# Comparing Electronic Examination Methods for Assessing Engineering Students The Case of Multiple-Choice Questions and Constructed Response Questions 

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#### Abstract

The aim of this work is the comparison of two well-known examination methods, the first consisted of multiple-choice questions (MCQs) and the second based on constructed-response questions (CRQs). During this research MCQ and CRQ tests were created for examining the undergraduate engineering module of "project management" and were given to a group of students. Computers and a special software package were used to support the process. During the first part the examinees had to answer a set of CRQs. Afterwards, they had to answer a set of MCQs. Both sets covered the same topics and had the same level of difficulty. The second method (MCQs) is more objective in terms of grading, though it may conceal an error in the final formulation of the score when a student gives an answer based on an instinctive feeling. To eliminate this problem a set of MCQs pairs was composed taking care that each question of the pair addressed the same topic in a way that the similarity would not be evident to a student who did not possess adequate knowledge. By applying a suitable scoring rule to the MCQs, very similar results are obtained when comparing these two examination methods.


## 1 INTRODUCTION

Modern IT can provide a set of tools for the enhancement of the educational process such as material of digital polymorphic content and software applications (Reiser \& Dempsey, 2011; Dede, 2005; Friedl et al., 2006). The penetration and incorporation of such tools in the modern academic learning practice has been widely accepted since many years (DeBord et al., 2004). It can potentially contribute to the enrichment of the traditional examination and assessment methods of students by the use of computer aided systems and the introduction of innovative examination techniques (Tsiakas et al., 2007).

Multiple Choice Question (MCQs) tests belong to the category of objective evaluation methods as the score can be rapidly calculated without putting the examiner in the position of deciding the grade. Moreover, it does not depend upon the writing speed and skill of the examinee (Bush, 2006; Freeman\& Lewis, 1998; Scharf \& Baldwin, 2007). The time
efficiency, combined with the grading objectivity, enables the provision of prompt feedback to the examinee, after the termination of the examination, regarding the overall score along with specific information in a form of report about correct and incorrect answers.

A significant problem of the MCQs is the infiltration of the "guessing" factor during the time of selecting one of the possible answers. The application of a simple grading rule of positive score only for the correct answers and no loss for the incorrect ones could form a score that a part of it may be based on guessing or sheer luck and does not objectively reflect the student's knowledge. A potential solution to this problem can be the application of special grading rules that may include a penalty (i.e. subtraction of points) in case of wrong answer (Scharf \& Baldwin, 2007). This fact can affect the students' behavior and mislead them in terms of decision making. Their uncertainty will eventually generate variance regarding the test scores which is related to the expectations of the examinees and not to the knowledge that is tested
(Bereby-Meyer et al., 2002; Bereby-Meyer et al., 2003).

One of the most widely used examination methods include sets of constructed-response questions (CRQs). These questions request as an answer a short text or essay. The answer is evaluated and graded by the examiner. Previous works exhibit that MCQs have the same validity as the ones coming from CRQs tests and they are at the same time highly reliable (Lukhele et al., 1994; Wainer \& Thissen, 1993; Wainer \& Thissen, 2001). There are two works (Ventouras et al., 2010; Triantis \& Ventouras., 2011) that compare the results coming from both methods (CRQs and MCQs) that are statistically identical when using a special grading rule applied to the MCQs examination. Another work (Ventouras et al., 2011) is comparing oral examination and MCQs examination using the same special grading rule. The modules that the method was applied were core engineering courses thus there was a great interest to objectively evaluate students in order to identify any potential gaps in their knowledge that may affect their further studies. This method is based on the formulation of questions in pairs. Every pair addressed the same topic in a way that this fact is not evident to the student that did not possess adequate knowledge. A cumulative grade for the pair is calculated including bonus points if both questions are answered correctly or subtracting points as a penalty if one question is answered correctly. The aim of that scoring rule is to penalize guessing, in a way that might not positively induce the dissuading effects mentioned above, which are related to the negative marking part of the commonly used mixed-scoring schemes.

The aim of the present work is to further investigate the similarity of results when applying both methods in another engineering course and exploit the possibilities offered by the use of IT in the educational process. An objective of this work is to use MCQs examination methods, in conjunction or alternatively, with examination methods which are not suited for the PC environment, such as CR tests.

This study belongs to an ongoing research framework regarding assessment methods and parameters that can be potentially used as reliability and validity markers of the examination methods. There exist substantial indications that MC scores provide higher reliability and are as valid as scores extracted from examinations based on the CRQs method (Wainer \& Thissen, 1993; Lukhele, Thissen, \& Wainer, 1994). These indications would help in
promoting the use of MCQs tests in most educational settings where CRQs are still used, especially taking into account the drawbacks of the CRQs examination as the subjects that might be examined cannot cover a significant amount of the material taught during the courses along with their inherent inability of introducing automated grading in essay-like responses to questions. Concerning the interest and motivation of engineering students to use new technological tools as part of their educational process an electronic examination will provide immediate results and could be an essential enhancement in the context of a larger effort already began in the Technological Education Institute of Athens of introducing computer aided and web tools for supporting teaching. This fact requires research and well defined methods for creating objective


During the academic period 2012-2013, a course was selected, in order to compare the results produced by both examination methods. The course is entitled "Project Management" and belongs to the group of supplementary engineering courses taught in the Department of Electronics hosted by the Technological Educational Institute (T.E.I.) of Athens. The same group of 37 students participated in both examinations (MCQs and CRQs). All students had completed the course and polymorphic material (notes, videos, etc.) in digital format had been provided to them. Moreover, all students were familiarized with the electronic examination platform which would be used for both examinations. During the CRQs examination the students had to type their answer into the appropriate text field. For the case of MCQs examination the students had to answer the question by clicking one of the possible answers. The examination took place in a PC laboratory room using an application called "e-examination". This application had been implemented in an effort to introduce at the Technological Educational Institute (T.E.I.) of Athens, LMS tools to support the educational process (Tsiakas et al., 2007; Stergiopoulos et al., 2006). At the end of the MCQs test an electronic report was produced for each student. This report included all questions with the correct answer and the indication of whether it was correctly or wrongly answered, as well as the final score. One copy was given to the student and one to the examiner, for
processing the scores．
For the CRQs examination，a set of twenty（20） questions was created．The distribution of CRQs was designed in a way that they covered all topics taught during the course．Their difficulty level varied and a special weight in terms of grading was appointed to each one according to the level of difficulty．The total score that a student could achieve was 100 points．

For constructing the MCQs examination the questions were selected by a database that contains a large number（ $\mathrm{N}=300$ ）of questions which also addressed all the topics taught during the course．By using a special software，a first set of MCQs $\left\{q_{a 1}\right.$ ， $\left.\mathrm{q}_{\mathrm{a} 2}, \ldots, \mathrm{q}_{\mathrm{ak}}\right\}(\mathrm{k}=20)$ was randomly selected from the database．Once again，a weight $\mathrm{w}_{\mathrm{ai}}$ was assigned to each question $\mathrm{i}=1, \ldots, \mathrm{k}$ ，depending on its level of difficulty．In order to form 20 pairs of questions， another set was selected from the same database $\left\{\mathrm{q}_{\mathrm{b} 1}, \mathrm{q}_{\mathrm{b} 2}, \ldots, \mathrm{q}_{\mathrm{bk}}\right\}(\mathrm{k}=20)$ ．Each pair addressed the same topic and the knowledge of the correct answer for question $q_{a i}$ ，from a student who had performed a thorough study implied the knowledge of the correct answer for $\mathrm{q}_{\mathrm{bi}}$ and vice versa．The total score that a student could achieve was 100 points．The examiners took special care that both examinations were of the same level of difficulty in order that the results could be comparable．During this examination all questions form pairs in order to apply the scoring rules in all the set and trying to eliminate the guessing factor from each and every one of the questions addressed by the students．

## 3 SCORING METHODOLOGY

As mentioned above，the CRQ＇s examination includes twenty questions．Each question corresponds to a certain grade according to its difficulty．The way that the student answers the question is evaluated by the teacher．The overall examination score $m l$ was extracted，as the sum of the partial grades，and is by definition normalized to a maximum value of 100 ．

For the MCQs the score was calculated as follows：For each MCQs pair $\mathrm{i}=1, \ldots, 20$ ，the ＂paired＂partial score $p_{i}$ is：

$$
\begin{equation*}
p_{i}=\left(q_{a i} w_{a i}+q_{b i} w_{b i}\right)\left(1+k_{\text {bonus }}\right) \tag{1.a}
\end{equation*}
$$

if both $q_{a i}$ and $q_{b i}$ were correct $\left(q_{a i}=q_{b i}=1\right)$ or

$$
\begin{equation*}
p_{i}=\left(q_{a i} w_{a i}+q_{b i} w_{b i}\right)\left(1-k_{\text {penaly }}\right) \tag{1.b}
\end{equation*}
$$

if $q_{a i}$ or $q_{b i}$ was correct $\left(q_{a i}=1\right.$ and $q_{b i}=0$ ，or $q_{a i}=0$ and
$\left.q_{b i}=1\right)$.

$$
\begin{equation*}
p_{i}=0 \tag{1.c}
\end{equation*}
$$

if both $q_{a i}$ and $q_{b i}$ were incorrect，in which case $q_{a i}=q_{b i}=0$ ．

The parameters $k_{\text {bonus }}$ and $k_{\text {penalty }}$ were variables that are used for the calibration of the bonus／penalty mechanism applied to the scoring rule．For most pairs，the questions of the pair had the same weight． This means that $w_{a i}=w_{b i}$ ．

In some cases though，the weight of the two paired questions differed slightly（i．e．，by 0．5） because it is not possible for some topics to create a pair of questions that referred to the same topic and the knowledge of the correct answer for question $q_{a i}$ ， from a student who systematically studied implied the knowledge of the correct answer for $q_{b i}$ and vice versa and were also absolutely equal in their level of difficulty

The total score $m 2$ ，with maximum value equal to 100 ，was then computed as：

$$
\begin{equation*}
m 2=\frac{\sum_{i=1}^{20} p_{i} \text { LIロATIロN引 }}{\left(1+k_{b o n u s}\right) \cdot \sum_{i=1}^{20}\left(w_{a i}+w_{b i}\right)} \tag{2}
\end{equation*}
$$

Therefore，for the calculation of score $m 2$ ，a bonus is given to the student for correctly answering both questions of the pair $\left(q_{a i}, q_{b i}\right)$ and a penalty for correctly answering only one question of the pair．In the case that a student left a question unanswered intentionally or because of running out of time，a penalty would be given regarding the pair that the question belonged to．Following this scoring algorithm，the final score corresponds to the paired MCQs examination method．

Another scoring method was applied to the same group of questions．This method is characterized by a classic scoring rule applied to MCQs examinations．When a student gave a correct answer the score that corresponded to this question was added to the overall one．Otherwise，in case of a wrong answer，the student got no points at all．This method ignores any relation existed between the questions of a pair．Moreover，no penalty or bonus was considered during the scoring process．The overall score（ $m 3$ ）for this method was calculated using the following equation：

$$
\begin{equation*}
m 3=\frac{\sum_{i=1}^{20}\left(q_{a i} w_{a i}+q_{b i} w_{b i}\right)}{\sum_{i=1}^{20}\left(w_{a i}+w_{b i}\right)} \tag{3}
\end{equation*}
$$

The weights ( $w$ ) as well as the points assigned to each question in case of a correct answer remained the same. Eq. 3 is a special case of Eq. 2 when $k$ was omitted.

## 4 VALIDITY THREATS

Validity is the most important characteristic of assessment data. The threats to validity are circumstances or processes that undermine the assessment. The most important threats to the validity of the study are discussed below:

The issue of poorly crafted questions is very significant as writing effective MCQs as well as CRQs which test important cognitive knowledge is a demanded task. The teacher should be able to create sets of questions comprised of the MCQ type supported by the application. This depends on the structure of the module and the nature of the examination topics. The challenge was to fragmentise big problems and exercises into MC questions covering at the same time a wide range of the module topic. The questions can be separated into groups of different level of difficulty. There was previous experience in organizing and conducting electronic examinations for the specific module (Ventouras et al., 2010).

Various testing irregularities can be that the students have prior knowledge of the test questions or that they perform unethical actions (i.e. cheating) during the examination. Such action can severely affect the score. Students from the specific department were more or less accustomed to new technologies and the use of computers. They were also familiar with the concept of MCQs examined electronically and they had access to sample MCQs tests for self-evaluation purposes. These questions were not part of the current examination. Moreover, the software package used for the electronic examination had the feature to present to each student's monitor the set of the questions along with their corresponding answers in random order. This way any attempt of cheating or communication among the examinees could be immediately apparent by the supervisor.

All students were "testwise" in terms of been familiar with the MCQ exam process. The teachers of the module had taken special care during the construction of the questions in order to create sets that could not easily answered by guessing. In any case the "paired questions" concept also contributed to the solution of this issue.

Test Item Bias refers to the fairness of the test
item for different groups of students. In case that the test item is biased different group of students have different probabilities of correctly responding. For the purposes of the current study the same group of students took part in both examinations which were constructed and controlled by experienced teachers

## 5 RESULTS \& DISCUSSION

In the present study the effects of changing the value of parameter k were investigated. Regarding MCQs examination Eq. 3 was initially used for the calculation of the MCQs examination results. This equation corresponds to the classic scoring rule meaning that no bonus nor penalty points were taken into consideration. This simplified scoring rule produced results that were higher than the ones produced by the CRQs examination. Apart from the top scores that well prepared students achieved and did not present significant differences, all other scores presented a deviation. A possible explanation could be the absence of a mechanism that fixed the "guessing" factor when answering the questions. In Figure 1 the regression line of score ( ml ) to score (m3) are presented. The fitting is based on a second degree polynomial. It is observed that most students' scores are above the bisector as shown in Figure 1. A fit for the score can be quantified using parameter $R^{2}$ which is related to the regression line of CRQ score of each student $(\mathrm{ml})$ to the MCQ score $(\mathrm{m} 3)$ of the same student. Its best possible value is 1 . The value of $R^{2}$ for this case is equal to 0.9554 .


Figure 1: Regression line of CRQ score of each student ( $m 1$ ) to the MCQ score ( $m 3$ ).

It must be noted that in order to have comparable results, students had been informed that incorrect
answers did not have any additional penalty in terms of negative marking. This way they were encouraged to attempt answering any questions that might have a rough knowledge on the topic. During this examination the students were not aware of the scoring rule based on paired questions as this knowledge might be a factor that affect decision making under uncertainty. In turn, this might produce variance in the test scores that is related to the expectations of the examinees and not to the knowledge that is tested (Bereby-Meyer et al., 2002; Bereby-Meyer et al., 2003). The final report produced by the system included only the scores calculated based on the classic scoring rule meaning that no bonus nor penalty points were taken into consideration (m3).

The bias that is probably caused by the "guessing" factor is clearly corrected when using the scoring rule of paired questions. This is shown in Figure 2 if the regression line is compared to the one shown in Figure 1. An attempt to find the optimal values was made in order to have a better fit of the scores achieved by the examinees during both examination methods. For this the case the $k_{b o n u s}$ and $k_{\text {penalty }}$ parameters are considered as one parameter $k$. This means that the same value is assigned to both parameters. This value is added to the score if the student correctly answered both questions of the pair and it is subtracted if the student failed to correctly answer one question of the pair. The results produced by the system were only available for the examiners in order to perform the research.

Table 1: Results of the examination methods.

| CRQ <br> method | MCQ method (paired questions) |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | $\mathrm{k}=0.26$ | $\mathrm{k}=0.28$ | $\mathrm{k}=0.30$ | $\mathrm{k}=0.32$ | $\mathrm{k}=0.34$ |
| 64.97 | 65.50 | 65.14 | 65.20 | 64.70 | 64.41 |

In Table 1 the results using CRQs and MCQs with paired questions are shown. For the MCQs examination method different values of $k$ parameter were set when calculating the overall score of each student using Eq. 2. It is shown that for the parameter $k=k_{\text {bonus }}=k_{\text {penalty }}=0.30$ the mean value of the distribution of scores calculated for the MCQ method is very close to the mean value of the distribution of scores of the CRQ method. This is in agreement with the results of previous electronic examinations using the Bonus/penalty scoring methodology (Triantis \& Ventouras, 2011). Further research and more examination results of various courses are required in order to evaluate the optimized value parameter k which seems to be
approximately equal to 0.3 . A fit for the score can be quantified using parameter $R^{2}$ which is related to the regression line of CRQ score of each student ( ml ) to the MCQ score ( $m 2$ ) of the same student. Its best possible value is 1 . In Figure 2 the regression line of score $(m 1)$ to score ( $m 2$ ) are presented for $k=0.30$. It is observed that $R^{2}$ remained at a high level ( $>0.98$ ) close to a value equal to 1 for $0.30 \leq k \leq 0.34$.


Figure 2: Regression line of CRQ score of each student ( $m 1$ ) to the MCQ score ( $m 2$ ).

A metric related to the variation of the $k$ parameter value is the sum of the squared differences of the students' scores during MCQs (paired questions) and CRQs examination. The sum of squared error (SSE) is calculated by the following equation:

$$
\begin{equation*}
S S E=\sum_{j=1}^{37}\left(m 1_{j}-m 2_{j}\right)^{2} \tag{4}
\end{equation*}
$$



Figure 3: Sum of squared differences of $m 1$ and $m 2$ as related to $k$ parameter. $R^{2}$ related to $k$ parameter.

The optimum value that the sum could have reached was zero. In Figure 3 is shown that the function of sum to parameter $k$ is smoothly varying
within the space of $k=0.26$ and $k=0.34$ having a minimum at $k=0.30$. This value of k parameter is the optimum one to apply to the scoring rule. In the same figure the relation of $R^{2}$ to parameter $k$ is also shown. It is observed that the maximum value of $R^{2}$ was also found for $k=0.3$. This value which seems to be the optimal one and has been also observed during the implementation of this method to other modules already published (Ventouras et al., 2010; Triantis \& Ventouras., 2011) and optimses the students' overall score in a way that they objectively reflect their level of knowledge.

## 6 CONCLUSIONS

Electronic examinations supported by special software tools are very helpful for the educational process as they provide the means for the automatic production of the results and the ability to easily apply different scoring rules. This way the lecturer can have a clear image of the results which may be used for optimizing the way of teaching and disseminated material.

During the comparison of the CRQs examination method and the MCQs examination method it was observed that the classic scoring rule of positive score for correct answers introduced a bias due to the failure of eliminating the "guessing" factor, a common phenomenon of MCQs examinations. Therefore, such a simple scoring rule cannot advance MCQs examination for potentially substituting a CQRs examination method. Nevertheless, by applying a scoring rule that introduces the use of a special parameter that its value is added or subtracted to the overall score according to the correct or wrong answers along with the concept of pairs of questions addressed the same topic, can give results that are very close to the ones produced by the CQRs method. To the extent of the results of the present study, indication is provided that a value of k parameter approximately equal to 0.3 can optimally give results that clearly and objectively reflect the level of student's knowledge.

The key factor for applying this rule is a thorough preparation of the questions from the examiner in such a way that they cover all topics of interest and can form pairs in a way that their relation to a specific topic will not be evident to a student that is not well prepared.

Part of future work will be the research on results when assigning different values to $k_{\text {bonus }}$ and $k_{\text {penalty }}$ parameters, respectively. During this research an
algorithm might also designed for enhancing the electronic examination application by automatically selecting the optimized value of $k$ parameter. The scoring rule has to be tested in other modules as well in order to further verify its usefulness as an objective evaluation tool.

## REFERENCES

Bereby-Meyer, Y., Meyer, J., \& Flascher, O. M. 2002. Prospect theory analysis of guessing in multiple choice tests. Journal of Behavioral Decision Making, 15(4), pp. 313-327.
Bereby-Meyer, Y., Meyer, J., \& Budescu, D. V. 2003. Decision making under internal uncertainty: The case of multiple-choice tests with different scoring rules. Acta psychologica, 11(2), pp. 207-220.
Bush, M. E. 2006. Quality assurance of multiple-choice tests. Quality Assurance in Education, 14(4), pp. 398404.

DeBord, K. A., Aruguete, M. S., \& Muhlig, J. 2004. Are computer-assisted teaching methods effective?, Teaching of Psychology, 31(1), pp. 65-68.
Dede, C. 2005. Planning for neomillennial learning styles. Educause Quarterly, 28(1), 7-12.
Friedl, R., Höppler, H., Ecard, K., Scholz, W., Hannekum, A., Öchsner, W., \& Stracke, S. 2006. Multimediadriven teaching significantly improves students’ performance when compared with a print medium, The Annals of thoracic surgery, 81(5), pp. 1760-1766.
Freeman, R., \& Lewis, R. 1998. Planning and implementing assessment. Routledge.
Lukhele, R., Thissen, D., \& Wainer, H. 1994. On the Relative Value of Multiple Choice, Constructed Response, and Examinee Selected Items on Two Achievement Tests, Journal of Educational Measurement, 31(3), pp. 234-250.
Reiser, R. A., \& Dempsey, J. V. 2011. Trends and issues in instructional design and technology. Pearson.
Scharf, E. M., \& Baldwin, L. P. 2007. Assessing multiple choice question (MCQ) tests-a mathematical perspective, Active Learning in Higher Education, 8(1), pp. 31-47.
Stergiopoulos, C., Tsiakas, P., Triantis, D., \& Kaitsa, M. 2006. Evaluating Electronic Examination Methods Applied to Students of Electronics. Effectiveness and Comparison to the Paper-and-Pencil Method. In Sensor Networks, Ubiquitous, and Trustworthy Computing, 2006. IEEE International Conference on, 2, pp. 143-151..
Tsiakas, P., Stergiopoulos, C., Nafpaktitis, D., Triantis, D., \& Stavrakas, I. 2007. Computer as a tool in teaching, examining and assessing electronic engineering students. In EUROCON'07, The International Conference on "Computer as a Tool", pp. 2490-2497.
Triantis, D., \& Ventouras, E. 2011. Enhancing Electronic Examinations through Advanced Multiple-Choice Questionnaires. Higher Education Institutions and

Learning Management Systems: Adoption and Standardization, 178.
Ventouras, E., Triantis, D., Tsiakas, P., \& Stergiopoulos, C. 2010. Comparison of examination methods based on multiple-choice questions and constructed-response questions using personal computers, Computers \& Education, 54(2), pp. 455-461.
Ventouras, E., Triantis, D., Tsiakas, P., \& Stergiopoulos, C. 2011. Comparison of oral examination and electronic examination using paired multiple-choice questions. Computers \& Education, 56(3), pp. 616624.

Wainer, H., \& Thissen, D. 1993. Combining multiplechoice and constructed-response test scores: Toward a Marxist theory of test construction. Applied Measurement in Education, 6(2), pp. 103-118.
Wainer, H., \& Thissen, D. 2001. True score theory: The traditional method. Test scoring, 23-72.


