4 METHODOLOGY

In this section, how to train agent is described. The reinforcement learning model and the dynamic traffic environment are explained in detail.

4.1 Reinforcement Learning Model

We consider the process of an autonomous vehicle making a lane-changing decision as MDP. The autonomous vehicle is the agent which needs to be trained. The environment includes lanes, the conditions of the ego vehicle and vehicles in the target lane.

As described in Fig. 1, when the autonomous vehicle makes a lane-changing decision, the main basis is the condition of the ego vehicle and the condition of the ego vehicle relative to the vehicles in the target lane. So we took the absolute velocity of the ego vehicle v_e , the relative velocity between the ego vehicle and the obstacle vehicle $\Delta v_i = v_i - v_e$, and the relative distance d_i as the state representations. i represents 1 or f, that is, leading vehicle or following vehicle. If there is no vehicle in the position of leading vehicle or following vehicle, the relative distance d_i is set to the maximum distance of the sensor which is 200 m, and the relative velocity Δv_i is set to 0. The state vector consists of five continuous variables:

$$\mathbf{s} = [\mathbf{v}_{\mathbf{e}}, \mathbf{d}_{\mathbf{l}}, \Delta \mathbf{v}_{\mathbf{l}}, \mathbf{d}_{\mathbf{f}}, \Delta \mathbf{v}_{\mathbf{f}}]^{\mathrm{T}}$$
(10)

Generally, there are two actions that can be selected for autonomous vehicle: lane-changing or no lane-changing. In this paper, when the autonomous vehicle makes a lane-changing decision, the order cannot be withdrawn, which means the lane-changing decision must be the last step of each training episode. In addition, since the reward obtained by the agent after a decision of not changing lane is a fixed value, then an output of the neural network is also a fixed value, which does not make sense. Therefore, when training the agent, this paper only studies the last step of each training episode, that is, the step where the agent makes a lane-changing decision. In other words, there is only one action of the reinforcement learning model:

a: change lane.

The reward function is defined as follows:

$$r = \begin{cases} 1, & successful lane - changing \\ -5, & collision \end{cases}$$
(11)

The problem studied in this paper is a maximal single-step reward reinforcement learning problem

which is similar to the "K-armed Bandit Problem". Since there is only one action, the state-action value function is expressed as follows:

$$Q(s) = E(r_t | s_t = s)$$
 (12)

Where Q(s) represents the expected reward obtained when the lane-changing decision is performed in state s. It can be written as below:

$$\begin{cases} Q(s) = p_s(s)r_s + p_c(s)r_c \\ s.t. \quad p_s(s) + p_c(s) = 1 \end{cases}$$
(13)

Where $p_s(s)$ and $p_c(s)$ are the probability of successful lane-changing and collision after executing lane-changing in state s, respectively; r_s and r_c are the reward for successful lane-changing and collision, respectively. According to (11), $r_s = 1$ and $r_c = -5$.

The state variables are continuous values, so a neural network will be used to represent Q(s) combined with deep reinforcement learning. The parameters of the neural network were updated to minimize the loss function:

$$L = \frac{1}{m} \sum_{m} \left(r_t - Q(s) \right)^2 \tag{14}$$

Although only one action is set when establishing a reinforcement learning model, it does not mean that the autonomous vehicle can only execute lanechanging action. Autonomous vehicle will execute the action based on the value of Q(s). In this paper, as shown in (11), a successful lane-changing gets a positive reward while a failed lane-changing gets a negative reward, so the reward for not changing lane is set to a constant 0, which can be considered as the state-action value function that does not execute lanechanging. Therefore, the autonomous vehicle will choose whether to execute lane-changing based on Q(s):

 $Q(s) \ge 0$: change lane, and Q(s) < 0: not change lane.

4.2 Environment

In this paper, CarMaker developed by IPG Automotive GmbH is utilized as the simulator to build the traffic environment for training the autonomous vehicle. Compared to general traffic simulators, CarMaker is more focused on the vehicle itself, and has a better vehicle dynamics model. An illustration of CarMaker is shown in Fig. 2.



Figure 2: Screenshot of CarMaker.

A one-way road with two lanes is built in CarMaker as shown in Fig. 2. The yellow vehicle in the left lane is the autonomous vehicle studied in this paper. Its behaviour is controlled by our algorithm. There are several vehicles in the right lane. Their behaviours are controlled by both our settings and the IPG Driver model set by CarMaker. They run at random speeds according to our settings, but at the same time they meet the restrictions of the IPG Driver model. The minimum distance between them is $d_{min} = t_{safe}v + d_0$, where $t_{safe} = 1.5s$ is the headway time, $d_0 = 3m$ is the static distance to the front vehicle. All data of all vehicles, including vehicle speed and longitudinal position, can be provided directly by CarMaker.

5 TRAINING AND RESULT

5.1 Training Setup

In this paper, MATLAB is utilized to build and train the neural network, which is the Q value network. During the training process, the interaction between MATLAB and CarMaker-Simulink is shown in Fig. 3.

While training the agent, there is a balance between exploration and exploitation. If the agent chooses to explore only, then all the trial opportunities are evenly distributed to each state, and eventually the expected Q value of each state can be obtained, but obviously the training time is very long. On the other hand, if the agent chooses to exploit only, each time it only executes the action with the highest Q value. The training time is short, but it is difficult to get the global optimal solution.

Train Q-Value Network	Parameters of Network	Make Lane-Changing Decision
MATLAB	(s,r)	CarMaker-Simulink

Figure 3: Interaction between MATLAB and CarMaker-Simulink.

 ϵ -greedy algorithm is used to solve the problem of exploration and exploitation. The agent explores with a probability of ϵ and exploits with a probability of $(1 - \epsilon)$. When $\epsilon = 0$, the optimal action is chosen, and when $\epsilon = 1$, the agent chooses the action completely randomly. In this paper, instead of being a constant, ϵ will gradually decrease with training as below:

Algorithm 1: Single-Step DQN for Lane-			
Changing.			
Initialize replay memory D with infinite capacity			
Initialize state value function Q with random			
weights θ			
for episode $= 1$, M do			
Initialize action a: not change lane			
while a: not change lane do			
Read the state s from CarMaker			
Initialize a random number rnd \in (0,1)			
if $t > t_{start}$ then			
if rnd $< \varepsilon$ then			
Randomly select action a: change lane or not			
change lane			
else			
if $Q(s) > 0$ then			
a: change lane			
else			
a: not change lane			
end if			
end if			
end if			
end while			
Start lane-changing			
if collision then			
r = -5			
else			
r = 1			
end If			
Store transition (s, r) in D			
In episode > N_{start} then Source and any mini batch of transitions (2, 2)			
Sample random mini-batch of transitions (s_i, r_i)			
Perform a gradient descent step on $(r_i - Q(s_i))^-$			
with respect to θ			
end if			
end for			

$$\varepsilon = (\varepsilon_{\text{start}} - \varepsilon_{\text{end}})e^{\frac{-\frac{\text{episode}}{\varepsilon_{\text{decay}}}} + \varepsilon_{\text{end}}}$$
(15)

In the simulator, the speeds of all vehicles, including the ego-vehicle and traffic vehicles, change randomly and constantly. During the lane-changing process, the speed of the ego-vehicle will be constant, and the speeds of traffic vehicles are changing all the time to simulate the unknown behaviour of the surrounding vehicles in actual traffic.

In addition, to ensure the randomness of the initial conditions, we set a random start time $t_{start} \in (0,50)$ s. The training starts when the simulation time is bigger than t_{start} . This can be understood as the higher-level path-planning module making a lane-changing plan at t_{start} .

During training, in order to ensure that the agent has enough experience, we set a threshold for the number of replay memory N_{start} , and training will only start when the number of replay memory is greater than N_{start} .

The details of the single-step DQN algorithm used in this paper for the lane-changing decision are shown in Algorithm 1.

The algorithm consists of three steps. The first step is to determine whether a lane-changing decision could be made before making a lane-changing decision. The second step is that after the agent has made a lane-changing decision, the agent begins to change lane. The third step is to store the data in the replay memory after the lane-changing is completed (there may be a successful lane-changing or a collision), and train the agent with the data in the replay memory.

5.2 Training Configurations

A neural network with the structure shown in Fig. 4 is used to approximate the Q value function. It consists of two fully connected layers, each consisting of 50 nodes. The input is the state, and the output is the Q value for executing the action in that state, that is, the expected reward obtained by executing a lane-changing in the given state. The tanh function is selected as the hidden layer activation function.



Figure 4: Structure of the Neural Network.

The maximum training episodes M was set to 6,000. The threshold of the replay memory at the beginning of training N_{start} is 200, that is, the training does not start until the agent has completed 200 explorations. The Adam optimizer is selected to update neural network parameters with a learning rate of 0.001 and the mini-batch of 32. For ϵ -greedy algorithm, we set $\epsilon_{start} = 0.9$, $\epsilon_{end} = 0$ and $\epsilon_{decay} = 200$.

5.3 Results DELICATIONE

Since the initial state of each training episode is completely random, it is very likely that there is no obstacle vehicle in the target lane when the autonomous vehicle starts to make lane-changing decision, so the result of a single training episode cannot be used to evaluate the algorithm. In this paper, we use the number of collisions of the autonomous vehicle per 100 training episodes to evaluate the result. The result is shown in Fig. 5.

In addition, a general DQN method is used to solve the same problem as a comparison. The general DQN uses two actions, that is, the Q network has two outputs, one is the Q value for executing lanechanging, and the other is the Q value for not executing lane-changing. The reward is set as (16). The discount factor is 0.99. The replay memory capacity is 10,000. The frequency of updating the target Q network is 2,000. The result is also shown in Fig. 5.

$$r = \begin{cases} 1, & \text{successful lane} - \text{changing} \\ -5, & \text{collision} \\ 0, & \text{not execute lane} - \text{changing} \end{cases}$$
(16)

As shown in Fig. 5, the numbers of collisions for single-step DQN and general DQN both decrease during training. After 1,700 training episodes, there is no more collisions happening for single-step DQN. But general DQN cannot completely converge to 0. This shows that our algorithm can converge better. It can teach the autonomous vehicle to learn to judge the feasibility of lane-changing ensuring absolute safety.



Figure 5: Training Results.

6 CONCLUSIONS

In this paper, we proposed a new method to judge the feasibility when the autonomous vehicle is going to change the lane. The method combines the single-step reinforcement learning and the deep reinforcement learning. We use the single-step reinforcement learning framework that learns by solving the expected reward for executing different actions in the same state. Aiming at the problem of discontinuous states or actions in this framework, combined with the idea of DQN, a neural network is used to approximate the Q value function. The proposed single-step DQN algorithm judges the feasibility of lane-changing based on the lane-changing plan made by the highlayer path planning module and the surrounding vehicle state obtained by sensors. The instruction is sent to the low-level control module, which uses the LQR-based method to complete the lane-changing. The final results indicate that the proposed method in this paper can ensure that the lane-changing process of autonomous vehicle is absolutely safe.

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