Study on the Use and Adaptation of Bottleneck Features for Robust Speech Recognition of Nonlinearly Distorted Speech

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Abstract: This paper focuses on the robust recognition of nonlinearly distorted speech. We have reported (Seps et al., 2014) that hybrid acoustic models based on a combination of Hidden Markov Models and Deep Neural Networks (HMM-DNNs) are better suited to this task than conventional HMMs utilizing Gaussian Mixture Models (HMM-GMMs). To further improve recognition accuracy, this paper investigates the possibility of combining the modeling power of deep neural networks with the adaptation to given acoustic conditions. For this purpose, the deep neural networks are utilized to produce bottleneck coefficients / features (BNC). The BNCs are subsequently used for training of HMM-GMM based acoustic models and then adapted using Constrained Maximum Likelihood Linear Regression (CMLLR). Our results obtained for three types of nonlinear distortions and three types of input features show that the adapted BNC-based system (a) outperforms HMM-DNN acoustic models in the case of strong compression and (b) yields comparable performance for speech affected by nonlinear amplification in the analog domain.

1 INTRODUCTION

In recent years, it has been shown that hybrid HMM-DNN acoustic models (we further abbreviate HMM-DNN to DNN) yield significant Word Error Rate (WER) reduction over conventional HMM-GMM based systems for various speech recognition tasks, e.g., large-vocabulary recognition of clean speech (Dahl et al., 2012; Dahl et al., 2013) or multilingual acoustic modeling (Heigold et al., 2013).

This success motivates the utilization of DNNs for recognition of speech distorted by environmental conditions, such as additive noise or convolutive channel distortion. The work (Seltzer et al., 2013) demonstrates robustness of DNNs in a medium vocabulary task from the Aurora 4 noise database (Parihar and Picone, 2002). This paper shows that the featureextraction strategy employed in DNNs automatically derives noise-robust features from input data when multi-style training is available. However, the noiserobustness technologies can still be of value to DNN architecture (Delcroix et al., 2013), especially when the network is trained on clean data and tested on noisy data.

The utilization of many of the traditional robust speech recognition techniques is complicated in con-

nection with DNNs. Some of the methods need an underlying assumption that HMM-GMMs (we further abbreviate HMM-GMM to GMM) are used for the state likelihood evaluation. The potential solution to this problem is proposed in (Li et al., 2014). It consists of computing DNN-derived bottleneck coefficients (BNC, see for example (Deng et al., 2010)) and subsequently utilizing them in training of GMMs. The GMM based model can then be endowed with conventional robust speech recognition techniques, such as CMLLR (Gales, 1998).

In this paper, we investigate the usefulness and possibility of adaptation of BNC features to robust recognition of speech affected by *real-world nonlinear* distortions. Our goal is to take advantage of the modeling power of neural networks in combination with a channel adaptation method. As already mentioned, our work is motivated by findings in (Seps et al., 2014). It was shown there that DNNs are more robust with respect to nonlinear distortions than GMMs. However, GMMs endowed with adaptation to environmental conditions via CMLLR are able to match the performance of the former and even yield lower WER in some cases. We focus on:

1. Utterances distorted by nonlinear amplification (and potential clipping) in the analog domain and

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coded via a lossy codec optimized for speech perceptual quality.

- 2. Speech compressed via lossy compression to very low bit-rate quality.
- 3. Recordings denoised via spectral subtraction algorithms, which exhibit an unnaturally sparse spectrum.

In all these cases, we investigate mismatched training conditions, i.e., we train the models on clean data and test them on distorted datasets. This stems from the fact that the considered distorted data (with exception of the low bit-rate compression) are difficult to simulate or collect for multi-style training. Due to this fact, we do not consider any adaptation techniques, which need training and training data, such as i-vector computation proposed in (Saon et al., 2013) or training of the DNN on features adapted to considered distortions. We derive BNC features from three different types of input features including classical Mel Frequency Cepstral Coefficients (MFCCs) (Davis and Mermelstein, 1980), Filter Bank Coefficients (FBCs) (Deng et al., 2013) and Tempo-RAl Patterns (TRAPs) (Grézl and Fousek, 2008).

The paper is structured as follows. In Section 2 we describe the considered datasets of distorted speech. Section 3 presents our implementation of the bottle-neck features. Section 4 specifies the details of our experimental setup. Section 5 summarizes the results of our investigation and conclusions are drawn.

2 CONSIDERED DISTORTIONS

In our study, we consider the types of real-world nonlinear distortions mentioned below. More information on the datasets and distortions can be found in (Seps et al., 2014).

2.1 Nonlinear Amplification in the Analog Domain

This distortion is caused by an erroneous excessive setting of the analog preamplifier. Then the preamplifier becomes saturated and amplifies the input signal in a nonlinear way. In extreme, the signal becomes clipped prior to sampling. Subsequently, the signal is sampled and coded by a lossy codec. After coding, the potential clipping becomes difficult to detect, as the characteristic flat amplitude level disappears in the signal domain. Both the nonlinear amplification and the potential clipping may affect perceptual quality of the speech (Licklider and Pollack, 1948). Our distorted dataset consists of eight lectures given in Czech (11 hours and 45 minutes of speech, 85396 words), recorded for streaming purposes at our university. The signal is captured by a close-talk microphone. The common background noise of a lecture hall is present in the recording. The recordings were originally sampled at 44.1 kHz and then compressed by wma2 lossy codec (bit-rate 266 kbps), optimized for perceptual quality suitable for human listeners. Prior to recognition, the signals were downsampled to 16 kHz. The dataset is denoted as "Lectures" in the experiments.

2.2 Lossy mp3 Compression to Low Bit-rate

Low-bit-rate *mp3 compression* neglects frequency components which are considered inaudible based on a psychoacoustic model. The decompressed signal exhibits many zeros in the time-frequency domain. The compression to low bit-rates (<24 kbit/s) causes suppression of phonemes at word boundaries, which deteriorates the ASR accuracy (Pollak and Behunek, 2011; Seps et al., 2014).

Our dataset of compressed utterances consists of 22 recordings (1 hour and 12 minutes of speech, 8096 words) of *radio broadcasts*. Spontaneous speech by various speakers was recorded at a sample rate of 16kHz. Subsequently, an mp3 compression was applied at a bit-rate of 16 kbit/s in order to present the recordings on the web page of a radio station. The dataset is denoted as "MP3" in the experiments.

2.3 Spectral Subtraction Denoising

The *denoising* based on spectral subtraction estimates the magnitude/power spectrum of the noise. This estimate is subsequently subtracted from the spectrum of speech. Excessive denoising may lead to unnaturally sparse speech spectrum and/or various artifacts, such as musical noise. These artifacts deteriorate the performance of ASR (Vaseghi, 2008).

The dataset affected by excessive denoising consists of 1161 *short Czech utterances* read by various speakers, recorded with a close-talk microphone. The total duration of the dataset is 1 hour and 45 minutes, and it contains 12780 words. The original sampling frequency of 44.1 kHz was downsampled to 16 kHz. During the recording, a denoising method provided by software drivers of the sound device was turned on. No additional compression was applied to the data. The dataset is denoted as "Denoised" in the experiments.



Figure 1: The process of generation of bottleneck coefficients.

3 EXTRACTION OF BOTTLENECK COEFFICIENTS

Bottleneck coefficients are generated via a deep neural network containing one hidden layer with a small number of neurons compared to other layers. This small layer forces the network to concentrate the crucial information for the classification into a lowdimensional representation. The output of the small layer forms the BNC features. The original method of extraction is based on auto-encoders, i.e., the network is trained to predict the input features (Deng et al., 2010). Other implementations include prediction of (a) states of context-independent monophones (Grézl et al., 2007) or (b) physical states (socalled "senones") of context-dependent tied-state triphones (Yu and Seltzer, 2011). The input features can be classical MFCCs or short/long-term energy of speech in critical bands (Grézl and Fousek, 2008).

In this paper, we adopted the process of generating BNCs and their utilization in a GMM acoustic model as depicted in Fig. 1. It can be described as follows:

- 1. A type of *input features* is computed. We consider three different types as described in the next Section 4.1.
- 2. A *deep neural network* is trained using state alignments generated by the baseline tied-state context-dependent GMM system which utilizes conventional MFCC features. The network has five hidden layers, all but one having 1024 units. The middle (third) layer forms the bottleneck with only 128 units and its output gives the raw bottleneck features. Details on the training configuration can be found in Section 4.2.
- 3. An optional third step consists in a concatenation

of the raw bottleneck feature vector with the conventional MFCC features. This stems from the fact that MFCCs are considered to be highly effective features. When alternative long-term features are used as the input for the neural network, the resulting bottleneck coefficients have the potential to capture information complementary to MFCCs (derived from the short-time spectra).

4. The raw/concatenated BNCs are analyzed using the *Principal Component Analysis* (PCA, (Jolliffe, 2002)), in order to decorrelate the features and lower the dimension of the resulting feature vectors. After the application of PCA, 39 decorrelated features are always kept, which form the final bottleneck features. The number of 39 features is the common length of a traditional MFCC feature vector. The reduction performed in this manner always keeps more than 97% of the energy of the analyzed features.

4 EXPERIMENTAL SETUP

4.1 Types of Features Used

We consider the following three types of input features. All are computed from recordings sampled at 16 kHz. We use frames of a 25 ms length and a frameshift of 10 ms as is standard in speech processing.

MFCC - We utilize 13 static coefficients, with delta and delta delta parameters. The input feature vector consists of coefficients from 11 concatenated frames, five preceding and five following the current frame. It thus contains $11 \times 39 = 429$ features.

FBC - Filter Bank Coefficients (described for example in (Deng et al., 2013)) are given as short-term mel-scaled log energy given in 29 critical frequency bands, supplemented by the total log energy of the current frame. We add the delta and delta-delta parameters to the static coefficients. The input feature vector consists of coefficients from 11 concatenated frames, five preceding and five following the current frame. It thus contains $11 \times 90 = 990$ features.

TRAP - TempoRAl Patterns (Grézl and Fousek, 2008) are defined as short-term mel-scaled log energy given in 23 critical frequency bands, *supplemented by the total log energy* of the current frame. Next, 300 ms (31 frames) long energy trajectories are transformed by Discrete Cosine Transform and the first 16 coefficients are retained. The input feature vector consists of $24 \times 31 = 384$ elements.

Potentially, various combinations of the above input features can be considered and submitted to the network for selection of the most representative bottleneck features. This is however beyond the scope of the current paper.

4.2 Training of Deep Neural Networks

The DNN-based acoustic models as well as networks for generating the bottleneck features are trained to provide scaled likelihood estimates for physical states of the baseline GMM model using MFCC input features. The Theano library (Bergstra et al., 2010) is used for training, which has a fixed duration of 50 epochs and is carried out using settings from (Grézl and Fousek, 2008): The activation function is sigmoid. Each hidden layer consists of 1024 units. The potential bottleneck layer has 128 units. The mini-batch size is 1000 and the learning rate is 0.08.

4.3 GMM Acoustic Models and CMLLR Adaptation

Regardless of the input features, speaker-independent and context-dependent tied-state HMMs of Czech phonemes and several types of non-speech events (e.g., breathing, various hesitation sounds, cough, lipsmack, etc.) are utilized.

In all these cases, the training parameter which controls the tying of states is set to the same value so that the resulting model contains 4k physical states with up to 32 Gaussian components per state (i.e., 120k components in total).

The models are adapted to given acoustic conditions using an unsupervised procedure, which runs in two recognition passes as follows:

In the first pass, we utilize the default model to obtain phonetic transcript of the given recording. The recording is then split into 5-minute-long segments. For each such segment, CMLLR is employed to estimate a global linear transformation matrix using the created phonetic transcript and the given acoustic model. Then, the second speech recognition pass is performed, where the estimated transforms are applied on all feature vectors belonging to the corresponding segments. We estimate the CMLLR transform using the frames containing speech only; the frames corresponding to noises are left out.

4.4 Recognition System Employed

The investigation is performed using our own ASR system for Czech language. Its core is formed by a one-pass speech decoder performing a time-synchronous Viterbi search.

The lexicon of the system contains 550k entries (word forms and multi-word collocations) that were observed most frequently in a 10 GB large corpus covering newspaper texts and broadcast program transcripts. Some of the lexical entries have multiple pronunciation variants. Their total number is 580k.

The employed Language Model (LM) is based on N-grams. For practical reasons (mainly with respect to the very large vocabulary size), the system uses bigrams. In the training word corpus, 159 million unique word-pairs (1062 million in total) belonging to the items in the 550k lexicon were observed. However, 20 percent of all "word-pairs" actually include sequences containing three or more words, as the lexicon contains 4k multi-word collocations. The unseen bigrams are backed-off by the Kneser-Ney smoothing technique (Kneser and Ney, 1995).

5 EXPERIMENTAL EVALUATION

We present a comparison of WER achieved by the investigated acoustic models. The results are summarized in Table 1. All discussed WER improvements are meant as absolute. We use the notation "Acoustic Model: Features" (for example GMM:MFCC) to describe the considered configurations of our systems. By "aGMM" we denote the adapted GMM acoustic models.

Along with the three distorted datasets described in Section 2, we also present baseline accuracy achieved on recordings without any nonlinear distortion. The dataset, denoted as "News", consists of radio broadcasts of Czech news (2 hours and 59 minutes of speech, 25991 words). The recordings contain read utterances as well as the spontaneous speech of several speakers. The recordings are sampled at 16 kHz.

5.1 Comparison of BNC and MFCC Features within the GMM System

The baseline GMM:MFCC system exhibits performance comparable to all GMM:BNC systems on the undistorted dataset "News". On distorted data sets "MP3" and "Denoised", almost all of the GMM:BNC systems achieve significantly lower WER (by 9.8-17.5% or 16.2-21.3%, respectively). We explain it partly by the fact that the neural network is able to use the temporal context of the input features to complement the information that is missing within short-term MFCCs computed from distorted utterances.

This holds for neural network used for feature extraction as well as for DNN acoustic model. It is noticeable especially for the "MP3" dataset, which we

Model	Features	News	Mp3	Denoised	Lectures
DNN	MFCC	10.08	19.45	15.29	47.85
DNN	TRAP	9.72	22.84	13.69	46.65
DNN	FBC	9.38	26.10	12.94	44.80
DNN	FBC (No context)	10.35	43.00	15.73	50.56
GMM (Baseline)	MFCC	13.48	43.42	45.22	56.11
GMM	BNC(MFCC)	16.20	25.89	29.05	58.88
GMM	BNC(FBC)	13.99	33.67	23.90	54.86
GMM	BNC(TRAP)	14.13	26.45	24.19	55.20
GMM	BNC(FBC)+MFCC	12.61	28.50	19.85	52.59
GMM	BNC(TRAP)+MFCC	12.87	23.79	21.21	53.93
aGMM	MFCC	11.32	21.44	37.94	48.22
aGMM	BNC(MFCC)	14.95	21.32	28.35	53.87
aGMM	BNC(FBC)	13.09	22.49	23.10	48.00
aGMM	BNC(TRAP)	13.08	20.41	23.35	48.53
aGMM	BNC(FBC)+MFCC	11.78	19.05	18.73	45.65
aGMM	BNC(TRAP)+MFCC	11.90	18.61	20.10	47.04

Table 1: Word Error Rates (WER) achieved on the considered datasets. Bold numbers indicate the best results among competing systems. Abbreviation "aGMM" denotes the adapted GMM acoustic models.

demonstrate in Table 1 in row "DNN:FBC(no context)". Here, the performance drops significantly, when the input features consist of only the current frame, not the 11 consecutive frames.

The GMM:BNC systems achieve only slightly better WER on the "Lecture" dataset (by 1.3% at most), which suggests that neural networks are not inherently robust with respect to this type of distortion, as discussed in more detail in Section 5.3.

The concatenation of MFCC and BNC features is beneficial for the GMM:BNC systems (as was reported for undistorted data in (Grézl and Fousek, 2008)). It reduces the WER values by 1.3-5.2% compared to non-concatenated BNCs, depending on the dataset and input features.

The CMLLR enhances the performance of GMM:BNC systems on all distorted datasets. The adaptation leads to the highest WER reduction for compressed utterances (11.2%) and the "Lecture" dataset (6.9%).

5.2 Comparison of DNN and aGMM:BNC Acoustic Models

The aGMM:BNC systems, based on either TRAP or FBC, outperform the DNN systems on the "MP3" dataset and yield comparable results on the "Lectures" dataset. For the other datasets, the DNN systems achieve lower values of WER.

The best input features, for both DNN acoustic models and bottleneck feature extraction, consists of the FBC. This observation confirms that the less processed short-term features form a more suitable input for DNN models than conventional MFCC parameters, as suggested, for example, in (Deng et al., 2013).

The computational demands of the aGMM:BNC systems are high compared to DNN acoustic models. Two models need to be trained (neural network and the subsequent GMM acoustic model) and two recognition passes are required to adapt the bottleneck features.

5.3 Robustness of Investigated Systems with Respect to Considered Distortions

For the "MP3" dataset, the performance of the best DNN:FBC system deteriorated and was surpassed by both other DNN systems and aGMM:BNC. We argue (based on a complementary experiment) that this is caused by a sensitivity of the DNN:FBC system to the normalization of the input features. In all of our experiments, we perform a robust normalization by subtraction of the mean value estimated on the training dataset as a whole. Due to the compression of the test set, the true mean value of the test set significantly differs from the mean estimated in this manner, which deteriorates the results of DNN:FBC. On other datasets, this deteriorating effect is not significant. The DNN:MFCC is more robust in this context, because the conventional computation of MFCCs includes Cepstral Mean Subtraction (CMS), i.e. a mean normalization within each training and test utterance. The performance of GMM:BNC systems seems to be

uninfluenced by the effects of the normalization.

The DNN models appear insensitive to the spectral subtraction artifacts contained in the "Denoised" dataset. The performance of the DNN system is near to the level achieved on undistorted data. The best GMM:BNC system is outperformed by 5.7% due to the low efficiency of the CMLLR adaptation. The reason is that the test data consists of very short sentences (3 - 10 s long), which provide an amount of data too small for estimating CMLLR.

The nonlinear analog amplification (and potential clipping) within the "Lecture" dataset is very harmful to both types of models and all feature configurations. Additional robust recognition techniques need to be utilized for this type of distorted data (a partial solution can be offered, e.g., by clipping removal proposed in (Eaton and Naylor, 2013)).

6 CONCLUSIONS

We investigated the robustness of bottleneck-based systems endowed with feature adaptation with respect to nonlinear distortions in speech. We showed that the bottleneck features are more robust than the conventional MFCCs. On most considered datasets, the bottleneck-based GMM models, adapted to given distortions, achieve performance comparable to the DNN models. However, the BNC-based systems are much more demanding computationally, which hinders their utilization.

The most robust acoustic model in our experiments was the DNN model using FBC input features. This is in accord with the results presented for clean speech in literature; low-level frequency features represent an input more suitable for DNN systems than conventional MFCCs.

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