Search-based Decision Ordering to Facilitate Product Line Engineering of Cyber-Physical System

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Abstract:

Industrial Cyber Physical Systems (CPSs) are naturally complex. Manual configuration of CPS product lines is error-prone and inefficient, which warrants the need for automated support of product configuration activities such as decision inference and decision ordering. A fully automated solution is often impossible for CPSs since some decisions must be made manually by configuration engineers and thus requiring an interactive and step-by-step configuration solution. Having an interactive solution with tool support in mind, we propose a search-based solution (named as Zen-DO) to support optimal ordering of configuration steps. The optimization objective has three parts: 1) minimizing overall manual configuration steps, 2) configuring most constraining decisions first, and 3) satisfying ordering dependencies among variabilities. We formulated our optimization objective as a fitness function and investigated it along with four search algorithms: Alternating Variable Method (AVM), (1+1) Evolutionary Algorithm (EA), Genetic Algorithm, and Random Search (a comparison baseline). Their performance is evaluated in terms of finding an optimal solution for two real-world case studies of varying complexity and results show that AVM and (1+1) EA significantly outperformed the others.

1 INTRODUCTION

Cyber-Physical Systems (CPSs) are large-scale systems of systems communicating with each other based on digital cyber technologies, integrating software and physical components, and interacting with environment and human actors. CPSs are often seen in various domains including aerospace, energy and maritime, and healthcare. Product Line Engineering (PLE) is gaining increasing attention of researchers and practitioners because of its capability to deal with the increasing complexity and variation in software/system product lines (Frakes and Kang, 2005). Adopting PLE has shown to be effective for improving the quality of products and the productivity of developing the products. It has been reported in (Ali et al., 2012) that PLE can effectively speed up time-to-market in many organizations such as Boeing, Lucent, and Nokia.

Due to the inherent complexity of CPSs, hundreds and thousands of reusable components (e.g., electronic components, software components or network component) are typically and integrated and configured. Therefore automated support based on concise abstractions of reusable artifacts becomes crucial to the configuration process, where abstraction plays a central role for software reuse while automation can facilitate effective selection and customization of reusable components. Such an automated configuration solution heavily relies on a large number of constraints, which can be formally specified using e.g., the Object Constraint Language (OCL) (OMG) to facilitate, for instance, automated decision inference based on dependencies of Variation Points (VPs) (i.e., configurable parameters) and the optimization of configuration steps. Our previous work (Nie et al., 2013b) classifies different types of constraints that should be explicitly captured and specified on product line or product models to enable automation in the context of CPS PLE.

We have proposed an interactive configuration framework, named as Zen-Configurator (Kunming Nie, 2013, Hong et al., 2014, Hong et al., 2015, Nie et al., 2013), with the aim to implement at least three functionalities: Decision Inference, Decision

Ordering and Conformance Checking. A user interface has been developed; the decision inference and conformance checking functionalities have been implemented (Hong et al., 2014). The decision ordering functionality of Zen-Configurator should take the product line architecture model (including constraints) as input, order configuration decisions (VPs) in an optimized way such that overall manual configuration steps are minimized, which is the focus of this paper.

In the literature, different methods have been proposed to address this problem such as applying SAT Solvers for ordering decisions (Nohrer and Egyed, 2011), relying on Constraint Satisfactory Problems (CPS) solvers to derive valid feature selection sequences (White et al., 2009), and prioritizing features based on their selectivity (Chen and Erwig, 2011). All these works handle relatively simple dependencies among variabilities, i.e., decision or feature selection. However, based on our previous experience of stusdying three industrial CPS product line families (Nie et al., 2013b), configuring CPSs require handling complex constraints, thus indicating the insufficiency of these work. Some configuration tools (e.g., Pure::Variants (Beuche, 2008), Dopler (Dhungana et al., 2011), Covamof (Sinnema et al., 2004), SPLOT (Mendonca et al., 2009), FMP (Czarnecki et al., 2005), and Questionnaire (La Rosa et al., 2009)) implemented the decision ordering functionality in various ways: based on user predefined configuration sequences, deriving configuration sequences from dependencies of variabilities, and simply applying depth first strategy to traverse feature models. None of these tools implemented the objective of minimizing manual configuration steps—the main objective of this work. As reported in (El-Sharkawy and Schmid, 2012), the Dopler tool suite (Dhungana et al., 2011) is the only tool that implements the heuristic of configuring most constraining decisions first to reduce overall configuration effort, which aligns with part of our objective.

In this paper, we propose a search-based solution (named as Zen-DO) to support optimal ordering of configuration decisions of CPS product lines. We propose and assess a fitness function for minimizing manual steps required to configure a product, while fulfilling configuration ordering dependencies of VPs to the maximum extent and starting from most constraining configuration decisions first. We evaluate the fitness function together with four search algorithms: Alternating Variable Method Genetic Algorithms (1+1)(AVM), (GA),Evolutionary Algorithm (EA) and Random Search

(RS). RS was used as the baseline to evaluate the performance of the other three algorithms. Two real-world case studies and 130 artificial problems have been used to evaluate the selected search algorithms and the fitness function. Results show that AVM and (1+1) EA significantly outperformed the other two algorithms for both of the real-world case studies and most of the artificial problems.

The rest of the paper is organized as follows. In Section 2, we provide an overview of Zen-Configurator and Zen-DO, and relevant background information. Section 3 presents the formalization of the optimization problem and the fitness function. The empirical study and the controlled experiment are discussed in detail in Section 5 and Section 6, respectively. We present the overall discussion in Section 6. We addresses the threats to validity of the empirical study in Section 7. Section 8 discusses the related work. We conclude the paper in Section 9.

2 OVERVIEW

In this section, we first introduce Zen-Configurator and then the overview of Zen-DO.

2.1 Zen-Configurator

As previously discussed, in the context of CPS PLE, there are a large number of VPs that have to be configured correctly by conforming to a large number of constraints. Product configuration is therefore an error-prone and time-consuming activity when it is totally manual. Hence, it is important to have an interactive and semi-automated configuration solution for CPS PLE.

PLE is composed of two distinct phases: Domain Engineering and Application Engineering. In domain engineering, PLA modelling and constraint specification approaches are used by a Domain Expert to capture commonalities and variabilities in the system architecture and design and constraints relevant to the configuration of a valid product. In different contexts, different modelling and specification approaches can be used. As part of the Zen-Configurator solution, we rely on SimPL (Behjati et al., 2013), which is a modeling methodology with a UML profile for specifying commonalities and variabilities of a product line of integrated control systems at the architecture and design level. SimPL was developed to deal with four types of variabilities: Cardinality, Attribute, Topology and Type. As shown in Figure 1, a subsea production system that may have more than one

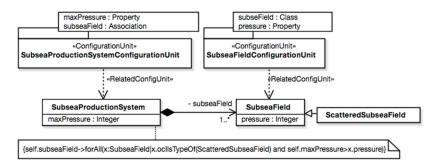


Figure 1: An Example of SimPL Model (Excerpted From (Behjati et al., 2013)).

subsea fields with various types, such as scattered subsea fields. Two template packages are stereotyped with <<ConfigurationUnit>> and associated to classes SubseaProductionSystem and SubseaField to specify the VPs of each of these two classes. As an example, we specify one OCL constraint for this model, that is, all the subsea fields are scattered subsea fields and the pressure of all subsea fields is less than the max pressure of a subsea production system.

In the application-engineering phase, Zen-Configurator has three key functionalities (*Decision Inference*, *Decision Ordering* and *Conformance Checking*), to assist configuration engineers to configure a product. PLA models and constraints of the product line are considered as product line assets stored in a repository, which are used as the input to facilitate the automation of configuring products. Configured products are therefore stored in the *Product Artifacts Repository*. We have previously implemented an automated and incremental conformance checking approach, named Zen-CC, to ensure that the manual configuration of each VP conforms to a set of pre-defined conformance rules specified in OCL (Hong et al., 2014).

Zen-Configurator relies on a set of algorithms that implement a set of heuristics (e.g., determining optimal decision orders), which are identified as key elements to optimize the effectiveness and efficiency of the configuration solution. These algorithms need to access the PLA models and constraints at runtime and therefore, it is crucial to have a lightweight internal representation capturing sufficient information for supporting efficient configuration. In Zen-Configurator, we use Trees (e.g., with nodes representing VPs and edges denoting dependencies) for this purpose. Automated transformation from the PLA models and constraints (SimPL and OCL respectively) to *Trees* is needed in Zen-Configurator. Zen-Configurator also needs to employ search algorithms for optimal decision ordering, which require encoding of the problem, a

fitness function to assess a solution, and parameter settings specific to each search algorithm. The focus of the paper is to propose such a search-based decision ordering solution.

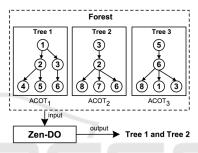


Figure 2: Illustrative Example of Zen-DO.

2.2 Zen-DO

In a typical PLE practice, a product line specification captures commonalties and variabilities of a product line. For example, feature models (Czarnecki et al., 2005) are commonly used for this purpose. VP is a configurable element of a product line specification and it defines the place of the variability. A variant is one of the possible choices to be bound for a VP. VPs can be specified in different ways, including value range, constraints, or enumeration literals, depending on applications. When resolving a VP, a variant is bound to the respective VP. A Constraint, in our context, is an element of system specification constraining one or more other elements to support automated product configuration.

Zen-Configurator is an interactive configuration tool that interacts with users, in our context *Configuration Engineers*, to configure a product line family and derive a set of family members: products. Configuration engineers in this configuration environment are considered as part of the optimization as they receive feedback (on which decisions to make first) from the tool and configuration engineers' manual decisions trigger the configuration tool to dynamically find other

optimized configuration orders based on the remaining VPs to be configured in the whole configuration space (all VPs should be configured and all constraints should be satisfied to various extents). This kind of configuration design is called "User-in-the-loop" (Sayyad et al., 2013).

VPs and constraints are taken as input by the tool. Note that as we investigated in our previous work (Nie et al., 2013b), decision ordering in such a user-in-the-loop interactive configuration environment relies on two types of constraints: variability dependencies and ordering constraints. These constraints can be either user defined, derived from system specifications, or enforced by a particular system development process. These constraints, together with the product line architecture model, contribute to the formation of the internal representation: *Forest* consisting of a set of *Trees*, which are necessary to formulate our optimization problem, thereby proposing the fitness function.

Suppose we have obtained such a set of constraints, applying each constraint will form an ordering tree with nodes representing VPs to be configured and edges describing which VP should be configured before or after which other VP(s). By applying all the identified constraints, a forest is formed, containing a set of trees (each of which corresponds to a constraint constraining the configuration sequence of a set of VPs) and having each yet-to-be configured VP covered in the forest. In the forest, all the yet-to-be configured VPs must be configured to obtain a product.

We then apply search algorithms to derive a set of trees based on three heuristics: 1) covering yet-tobe configured VPs as many as possible, 2) minimizing the number of Abstract Configuration Ordering Trees (ACOTs) to be contained in a solution, and 3) minimizing the manual steps required to configure a product. For example, as shown in Figure 2, Tree 1 and Tree 2 were selected as the optimal solution given the forest, because these two trees cover all the VPs (1-8) and form a solution with the minimum number of trees (i.e., 2). An optimal solution (Tree 1 and Tree 2) will be provided to configuration engineers and they will select any of the root nodes of these trees (representing VP1 and VP3) to configure them manually. The consequence of this manual configuration is that the remaining VPs to configure will be updated. Therefore, the forest will be updated and the optimization process will start to find another solution for the new updated forest.

It is important to notice that our optimization solution is independent of any product line

specification or modeling methodology as the optimization starts from the forest, which captures all the required information for the optimization. This gives us the freedom to make this work applicable to different contexts such as combing with feature models or architecture and design based variability modeling methodologies. However, as an integrated part of Zen-Configurator, a transformation from SimPL to the internal representation (Trees) has been implemented.

3 PROBLEM REPRESENTATION AND FITNESS FUNCTION

3.1 Definitions

A forest F is a set of Configuration Ordering Trees and is defined as $F = \{COT_1, COT_2, ..., COT_{ncot}\}$, where *ncot* is the total number of configuration ordering trees.

 $VP = \{vp_1, vp_2, ..., vp_{nvp}\}\$ is a set of VPs, where nvp is the total number of VPs to be configured. Each vp_i in VP has an attribute Configured of type Boolean.

Configuration Ordering Tree (COT) is a tree of in the F forest defined above. $COT = \{\{Node\}\}\$ {Edge}}. Note that it is also possible that a COT only constrains one node. Each node represents a VP from VP. Each edge represents an ordering dependency of two VPs. $Edge = \{e_1, e_2, ..., e_{ne}\},\$ where each edge e_i connects a pair of vp_k and vp_j from *Node*. Each edge e_i has a set of attributes: Manual and Infer of type Boolean, respectively indicating whether a configuration step is manual or can be automatically inferred. Such information can only be obtained using heuristic rules, as it is impossible to know in advance which step is manual and which step can be automatically inferred based on pre-defined constraints, as the whole process is dynamic and interactive. For example, one simple heuristic rule could be that VPs that are configurable parameters with primitive types but are not involved in any pre-defined constraint are most probably required to be manually configured. Another example is that for VPs with primitive types have high chance to be automatically inferred when they are involved in constraints with other VPs that are already configured. Note that implementing these heuristics to predict this property of a configuration step is out of the scope of this paper and will be automated in the future.

Each edge of a COT is also characterized with

another attribute *Weight* with three categories: *High*, *Medium* and *Low*, each of which respectively indicates the extent of dependency of two VPs. There are several ways to obtain this information. One commonly used way is to ask user's preference on the configuration order, which might not be classified as *Medium* and *Low*. Some dependencies should be classified *High* as configuring one VP depends on the decision made for another VP. Such information can be automatically obtained by querying variability models or constraints on VPs.

Abstract Configuration Ordering Graph (ACOG) consists of a set of nodes and edges: $ACOG = \{\{AbstractCOT\}, \{AbstractEdge\}\}\}$. AbstractCOT = $\{acot_1, acot_2, ..., acot_{nan}\}$, where each $acot_i$ is a COT. AbstractEdge = $\{ae_1, ae_2, ..., ae_{nae}\}$, each ae_i connects a pair of $acot_i$ and $acot_k$. Note that edges in AbstractEdge do not have attributes.

3.2 Optimization Problem

For configuration, there is a subset of *AbstractCOT*: $\{acot_1, acot_2, ... acot_{n_{acot}}\}$, based on which a set of potential solutions $S_{AbstractCOT} = \{s_1, s_2, ... s_{ns}\}$ can be derived, where ns is the total number of solutions and can be calculated as $2^{n_{acot}} - 1$. For each s_i , there is $nacot_i$ belonging to $S_{NACOT} = \{nacot_i, nacot_2, ..., nacot_{ns}\}$, where $l = \langle nacot_i \rangle = \{nacot_i, nacot_i \rangle = \{vpcot_i, vpcot_2, ..., vpcot_{ns}\}$, where $l = \langle vpcot_i \rangle = \{vpcot_i, vpcot_2, ..., vpcot_{ns}\}$, where $l = \langle vpcot_i \rangle = \{vpcot_i, vpcot_2, ..., vpcot_{ns}\}$, where $l = \langle vpcot_i \rangle = \{vpcot_i, vpcot_2, ..., vpcot_{ns}\}$, where $l = \langle vpcot_i \rangle = \{vpcot_i, vpcot_2, ..., vpcot_{ns}\}$, where $l = \langle vpcot_i \rangle = \{vpcot_i, vpcot_2, ..., vpcot_{ns}\}$, where $l = \langle vpcot_i \rangle = \{vpcot_i, vpcot_2, ..., vpcot_{ns}\}$, where $l = \langle vpcot_i \rangle = \{vpcot_i, vpcot_2, ..., vpcot_{ns}\}$, where $l = \langle vpcot_i \rangle = \{vpcot_i, vpcot_2, ..., vpcot_{ns}\}$, where $l = \langle vpcot_i, vpcot_3, vpc$

- Covering VPs that appear in the forest as many as possible. Our aim is to find s_i such that the maximum number of VPs that appear in the forest should be included in the abstract nodes of s_i . This is to ensure that most of the VPs in the forest should be taken into account when making a configuration ordering plan (a solution to search). We define the following formula for this aim: $\forall k: S_{NACOT}, vpcot_i > vpcot_k, where i \neq k$. This heuristic tries to find a solution s_i with the maximum number of VPs.
- Starting from most constraining configuration decisions. To achieve this, a search algorithm must guide the search towards large abstract nodes having the largest number of VPs connected to them. Recall that when constructing the forest, a constraint is applied to form a tree in the forest. Therefore, large trees (i.e., large abstract nodes) reflect complex constraints restricting large numbers of VPs. Hence, we define this formula for this heuristic, which later

- on is translated into a part of the fitness function: $\forall k: S_{NACOT}, nacot_i < nacot_k, where i \neq k$, meaning to find a solution s_i with the minimum number of abstract nodes in *AbstractCOT*.
- Searching for a solution with the minimum number of manual configuration steps. To achieve this, we defined formula:

$$(\sum_{k=1}^{n_{eS_i}} 1, where \ e_k.manual = true) < (\forall j = 1 \ to \ ns \ and \ i \neq j, \sum_{l=1}^{n_{eS_j}} 1, where \ e_l.manual = true).$$

• Guiding the search towards the direction of satisfying dependencies of VPs to the maximum extent. Recall that the edges in the trees of the forest are weighted with three categories: High (0), Medium (1), Low (2), indicating to which extent configuration ordering dependencies of VPs should be satisfied while deriving a solution. We use the following formula to formulate the heuristic:

$$(\sum_{k=1}^{n_{eS_{i}}} \begin{cases} 0, where \ e_{k}. weight = 'High' \\ 1, where \ e_{k}. weight = 'Medium' < (\forall \ j = 1 \ to \ ns \ and \ i \\ 2, where \ e_{k}. weight = 'Low' \end{cases}$$

$$\neq j, \sum_{l=1}^{n_{eS_{j}}} \begin{cases} 0, where \ e_{l}. weight = 'High' \\ 1, where \ e_{l}. weight = 'Medium' \\ 2, where \ e_{l}. weight = 'Low' \end{cases}$$

3.3 Fitness Function

Based on the definitions and the formulated optimization problem, we derive the fitness function that is used along with the six selected search algorithms to find optimal solutions for our optimization problem.

The fitness function (formula (1)) is composed of four parts, which are defined in formulas (2)-(5), respectively. These four formulas correspond to the heuristics described in the previous section. We applied the division method in the fitness function to normalize values produced by formulas (2)-(5) so that each heuristic has equal importance. n_{acot} is the total number of nodes in AbstractCOT. $\sum_{l=1}^{n_{acot}} ne_l$ represents the total number of edges in AbstractCOT. Our objective is to minimize $f(s_i)$, i.e., searching a value of $f(s_i)$ closer to 0 (fittest solution).

4 EMPIRICAL STUDY

We conducted experiments to evaluate the fitness function with the four search algorithms for addressing our optimization problem: minimizing the manual steps required to configure a product, while covering the VPs, fulfilling the configuration ordering dependencies to the maximum extent and

$$f(s_i) = \frac{mostCovering_i + mostConstrainting_i + minManualSteps_i + maxDepSatisfatory_i}{\Lambda}$$
 (1)

$$mostCovering_i = 1 - \frac{vpcot_i}{total\ number\ of\ the\ variation\ points} \tag{2}$$

$$mostConstraining_i = \frac{(nacot_i)}{n_{acot}}$$
(3)

$$minManualSteps_{i} = \frac{\left(\sum_{l=1}^{n_{eS_{i}}} 1, where e_{l}.manual = true\right)}{\sum_{l=1}^{n_{acot}} ne_{l}}$$
(4)

$$maxDepSatisfatory = \frac{\sum_{l=1}^{n_{eS_i}} \begin{cases} 0, & where \ e_l. \ weight =' \ High' \\ 1, & where \ e_l. \ weight =' \ Medium' \\ 2, & where \ e_l. \ weight =' \ Low' \\ \hline \sum_{l=1}^{n_{acot}} ne_l \end{cases}$$
 (5)

starting from most constraining configuration decisions. Details are reported in Section 5.

In Section 4.1, we present the research questions of the empirical study. In Section 4.2, we discuss two case studies used in the empirical evaluation.

4.1 **Research Questions**

In the empirical study, we aim to investigate the following five research questions (RQs): **RQ1:** Are the search algorithms effective to solve our optimization problem, to compare with RS? RQ2: Among the studied search algorithms, which one fares best in solving our optimization problem? RQ3: How does the configuration of VPs impact the performance of the search algorithms? RQ4. How does the number of VPs and the number of trees impact the performance of the search algorithms?

4.2 **Case Studies**

Crisis Management System (CMS): We the scope of Crisis significantly extended (CMS) based on Management System the defined by Capozucca et requirements (Capozucca et al., 2012), modeled the architecture of CMS containing CMS police, rescue, traffic control etc., as well as corresponding VPs using SimPL, and specified ordering and conformance rules as OCL constraints. Part of the SimPL model (Table 1) has been presented in the CMA@MODELS 2013 workshop, evaluated by modeling experts and was deposited to the ReDoMM repository 1 for public access.

Subsea Control: Based on several years of experience of conducting industry-oriented research in subsea oil and gas and in the context of PLE

(Behjati et al., 2013, Briand et al., 2012), we modeled the main concepts presented in Part 6 (subsea production systems) of the ISO 13628-6:2006 standard (ISO13628-6, 2006) using SimPL. The developed SimPL (Table 1) was further enriched with the well-known subsea engineering hand-book (Bai and Bai, 2012).

Table 1: Descriptive Statistics of CMS and Subsea Control.

Model Elements		CMS	Subsea Control
Packages		30	13
Classes		188	71
VP Types	Cardinality	62	13
	Attribute	49	91
	Topology	9	7
	All	120	111
OCL Constraints		31	25

EVALUATING SEARCH ALGORITHMS

This section reports the evaluation for answering RQ1-RQ4. The experiment design and execution is presented in Section 5.1 and analyses and results are discussed in Section 5.2.

Experiment Design and Execution 5.1

In our experiments, we compared three search algorithms: AVM, GA, (1+1) EA, and used RS as a comparison baseline to assess the difficulty of the addressed problems. AVM represents typical local search algorithms. GA is the most commonly applied global search algorithm. (1+1) EA has been proved effective for software engineering problems (e.g., see (Huihui et al., 2015, Yan et al., 2015)). In terms of GA, we set the population size to 100 and the crossover rate to 0.75, and a 1.5 bias for rank selection. We use a standard one-point crossover,

http://www.cs.colostate.edu/remodd/v1/content/modeling-architectureand-design-crisis-management-system-product-line-using-simpl

and mutation of a variable is done with the standard probability 1/n, where n is the number of variables.

5.1.1 Design of Search Problems

Real-world Configuration Problems: To answer RO1-RO3, we simulated two configuration processes of the two case studies (Section 4.2) and evaluated the performance of the search algorithms at each manual configuration step. Notice that Zen-DO is invoked as a result of manual configuration of a VP in Zen-Configurator, which can lead to the automated decision inference of other VPs. At each manual configuration step, a new search problem is formed and then solved by the search algorithms. As shown in Table 1, the VPs defined in the PLA models of CMS and Subsea Control are 120 and 111 respectively. We simulated a large part of a complete configuration process for each case study and as a result, we obtained 106 search problems for CMS and 64 search problems for Subsea Control. Notice that during the configuration process, instances of a cardinality VP are populated based on the configuration value to the cardinality VP. The populated instances usually contain attribute VPs, which need to be further configured. In short, the number of VPs in a product model dynamically changes while the configuration progresses.

Artificial Problem Design: To empirically evaluate the scalability of our approach, we created 130 artificial problems. We used a range of 100 to 4600 with an increment of 500 for the number of VPs, and a range from 10 to 250 with an increment of 20 for the number of trees. In total we had 10 options for the number of VPs and 13 options for the number of trees and defined 10*13 = 130 artificial problems.

5.1.2 Dependent and Independent Variables

We used fitness value (FV) as the main dependent variable, which is the best fitness value obtained after a certain number of generations by an algorithm (2000 in our experiments). In addition, we used two additional dependent variables: mean fitness value (MFV_p) for each problem and mean fitness value for a specific number of problems (MFV_{ps}) . The independent variables include: type of search algorithm (TSA), number of VPs (NVPs), and number of trees (NTs).

For each problem, both NVP_S and NT_S are fixed. MFV_p is calculated for each algorithm using the formula $MFV_p = \frac{\sum_{l=1}^{100} FV}{100}$. FV is the fitness value of one run, while l is the number of runs (100 in our

experiments).

For MFV_{ps} , there are two situations. With the fixed NVPs and various NTs, mean fitness values are calculated for each algorithm using the formula $MFV_{ps,v} = \frac{\sum_{t=1}^{13} \sum_{l=1}^{100} FV_v}{13*100}$. FV_v is the fitness value of one run for a given NVPs. l is the number of runs while t is NTs. With the fixed NTs and various NVPs, mean fitness values are calculated for each algorithm using the formula $MFV_{ps,t} = \frac{\sum_{v=1}^{10} \sum_{l=1}^{100} FV_t}{10*100}$. FV_t is the fitness value of one run for a given NTs. l is the number of runs while v is NVPs.

5.1.3 Statistical Tests

To compare the obtained results of the search algorithms, we applied the Wilcoxon signed-rank test and the Vargha and Delaney statistics (Arcuri, 2011). For all pairs, we conducted two samples Wilcoxon signed-rank test to obtain a p-value which determines the significance of results (with the significance level of 0.05). The Vargha and Delaney statistics (\widehat{A}_{12}) was used to calculate the effect size measure. If \widehat{A}_{12} is equal to 0.5, the two algorithms A and B are equivalent. \widehat{A}_{12} is more than 0.5 implies that A has higher chances of obtaining higher fitness value than B. To study the correlation between the performance of the search algorithms and NVPs as well as NTs, we use the Spearman's rank correlation coefficient. Prob > |p| is used to determine the significance of results with a significance level 0.0001. If ρ is greater than 0, there is a positive correlation; otherwise, a negative correlation exists.

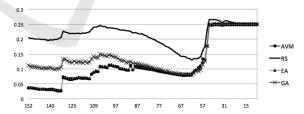


Figure 3: MFVs along with NVPs (CMS).

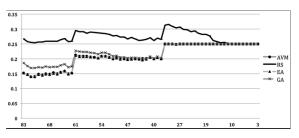


Figure 4: MFVs along with NVPs (Subsea Control).

5.1.4 Experiment Execution

Each configuration problem was repeated 100 times for each search algorithm to counter random variation. Each algorithm was run up to 2000 generations and the best FV obtained in the 2000 generations was recorded.

5.2 Analyses and Results

In Section 5.2.1, we report analyses and results for the two real-world case studies for answering RQ1-RQ3. In Section 5.2.2, we present analyses and results for the 130 artificial problems for answering RQ1-RQ2 and RQ4.

5.2.1 Results for the Real-World Case Study

RQ1 and RQ2: We compare RS with AVM, (1+1) EA and GA, based on FV for each problem (Table 2). Notice that the CMS case study has in total 106 problems and the Subsea Control case study has in total 64 problems (Section 5.1.1).

For the CMS case study, all the three search algorithms performed significantly better than RS for all the 106 problems (Table 1). A similar pattern can be observed for the Subsea Control case study, where AVM, (1+1) EA and GA performed significantly better than RS for 64, 63 and 63 problems, respectively. We therefore can answer RQ1 as follows: AVM, (1+1) EA and GA significantly outperformed RS for most of the problems suggesting the search algorithms are effective to solve our optimization problem compared with RS.

Regarding RQ2, for CMS, (1+1) EA outperformed AVM for 93 problems, out of which for 51 problems (1+1) EA performed significantly better than AVM. There were no significant differences observed for 48 problems. AVM performed better than (1+1) EA for 12 problems and only for 6 of them AVM significantly outperformed (1+1) EA. AVM significantly outperformed GA for problems and (1+1) EA significantly outperformed GA for all the 106 problems. For Subsea Control, (1+1)EA significantly outperformed AVM for 59 problems and GA for all the problems. AVM significantly outperformed GA for 62 problems. We therefore can answer RQ2 as follows: (1+1) EA is the best search algorithm to solve our optimization problem followed by AVM and GA.

RQ3: To answer RQ3, we plot the graphs shown in Figure 3 and Figure 4, where for a given NVP

during the configuration process, the mean fitness value is calculated for each algorithm using the formula MFV_p defined in Section 5.1.2. It is important to notice that for CMS and Subsea Control there are 106 and 64 problems respectively; the x-axes in Figure 3 and Figure 4 should have 106 and 64 data points respectively. To avoid cluttering the figures, only some of them are shown on the x-axis of the figures.

Table 2: Results for the Wilcoxon signed-rank and the Vargha and Delaney \widehat{A}_{12} statistics*.

RQ	Pair of Algorithms	CMS				
	(A vs. B)	A>B	A <b< th=""><th>A=B</th></b<>	A=B		
1	AVM vs. RS	106/106	0/0	0/0		
	(1+1) EA vs. RS	106/106	0/0	0/0		
	GA vs. RS	106/106	0/0	0/0		
2	AVM vs. (1+1) EA	6/12	51/93	48/1		
	AVM vs. GA	105/106	0/0	1/0		
	GA vs. (1+1) EA	0/0	106/106	0/0		
RQ	Pair of Algorithms	Subsea Control				
	(A vs. B)	A>B	A <b< th=""><th>A=B</th></b<>	A=B		
1	AVM vs. RS	63/64	0/0	1/0		
	(1+1) EA vs. RS	64/64	0/0	0/0		
	GA vs. RS	63/63	0/1	1/0		
2	AVM vs. (1+1) EA	0/0	59/64	5/0		
	AVM vs. GA	62/63	1/1	1/0		
	GA vs. (1+1) EA	0/0	64/64	0/0		

* In columns 'A>B' and ('A<B'), the values before the slashes are the number of problems that A is significantly better (worse) than B, while the values after the slashes are the number of problems that A has higher probability to be better (worse) than B. Column 'A=B' tells that the number of problems that there is no difference between A and B.

For both case studies, as shown in Figure 3 and Figure 4 along with the configuration of the VPs, (1+1) EA, AVM and GA are consistently better than RS, until the value of NVPs reaches less than 30 (for CMS) and 15 (for Subsea Control). The reason for this may be explained by the dynamic change of the forest itself. Along with the configuration of VPs, the trees in the forest are becoming smaller and there may be fewer trees in the forest. So in order to cover as many as possible the remaining VPs, more trees are selected, which subsequently leads to higher fitness values. In addition, along with the configuration, the remaining trees may have a higher percentage of manual steps and a higher percentage of low weight, both of which contribute to higher fitness values. In other words, we think when reaching the point of having less number of VPs to configure, there is no much space for optimization.

(1+1) EA and AVM performed in a very similar pattern for all the problems. GA performed worse than AVM and (1+1) EA when the value of NVPs is larger than 70 (for CMS) and 50 (for Subsea Control). This is mostly because GA uses both

mutation and crossover operators to explore more search space as compared to (1+1) EA that uses only mutation operator and thus GA needs more generations (greater than 2000) to obtain better solutions for problems with a large number of VPs.

We also calculated the Spearman's rank correlation between MVPs for each search algorithm with increasing NVPs. Results (Table 3) show that for all the algorithms except for RS, along with the increase of NVPs, MVPs decreases. Therefore, the performance of all the algorithms in terms of finding optimal solutions increases. Notice that the results are consistent with what we can observe from Figure 3 and Figure 4 along with the decrease of NVPs, MPVs increases in general. Therefore, the explanation described above applies to here as well.

Table 3: Results of the Spearman's correlation analysis with the increasing NVPs.

Case Study	Algorithm	Spearman's ρ	Prob> p
	AVM	-0.8167	<.0001
CMS	(1+1) EA	-0.8156	<.0001
CIVIS	GA	-0.3412	0.0003
	RS	-0.2943	0.0022
	AVM	-0.8756	<.0001
Subsea Control	(1+1) EA	-0.8713	<.0001
Subsea Control	GA	-0.7966	<.0001
	RS	0.1458	0.2502

5.2.2 Results for the Artificial Problems

RQ1 and RQ2: To answer RQ1 and RQ2, we compared the selected search algorithms with RS and then compared each pair of them based on MFV for each algorithm and each of the 130 artificial problems. From Table 4, one can see that 1) AVM, (1+1) EA and GA significantly outperformed RS for most of the artificial problems (RQ1), 2) (1+1) EA and AVM significantly outperformed GA for most of the problems (RQ2) and 3) AVM is significantly better than (1+1) EA for 62 problems while (1+1) EA is significantly outperformed AVM for 50 problems (RQ2).

RQ4: Recall that RQ4 aims to study the impact of the increasing number of VPs and trees on the

performance of the search algorithms. We therefore plot surface plots as shown in Figure 5 for each algorithm. In each plot, MFVs decrease when the color of curves goes from black to white.

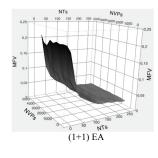
From Figure 5, we can observe that (1+1) EA and AVM performed in a very similar pattern: achieving very low MFVs when NTs is over 150 and performing worse when NTs is getting smaller. The performance of GA is the best when NTs is around 100. Its performance degraded when NTs increases over 150. This might be because more generations are required for GA to get better solutions when the number of trees is large since the problems are getting more complex. The performance of RS follows a similar pattern as GA but RS achieved much worse MFVs when NTs is over 100 than GA.

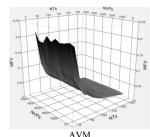
Table 4: Results for the Wilcoxon signed-rank test and the Vargha and Delaney \widehat{A}_{12} statistics.

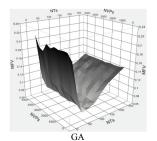
DO.	Pair of Algorithms	CMS			
RQ	(A vs. B)	A>B	A <b< th=""><th>A=B</th></b<>	A=B	
	AVM vs. RS	122/123	6/7	2/0	
1	(1+1) EA vs. RS	129/130	0/0	1/0	
	GA vs. RS	130/130	0/0	0/0	
	AVM vs. (1+1) EA	62/70	50/58	18/2	
2	AVM vs. GA	111/112	14/16	5/2	
	GA vs. (1+1) EA	0/5	120/120	10/5	

When NTs decreases below 100, the performance of all the algorithms degrades significantly. This might be because along with the configuration, the remaining trees may have a higher percentage of manual steps and a higher percentage of low weight, both of which will make a higher fitness value. In other words, we think when reaching this point, there will be no much space for optimization, as we discussed previously.

To further analyze the correlation between the performance and NTs and NVPs, we conducted the Spearman correlation analysis. Results are presented in Table 5. For AVM and (1+1) EA, NTs has a significant negative correlation with MFVs, implying that increasing NTs leads to the improvement of the performance of these two







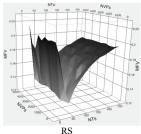


Figure 5: Surface Plots of MFVs, NVPs and NTs.

algorithms. For GA, a positive (but not significant) correlation was discovered, while a significant positive correlation was obtained for RS. When looking into NVPs, a significant positive correlation with MFVs for (1+1) EA was obtained, implying that it increasing NVPs leads to the degradation of the performance of (1+1) EA.

Table 5: Results of the Spearman's correlation analysis with the increasing NVPs and NTs.

Variable	Measure	AVM	(1+1) EA	GA	RS
NTs	ρ	-1	-1	0.4396	0.5659
	Prob> ρ	< 0.0001	< 0.0001	0.1329	0.0438
NVPs	ρ	0.6242	0.7212	0.4545	-0.1152
	Prob> o	0.0537	0.0186	0.1869	0.7514

6 OVERALL DISCUSSION

Based on the results of the empirical study, we suggest using either AVM or (1+1) EA together with our fitness function to solve the decision-ordering problem, since these two algorithms exhibit the best performance as compared to the other algorithms.

Recall that the mechanism of Zen-DO is based on ordering dependencies of VPs, which can be identified by querying the product line architecture and design model and from constraints explicitly capturing such dependency information. Therefore, if a product line has a larger number of such ordering dependencies specified, Zen-DO will perform more effectively. In other words, it is to document/specify ordering dependencies as product line assets and associate them (via suitable mechanisms) to VPs specified in the product line architecture and design model in the first place, to enable effective, automated decision ordering. In our Zen-Configurator tool, the SimPL methodology should be used to model the product line architecture and design and OCL should be used to specify constraints, which can naturally integrate with the SimPL model.

7 THREATS TO VALIDITY

Regarding construct validity, we applied the effectiveness measure: fitness value, which is comparable across all the algorithms. In addition, the number of generations was used in all the search algorithms as the stopping criterion. Random variations inherent in the search algorithms are the the most probable conclusion validity threat. To tackle it, we ran each experiment repeatedly 100

times to reduce the chance that the results were obtained by chance.

In our experiments, we used only one configuration setting for the search algorithms, which might form a possible threat to internal validity. It is however worth noting that these settings conform to common guidelines (Arcuri and Fraser, 2011) and our experience of applying search algorithms for addressing other software engineering optimization problems.

We ran our experiments on the 130 artificial problems of different complexity to test the scalability of the algorithms. However, one may say that the results may not be generalized to other case studies. Such threat to external validity is common to all empirical studies. In the future, we plan to evaluate our approach with more case studies.

8 RELATED WORK

As concluded in (Rabiser et al., 2012, El-Sharkawy and Schmid, 2012), an automated configuration solution should support product configuration with the ultimate objective of improving both the quality of configured products and the productivity of a configuration process. Especially for CPSs, hundreds and thousands of configuration parameters with complicated constraints among them have to be correctly configured, as reported in our previous work (Nie et al., 2013b). Automated solutions for configuring CPSs is therefore critically required to support, automated consistency checking, decision inference, etc., among which decision ordering has been recognized as one of the most important functionalities.

8.1 Literature Review

In (Nohrer and Egyed, 2011), an approach was proposed to optimize user guidance during decision making with the aim to automatically order decisions to minimize user input while giving users freedom to make decisions that are most important to them. SAT was used to reason about the impact of an answer given by a user and the ideal order of the remaining decisions. Note that this method considers two types of dependencies among questions and answers. For CPSs, as we reported in (Nie et al., 2013b) we encountered very complicated constraints as in some cases, configuring a VP is not just making a Boolean choice but also providing a value or selecting a type.

The authors of (White et al., 2009) proposed an

approach to derive a valid sequence of feature selections, while accounting for resource constraints such as budgetary constraints, in the context of multi-step feature model configuration process, which was formally formulated and mapped to CSP. CSP solvers were then applied to solve the problem. An approach is proposed in (Chen and Erwig, 2011) to identify feature selection sequences by prioritizing features that have high selectivity, such that the overall efficiency of the feature selection process can be improved. Each feature is associated with a value called selectivity, indicating the impact of selecting a feature on the selection and removal of other features. Feature models are translated to algebraic expressions to compute the selectivity. Guo et. al (Guo et al.) proposed a GA based approach to automatically optimize selections with resource constraints such as cost, CPU and memory. Evaluation results show that the proposed search based approach achieved promising optimal solutions.

Notice that all the above mentioned related work address decision ordering issues in the context of feature models or decision models. Therefore, constraints considered are relatively simple dependencies among variabilities. To configure CPSs, there exist a large number of complicated constraints on VPs with various types, considering that a configured product is typically an operational CPS system. Methods for decision/feature selection cannot meet the needs of configuring CPSs. Zen-DO aims to address the similar kind of challenges, but in the context of CPSs and because of their enormous complexity, we aimed for a scalable optimization solution and search algorithms seem to be a proper candidate for such a solution.

To compare with these related work, an approach proposed by Sayyad et al. in (Sayyad et al., 2013) is most closely related to our work. Their objective is to support feature model based automated configuration of product lines by accounting for user preferences. Five optimization objectives were defined and implemented, including minimizing rule violations, the number of deselected features, and the number of features that was not used before, known defects and cost. With these five objectives, the author investigated a series of well-known multiobjective evolutionary optimization algorithms and concluded, based a set of extensive and welldesigned experiments, that search algorithms in SBSE should be carefully selected and tailored for studving complex product configuration/decision space.

8.2 Configuration Tool Review

We reviewed 16 product configuration tools, among which six of them provide decision ordering support: Pure::Variants (Beuche, 2008), Dopler (Dhungana et al., 2011), Covamof (Sinnema et al., 2004), SPLOT (Mendonca et al., 2009), FMP (Czarnecki et al., 2005) and Questionnaire (La Rosa et al., 2009). We classify the approaches for these tools into three categories: *User Defined, Dependency Based* and *Depth First* approaches.

The *User Defined* approach relies on users to predefine configuration sequences. Some modeling methodologies have feature attributes (FMP and Pure::variants) or specific annotations (Covamof using Procedural Knowledge (Hotz et al., 2004)) to facilitate the specification of such additional information on top of variability models (mostly feature models). The Dependency Based ordering approach relies on the dependency or constraints defined as part of the product line models to derive valid configuration sequences of VPs. Dopler, Questionnaire and SPLOT implement this approach. The *Depth First* strategy is implemented in FMP to guide the configuration process by traversing feature models with a predetermined order (depth-first). Note that one of them implemented algorithms to minimize manual configuration steps.

El-Sharkawy and Schmid (El-Sharkawy and Schmid, 2012) categorized configuration problems into several categories, among which ensuring correct configuration is considered as the one that received the most attention in the past. To ensure correct configuration, different approaches have been taken, including validation of (partial) configurations, optimization based on, e.g., minimizing costs of resulting systems, value propagation to reduce the number of manual configuration steps, root analysis support for invalid configurations, and dependency based prioritization of configuration sequences. Our work follows into the last category of minimizing the amount of work that needs to be done by recommending a configuration ordering to users. Several heuristics based on analyzing dependencies among variabilities are summarized in the paper: 1) analyzing the impact of a decision on possible products that can be derived based on the current configuration (Benavides et al., 2005), 2) identifying local feature selection decisions to make such that reducing the impact of a decision on other parts of the feature hierarchy (Czarnecki and Kim), and 3) configuring most constraining decision first to reduce the amount of decisions to make manually.

According to the study of El-Sharkawy and Schmid (El-Sharkawy and Schmid, 2012), Dopler (Rabiser et al., 2007) is the only tool that implemented the heuristic: "most constraining decisions" should be configured first with the aim to minimize the number of decisions that must be made manually and therefore reducing the overall configuration effort. Our solution also includes this.

9 CONCLUSIONS

Due to the enormous complexity of Cyber-Physical Systems (CPSs), manual configuration of products based on a large number of various types of constraints in CPSs is a complicated and error prone. However, not all the steps in the configuration can be automated and some decisions must be taken by users. To this end, in this paper, we presented our search-based approach to identify an optimal set of decisions with the objectives to reduce overall manual configuration steps, configure most constraining decisions first, and satisfy ordering dependencies among VPs to the maximum extent. This objective was implemented as a fitness function used by the search algorithms to find an optimal solution. We empirically evaluated four search algorithms with the fitness function on two realworld case studies and 130 artificial problems. Results show that Alternating Variable Method (AVM) and (1+1) Evolutionary Algorithm (EA) significantly outperformed the others.

REFERENCES

- Cyber-Physical Systems (CPSs) [Online]. Available: http://cyberphysicalsystems.org/.
- Ali, S., Yue, T., Briand, L. & Walawege, S. 2012. A Product Line Modeling and Configuration Methodology to Support Model-Based Testing: An Industrial Case Study. In the 15th international conference on Model Driven Engineering Languages and Systems, 2012.
- Arcuri, A. 2011. It really does matter how you normalize the branch distance in search-based software testing. *Software Testing, Verification and Reliability.*
- Arcuri, A. & Fraser, G. 2011. On Parameter Tuning in Search Based Software Engineering. *International Symposium on Search Based Software Engineering* (SSBSE).
- Bai, Y. & Bai, Q. 2012. Subsea engineering handbook, Gulf Professional Publishing.
- Behjati, R., Yue, T., Briand, L. & Selic, B. 2013. SimPL: A Product-Line Modeling Methodology for Families

- of Integrated Control Systems. *Information and Software Technology*, 55, 607-629.
- Benavides, D., Trinidad, P. & Ruiz-Cortés, A. Automated reasoning on feature models. Advanced Information Systems Engineering, 2005. Springer, 491-503.
- Beuche, D. 2008. Modeling and building software product lines with pure:: variants. Software Product Line Conference, 2008. SPLC'08. 12th International, 2008...
- Briand, L., Falessi, D., Nejati, S., Sabetzadeh, M. & Yue, T. 2012. Research-based innovation: a tale of three projects in model-driven engineering. *Model Driven Engineering Languages and Systems*. Springer.
- Capozucca, A., Cheng, B. H., Georg, G., Guelfi, N., Istoan, P., Mussbacher, G., Jensen, A., Jézéquel, J.-M., Kienzle, J. & Klein, J. 2012. Requirements Definition Document for a Software Product Line of Car Crash Management Systems. *University of Nice Sophia Antipolis, I3S CNRS, Technical Report.*
- Chen, S. & Erwig, M. Optimizing the product derivation process. Software Product Line Conference (SPLC), 2011 15th International, 2011. IEEE, 35-44.
- Czarnecki, K., Antkiewicz, M., Kim, C. H. P., Lau, S. & Pietroszek, K. fmp and fmp2rsm: eclipse plug-ins for modeling features using model templates. Companion to the 20th annual ACM SIGPLAN conference on Object-oriented programming, systems, languages, and applications, 2005.
- Czarnecki, K. & Kim, C. H. P. Cardinality-based feature modeling and constraints: A progress report.
- Dhungana, D., Grünbacher, P. & Rabiser, R. 2011. The DOPLER meta-tool for decision-oriented variability modeling: a multiple case study. *Automated Software Engineering*, 18, 77-114.
- El-Sharkawy, S. & Schmid, K. Supporting the effective configuration of software product lines. Proceedings of the 16th International Software Product Line Conference-Volume 2, 2012. ACM, 119-126.
- Frakes, W. B. & Kang, K. 2005. Software reuse research: Status and future. Software Engineering, IEEE Transactions on, 31, 529-536.
- Guo, J., White, J., Wang, G., Li, J. & Wang, Y. A genetic algorithm for optimized feature selection with resource constraints in software product lines. *Journal of Systems and Software*, 84, 2208-2221.
- Hong, L., Tao, Y., Ali, S., Kunming, N. & Li, Z. 2014.
 Zen-CC: An Automated and Incremental Conformance Checking Solution to Support Interactive Product Configuration. Software Reliability Engineering (ISSRE), 2014 IEEE 25th International Symposium on.
- Hong, L., Tao, Y., Shaukat, A. & Li, Z. 2015. Model-based Incremental Conformance Checking to Enable Interactive Product Configuration. accetped in Information and Software Technology.
- Hotz, L., Krebs, T. & Wolter, K. Combining software product lines and structure-based configuration methods and experiences. Proceedings of the Workshop on Software Variability Management for Product Derivation, at Software Product Line Conference (SPLC), 2004.

- Huihui, Z., Tao, Y., Shaukat, A. & Chao, L. 2015.
 Facilitating Requirements Inspection with Search-Based Selection of Diverse Use Case Scenarios. 9th
 EAI International Conference on Bio-inspired Information and Communications Technologies (formerly BIONETICS).
- ISO13628-6 2006. Petroleum and natural gas industries— Design and operation of subsea production system— Part 6:Subsea production control systems.
- La Rosa, M., Van Der Aalst, W. M., Dumas, M. & Ter Hofstede, A. H. 2009. Questionnaire-based variability modeling for system configuration. Software and Systems Modeling, 8, 251-274.
- Mendonca, M., Branco, M. & Cowan, D. SPLOT: software product lines online tools. Proceedings of the 24th ACM SIGPLAN conference companion on Object oriented programming systems languages and applications, 2009. ACM, 761-762.
- Nie, K., Yue, T. & Ali, S. Towards a Search-based Interactive Configuration of Cyber Physical System Product Lines. Demos/Posters/StudentResearch@ MoDELS, 2013a. 71-75.
- Nie, K., Yue, T., Ali, S., Zhang, L. & Fan, Z. Constraints: The Core of Supporting Automated Product Configuration of Cyber-Physical Systems. ACM/IEEE 16th International Conferene on Model Driven Engineering Languages and Systems (MODELS),, 2013b
- Nohrer, A. & Egyed, A. Optimizing user guidance during decision-making. Software Product Line Conference (SPLC), 2011 15th International, 2011. IEEE, 25-34.
- OMG Accessed: 2015. OCL 2.0 Specification, http://www.omg.org/spec/OCL/2.2/.
- Rabiser, R., Dhungana, D. & Grünbacher, P. Tool support for product derivation in large-scale product lines: A wizard-based approach. Workshop on Visualisation in Software Product Line Engineering (ViSPLE), IEEE Computer Society, 2007. 119-124.
- Rabiser, R., Grünbacher, P. & Lehofer, M. A qualitative study on user guidance capabilities in product configuration tools. The 27th IEEE/ACM International Conference on Automated Software Engineering, 2012.
- Sayyad, A. S., Menzies, T. & Ammar, H. 2013. On the Value of User Preferences in Search-Based Software Engineering: A Case Study in Software Product Lines. Software Engineering (ICSE), 2013 35th International Conference on.
- Sinnema, M., Deelstra, S., Nijhuis, J. & Bosch, J. 2004. Covamof: A framework for modeling variability in software product families. Software product lines, 25-27.
- White, J., Dougherty, B., Schmidt, D. C. & Benavides, D. Automated reasoning for multi-step feature model configuration problems. The 13th International Software Product Line Conference, 2009. Carnegie Mellon University, 11-20.
- Yan, L., Tao, Y., Shaukat, A. & Li, Z. 2015. Zen-ReqOptimizer: A Search-based Approach for

Requirements Assignment Optimization. Accepted in Empirical Software Engineering (EMSE).