

# Evolutionary Algorithms Applied to Agribusiness Scheduling Problem

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**Abstract:** This paper addresses a scheduling problem in agribusiness context, specifically about chicken catching. To solve that problem, memetic algorithms combined with local search in a two-phase algorithm were proposed and investigated. Four versions of memetic algorithms were implemented and compared. Also, to apply local search, k-swap and SRP is proposed and experimented. At last we analyze the results, comparing performances. The obtained results show a good improvement in solutions, especially when compared to the manual scheduling actually performed by the company that provides the data to this study.

## 1 INTRODUCTION

Scheduling Problem (SP) is a common name to a computing problem set, often at NP-hard class, which has the purpose of allocate event or resource sets throughout a time period, satisfying a set of constraints, usually to optimize a fitness function. That resource might be persons, machines, vehicles, physical location, etc. The SP class arises from real problems on industry and organizations. These problems are also observed on software engineering, according (Xiao et al., 2013). The main challenge is usually to find a computational methodology to solve these problems in a efficient and effective way, making possible to generate computational systems to automate real-problem resolutions.

In this paper, we examine a SP class variant, the Agribusiness Scheduling Problem (ASP), at a Poultry Industry context. It is a combinatorial optimization problem with great computational complexity which has been poorly addressed (Hart et al., 1999; Constantino et al., 2011). The ASP is shown as a NP-complete problem, as the mostly of scheduling problems (Bodin, 1983), without any polynomial-time complexity algorithm that solves it with an optimal solution.

The purpose of this work is to compare some evolutionary algorithms applied to the ASP. So, in Section 2 is explained what do we expect from a shift at the chicken factory. In Section 3 the problem is described in a way we can develop a solution, which is proposed in Section 4. In Section 5 we discuss the experiments and the obtained results. At the end, some

conclusions in Section 6.

## 2 CHICKEN CATCHING SQUAD SCHEDULING

Our problem occurs on agribusiness context, dealing with chicken transport to the factories. As chickens are fragile animals, they can't stay longer at the lorries, exposed to high temperatures. So, the squad's shift for transport and discharging must be careful planned to not create long queues at the factories.

There are different farms, which has different distances to the factories. When they get at the right age, they will be caught and sent to slaughter.

Also, we have the catcher squads, who are responsible to catch the chickens to transport them to the factories. To generate the schedule, we need to observe labor law and constraints about work time and rest time.

At last, the vehicles to transport the chickens must be considered, calculating the capacity, velocity and availability. All that factors may change the problem modeling.

## 3 PROBLEM DESCRIPTION

The problem described here is a real-world scheduling problem of a brazilian company, which daily has to catch chicken at different farms and carry them to three factories (slaughterhouses).

The farms are located far from until 150 km of each factory and different farms can be added to the problem. So, the schedule has to be daily generated according all different variables.

There are some squads to travel from their base to the farms. A squad must travel to one farm, catch the chickens, load the lorries and travel to the next farm to do the same.

The lorries and drivers will be considered as an unique entity, so we'll just think about the lorry, which may have known capacity and average velocity. Also, the distance between each farm to the factories is known.

Our work has to determine what load will be designed to each factory and the schedule to minimize the costs of idle factories and paid time. So, the catches and the travels has to be calculated in a way to avoid long queues at the factories and to catch the chickens at the right moment.

The factories has a ventilated hangar where the lorries can wait a determined period. Obviously it has a limited size, so our goal is to not admit more lorries at the queue than the hangar capacity. And even being ventilated there is a time limit that the the chickens can wait.

Figure 1 illustrates how it all works. At this example, we have two squads to catch the chickens to three factories. The continuous lines represent the travel sequence of each squad and the dashed lines represent the lorries' travels carrying the chickens from the farms to the factories. Also, the squads' bases are in different locations from the factories. Thus, we're interested on find some informations as the sequence of the farms to each squad, the squads' initial and final work times, the time of lorries' load and the destination of each load.

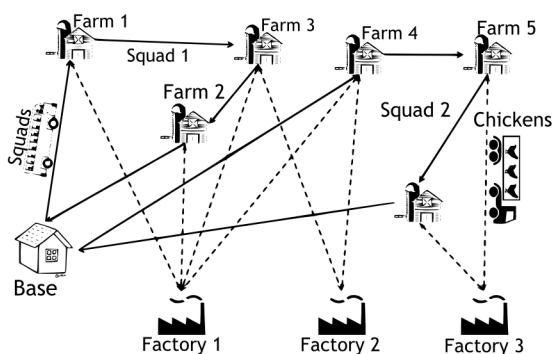


Figure 1: Daily the squads go to the farms, to catch the chickens and load the lorries, which carry them to the factories. When they finish the load, the squad travel to the next farm at the schedule.

To get clear, our purpose is to minimize the costs,

minimizing the work time and the idle time. To achieve this, we have to observe some restrictions and local laws, but we won't take time explaining they at this work.

## 4 PROPOSAL

In our approach the problem is divided into several subproblems. At this section we present the first subproblem solved, that is the assignment problem, which assign each farm load to one factory. After, we present the subproblems of the initial solutions and the local search. At last, the general algorithm to generate solutions to the general problem.

### 4.1 The Assignment Problem

To solve the load's destination subproblem, we use a mathematical model. This model is similar to the Zero-One Knapsack Problem (Kellerer et al., 2004).

We get the loads by dividing the number of chickens by the lorry capacity. Here we suppose an equal capacity for the lorries. Each load is associated to:

- Origin (farm);
- Destination (factory);
- Load start time;
- Load duration;
- Responsible squad; and
- Number of chickens.

As we know the farm set and their informations, as location and number of chickens, the number of loads and load duration are automatically retrieved. So, we still need to discover the destination, the squad and the start time to catch the chickens.

Then, to minimize the costs, a fundamental phase is to find the assignment of the loads to the factories. To do this, we use a binary integer linear programming model which is solved using LP-Solve software. But this model solves just part of the problem, minimizing transport costs only. Still, the scheduling has to be solved by using heuristic algorithms.

The evolutive algorithms in this paper use the linear assignment model on two phases: at the construction phase and at the improvement phase (local search). The assignment problem (AP), denoted by  $PD([C_{ij}])$ , is the following:

$$\text{Min} \sum_{i=1}^{n_1} \sum_{j=1}^{n_2} c_{ij} x_{ij}$$

$$\text{Subject to: } \sum_{i=1}^{n_1} x_{ij} = 1, \forall j = 1, \dots, n_2$$

$$\sum_{j=1}^{n_2} x_{ij} = 1, \forall i = 1, \dots, n_1$$

$$x_{ij} \in \{0, 1\}, \forall i = 1, \dots, n_1, \forall j = 1, \dots, n_2$$

Let be  $x_{ij}$  is a binary decision variable  $\{0, 1\}$ , where  $x_{ij} = 1$  if  $i$  is associated to  $j$ , or  $x_{ij} = 0$  otherwise. And let be  $c_{ij}$  the cost to associate  $i$  to  $j$ .

The  $n_1$  value must be the same as  $n_2$  value. At the first phase,  $n_1$  represents the number of squads and  $n_2$  the number of loads. As the number of loads is always greater than the number of squads, thus fictitious squads are created to get a squared matrix  $[c_{ij}]$ . At improvement phase,  $n_1$  and  $n_2$  are always the maximum number of squads ( $ne_{max}$ ) allowed for scheduling. Even though the algorithm takes the max number of available squads, the goal is to minimize the global cost of human resources. This model is used both on construction and improvement phases.

In order to generate the scheduling, we can define it as an activity sequence to be taken throughout the day, with average lorry loading time of about one hour. So, to simplify our problem, we can discretize the day on one-hour time slot. Thus, we consider  $t$  as the time index, with  $t = 1, \dots, 24$ , where  $t = 1$  represents the first time slot of the day, when some squad starts its work.

### 4.2 Construction Phase

We can use the assignment model to create the initial solution. Initially, all sequence of each squad (from  $ne_{max}$  squads) are empty. So, the loads are successively assigned to the squads until assign to all squads, using  $t = 1$ , starting the squad work at the first time slot. As we always have more loads than squads, to the others time slots ( $t > 1$ ) the assignment is solved using the assignment problem.

After the initial process, we get a initial schedule, as illustrated by Figure 2.

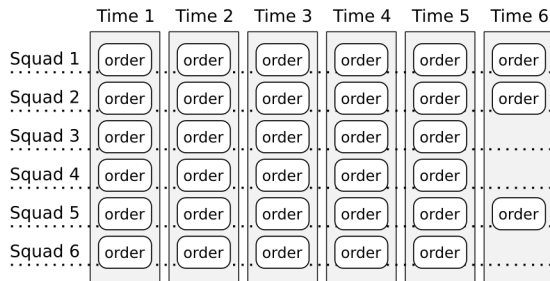


Figure 2: Example of an initial load distribution among the squads.

### 4.3 Local Search

From initial solution, local search is a good method to get improved solutions. In this work we use search procedures based on VND (Variable Neighborhood Descent), a particular case of Variable Neighborhood Search (Hansen and Mladenović, 2001).

#### 4.3.1 k-swap

The first local search method we used is the  $k$ -swap, which consists on slice our schedule on  $k$  time slots, starting at a  $t$  time, generating activity blocks. So,  $k$ -swap investigates the swaps between the blocks to get a improved solution.

The investigation uses successive assignment problems, calculating the cost of assignment to different instances. Considering  $st$  as the starting time at the squads schedules and  $et$  the end time, or the last time slot of work, we can write the  $k$ -swap algorithm as follows.

```

start;
z* ← ∞;
for t ← (st + 1) to (et - k - 1) do
    Creates a cost matrix [cij] to load ba(k, t);
    Solves assignment problem AP([cij]);
    if z < z* then
        z* ← z; //saving the best z value till now
        t* ← t; //saving the best t value till now
    end if
end for
Associates loads to squads according AP([cij])
on t*;
end
    
```

Figure 3 illustrates an example of 1-swap for  $t = 4$ , using a graph to represent the activities that 4 squads would perform in a seven-hour period to load 18 loads. The labeled vertices represent the loads, while blank vertices represent time slots without any loading (rest or travel). The continuous edges represent the predefined activity sequence and dashed edges represents the possible swaps.

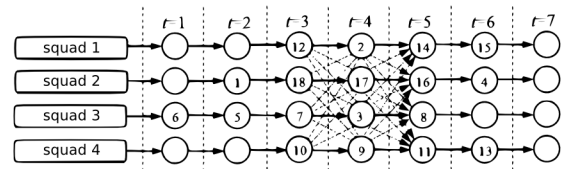


Figure 3: 1-swap considering only one interval at  $t = 4$ .

At Figure 4, we observe an example of 2-swap, considering times  $t = 4$  and  $t = 5$ , using consecutive time slots.

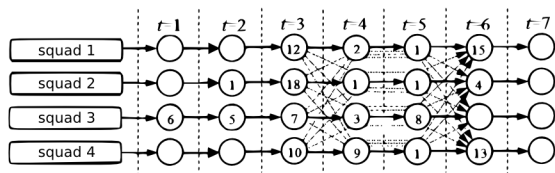


Figure 4: 2-swap considering the consecutive intervals  $t = 4$  and  $t = 5$ .

### 4.3.2 Split and Recombination Procedure

Another local search investigated is the Split and Recombination Procedure (SRP). This procedure works slicing the schedule between two work times, dividing the schedule on two parts, and recombines it using the assignment problem. Figure 5 illustrates that process.

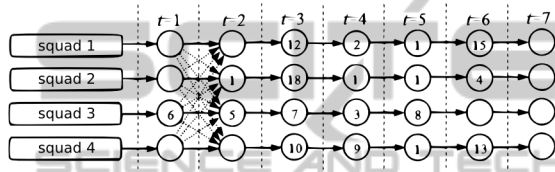


Figure 5: SRP applied at interval between  $t = 1$  and  $t = 2$ .

### 4.3.3 bl-VND General Algorithm

The bl-VND algorithm is based on VND (Variable Neighborhood Descent), which explores the solution space with systematic neighborhood changes (Hansen and Mladenović, 2001), if current solution weren't improved on a particular neighborhood, a next neighborhood is explored and so on. Let's state  $R$  as the neighborhood set,  $N_1, N_2, \dots, N_R$ . On our algorithm, we use  $R = 6$ , where  $N_1 = 1$ -swap,  $N_2 = 2$ -swap, ...,  $N_5 = 5$ -swap and  $N_6 = \text{SRP}$ .

Each iteration of bl-VND explores all neighborhoods and the algorithm stops when no improvement occurs on any of iterations. The algorithm is presented below.

```

start
  Initialization:
  start
    selects a neighborhood structure set  $N$ ,
    ( $r = 1, \dots, 6$ );
    selects a initial solution  $S$ ;
  end
  repeat
     $r \leftarrow 1$ ;
    repeat
      Local search: Find  $s'$  solution from  $s$ 
      ( $s' \in N_r(s)$ );
      if  $f1(s') < f1(s)$  then
         $s \leftarrow s'$ ;
         $r \leftarrow 1$ ;
      end if
    end repeat
  end repeat

```

```

else
   $r \leftarrow r + 1$ ;
end else
until  $r = R$ ;
until satisfies break criteria;
end

```

## 4.4 Local Search at Queues

The construction phase and the previous local searches aim to minimize the costs with paid time. So, until now we didn't consider the impact on the factories' work, as idle time or lorries' wait time at the queues.

To take care of that problem a penalty was introduced to evaluate the idle time under our objective function.

Then, to minimize the idle time and the wait time at the hangars, a local search algorithm, named bl-Queue, was designed. The main role of it is to change the initial time of each squad's schedule, in order to don't have many loads waiting at the same time on the same factories.

bl-Queue algorithm then evaluates the impact of each schedule starting at the times  $t = 1, \dots, t_{max}$ , where  $t_{max}$  is the max time allowed to unload the loads on time to slaughter. This is done successively to each of the squads. The below algorithm presents how bl-Queue works.

```

start;
for  $s \leftarrow 1$  to  $s_n$  do
  Finds a  $t$  time to starts the schedule
  to  $s$  squad with minor cost;
  Changes  $s$  initial time to  $t$ ;
end for
end

```

To determine the time of the queues, a simulation is performed, using the 3-phases method (Medina and Chwif, 2007). In short, this method does:

- Checks the time of all events in schedule to select the one who occurs first. Update the simulation clock to the selected time.
- Executes the selected event and the entities (loads) are moved to the waiting queues to the next activity.
- Searches the entities at the queue and starts the events that satisfies current conditions. Moves the entities from queues to activities and calculates the time each entity stayed at the queues.

The loads analyzed before can be the entities whose realizes the simulation events. Once we know the squads initial work time, is possible to determine at what time the loads will arrive at the destination. So, we can calculate how many time each entity stayed at queue. At the end of simulation we get

statistics about the queues, as total time of wait and average queue size.

#### 4.5 Memetic Algorithms

Memetic Algorithms belongs to the populational algorithms class. It uses several solutions searching feasible solutions in a search space. The main feature of that approach is to uses hybridization of different algorithmic techniques to a specific problem (Neri et al., 2011).

That class of algorithms was introduced by Moscato (Moscato, 1989) describing an evolutionary process that uses local search as a decisive part of the evolution. It may be seen as an local refinement inside a search space, in a way an agent can has his adaption level increased after a refinement stage.

The fundamentals of Memetic Algorithms consists on combine different meta-heuristics concepts and strategies, as the population-based search with local search, intending to join the advantages of them (Neri et al., 2011).

Four different versions of Memetic Algorithms were developed in this work. They're evolutive algorithms with construction procedures, local search and other techniques. The new algorithms are: Hierarchical Memetic Algorithm (HMA), Hierarchical-generational Memetic Algorithm (HGMA), Alternate Memetic Algorithm (AMA) and Coevolutive Cooperative Memetic Algorithm (CCMA).

### 5 EXPERIMENTS AND RESULTS

Some experiments were performed in order of analyze and compare different implementations. The four memetic algorithms of previous section were used, as the existing version proposed by (Constantino et al., 2011).

First of all, we define the parameters. Then we analyze the impact of local search. At last, we show the results using real data.

#### 5.1 Defining Parameters

To perform the experiments, we had to set up all the parameters in a way to get a better performance using genetic algorithms.

As observed, the crossing genetic operator generates many infeasible solutions. So, empirically, was defined a Crossover Rate of 100% to force the algorithm to always use that operator.

After some experiments to calibrate our parameters and some statistical analysis, we adjust the algorithm parameters as showed on Table 1.

Table 1: Initial parameters for genetic algorithm.

Parameter	Value
Population size	120
Mutation tax	3%
Number of iterations (MaxIt)	2000
$\Omega$	50%

#### 5.2 Local Search Impact

To identify the real contribution of local search to obtain the solutions, a experiment was performed with the aim to quantify the acting of the search at each current best global solution, comparing to the other solutions obtained by genetic algorithm.

The Figures 6, 7 and 8 show graphs generated from tests using real data for test cases A, B and C.

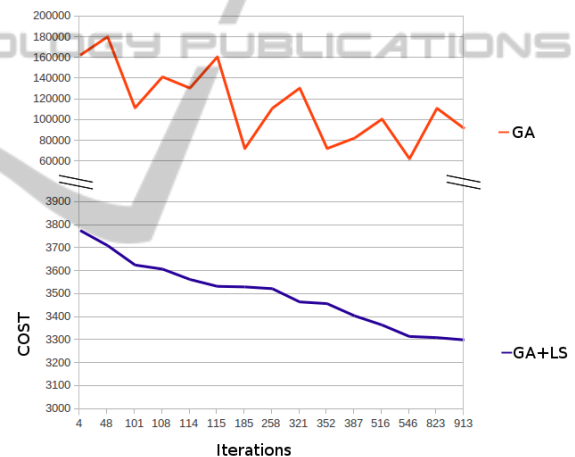


Figure 6: Obtained results using GA and GA + Local Search - Test case A.

Two scales were used for cost axis, because there is a great distance between costs of using only GA or GA combined with local search. After analyze these graphs, we observed that the genetic algorithms have the task to create potential good solutions, not necessarily having good costs, whilst local search algorithms are responsible to get solutions with acceptable costs.

Another observation at these graphs is that in none of the cases the solution was improved after 1000 iterations. Even though, there are some cases where higher values of iterations has proved to be useful.

#### 5.3 Computational Results

The experiments were performed using a CPU Intel

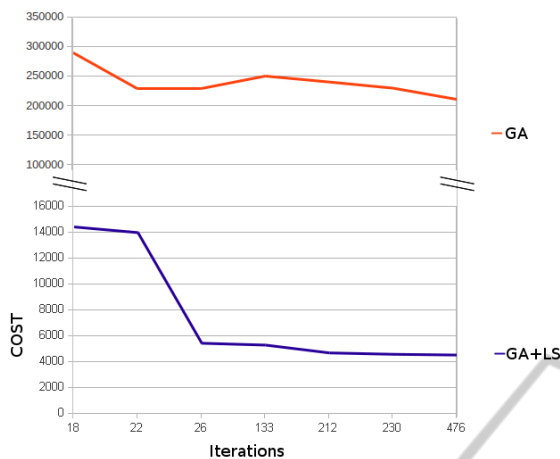


Figure 7: Obtained results using GA and GA + Local Search - Test case B.

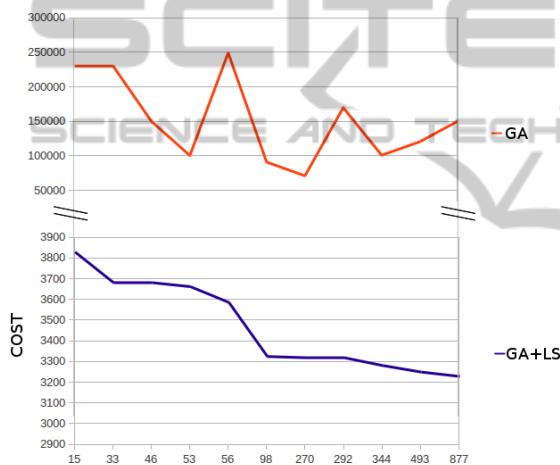


Figure 8: Obtained results using GA and GA + Local Search - Test case C.

Core I5, 2.3 GHz, under Ubuntu 11.04 64 bits, kernel Linux 2.6.38, using C++ language, compiled with GCC, from GNU. These experiments used real data, collected from a real company over a three months operation period (62 data instances). This period involves 112 catchers, divided on squads of 14 persons (including the driver).

To solve the mathematical model we used the *LP-Solve*, a solver used to solve linear models, non-linear models and integer mathematical programming, as the proposed model.

A implementation of Kuhn-Munkres algorithm (Kuhn, 1955), also known as Hungarian Algorithm, was used to solve the Assignment Problem.

At Table 2 shows the instances used to the experiments. Each instance represents a work day. So, at the table is possible to observe the problem size, observing how many farms (*fq*) and loads (*oq*) are involved.

Table 2: Instances of the problem used on the experiments.

Instance	<i>fq</i>	<i>oq</i>	Instance	<i>fq</i>	<i>oq</i>
1	10	48	32	7	52
2	9	46	33	6	52
3	9	47	34	5	44
4	8	44	35	5	38
5	9	50	36	7	54
6	9	48	37	7	26
7	10	46	38	5	42
8	6	37	39	9	48
9	7	52	40	8	55
10	6	43	41	9	53
11	7	47	42	8	45
12	5	37	43	10	57
13	6	46	44	12	55
14	5	37	45	9	43
15	5	49	46	8	35
16	5	38	47	9	42
17	4	49	48	12	41
18	7	49	49	8	45
19	7	43	50	10	45
20	10	44	51	7	52
21	5	44	52	9	47
22	2	45	53	5	49
23	4	46	54	7	46
24	4	39	55	6	50
25	7	41	56	7	54
26	7	53	57	6	49
27	5	52	58	7	44
28	4	52	59	7	46
29	3	37	60	3	26
30	4	46	61	2	16
31	7	54	62	8	54

Overall, the average of farms visited by day is 6.8, with an average of 45.4 loads transported.

### 5.4 Explained Results

Table 3 shows the obtained results separated by the different implementations of memetic algorithms. Explaining, we have:

- The results about total distance traveled are the same in all versions because it's obtained from the same mathematical model.
- Although the computational time has vary among the versions, in no one the time has increased in a way that prejudices any version. It all finished in a feasible computational time.
- The *Manual* column has the cost of the original scheduling, manually generated by the company.
- The *HMA* column shows the results using the HMA algorithm with initial parameters configuration.
- The *AHMA* column shows the results using the

Table 3: Results summary from performed implementations.

	Manual	HMA	AHMA	HGMA	AMA	CCMA
Total paid time (hours)	4060.25	3843.45	3766.54	3672.29	3837.28	<b>3656.51</b>
Total dist. travelled (km)	370436.8	<b>347834.4</b>	<b>347834.4</b>	<b>347834.4</b>	<b>347834.4</b>	<b>347834.4</b>
Total idle time (hours)	60.12	17.15	14.68	6.03	17.21	<b>0.00</b>
Avg lorries at queue	4.01	2.35	<b>2.14</b>	2.48	3.74	2.24
Avg wait time (minutes)	119.04	<b>4.33</b>	<b>4.33</b>	26.82	26.24	4.93
Lorries overflow at queue	92	9	8	2	10	<b>0</b>
Infeasible schedule quantity	51	7	7	4	13	<b>0</b>
Computational time (minutes)	-	<b>115</b>	130	160	120	180

Table 4: Qualitative results for some instances of the problem.

	Manual	HMA	AHMA	HGMA	AMA	CCMA
<b>Instance A</b>						
Factory got stopped?	Y	Y	N	N	Y	N
Got lorries overflow?	Y	Y	Y	N	Y	N
Was schedule infeasible?	Y	Y	Y	Y	Y	N
<b>Instance B</b>						
Factory got stopped?	Y	Y	Y	Y	Y	N
Got lorries overflow?	Y	Y	N	N	Y	N
Was schedule infeasible?	Y	Y	Y	Y	Y	N
<b>Instance C</b>						
Factory got stopped?	Y	Y	Y	N	Y	N
Got lorries overflow?	Y	Y	Y	Y	Y	N
Was schedule infeasible?	Y	Y	Y	N	Y	N

Adjusted-HMA algorithm, which has the parameters adjusted, as shown at section 5.1 (Table 1)

- From *HGMA* column, we observe that the Generational approach provides better results, despite of a increasing at the wait time at the factories.
- The *AMA* column shows the results using the *AMA* algorithm, based on joining both phases of *HMA* algorithm, but it didn't improves the results, getting worse at some aspects.
- The *CCMA* column shows the results using the *CCMA* algorithm, based on coevolutionary and previous versions to get a version that presented the best results. It shows evidences that this approach is more flexible and makes a better exploration of the search space.

## 5.5 About CCMA Version

The main contribution of *CCMA* version is the better performance to generate scheduling to the test cases previous versions was not able to find good solutions.

Table 4 shows qualitative results about proposed algorithms to some instances of the problem.

Table 5 compares *CCMA* results with the manual scheduling generated by the company, evaluating the difference between the solutions.

The results present a significant reduction of operational costs. The paid time is related to the squads, so the cost must be multiplied by 14, the number of persons at each squad.

Also, it reduces infeasible duties, which are schedules with erroneous calculation of travel time between farms. It generates extra costs to the company. 100% of these cases were reduced using *CCMA*. Still it removes some undesirable schedules, with long work time without rest.

The factories idle time was also reduced to zero. The cost of an idle factory is usually very high, reaching the value of US\$6000.00/hour.

It still reduces the number of lorries parked in the factories' hangars in about 50% and the average wait time was reduced in more than 95%. Also, a reduction of 100% of the lorries overflow. When more lorries

Table 5: Comparison between manual and CCMA computational scheduling.

	Manual	CCMA	Reduction	% reduction
Total paid time (hours)	4060.25	3656.51	403.74	9.94
Total dist. travelled (km)	370436.8	347834.4	22602.4	6.1
Total idle time (hours)	60.12	0.00	60.12	100
Avg lorries at queue	4.01	2.24	1.77	44.1
Avg wait time (minutes)	119.04	4.93	114.11	95.86
Lorries overflow at queue	92	0	92	100
Infeasible schedule quantity	51	0	51	100

are stopped than the factory capacity, the lorry has to go to some unappropriated place, which may cause chickens mortality and increase of operational costs.

## 6 CONCLUSIONS

This work presented a study on heuristic algorithms to solve a scheduling problem in agribusiness context. After all study and experiments, we can conclude:

- Memetic algorithms had an important role in this work due their flexibility and facility to incorporate new procedures. Also, they ease solving problems with hard mathematical modeling.
- Performed experiments had demonstrated the feasibility of using computational systems to automate the schedule generation to solve real problems.
- Local search had a great importance to reduce the costs on obtained solutions.
- Comparing the obtained solutions with manual solutions of the company, evolutive algorithms had a very great reduction on operational costs, generating schedules in feasible computational time. The final solutions presents improvements both on quality and in reduction of the costs.

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