

Expression, Pose, and Illumination Invariant Face Recognition using Lower Order Pseudo Zernike Moments

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Abstract: Face recognition is an extremely challenging task with the presence of expression, orientation, and lightning variation. This paper presents a novel expression and pose invariant feature descriptor by combining Daubechies discrete wavelets transform and lower order pseudo Zernike moments. A novel normalization method is also proposed to obtain illumination invariance. The proposed method can recognize face images regardless of facial orientation, expression, and illumination variation using small number of features. An extensive experimental investigation is conducted using a large variation of facial orientation, expression, and illumination to evaluate the performance of the proposed method. Experimental results confirm that the proposed approach obtains high recognition accuracy and computational efficiency under different pose, expression, and illumination conditions.

1 INTRODUCTION

Face recognition remains an actively researched domain due to constantly increasing demands on performance in a wide range of applications. Following two decades of research, current face recognition systems have reached a certain state of maturity. However, this success is limited to some controlled settings. It has been noted that performance of many benchmark face recognition methods deteriorates significantly in uncontrolled, real world environment (Herman et al., 2009, Sultana and Gavrilova, 2013). The main constraints of current face recognition systems are varying illumination, viewing directions, poses, head tilts, and facial expressions. Due to the aforementioned natural constraints, intra-class variation of face images might be very large while interclass difference becomes quite small – consequently making the face recognition systems performance deteriorate. Thus, at present time, an efficient face recognition system should have the following properties (Wang et al., 2013, Bairagi et al., 2012):

- 1) High recognition accuracy.
- 2) Pose and facial expression invariance.
- 3) Insensitiveness to lightning variation.

- 4) Low computation time.

Most of the existing face recognition methods are inclined to accomplish one or two of the above properties by controlling or disregarding the other conditions. For example, Demirel and Anbarjafari (Demirel and Anbarjafari, 2008) proposed a pose invariant face recognition method using grey level histograms disregarding lightning variation. An expression invariant face recognition method with computational efficiency is proposed by Bairagi et al. (Bairagi et al., 2012), but does not consider lightning variation. In 2013, Wang et al. (Wang et al., 2013) resolved the illumination problem without considering the varying facial expression and pose. Therefore, a face recognition system combining accuracy, computational efficiency, and robustness to pose, expression, and illumination is still a challenge.

In the proposed method, we combined Daubechies Discrete Wavelet Transform (DWT) (Shen and Strang, 1998) with lower order Pseudo Zernike Moments (PZMs) (The and Chin, 1988) as feature vector. It is evident from the previous research works that discrete wavelet transform is insensitive to facial expression and small occlusions (Foon et al., 2004). Haddadnia et al. (Haddadnia et

al., 2003) has identified that PZMs can be used as rotation, scale, and translation invariant facial features. Moreover, an optimum choice of orders of PZMs can effectively reduce feature dimensions leading to high-speed processing without deteriorating the recognition accuracy. In our approach, we combined lower order pseudo Zernike moments, discrete wavelet transform, and k-NN classifier to develop an expression and pose invariant as well as computationally efficient face recognition system. A novel normalization method is proposed and utilized in preprocessing stage to eliminate extensive lighting variations.

Therefore, the major contributions of this research work is twofold: 1. Presenting a novel expression and pose invariant face descriptor by fusing optimal features of PZM and DWT; 2. Integrating a novel face normalization method to achieve illumination invariance.

2 RELEVANT WORK

For more than two decades, moment invariants are considered as an important global shape feature for many pattern recognition applications. Authors of (Foon et al., 2004) confirmed that a small set of orthogonal moments such as Zernike moments and PZMs can efficiently represent images by their discriminative and non-redundant features. However, moment based face recognition system is still an undermined research area. In this section, a discussion of some of the previous works on orthogonal moment based face recognition is presented.

PZMs were first utilized for face recognition by Haddadnia et al. (Haddadnia et al., 2003). In their study, it is shown that PZM performs better than Zernike and Legendre moments. A comparatively recent study (Nabatchian et al., 2008) also demonstrates that PZM performs the best among other commonly used moment invariants for face recognition. In 2004, Pang et al. (Pang et al., 2006) gained 36.23% reduction in computation time by combining Symmlet orthonormal wavelet filter of order 5 and PZM. However, this study lacks investigation of optimum order of PZM and experimentation is conducted using only one database, where expression and pose invariant features were not studied as well. Behbahani and Bastani (Behbahani and Bastani, 2011) used PZM with probabilistic neural network classifier for face recognition. A very recent study (Farokhi et al., 2013) has confirmed that ZM can also be used for

noise and rotation insensitive infrared face recognition. Although from the above discussion it is apparent that ZM and PZMs are producing very promising result for face recognition, most of the previous works lack the following studies:

- 1) Majority the experiments are conducted using only one trivial database (e.g. AT&T).
- 2) Performance evaluation of the methods under pose, expression, and illumination changes remained unconsidered.

Along with presenting a novel PZM based face recognition method these issues are also addressed in experimentation section of this paper.

3 PROPOSED METHOD

The proposed face recognition system has three stages: image normalization, features extraction by DWT and PZM, and classification of faces by k-NN. The novelty of the proposed method lies in a new normalization method, and in fusing DWT and PZM with optimal parameters for recognition of face images under unconstraint environment. Each of the stages is described in the following sub-sections.

3.1 Normalization

In this section, a novel face normalization method is proposed that eliminates the variation in illumination and shadowing while preserving enough details to be used for the recognition purpose. The novelty of this method lies in improving a well-known normalization method Weber-face (Wang et al., 2011) by applying bi-lateral filter (Paris et al., 2007) and integrating gamma correction (Tan and Triggs, 2007) for detail enhancement. We refer this normalization method as *Improved Weber-face*. In the proposed normalization method, gamma is applied at first to enhance details of the darker regions and compress highlights of the brighter regions. It reduces the intra-class variability due to extensive illumination change. Next, illumination invariant face is generated using Weber-face and bi-lateral filter since gamma correction cannot remove the influence of the overall intensity gradients. Weber-face normalization is proposed by Wang et al. in 2011 which outperformed a number of state-of-the-art normalization methods. In this method, at first Gaussian filter smoothens the image then Weber's local descriptor is used to generate a ratio image called Weber-face. Gaussian filter blurs the edges since it averages the pixel values using the

same kernel everywhere in the image. Whereas, bilateral filter uses different size of kernels depending on the content of the image which consequently preserves edges better than Gaussian filter (Paris et al., 2007). To improve the smoothing and edge preserving feature of Weber-face method, we replaced the Gaussian filter by bilateral filter. As a result, the proposed method will normalize face images with less intra-class variability while preserving more interclass details. This stage can be considered as image pre-processing where face images will be normalized if required. The normalization method is as follows:

Step 1: Apply gamma correction on the input image I for detail enhancement. Gamma correction of a grayscale image I is as follows (Gamma correction):

$$\text{If } I(x, y) < 0.018 \text{ then } I'(x, y) = 5.5I(x, y) \quad (1)$$

$$\text{If } I(x, y) \geq 0.018$$

$$\text{then } I'(x, y) = 1.099I(x, y)^{0.55} - 0.099, \quad (2)$$

where $I(x, y)$ and $I'(x, y)$ are the pixels at (x, y) coordinate of the grayscale and gamma corrected grayscale images, respectively. The gamma correction of a color image is as follows:

$$\text{If } R, G, B < 0.018$$

$$\text{then } R' = 5.5R, G' = 5.5G, B' = 5.5B \quad (3)$$

$$\text{If } R, G, B \geq 0.018$$

$$\text{then } R' = 1.099R^{0.55} - 0.099,$$

$$G' = 1.099G^{0.55} - 0.099, \text{ and}$$

$$B' = 1.099B^{0.55} - 0.099, \quad (4)$$

where R' , G' , B' are the gamma corrected red (R), green (G), and blue (B) channels of the color image. The gamma corrected color image then converted to grayscale image (Y) using the following equation:

$$Y = 0.299R' + 0.587G' + 0.114B' \quad (5)$$

Step 2: Smoothen the input image Y while preserving the interclass details (e.g. edges) using bilateral filter $B(\sigma_s, \sigma_r)$

$$Y' = Y * B(\sigma_s, \sigma_r), \quad (6)$$

Where $*$ is the convolution operator and $B(\sigma_s, \sigma_r)$ is the kernel function of bilateral filter with space parameter σ_s and range parameter σ_r .

Step 3: Finally, generate the improved Weber-face (W) from Y' by applying Weber local descriptor (Wang et al., 2011):

$$W = \arctan \left(\alpha \frac{\sum_{i \in A} \sum_{j \in A} \frac{Y'(x, y) - Y'(x - i\Delta x, y - j\Delta y)}{Y'(x, y)}}{\sum_{i \in A} \sum_{j \in A} \frac{Y'(x, y) - Y'(x - i\Delta x, y - j\Delta y)}{Y'(x, y)}} \right),$$

where $A = \{-1, 0, 1\}$. (7)

3.2 Feature Extraction

This section presents a novel feature descriptor by combining Daubechies DWT and lower order pseudo Zernike moments to obtain expression and pose invariance. We used DWT for the following three reasons (Foon et al., 2004, Pang et al., 2006):

- Low frequency subband is expression and small occlusion invariant.
- Lower resolution image facilitates fast computation and low storage.
- Decomposition to low frequency subband smoothens image thus reduces noise.

Two-dimensional (2D) DWT decomposes an input image into four sub-bands, one low frequency component (LL) and three detail components (LH, HL, HH). From experimentation we found that expression features are mostly eliminated at the 3rd level of decomposition, yet it preserves enough details to represent facial features of the individual. Therefore, we decomposed all face images up to 3rd level and considered the LL subband as DWT face feature. All the images are resized to 128×128 pixels as part of pre-processing. Thus, size of the final low frequency component image (LL) after 3rd level of decomposition is 16×16. Pseudo Zernike moment invariants are then computed from LL subband to represent the feature vector of the face image.

The orthogonal property of PZMs can uniquely represent an image regardless of geometric rotation and also reduces information redundancy (Teh et al., 1988). The kernel of PZM is a set of orthogonal moments inside a unit circle and is defined in polar coordinates (Behbahani and Bastani, 2011). The two dimensional PZM of order n and repetition m of an image in polar coordinate $f(r, \theta)$ are defined as (The et al., 1988, Behbahani and Bastani, 2011):

$$Z_{nm} = \frac{n+1}{\pi} \int_0^{2\pi} \int_0^1 V_{nm}(r, \theta) f(r, \theta) r dr d\theta, \quad (8)$$

$$\text{where } V_{nm}(r, \theta) = R_{nm}(r) e^{-jm\theta}, j = \sqrt{-1}$$

and $r = \sqrt{x^2 + y^2}$, $\theta = \tan^{-1} \left(\frac{y}{x} \right)$, $x, y \in [-1, 1]$, $R_{nm}(r)$ is the radial polynomial and is defined as follows:

$$R_{nm}(r) = \sum_{s=0}^{n-|m|} (-1)^s \frac{(2n+1-s)!}{s!(n+|m|+1-s)!(n-|m|-s)!} r^{n-s} \quad (9)$$

PZMs of different orders are non-redundant which can act as discriminative features for face recognition. In addition, the rotation invariant property of PZM will facilitate pose invariance.

3.3 Classification

Finally, the query image is classified by matching its feature vector to that of database images. The feature vectors of the database images are obtained from feature database. The k-NN classifier (Cover and Hart, 1967) is chosen since it performs better than PNN and LDA for lower dimension of Zernike moments (Nabatchian et al., 2008). Moreover, k-NN is simple and has a wide range of applications. K-NN classifier classifies objects based on the closest training samples in the feature space. The closest k neighbors are determined by applying a distance function. In the proposed method, we considered Euclidean distance and k=1.

From existing works we know that higher order PZMs have better discriminative features but they are more noise sensitive and computationally expensive. Conversely, the lower order PZMs have less feature dimension, ease of computation, better noise tolerance but less discriminative features. Therefore, it is very important to optimally combine the PZM features to achieve the best performance in terms of both recognition rate and computation time. The following section describes feature set optimization process to obtain the best result from the proposed system.

4 FEATURE OPTIMIZATION

We optimized the order of the PZM, and the order and type of DWT to obtain the best performance. Also, we investigated how the performance of the proposed system vary for different values of k of k-NN classifier with different distance functions. This process can be considered as selection of best feature set and all experimentations are done only once on AT&T database (AT&T Lab). The obtained feature set can be applied to any database and there is no need to fine tune the feature set again for any application of this method.

It is obvious that higher order PZM has greater number of features which consequently increase the computation time. On the other hand, lower order PZM has ease of computation due to their small number of features but individually does not possess enough discriminating information for pattern recognition. Therefore, 1st to 12th order moments are combined and experimented to find the optimum combination which produces the best result. Fig. 1 illustrates the number of features of PZM at different orders and corresponding recognition accuracy. The best result is achieved for 44 features which is the

combination of 1st to 8th order PZMs. A performance drop is also observed for the combination of higher order PZM features in Fig. 1. This is probably because higher order PZM features are more sensitive to noise and contain information which reduces the inter-class variation of face images. Next, a choice of the best wavelet basis among Haar, Daubechies, and Symmlet filters of different orders is obtained. From Fig. 2 one can see that Daubechies filter of order 6 (db6) has the best recognition rate with 1st to 8th order PZM features.

Finally, the performance of Euclidean, cosine, Manhattan distance and correlation with k=1 and 3 of k-NN classifier is investigated and the best result is obtained for Euclidean distance with k=1. Table 1 summarizes the results of this experimentation.

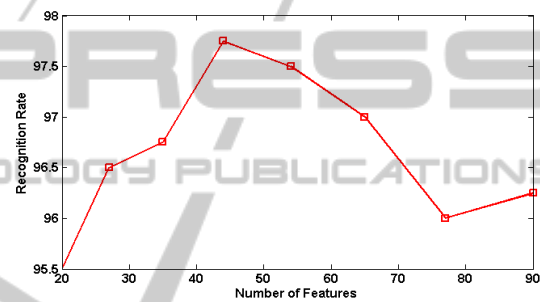


Figure 1: Variation of recognition rate for different number of PZM features

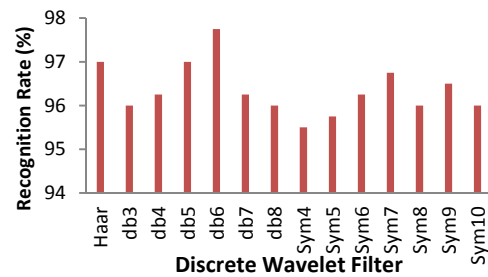


Figure 2: Recognition rate of various wavelets filters

Table 1: Classification accuracy of various distance methods for k=1, 3 on AT&T database.

Distance	Accuracy (k=1)	Accuracy (k=3)
Euclidean	97.75	91.25
Cosine	96.75	89.75
Manhattan	96.5	90
Correlation	95.5	85

5 EXPERIMENTAL RESULTS

Performance of the proposed method is evaluated on

the following four standard face image databases:

AT&T (AT&T Lab): It contains 400 greyscale images of size 92×112 pixels. There are 10 different images for each of the 40 distinct subjects. Images were taken at different times, illumination, facial expressions, side movements, and facial details.

AR (Martinez and Kak, 2001): It contains color images of 70 males and 56 females. Each subject has 26 different images in two sessions. Each session has 13 different images per subjects in different conditions expression (natural, smile, anger, screaming), illumination (left light on, right light on, both lights on), and occluded conditions.

Yale (Yale database): It contains total 165 images of 15 subjects. Images were taken in different facial expressions: happy, normal, sad, sleepy, surprised, wink and lightning conditions with/without glasses.

Sheffield (Sheffield database): It contains facial images of mixed race/gender/appearance of 20 individuals. Each individual is shown in a range of poses from profile to frontal views.

The above four databases contain face images with large variations in expression, pose, and illumination. During experimentation we created three databases by randomly picking images from these four databases to evaluate the performance our system in different conditions in varying conditions:

- **DB1**: We created this database by randomly picking 40 subjects from AT&T, AR, and Sheffield database. Therefore, this database comprises of images with large variation of pose and expression with little or no illumination change.
- **DB2**: This database is created by randomly picking 40 images from Yale and AR database. Therefore, it contains facial images with large variation of illumination conditions with little or no expression change.
- **DB3**: This database contains all images from DB1 and DB2.

Fig. 3 shows some sample images from DB1 and DB2.

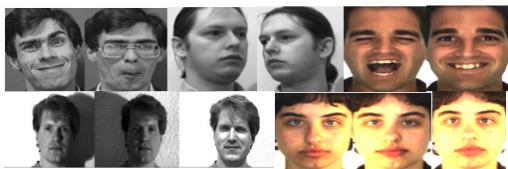


Figure 3: Sample face images from DB1 (row 1) and DB2 (row 2).

Fig. 4. shows 10 fold cross validation results of well-known Principle Component Analysis (PCA) and the proposed method on DB1, DB2, and DB3.

From Fig. 4 one can see that the proposed method consistently maintains highest recognition rate regardless of expression, pose, and illumination changes. We compared the performance of the proposed normalization method and Weber-face normalization method. For this experimentation, the proposed feature descriptor is combined with Weber-face and improved Weber-face methods, respectively.

The performance comparison of the Weber-face and proposed improved Weber-face method on DB2 and DB3 is shown in Fig. 5. Fig. 5 shows that the proposed improved weber-face method has better recognition rate under varying illumination conditions than Weber-face method. The computational efficiency of the proposed method is evaluated as well. The extraction time of 44 features and the classification time of the proposed method are computed on AT&T database. The result is compared to solely PZM based method using the same experimental setup.

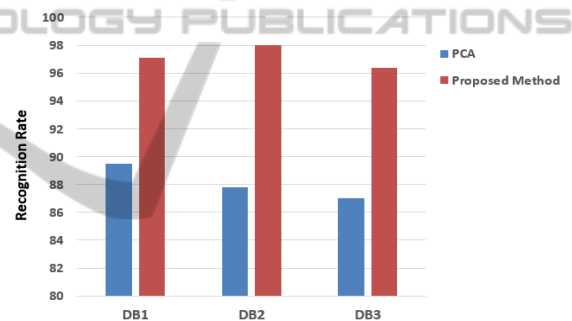


Figure 4: Recognition rate of PCA and the proposed method on different databases.

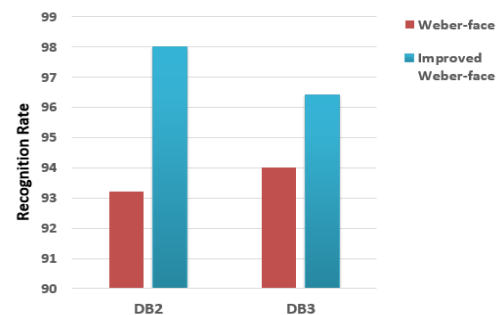


Figure 5: Recognition rate of Weber-face and Improved Weber-face method on DB2 and DB3.

Table 2 shows that proposed integrated DWT and PZM based feature extraction obtains **12.57** times reduction in computation time over solely PZM based feature extraction. Therefore, it has been demonstrated that the use of low dimensional subband image and small number of features makes

our system computationally very efficient. All experiments are carried out on MATLAB R2013a, Windows 7 OS, Intel Core i3 2310M processor with 4GB RAM.

Table 2: Computation time (in seconds) on AT&T database.

Method	Feature extraction time of 400 images (s)	Classification time per fold (s)	Overall time (s)
PZM	227.21	0.016	227.226
Proposed Method	18.07		18.086

6 CONCLUSIONS

Recognizing faces in varying illumination, pose, and expression condition with computational efficiency is the most difficult problem of today's face recognition systems. An efficient face recognition system should be able to cope with all of these problems. In this paper, a novel lower order PZM based method is presented which can efficiently recognize faces regardless of illumination, pose, and expression change. Due to optimal choice of features the method obtains much better recognition rate with less computation time. Extensive experimentation confirms the high recognition rate, computational efficiency, and robustness of the proposed method under varying conditions. We believe that the proposed method has a very good potential to cope with the real challenges of current face recognition systems. Future works include analyzing the performance of the proposed method for other biometric recognition applications such as recognition of ear, palmprint etc.

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REFERENCES

AT&T Lab. Cambridge; www.cl.cam.ac.uk/research/dtg/attarchive/facedatabase.html, Accessed on 8 Oct., 2013.
 Bairagi, B. K., Chatterjee, A., Das, S. C., Tudu, B., 2012. Expressions invariant face recognition using SURF and Gabor features, *3rd Int. Conf. on Emerging Applications of Information Tech. (EAIT)*, 170-173.
 Behbahani, E. F., Bastani, A., 2011. Human face recognition by pseudo Zernike moment and

probabilistic neural network, *Int. J. of Engineering Science and Tech.*, 3(7), 5466-5469.
 Cover, T., Hart, P., 1967. Nearest neighbor pattern classification. *IEEE Trans. Inf. Theory*, 13(1), 21-27.
 Demirel, H., Anbarjafari, G., 2008. High performance pose invariant face recognition, *VISAPP*, 282-285.
 Farokhi, S., Shamsuddin, S. M., Flusser, J., Sheikh, U. U., Khansari, M., Jafari-Khouzani, K., 2013. Rotation and noise invariant near-infrared face recognition by means of Zernike moments and spectral regression discriminant analysis. *Journal of Electronic Imaging*, 22(1), 013030-013030.
 Foon, N. H., Pang, Y. H., Jin, A. T. B., Ling, D. N. C., 2004. An efficient method for human face recognition using wavelet transform and Zernike moments, *Int. Conf. on Computer Graphics, Imaging and Visualization (CGIV)*, 65-69.
 Gamma correction; http://software.intel.com/sites/products/documentation/hpc/ipp/ippi/ippi_ch6/ch6_gamma_correction.html#ch6_gamma_correction, Accessed on 8 Oct., 2013.
 Haddadnia, J., Ahmadi, M., Faez, K., 2003. An efficient feature extraction method with pseudo-Zernike moment in RBF neural network-based human face recognition system, *EURASIP journal on applied signal processing*, 890-901.
 Herman, J., Rani, S., Devaraj, D., 2009. Face recognition using generalized pseudo Zernike moment, *Annual IEEE India Conference*, 1-4.
 Martinez, A.M., Kak, A.C., 2001. PCA versus LDA, *IEEE TPAMI*, 23(2), 228-233.
 Nabatchian, A., Abdel-Raheem, E., Ahmadi, M., 2008. Human face recognition using different moment invariants: A comparative study, *Congress on Image and Signal Processing CISP'08*, 3, 661-666.
 Pang, Y. H., Teoh, A. B., Ngo, D. C., 2006. A discriminant pseudo Zernike moments in face recognition, *J. of Research and Practice in Information Technology*, 38(2), 197.
 Paris, S., Kornprobst, P., Tumblin, J., Durand, F., 2007. A gentle introduction to bilateral filtering and its applications, *ACM SIGGRAPH 2007 courses*, 1.
 Sultana, M., Gavrilova, M., 2013. A Content Based Feature Combination Method for Face Recognition, *CORES*, 197-206.
 Sheffield database; <http://www.sheffield.ac.uk/eee/research/iel/research/face>, Accessed on 8 Oct., 2013.
 Shen, J., Strang, G., 1998. Asymptotics of daubechies filters, scaling functions, and wavelets, *Applied and Computational Harmonic Analysis*, 5(3), 312-331.
 Tan, X., Triggs, B., 2007. Preprocessing and feature sets for robust face recognition, *CVPR*, 7, 1-8.
 Teh, C. H., Chin, R. T., 1988. On image analysis by the methods of moments, *IEEE TPAMI*, 10(4), 496-513.
 Wang, B., Li, W., Yang, W., Liao, Q., 2011. Illumination normalization based on Weber's law with application to face recognition. *Signal Proc. Lett.*, 18(8), 462-465.
 Wang, H., Ye, M., Yang, S., 2013. Shadow compensation and illumination normalization of face image, *Machine Vision and Applications*, 1-11.
 Yale database; <http://cvc.yale.edu/projects/yalefaces/yalefaces.html>, Accessed on 8 Oct., 2013.