# PERFORMANCE EVALUATION OF FEATURE DETECTION FOR LOCAL OPTICAL FLOW TRACKING

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Keywords: Feature detector, Feature detection Performance evaluation, Tracking, KLT.

Abstract:

Due to its high computational efficiency the Kanade Lucas Tomasi feature tracker is still widely accepted and a utilized method to compute sparse motion fields or trajectories in video sequences. This method is made up of a Good Feature To Track feature detection and a pyramidal Lucas Kanade feature tracking algorithm. It is well known that the Good Feature To Track takes into account the Aperture Problem, but it does not consider the Generalized Aperture Problem. In this paper we want to provide an evaluation of a set of alternative feature detection methods. These methods are taken from feature matching techniques like FAST, SIFT and MSER. The evaluation is based on the Middlebury dataset and performed by using an improved pyramidal Lucas Kanade method, called RLOF feature tracker. To compare the results of the feature detector and RLOF pair, we propose a methodology based on accuracy, efficiency and covering measurements.

#### 1 INTRODUCTION

Motion based analysis of a video sequence is an important topic in computer vision and visual surveillance. The KLT feature tracker (Tomasi and Kanade, 1991) still remains as a widely accepted and utilized method to compute sparse motion fields or trajectories in video sequences due to its high computational efficiency (Ali and Shah, 2007; Hu et al., 2008; Fradet et al., 2009). The KLT tracker is based on a GFT (Good Feature To Track) corner detector (Shi and Tomasi., 1994) and the Lucas/Kanade local optical flow method (Lucas and Kanade, 1981).

In the recent past several improvements of the Lucas/Kanade method have been developed: Pyramidal implementation (Bouguet, 2000) was proposed to estimate large motions, parallelizing using the GPU (Sinha et al., 2006) increases the runtime performance drastically, gain adaptive modifications (Zach et al., 2008) extend the robustness against varying illuminations and robust norms in association with a adaptive region size (Senst et al., 2011) improve the robustness against partial occlusion and non Gaussian noise. Whilst the tracking by local optical flow has been improved continually, the feature detecting is still based on the GFT method. This leads to several drawbacks. E.g. the GFT does not consider the multi scale approach of the pyramidal Lucas/Kanade implementation. Even the Lucas/Kanade local constant motion constraint is not taken into account by the GFT algorithm. In the recent decades feature detectors were developed for feature matching methods, e.g. SIFT (Scale Invariant Feature Transform) (Lowe, 1999), SURF (Speeded Up Robust Features) (Bay et al., 2008) and MSER (Maximally Stable Extremal Regions) (Matas et al., 2002). These techniques were applied e.g. in stereo, SLAM (Simultaneous Localization and Mapping) and image stitching applications

In this paper, we investigate the usability of several feature detectors related to local optical flow tracking. The evaluation is based on the Middlebury dataset (Baker et al., 2009). The dataset provides synthetic and realistic pairs of consecutively captured images and the optical flow as ground truth for each pair. We provide metrics for sparse motion estimation. These metrics take into account the accuracy, efficiency and the covering of the sparse motion field.

## 2 FEATURE DETECTION

In this section we briefly introduce the set of evaluated feature detectors. Most of the detectors are designed for feature matching, whose requirements differ from the tracking with local optical flow. Feature matching methods associate feature points of different images by extracting descriptors from the detected feature lo-

cation. Thus the features provide a limited set of well localized and individually identifiable anchor points. Important properties are repeatability and invariance against rotation, translation and scaling (Tuytelaars and Mikolajczyk, 2008).

The local optical flow estimates the feature motion by a first order Taylor approximation of the brightness constancy constraint equation of a specified region (Lucas and Kanade, 1981). Thus it depends on the appearance of vertical and horizontal derivatives of the image. This is known as the aperture problem. In addition it constrains that the specified region contains one moving pattern. This extends the aperture problem to the generalized aperture problem (Senst et al., 2011). As a consequence important properties of the patterns close to the feature points detected by a feature detector are cornerness and motion constancy.

**Good Features to Track.** The GFT method (Shi and Tomasi., 1994) is designed to detect cornerness patterns. The Gradient matrix **G** is computed for each pixel as:

$$\mathbf{G} = \sum_{\mathcal{O}} \begin{bmatrix} I_x^2 & I_x I_y \\ I_x I_y & I_y^2 \end{bmatrix} \tag{1}$$

with the intensity values I(x,y) of a grayscaled image and the spatial derivatives  $I_x,I_y$  for a specified region  $\Omega$ . The gradient matrix is implemented by means of integral images for  $I_x^2$ ,  $I_y^2$  and  $I_xI_y$ . Due to the use of integral images the computational complexity of the gradient matrix is constant and independent of the size of  $\Omega$ . A good feature can be identified by the maxima of  $\lambda(x,y)$ , the smallest eigenvalue of G. Thus good features prevent the aperture problem. Certainly strong corners appear at object boundaries, where multiple motions are very likely. This leads to the generalized aperture problem. Post processing is applied by non-maximal suppression and thresholds at  $q \cdot max(\lambda(x,y))$ , with q the cornerness quality constant.

**Pyramidal Good Features to Track.** The PGFT method is the pyramidal extension of the GFT method. The pyramidal implementation is done by up-scaling the region  $\Omega$  based on integral images. That is more efficient than down-scaling the image. For each scale the smallest eigenvalue  $\lambda_s(x,y)$  of the corresponding Gradient matrix is computed. A good feature can be identified by the maxima of  $\lambda(x,y)$ , whereby:

$$\lambda(x,y) = \max_{s}(\lambda_{s}(x,y)) \tag{2}$$

is the maximal eigenvalue of each scale.

**Feature from Accelerated Segment Test.** The FAST (Rosten and Drummond, 2006) method is de-

signed as runtime efficient corner detector. Corners are assumed at positions with not self-similar patches. This is measured by considering a circle, where  $I_C$  is the intensity from the centre of the circle and  $I_P$  and  $I_{P'}$  are the intensity values on the diameter line through the center and at the circle, hence at opposite positions. Thus a patch is not self-similar if pixels at the circle look different from the centre. The filter response is performed on a Bresenham circle and given by:

$$C = \min_{P} (I_P - I_C)^2 + (I_{P'} - I_C)^2.$$
 (3)

Rosten and Drummond proposed a high-speed test to find the minimum in computationally efficient way.

Scale Invariant Feature Transform. The SIFT (Lowe, 1999) method provides features that are translation, rotation and scale invariant. To achieve this, features are selected at maxima and minima of a DoG (Difference of Gaussian) function applied in scale space by building an image pyramid with resampling between each level. Focusing on speed the DoG is used to approximate the LoG (Laplacian of Gaussian). The local maxima or minima are found by comparing the 8 neighbors at the same level. These maxima or minima are compared to the next lowest level of the pyramid.

**Speeded Up Robust Features.** The SURF (Bay et al., 2008) are designed with a fast scale space method using DoB (Difference of Box) filters as a very basic Hessian matrix approximation. The Hessian matrix **H** at each scale is defined as:

$$\mathbf{H} = \begin{bmatrix} I_{xx} & I_{xy} \\ I_{xy} & I_{yy} \end{bmatrix} \tag{4}$$

where  $I_{xx}$  is the convolution of the Gaussian second order derivative with the image I. The DoB filters are implemented by integral images, hence the computation time is independent of the filter size. The filter response is defined as the weighted approximated Hessian determinant, where local maxima identify blob like structures. The scale space is analysed by upscaling the box filter, which is more efficient than down-scaling the image, followed by a scale space non-maximum suppression.

**STAR.** The STAR detector is derived from the CenSurE (Center Surround Extrema) detector (Agrawal et al., 2008). As well as the SURF the CenSurE is based on box filters. While DoB filters are not invariant to rotation, Agrawal introduced center-surround filters that are bi-level. The STAR feature detector uses a center-surrounded bi-level filter of two rotated

squares. The filter response is computed for seven scales and each pixel of the image. In contrast to SIFT and SURF the sample size is constant on each scale and is leading to a full spatial resolution at every scale. Post processing steps are done by non-maximal and line suppression. Features that lie along an edge or line are detected due to the Gradient matrix, see Eq. 1.

Maximal Stable Extremal Regions. The MSER detector (Matas et al., 2002) is designed to detect affine invariant subsets of maximal stable extremal regions. MSER are detected by consecutivly binarizing an image by a threshold. The threshold is applied from the maximal image intensity value to its minimal. At each step a set of regions  $\Phi$  is computed by connected components analysis. The filter response for each region i is defined as:

$$q_i = |\Phi_{i+\Delta} \backslash \Phi_{i-\Delta}| / |\Phi_i| \tag{5}$$

where |...| denotes the cardinality and  $i \pm \Delta$  the region at  $\Delta$ th lower or higher threshold level. The MSER are identified by the local minimum of q.

#### 3 FEATURE TRACKING

The motion estimation of the detected features is performed using RLOF (Robust Local Optical Flow) method (Senst et al., 2011) which is derived from the pyramidal Lucas/Kanade method (Bouguet, 2000). Based on the spatial and temporal derivatives of a specified region  $\Omega$  the RLOF computes the feature motion using a robust regression framework. A robust redescending composed quadratic norm was introduced to increase the robustness of motion estimation compared to pyramidal Lucas/Kanade method. To improve the behaviour at motion boundaries an adaptive region size strategy is applied to decrease  $\Omega$ . The region  $\Omega$  of a feature is decreased until the feature is trackable or a minimal region size is reached. The decision of being trackable is done by analysing the smallest eigenvalue  $\lambda$ , see Section 2, and the residual error of the motion estimates.

For the experiment the following parameters are used: a minimal region size of  $7 \times 7$ , a maximal region size of  $15 \times 15$ , the robust norm parameters  $\sigma_{1/2} = (8,50)$ , 3 levels and maximal 20 iterations. The RLOF is performed bidirectional, thus incorrect tracked features could be detect. We identify these by checking the consistency of forward and backward flow using a threshold  $\varepsilon_d = 1$ :

$$||\mathbf{d}_{I(t)\to I(t+1)} + \mathbf{d}_{I(t+1)\to I(t)}|| < \varepsilon_d \tag{6}$$

where  $I(t) \rightarrow I(t+1)$  denote the forward motion and  $I(t+1) \rightarrow I(t)$  the reverse.

# 4 EVALUATION METHODOLOGY

The Middlebury dataset (Baker et al., 2009) has become an important benchmark regarding dense optical flow evaluation. It provides synthetic and realistic pairs of consecutively captured images. The ground truth is given by optical flow for each pair. We use the database to evaluate the sparse optical flow results of the features found by the respective detector and tracked with the RLOF. We refine the evaluation methodology of Baker et al., 2009) in terms of accuracy, efficiency and covering measures. For each algorithm and each sequence we record the  $T_D$  the set of detected features,  $T_T \subset T_D$  the set of tracked trajectories with  $\dot{x}_T$  the endpoint of each trajectory as well as the runtime. The respective ground truth motion is given by  $\dot{x}_{T_{GT}}$  the ground truth endpoint of each trajectory.

Accuracy Measures. A basic property is the accuracy of the estimated tracks. The most commonly used measure is the endpoint error (Otte and Nagel, 1994) defined by:

$$EE(\dot{x}_T) = ||\dot{x}_T - \dot{x}_{T_{GT}}||^2.$$
 (7)

The compact statistic of the EE is often only given by the averages. Thus the measurement is affected by the outliers. Baker *et al.* proposed robust statistics by applying a set of thresholds to the error measurements. This report is limited so we decide to use the Median of endpoint errors (MEE).

**Efficiency Measures.** We measure the feature detection runtime  $t_D$ , which describes the computational complexity of the detection method and the tracking efficiency is defined as:

$$\eta = \frac{|T_T|}{|T_{GT}|}. (8)$$

In most cases the computational complexity of feature tracking is dominant. Therefore the tracking efficiency is an important measurement to trace methods detecting features which produce small MEE but a large number of rejected trajectories. Finally the *t* denotes the overall detection and tracking runtime.

**Covering Measures.** Compared with the evaluation of a dense optical flow method the challenge of comparing methods producing sparse motion fields is not

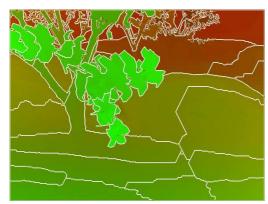


Figure 1: Ground truth optical flow and motion segments of the Grove2 sequence (The optical flow is shown as colorcode).

only to compare the outliers and the accuracy of the resulting track, but also to compare whether all the moving objects are assigned to tracks. In particular it depends on the application. For example methods as SLAM (Jonathan and Zhang, 2007) or GME (Tok et al., 2011) use trajectories of the background. In these examples it is not critical if the set of trajectories does not include all foreground objects. But for applications of motion based image retrieval e.g. object segmentation or extraction (Brostow and Cipolla, 2006) all objects have to be covered by trajectories. The covering measurement  $\rho$  is motivated by measuring the ability of the sparse motion field to represent all different moving objects in a scene. At first the ground truth is divided into a set of similar moving regions C by the color structure code segmentation method. This algorithm (Rehrmann and Priese, 1997) is modified to deal with a 2D motion field, see Figure 1. For each region C the density is computed as the quotient of the number of tracks  $|T_T \subset C|$  located at C and the area  $A_C$  of the region. The covering measurement  $\rho$  is defined as the mean density.

$$\rho = \frac{1}{|C|} \sum_{|C|} \frac{|T_T \subset C|}{A_C} \tag{9}$$

## 5 EVALUATION RESULTS

In this paper our goal is to provide a set of baseline results to allow researchers to get a feel for a feature detector that has a good performance on their specific problem. For this purpose we evaluate the proposed detection methods at the operating point of around 200 and 2500 feature points. We choose the operating point of around 200 points to analyze the performance of the feature detector with few feature points. Particularly in that case an ideal detector should provide a

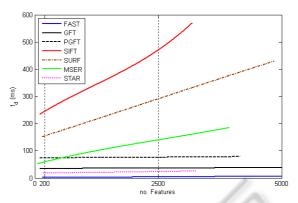


Figure 2: Feature detection runtime  $t_d$  related to the number of detected features for the *Grove3* sequence with VGA resolution.

high tracking performance, which indicates that the features are not set to motion boundaries where they are rejected more likely by the tracker. In contrast we want to analyze the performance regarding to the coverage with a denser motion field of around 2500 feature points.

The results for all algorithms are shown in Table 1. The experiments are performed on an AMD Phenom II X4 960 running at 2.99 GHz. All feature detections are computed on the CPU. The feature tracking is implemented by the RLOF method running on a Nvidia GTX 480 graphic device. The results suggest the following conclusions:

**FAST.** The FAST detector is designed as a high speed runtime efficient corner detector, which our experiments confirm. For the  $640 \times 480$  *Grove3* sequence the features detection runtime takes only 2 ms. Figure 2 shows that  $t_d$  is nearly constant regarding to the number of detected features. The plain parameterization is an additional advantage of this detector. Summarizing the FAST detector is a very fast detector for a huge set of features with a uniform distribution regarding to the moving object.

**GFT.** The GFT is the third fastest detector in our benchmark. The runtime  $t_d$  is constant regarding to the number of detected features except for a small growing effort of sorting the features. For a small set of features the GFT has the best coverage rate at the *Grove2* and *Grove3*, where the texture is distributed uniformly. At the *Urban2* and *Urban3* the detector achieve the best MEE. However it becomes very inefficient when sequences include a large set of strong edges lying at motion boundaries. These features cannot be tracked. The GFT is a fast and reliable feature detector at standard scenarios. But it should be used with caution at sequences with occlusion and homogeneous objects.

Table 1: Evaluation results for the Middleburry dataset for approximate 200 feature points (left), 2500 feature points (right). Measurements are  $t_d$  detection time, t detection and tracking time, t tracking performance, MEE median of endpoint error and t mean feature density per motion segment.

	Method	$t_D$ (ms)	t (ms)	η (%)	MEE	ρ(%)	1	Method	$t_D$ (ms)	t (ms)	η (%)	MEE	ρ(%)
	GFT	35	98	2.3	0.113	0.42		GFT	1D (IIIS)	112	2.0	0.069	1.03
	PGFT	75	138	1.9	0.113	0.42		PGFT	77	156	1.5	0.073	0.90
G 2	FAST	2	63	1.5	0.108	0.30		FAST	4	73	2.1	0.077	2.10
Grove2	SIFT	240	304	3.9	0.082	0.26		SIFT	508	588	3.1	0.090	1.04
	SURF	156	215	5.1	0.116	0.12		SURF	280	355	2.3	0.079	0.72
	STAR	18	76	8.7	0.152	0.22		STAR	24	98	2.6	0.082	0.84
	MSER	63	124	4.8	0.094	0.18		MSER	142	215	2.2	0.071	1.62
	Method	$t_D$ (ms)	t (ms)	η (%)	MEE	ρ(%)		Method	$t_D$ (ms)	t (ms)	η (%)	MEE	ρ(%)
	GFT	35	100	6.7	0.168	0.07		GFT	37	113	7.7	0.099	0.35
	PGFT	74	135	8.0	0.165	0.07		PGFT	77	158	7.3	0.097	0.34
Grove3	FAST	2	64	6.2	0.147	0.03		FAST	4	77	9.6	0.138	0.59
	SIFT	251	318	5.2	0.099	0.06		SIFT	522	605	9.0	0.129	0.36
	SURF	151	212 80	5.4 9.7	0.150	0.01		SURF	282	358 99	8.4	0.129 0.151	0.40 0.31
	STAR MSER	19 60	123	14.2	0.134 0.210	0.03		STAR MSER	24 148	228	8.4 9.5	0.131	0.31
	Method	$t_D$ (ms)	t (ms)	η (%)	MEE	ρ(%)	1	Method	t <sub>D</sub> (ms)	t (ms)	η (%)	MEE	ρ (%)
Urban2	GFT	35	98	11.8	0.084	0.12	-	GFT	36	117	12.2	0.103	0.64
	PGFT	75	135	11.8	0.085	0.12		PGFT	76	159	12.6	0.103	0.59
	FAST	2	59	14.6	0.104	0.13		FAST	5	78	8.6	0.103	1.18
	SIFT	257	320	4.4	0.103	0.04		SIFT	506	584	11.8	0.104	0.62
	SURF	158	219	8.1	0.177	0.19		SURF	286	364	10.3	0.126	0.83
	STAR	19	78	18.6	0.207	0.05		STAR	24	99	10.7	0.105	0.63
	MSER	54	115	16.2	0.154	0.07		MSER	104	173	9.8	0.107	0.62
	Method	$t_D$ (ms)	t (ms)	η (%)	MEE	ρ(%)	T I	Method	$t_D$ (ms)	t (ms)	η (%)	MEE	ρ(%)
Urban3	GFT	35	101	11.6	0.057	0.12	4	GFT	36	114	13.9	0.089	0.45
	PGFT	74	134	9.5	0.062	0.19		PGFT	77	161	12.2	0.085	0.48
	FAST	2	59	11.3	0.063	0.21		FAST	5	76	9.1	0.071	0.82
	SIFT	272	336	6.6	0.066	0.07		SIFT	534	616	12.5	0.110	0.54
	SURF	158	216	10.4	0.107	0.13		SURF	300	382	11.5	0.100	0.56
	STAR	18	78	9.1	0.089	0.22		STAR	25	102	10.7	0.081	0.59
	MSER	51	112	19.7	0.127	0.06		MSER	94	158	18.0	0.100	0.34
	Method	t <sub>D</sub> (ms)	t (ms)	η (%)	MEE	ρ(%)		Method	t <sub>D</sub> (ms)	t (ms)	η (%)	MEE	ρ(%)
	GFT	26	77	2.2	0.055	0.06		GFT	27	89	3.2	0.057	0.99
												0.057	
	PGFT	55	106	1.8	0.059	0.07	9	PGFT	56	119	3.2	0.057	1.12
RubberWhale	FAST	1	50	0.5	0.051	0.08		FAST	4	63	2.2	0.050	1.25
RubberWhale	FAST SIFT	1 183	<b>5</b> 0 233	<b>0.5</b> 1.1	<b>0.051</b> 0.129	0.08 0.08	1	FAST SIFT	<b>4</b> 414	<b>63</b> 476	2.2 <b>1.9</b>	<b>0.050</b> 0.057	1.25 0.78
RubberWhale	FAST SIFT SURF	1 183 113	50 233 162	<b>0.5</b> 1.1 4.3	0.051 0.129 0.180	0.08 0.08 0.11	1	FAST SIFT SURF	4 414 237	<b>63</b> 476 299	2.2 <b>1.9</b> 3.3	0.050 0.057 0.066	1.25 0.78 1.06
RubberWhale	FAST SIFT SURF STAR	1 183 113 13	<b>5</b> 0 233	<b>0.5</b> 1.1	0.051 0.129 0.180 0.127	0.08 0.08 0.11 0.10	1	FAST SIFT SURF STAR	<b>4</b> 414	<b>63</b> 476	2.2 <b>1.9</b>	0.050 0.057 0.066 0.057	1.25 0.78 1.06 0.94
RubberWhale	FAST SIFT SURF STAR MSER	1 183 113 13 51	50 233 162 62 101	0.5 1.1 4.3 3.3 3.0	0.051 0.129 0.180	0.08 0.08 0.11 0.10 <b>0.24</b>		FAST SIFT SURF STAR MSER	4 414 237 18 93	63 476 299 74 148	2.2 1.9 3.3 2.0 2.3	0.050 0.057 0.066	1.25 0.78 1.06 0.94 0.54
RubberWhale	FAST SIFT SURF STAR MSER Method	1 183 113 13 51 t <sub>D</sub> (ms)	50 233 162 62 101 t (ms)	0.5 1.1 4.3 3.3 3.0 η (%)	0.051 0.129 0.180 0.127 0.075 MEE	0.08 0.08 0.11 0.10 <b>0.24</b> ρ (%)		FAST SIFT SURF STAR MSER Method	4 414 237 18 93 t <sub>D</sub> (ms)	63 476 299 74 148 t (ms)	2.2 1.9 3.3 2.0 2.3 $\eta$ (%)	0.050 0.057 0.066 0.057 0.051 MEE	1.25 0.78 1.06 0.94 0.54 ρ (%)
RubberWhale	FAST SIFT SURF STAR MSER	1 183 113 13 51	50 233 162 62 101	0.5 1.1 4.3 3.3 3.0	0.051 0.129 0.180 0.127 0.075	0.08 0.08 0.11 0.10 <b>0.24</b>		FAST SIFT SURF STAR MSER	4 414 237 18 93	63 476 299 74 148	2.2 1.9 3.3 2.0 2.3	0.050 0.057 0.066 0.057 0.051	1.25 0.78 1.06 0.94 0.54
	FAST SIFT SURF STAR MSER Method	1 183 113 13 51 t <sub>D</sub> (ms)	50 233 162 62 101 t (ms)	0.5 1.1 4.3 3.3 3.0 η (%)	0.051 0.129 0.180 0.127 0.075 MEE 0.205	0.08 0.08 0.11 0.10 <b>0.24</b> ρ (%)		FAST SIFT SURF STAR MSER Method	4 414 237 18 93 t <sub>D</sub> (ms)	63 476 299 74 148 t (ms)	2.2 1.9 3.3 2.0 2.3 $\eta$ (%)	0.050 0.057 0.066 0.057 0.051 MEE 0.225	1.25 0.78 1.06 0.94 0.54 ρ (%)
RubberWhale Venus	FAST SIFT SURF STAR MSER Method GFT PGFT	1 183 113 13 51 t <sub>D</sub> (ms) 18 38	50 233 162 62 101 t (ms) 65 82	0.5 1.1 4.3 3.3 3.0 η (%) 0.6 1.7	0.051 0.129 0.180 0.127 0.075 MEE 0.205 0.208	0.08 0.08 0.11 0.10 <b>0.24</b> ρ (%) 0.16 0.17		FAST SIFT SURF STAR MSER Method GFT PGFT	4 414 237 18 93 t <sub>D</sub> (ms) 20 40	63 476 299 74 148 t (ms) 76 97	2.2 1.9 3.3 2.0 2.3 $\eta$ (%) 6.6 7.1	0.050 0.057 0.066 0.057 0.051 MEE 0.225 0.235	1.25 0.78 1.06 0.94 0.54 ρ (%) 1.40 1.14
	FAST SIFT SURF STAR MSER Method GFT PGFT FAST	1 183 113 13 51 t <sub>D</sub> (ms) 18 38 1	50 233 162 62 101 t (ms) 65 82 43	0.5 1.1 4.3 3.3 3.0 η (%) 0.6 1.7 4.5	0.051 0.129 0.180 0.127 0.075 MEE 0.205 0.208 0.202	0.08 0.08 0.11 0.10 <b>0.24</b> ρ(%) 0.16 0.17 0.20		FAST SIFT SURF STAR MSER Method GFT PGFT FAST	4 414 237 18 93 t <sub>D</sub> (ms) 20 40 4	63 476 299 74 148 t (ms) 76 97 57	2.2 1.9 3.3 2.0 2.3 η (%) 6.6 7.1 4.1	0.050 0.057 0.066 0.057 0.051 MEE 0.225 0.235 0.204 0.202 0.202	1.25 0.78 1.06 0.94 0.54 ρ (%) 1.40 1.14 2.28
	FAST SIFT SURF STAR MSER Method GFT PGFT FAST SIFT SURF STAR	1 183 113 13 51 t <sub>D</sub> (ms) 18 38 1 128 80 9	50 233 162 62 101 t (ms) 65 82 43 171 122 52	0.5 1.1 4.3 3.3 3.0 η (%) 0.6 1.7 4.5 1.5 2.5 3.3	0.051 0.129 0.180 0.127 0.075 MEE 0.205 0.208 0.202 0.188 0.185 0.210	0.08 0.08 0.11 0.10 <b>0.24</b> ρ (%) 0.16 0.17 0.20 0.17 0.13		FAST SIFT SURF STAR MSER Method GFT PGFT FAST SIFT SURF STAR	4 414 237 18 93  t <sub>D</sub> (ms) 20 40 4 267 218 12	63 476 299 74 148 t (ms) 76 97 57 319 276 60	2.2 1.9 3.3 2.0 2.3 n (%) 6.6 7.1 4.1 5.3 4.9 4.2	0.050 0.057 0.066 0.057 0.051 MEE 0.225 0.235 0.204 0.202 0.202	1.25 0.78 1.06 0.94 0.54 ρ (%) 1.40 1.14 2.28 0.83 1.67 0.75
	FAST SIFT SURF STAR MSER Method GFT PGFT FAST SIFT SURF STAR MSER	1 183 113 13 51 t <sub>D</sub> (ms) 18 38 1 128 80 9 33	50 233 162 62 101 t (ms) 65 82 43 171 122 52 76	0.5 1.1 4.3 3.3 3.0 η (%) 0.6 1.7 4.5 1.5 2.5 3.3 4.8	0.051 0.129 0.180 0.127 0.075 MEE 0.205 0.208 0.202 0.188 0.185 0.210 0.183	0.08 0.08 0.11 0.10 <b>0.24</b> p (%) 0.16 0.17 0.20 0.17 0.13 <b>0.21</b>	1	FAST SIFT SURF STAR MSER Method GFT PGFT FAST SIFT SURF STAR MSER	4 414 237 18 93 t <sub>D</sub> (ms) 20 40 4 267 218 12 62	63 476 299 74 148 t (ms) 76 97 57 319 276 60 108	2.2 1.9 3.3 2.0 2.3 7 (%) 6.6 7.1 4.1 5.3 4.9 4.2 5.6	0.050 0.057 0.066 0.057 0.051 MEE 0.225 0.235 0.204 0.202 0.202 0.227 0.189	1.25 0.78 1.06 0.94 0.54 ρ (%) 1.40 1.14 2.28 0.83 1.67 0.75 0.67
	FAST SIFT SURF STAR MSER Method GFT PGFT FAST SIFT SURF STAR MSER Method	1 183 113 13 51 tD (ms) 18 38 1 128 80 9 33 tD (ms)	50 233 162 62 101 t (ms) 65 82 43 171 122 52 76 t (ms)	0.5 1.1 4.3 3.3 3.0 η (%) 0.6 1.7 4.5 2.5 3.3 4.8 η (%)	0.051 0.129 0.180 0.127 0.075 MEE 0.205 0.208 0.202 0.188 0.185 0.210 0.183	0.08 0.08 0.11 0.10 <b>0.24</b> p (%) 0.16 0.17 0.20 0.17 0.13 <b>0.21</b> 0.16 p (%)	1	FAST SIFT SURF STAR MSER Method GFT PGFT FAST SIFT SURF STAR MSER Method	4 414 237 18 93  t <sub>D</sub> (ms) 20 40 4 267 218 12 62 t <sub>D</sub> (ms)	63 476 299 74 148 t (ms) 76 97 57 319 276 60 108 t (ms)	2.2 1.9 3.3 2.0 2.3 1) (%) 6.6 7.1 4.1 5.3 4.9 4.2 5.6 1) (%)	0.050 0.057 0.066 0.057 0.051 MEE 0.225 0.235 0.204 0.202 0.202 0.227 0.189 MEE	1.25 0.78 1.06 0.94 0.54 ρ(%) 1.40 1.14 2.28 0.83 1.67 0.75 0.67 ρ(%)
	FAST SIFT SURF STAR MSER Method GFT FAST SIFT SURF STAR MSER Method GFT	1 183 113 13 51 14D (ms) 18 38 1 128 80 9 33 14D (ms) 26	50 233 162 62 101 t (ms) 65 82 43 171 122 52 76 t (ms)	0.5 1.1 4.3 3.3 3.0 η (%) 0.6 1.7 4.5 1.5 2.5 3.3 4.8 η (%) 0.4	0.051 0.129 0.180 0.127 0.075 MEE 0.205 0.202 0.188 0.185 0.210 0.183 MEE	0.08 0.08 0.11 0.10 0.24 ρ (%) 0.16 0.17 0.20 0.17 0.13 0.21 0.16 ρ (%)	1	FAST SIFT SURF STAR MSER Method GFT FAST SIFT SURF STAR MSER Method GFT	4 414 237 18 93 tD (ms) 20 40 4 267 218 12 62 tD (ms) 27	63 476 299 74 148 t (ms) 76 97 57 319 276 60 108 t (ms)	2.2 1.9 3.3 2.0 2.3 η (%) 6.6 7.1 4.1 5.3 4.9 4.2 5.6 η (%)	0.050 0.057 0.066 0.057 0.051 MEE 0.225 0.235 0.204 0.202 0.202 0.202 0.202 0.207 0.189 MEE	1.25 0.78 1.06 0.94 0.54 ρ(%) 1.40 1.14 2.28 0.83 1.67 0.75 0.67 ρ(%)
	FAST SIFT SURF STAR MSER Method GFT PGFT FAST SIFT SURF STAR MSER MEthod GFT PGFT	1 183 113 13 51 120 (ms) 18 38 1 128 80 9 33 1 tD (ms) 26 54	50 233 162 62 101 t (ms) 65 82 43 171 122 52 76 t (ms)	0.5 1.1 4.3 3.3 3.0 η (%) 0.6 1.7 4.5 1.5 2.5 3.3 4.8 η (%) 0.4 0.0	0.051 0.129 0.180 0.127 0.075 MEE 0.205 0.202 0.188 0.210 0.183 MEE 0.283 0.306	0.08 0.08 0.11 0.10 <b>0.24</b> ρ (%) 0.16 0.17 0.20 0.17 0.13 <b>0.21</b> 0.16 ρ (%) 0.42 0.42		FAST SIFT SURF STAR MSER Method GFT PGFT FAST SIFT SURF STAR MSER Method GFT PGFT	4 414 237 18 8 50 (ms) 20 40 4 267 218 12 62 t <sub>D</sub> (ms) 27 57	63 476 299 74 148 t (ms) 76 97 57 319 276 60 108 t (ms) 93 124	2.2 1.9 3.3 2.0 2.3 7 (%) 6.6 7.1 4.1 5.3 4.9 4.2 5.6 7 (%)	0.050 0.057 0.066 0.057 0.051 MEE 0.225 0.204 0.202 0.202 0.202 0.218 MEE 0.091 0.090	1.25 0.78 1.06 0.94 0.54 ρ (%) 1.40 1.14 2.28 0.83 1.67 0.75 0.67 ρ (%) 1.24
	FAST SIFT SURF STAR MSER Method GFT FAST SIFT SURF STAR MSER Method GFT FAST SUFF STAR MSER Method GFT PGFT FAST	1 183 113 13 15 15 (ms) 18 38 1 128 80 9 33 16 (ms) 26 54 1	50 233 162 62 101 t (ms) 65 82 43 171 122 52 76 t (ms) 80 106 50	0.5 1.1 4.3 3.3 3.0 η (%) 0.6 1.7 4.5 1.5 2.5 3.3 4.8 η (%) 0.4 0.0 0.5	0.051 0.129 0.180 0.127 0.075 MEE 0.205 0.208 0.202 0.188 0.185 0.210 0.183 MEE 0.283 0.306 0.252	0.08 0.08 0.11 0.10 0.24 ρ (%) 0.16 0.17 0.20 0.17 0.13 0.21 ρ (%) 0.42 0.42 0.25	1	FAST SIFT SURF STAR MSER Method GFT FAST SIFT SURF STAR MSER Method GFT PGFT FAST	4 414 237 18 93  t <sub>D</sub> (ms) 20 40 4 267 218 12 6 t <sub>D</sub> (ms) 27 57	63 476 299 74 148 t (ms) 76 97 57 319 276 60 108 t (ms) 93 124 68	2.2 1.9 3.3 2.0 9 (%) 6.6 7.1 4.1 5.3 4.9 4.2 5.6 9 (%) 4.7 3.6 2.6	0.050 0.057 0.066 0.057 0.051 MEE 0.225 0.204 0.202 0.202 0.202 0.202 0.202 0.202 0.202 0.202	1.25 0.78 1.06 0.94 0.54 ρ (%) 1.40 1.14 2.28 0.83 1.67 0.75 0.67 ρ (%) 1.24 1.27 3.30
Venus	FAST SIFT SUFF STAR MSER Method GFT PGFT FAST SURF STAR MSER Method GFT PGFT FAST SIFT	1 183 113 13 151 120 (ms) 18 38 1 1 128 80 9 33 110 (ms) 26 54 1 177	50 233 162 62 101 t (ms) 65 82 43 171 122 52 76 t (ms) 80 106 50 228	0.5 1.1 4.3 3.3 3.0 η (%) 0.6 1.7 4.5 1.5 2.5 3.3 4.8 η (%) 0.4 0.0 0.5 1.7	0.051 0.129 0.180 0.127 0.075 MEE 0.205 0.208 0.202 0.185 0.210 0.183 MEE 0.283 0.306 0.252 0.260	0.08 0.08 0.11 0.10 0.24 ρ (%) 0.16 0.17 0.20 0.17 0.13 0.21 0.16 ρ (%) 0.42 0.42 0.42 0.42 0.42	1	FAST SIFT SURF STAR MSER Method GFT FAST SURF STAR MSER Method GFT PGFT FAST SIFT	4 414 237 18 93 t <sub>D</sub> (ms) 20 40 4 267 218 12 62 t <sub>D</sub> (ms) 27 57 411	63 476 299 74 148 t (ms) 76 97 57 319 276 60 108 t (ms) 93 124 68	2.2 1.9 3.3 2.0 0.2 3.3 10(%) 6.6 7.1 4.1 5.3 4.9 4.2 5.6 10(%) 4.7 3.6 5.7	0.050 0.057 0.066 0.057 0.051 MEE 0.225 0.235 0.204 0.202 0.202 0.202 0.202 0.207 0.189 MEE 0.091 0.090	1.25 0.78 1.06 0.94 0.54 ρ (%) 1.40 1.14 2.28 0.83 1.67 0.75 0.67 ρ (%) 1.24 1.27
Venus	FAST SIFT SURF STAR MSER Method GFT PGFT FAST SIFT SURF STAR MSER Method GFT PGFT STAR MSER Method GFT STAR MSER Method GFT STAR SIFT SURF SURF SURF	1 183 113 13 151 tp (ms) 18 38 1 1 128 80 9 33 1tp (ms) 26 54 1 177 115	50 233 162 62 101 t (ms) 65 82 43 171 122 52 76 t (ms) 80 106 50 228	0.5 1.1 4.3 3.3 3.0 η (%) 0.6 1.7 4.5 1.5 2.5 3.3 4.8 η (%) 0.4 0.0 0.5 1.7 3.9	0.051 0.129 0.180 0.127 0.075 MEE 0.205 0.208 0.202 0.188 0.185 0.210 0.183 MEE 0.283 0.306 0.252 0.260 0.261	0.08 0.08 0.11 0.10 0.24 ρ (%) 0.16 0.17 0.20 0.17 0.13 0.21 0.16 ρ (%) 0.42 0.42 0.42 0.42 0.42		FAST SIFT SURF STAR MSER Method GFT PGFT FAST SIFT SURF STAR MSER Method GFT PGFT FAST SIFT SURF STAR SURF STAR MSER	4 414 237 18 93 t <sub>D</sub> (ms) 20 40 4 267 218 12 62 t <sub>D</sub> (ms) 27 5 411 257	63 476 299 74 148 t (ms) 76 97 57 319 276 60 108 t (ms) 93 124 68 484 324	2.2 1.9 3.3 2.0 2.3 7 (%) 6.6 7.1 4.1 5.3 4.9 4.2 5.6 7 (%) 4.7 3.6 5.7 4.6	0.050 0.057 0.066 0.057 0.066 0.057 0.051  MEE 0.225 0.235 0.204 0.202 0.202 0.227 0.189  MEE 0.091 0.090 0.271 0.117 0.102	1.25 0.78 1.06 0.94 0.54 ρ (%) 1.40 1.14 2.28 0.83 1.67 0.75 0.67 ρ (%) 1.24 1.27 3.30 1.51 1.20
Venus	FAST SIFT SURF STAR MSEM Method GFT PGFT FAST SIFT SURF STAR MSER Method GFT PGFT FAST SIFT SURF STAR MSER	1 183 113 13 151 150 (ms) 18 38 1 128 80 9 33 150 (ms) 26 54 1 177 115 13	50 233 162 62 101 t (ms) 65 82 43 171 122 52 76 t (ms) 80 106 50 228 165 62	0.5 1.1 4.3 3.3 3.0 η (%) 0.6 1.7 4.5 1.5 2.5 3.3 4.8 η (%) 0.4 0.0 0.5 1.7 3.9 3.1	0.051 0.129 0.180 0.127 0.075 MEE 0.205 0.208 0.202 0.188 0.185 0.210 0.183 MEE 0.283 0.306 0.252 0.262 0.261 0.279	0.08 0.08 0.11 0.10 0.24 ρ (%) 0.16 0.17 0.20 0.17 0.13 0.21 0.16 ρ (%) 0.42 0.42 0.42 0.25 0.42 0.42 0.33		FAST SIFT SURF STAR MSER Method GFT PGFT FAST SIFT SURF STAR MSER Method GFT PGFT FAST SIFT SURF STAR MSER	4 414 237 18 93 10 (ms) 20 40 4 267 218 12 62 10 (ms) 27 57 51 411 257 18	63 476 299 74 148 t (ms) 76 97 57 319 276 60 108 t (ms) 93 124 68 484 324 80	2.2 1.9 3.3 2.0 2.3 7 (%) 6.6 7.1 4.1 5.3 4.9 4.2 5.6 7 (%) 4.7 3.6 2.6 5.7 4.6 3.1	0.050 0.057 0.066 0.057 0.066 0.057 0.051  MEE 0.225 0.235 0.204 0.202 0.202 0.202 0.202 0.202 0.209 0.189  MEE 0.091 0.090 0.271 0.117 0.102 0.105	1.25 0.78 1.06 0.94 0.54 ρ (%) 1.40 1.14 2.28 0.83 1.67 0.75 0.67 ρ (%) 1.24 1.27 3.30 1.51 1.20 1.34
Venus	FAST SIFT SURF STAR MSER Method GFT PGFT FAST SIFT SURF STAR MSER Method GFT PGFT FAST SIFT SURF STAR MSER	1 183 113 13 151 140 (ms) 18 38 1 128 80 9 33 140 (ms) 26 54 1 115 13 40	50 233 162 62 101 t (ms) 65 82 43 171 122 52 76 t (ms) 80 106 50 228 165 62 90	0.5 1.1 4.3 3.3 3.0 η (%) 0.6 1.7 4.5 1.5 2.5 3.3 4.8 η (%) 0.4 0.0 0.5 1.7 3.9 3.1 1.5	0.051 0.129 0.180 0.127 0.075 MEE 0.205 0.208 0.202 0.188 0.185 0.210 0.183 MEE 0.283 0.306 0.252 0.260 0.261 0.279 0.303	0.08 0.08 0.11 0.10 0.24 ρ (%) 0.16 0.17 0.20 0.17 0.13 0.21 0.16 ρ (%) 0.42 0.42 0.42 0.25 0.42 0.42 0.24		FAST SIFT SURF STAR MSER Method GFT PGFT FAST SIFT SURF STAR MSER Method GFT PGFT FAST SIFT SURF STAR MSER	4 414 237 18 83 10 (ms) 20 40 4 267 218 12 62 1p (ms) 27 57 5 411 257 18 89	63 476 299 74 148 t (ms) 76 97 57 319 276 60 108 t (ms) 93 124 68 484 324 80 151	2.2 1.9 3.3 2.0 2.3 7 (%) 6.6 7.1 4.1 5.3 4.9 4.2 5.6 7 (%) 4.7 3.6 2.6 5.7 4.6 3.1 3.0	0.050 0.057 0.066 0.057 0.066 0.057 0.051 MEE 0.225 0.235 0.204 0.202 0.202 0.202 0.227 0.189 MEE 0.091 0.090 0.271 0.1102 0.105 0.260	1.25 0.78 1.06 0.94 0.54 ρ (%) 1.40 1.14 2.28 0.83 1.67 0.75 0.67 ρ (%) 1.24 1.27 3.30 1.51 1.20 1.34 2.70
Venus	FAST SIFT SURF STAR MSER Method GFT PGFT FAST SIFT SURF STAR MSER Method GFT PGFT FAST SUFF STAR MSER Method GFT METHOD	1 183 113 13 151 150 (ms) 18 38 1 128 80 9 33 160 154 115 115 115 115 115 115 115 115 115	50 233 162 62 101 t (ms) 65 82 43 171 122 56 t (ms) 80 106 50 228 165 62 90 t (ms)	0.5 1.1 4.3 3.3 3.0 η (%) 0.6 1.7 4.5 1.5 2.5 3.3 4.8 η (%) 0.4 0.0 0.5 1.7 3.9 3.1 1.5 η (%)	0.051 0.129 0.180 0.127 0.075 MEE 0.205 0.208 0.202 0.188 0.185 0.210 0.183 MEE 0.283 0.306 0.252 0.260 0.261 0.279 0.303 MEE	0.08 0.08 0.11 0.10 0.24 ρ (%) 0.16 0.17 0.20 0.17 0.13 0.21 0.16 ρ (%) 0.42 0.42 0.25 0.24 0.47 0.33 0.54 ρ (%)		FAST SIFT SURF STAR MSER Method GFT FAST SIFT SURF STAR MSER Method GFT FAST SURF STAR MSER Method GFT FAST SURF STAR MSER Method	4 414 237 18 8 9 10 (ms) 20 40 4 267 218 12 62 12 62 15 (ms) 27 57 5 411 257 18 89 10 (ms)	63 476 299 74 148 t (ms) 76 97 57 319 276 60 108 t (ms) 93 124 68 484 324 80 151 t (ms)	2.2 1.9 3.3 2.0 2.3 η (%) 6.6 7.1 4.1 5.3 4.9 4.2 5.6 η (%) 4.7 3.6 2.6 5.7 4.6 3.1 3.0 η (%)	0.050 0.057 0.066 0.057 0.051 MEE 0.225 0.235 0.204 0.202 0.202 0.227 0.189 MEE 0.091 0.090 0.271 0.110 0.105 0.260 MEE	1.25 0.78 1.06 0.94 0.54 0.54 1.40 1.14 2.28 0.83 1.67 0.75 0.67 ρ(%) 1.24 1.27 3.30 1.51 1.20 1.34 2.70 ρ(%)
Venus	FAST SIFT SURF STAR MSER  Method  GFT PGFT FAST SIFT SURF STAR MSER  Method  GFT FAST SIFT SURF STAR MSER  Method  GFT  GFT  GFT  GFT  GFT  GTA  MSER	1 183 113 13 151 140 (ms) 18 38 1 128 80 9 33 140 (ms) 26 54 1 115 13 40	50 233 162 62 101 t (ms) 65 82 43 171 122 52 76 t (ms) 80 106 50 228 165 62 90	0.5 1.1 4.3 3.3 3.0 η (%) 0.6 1.7 4.5 1.5 2.5 3.3 4.8 η (%) 0.4 0.0 0.5 1.7 3.9 3.1 1.5	0.051 0.129 0.180 0.127 0.075 MEE 0.205 0.208 0.202 0.188 0.185 0.210 0.183 MEE 0.283 0.306 0.252 0.260 0.261 0.279 0.303	0.08 0.08 0.11 0.10 0.24 ρ (%) 0.16 0.17 0.20 0.17 0.13 0.21 0.16 ρ (%) 0.42 0.42 0.42 0.25 0.24 0.47 0.33 0.54 ρ (%)		FAST SIFT SURF STAR MSER Method GFT PGFT FAST SIFT SURF STAR MSER Method GFT PGFT FAST SIFT SURF STAR MSER	4 414 237 18 83 10 (ms) 20 40 4 267 218 12 62 1p (ms) 27 57 5 411 257 18 89	63 476 299 74 148 t (ms) 76 97 57 319 276 60 108 t (ms) 93 124 68 484 324 80 151	2.2 1.9 3.3 2.0 2.3 7 (%) 6.6 7.1 4.1 5.3 4.9 4.2 5.6 7 (%) 4.7 3.6 2.6 5.7 4.6 3.1 3.0	0.050 0.057 0.066 0.057 0.066 0.057 0.051 MEE 0.225 0.235 0.204 0.202 0.202 0.202 0.227 0.189 MEE 0.091 0.090 0.271 0.1102 0.105 0.260	1.25 0.78 1.06 0.94 0.54 ρ(%) 1.40 1.14 2.28 0.83 1.67 0.75 0.67 ρ(%) 1.24 1.27 3.30 1.51 1.20 1.34 2.70 ρ(%)
Venus Hydrangea	FAST SIFT SURF STAR MSER Method GFT PGFT FAST SIFT SURF STAR MSER Method GFT PGFT FAST SUFF STAR MSER Method GFT METHOD	1 183 113 13 151 120 (ms) 18 38 1 1 128 80 9 33 170 (ms) 26 54 1 177 115 13 40 170 (ms) 25	50 233 162 62 101 t (ms) 65 82 43 171 122 52 76 t (ms) 80 106 50 228 165 62 90 t (ms) 77	0.5 1.1 4.3 3.3 3.0 η (%) 0.6 1.7 4.5 2.5 3.3 4.8 η (%) 0.4 0.0 0.5 1.7 3.9 3.1 1.5 η (%) 0.00	0.051 0.129 0.180 0.127 0.075 MEE 0.205 0.208 0.202 0.183 MEE 0.283 0.306 0.252 0.260 0.261 0.279 0.303 MEE 0.049	0.08 0.08 0.11 0.10 0.24 ρ (%) 0.16 0.17 0.20 0.17 0.13 0.21 0.16 ρ (%) 0.42 0.42 0.25 0.24 0.47 0.33 0.54 ρ (%)		FAST SIFT SURF STAR MSER  Method  GFT FAST SIFT SURF STAR MSER  Method  GFT FAST SIFT SURF STAR MSER  Method  GFT  GFT  GFT  GFT  GFT  GFT  GFT  GF	4 414 237 18 93 tp (ms) 20 40 4 267 218 12 62 tp (ms) 27 5 411 257 18 89 tp (ms) 27	63 476 299 74 148 t (ms) 76 97 57 319 276 60 108 t (ms) 93 124 68 484 324 80 151 t (ms)	2.2 1.9 3.3 2.0 0.2.3 1 (%) 6.6 7.1 4.1 5.3 4.9 4.2 5.6 1 (%) 4.7 3.6 2.6 5.7 4.6 3.1 3.0 1 (%)	0.050 0.057 0.066 0.057 0.066 0.057 0.051  MEE 0.225 0.235 0.204 0.202 0.202 0.202 0.227 0.189  MEE 0.091 0.090 0.271 0.117 0.102 0.105 0.260  MEE 0.138	1.25 0.78 1.06 0.94 0.54 0.54 1.40 1.14 2.28 0.83 1.67 0.75 0.67 ρ(%) 1.24 1.27 3.30 1.51 1.20 1.34 2.70 ρ(%)
Venus	FAST SIFT SURF STAR MSER  Method  GFT PGFT SIFT SURF STAR MSER  Method  GFT PGFT SIFT SURF STAR MSER  Method  GFT PGFT SURF STAR MSER  Method  GFT PGFT SURF STAR MSER	1 183 113 13 151 120 (ms) 18 38 1 1 128 80 9 33 170 (ms) 26 54 1 177 115 13 40 170 (ms) 25 54	50 233 162 62 101 t (ms) 65 82 43 171 122 52 76 t (ms) 80 106 50 228 165 62 90 t (ms) 77	0.5 1.1 4.3 3.3 3.0 η (%) 0.6 1.7 4.5 1.5 2.5 3.3 4.8 η (%) 0.4 0.0 0.5 1.7 3.9 3.1 1.7 3.9 3.1 1.7 0.00 0.00	0.051 0.129 0.180 0.127 0.075 MEE 0.205 0.208 0.202 0.183 MEE 0.283 0.306 0.252 0.260 0.261 0.279 0.303 MEE	0.08 0.08 0.11 0.10 0.24 ρ (%) 0.16 0.17 0.20 0.17 0.13 0.21 0.16 ρ (%) 0.42 0.42 0.42 0.42 0.47 0.33 0.54 ρ (%)		FAST SIFT SURF STAR MSER  Method  GFT FAST SIFT SURF STAR MSER  Method  GFT FAST SIFT SURF STAR MSER  Method  GFT FAST SIFT SURF STAR MSER  Method GFT FAST SIFT SURF STAR MSER	4 414 237 18 93 t <sub>D</sub> (ms) 20 40 4 267 218 12 62 t <sub>D</sub> (ms) 27 55 411 257 18 8 9 t <sub>D</sub> (ms) 27 56	63 476 299 74 148 t (ms) 76 97 57 319 276 60 108 t (ms) 93 124 68 484 324 80 151 t (ms) 92 122	2.2 1.9 3.3 2.0 0.2 3 η (%) 6.6 7.1 4.1 5.3 4.9 4.2 5.6 η (%) 4.7 3.6 2.6 5.7 4.6 3.1 3.0 η (%) 0.5 0.6	0.050 0.057 0.066 0.057 0.066 0.057 0.051  MEE 0.225 0.235 0.204 0.202 0.202 0.227 0.189  MEE 0.091 0.090 0.271 0.117 0.102 0.105 0.260 MEE 0.138 0.138	1.25 0.78 1.06 0.94 0.54 ρ (%) 1.40 1.14 2.28 0.83 1.67 0.75 0.67 ρ (%) 1.24 1.27 3.30 1.51 1.20 1.34 2.70 ρ (%)
Venus Hydrangea	FAST SIFT SURF STAR MSER Method GFT PGFT FAST SIFT SURF STAR MSER Method GFT PGST FAST SIFT SURF STAR MSER Method GFT FAST SIFT SURF STAR MSER Method GFT FAST SURF STAR MSER	1 183 113 13 151 120 (ms) 18 38 1 128 80 9 33 120 (ms) 26 54 1 177 115 13 40 (ms) 25 54 1	50 233 162 62 101 t (ms) 65 82 43 171 122 52 76 t (ms) 80 106 50 228 165 62 90 t (ms) 77 104 49	0.5 1.1 4.3 3.3 3.0 η (%) 0.6 1.7 4.5 1.5 2.5 3.3 4.8 η (%) 0.4 0.0 0.5 1.7 3.9 3.1 1.5 η (%) 0.00 0.00 0.00	0.051 0.129 0.180 0.127 0.075 MEE 0.205 0.208 0.202 0.188 0.185 0.210 0.183 MEE 0.283 0.306 0.252 0.260 0.261 0.279 0.303 MEE	0.08 0.08 0.11 0.10 0.24 ρ (%) 0.16 0.17 0.20 0.17 0.13 0.21 0.16 ρ (%) 0.42 0.42 0.25 0.24 0.47 0.33 0.54 ρ (%)		FAST SIFT SURF STAR MSER Method GFT PGFT FAST SIFT SURF STAR MSER Method GFT PGFT FAST SIFT SURF STAR MSER Method GFT PGFT FAST SUFF STAR MSER METHOD MSER MSER MT MSER MSER MT MSER MSER MT MSER MSER MT MSER MSER MSER MSER MSER MSER MSER MSER	4 414 237 18 93 40 40 4 267 218 12 62 4D (ms)  27 5 18 899 4D (ms)  27 56 4	63 476 299 74 148 t (ms) 76 97 57 319 276 60 108 t (ms) 93 124 68 484 324 80 151 t (ms) 92 122 62	2.2 1.9 3.3 2.0 2.3 7 (%) 6.6 7.1 4.1 5.3 4.9 4.2 5.6 7 (%) 4.7 3.6 2.6 5.7 4.6 3.1 3.0 7 (%) 0.5 0.6 0.1	0.050 0.057 0.066 0.057 0.066 0.057 0.051  MEE 0.225 0.235 0.204 0.202 0.227 0.189  MEE 0.091 0.090 0.271 0.117 0.102 0.105 0.260  MEE 0.138 0.138	1.25 0.78 1.06 0.94 0.54 ρ (%) 1.40 1.14 2.28 0.83 1.67 0.75 0.67 ρ (%) 1.24 1.27 3.30 1.51 1.20 1.34 2.70 ρ (%) 0.23 0.21 0.19
Venus Hydrangea	FAST SIFT SURF STAR MSER  Method  GFT PGFT FAST SIFT SURF STAR MSER  Method  GFT PGFT FAST SIFT SURF STAR MSER  Method  GFT FAST SIFT SURF STAR MSER  METHOD	1 183 113 13 151 120 (ms) 18 38 1 128 80 9 33 17D (ms) 26 54 1 177 115 13 40 (ms) 25 5 178 178	50 233 162 62 101 t (ms) 65 82 43 171 122 52 76 t (ms) 80 106 50 228 165 62 90 t (ms) 77 104 49 230	0.5 1.1 4.3 3.3 3.0 η (%) 0.6 1.7 4.5 1.5 2.5 3.3 4.8 η (%) 0.4 0.0 0.5 1.7 3.9 3.1 1.5 η (%) 0.00 0.00 0.00 0.00	0.051 0.129 0.180 0.127 0.075 MEE 0.205 0.208 0.202 0.188 0.185 0.210 0.183 MEE 0.283 0.306 0.252 0.260 0.261 0.279 0.303 MEE 0.049 0.057 0.046 0.052	0.08 0.08 0.11 0.10 0.24 ρ (%) 0.16 0.17 0.20 0.17 0.13 0.21 0.16 ρ (%) 0.42 0.42 0.42 0.25 0.24 0.47 0.33 0.54 ρ (%) 0.018 0.017 0.018 0.019	1	FAST SIFT SURF STAR MSER Method GFT FAST SIFT SURF STAR MSER Method GFT PGFT FAST SIFT SURF STAR MSER Method GFT FAST SIFT SURF STAR MSER METHOD GFT FAST SIFT SURF STAR MSER METHOD GFT FAST SIFT SURF STAR MSER	## 414 237 188 93 ## 20 ## 20 ## 267 218 12 62 ## 27 55 ## 411 257 18 89 ## 27 ## 257 ## 89 ## 27 ## 257 ##	63 476 299 74 148 t (ms) 76 97 57 319 276 60 108 t (ms) 93 124 80 151 t (ms) 92 122 438	2.2 1.9 3.3 2.0 2.3 7 (%) 6.6 7.1 4.1 5.3 4.9 4.2 5.6 7 (%) 4.7 3.6 2.6 5.7 4.6 3.1 3.0 7 (%) 0.5 0.6 0.1	0.050 0.057 0.066 0.057 0.066 0.057 0.051  MEE 0.225 0.235 0.204 0.202 0.202 0.202 0.202 0.202 0.189  MEE 0.091 0.090 0.271 0.117 0.102 0.105 0.260  MEE 0.138 0.138 0.058	1.25 0.78 1.06 0.94 0.54 0.54 1.40 1.14 2.28 0.83 1.67 0.75 0.67 ρ(%) 1.24 1.27 3.30 1.51 1.20 1.34 2.70 ρ(%) 0.23 0.21 0.19 0.16
Venus Hydrangea	FAST SIFT SURF STAR MSEM Method GFT PGFT FAST SIFT SURF STAR MSER Method GFT PGFT FAST SIFT SURF STAR MSER Method GFT FAST SIFT SURF STAR MSER Method GFT PGFT STAR MSER Method GFT PGFT STAR MSER Method GFT PGFT STAR MSER	1 183 113 13 151 150 (ms) 18 38 1 128 80 9 33 150 (ms) 26 54 1 177 115 13 40 150 (ms) 25 54 1 178 113	50 233 162 62 101 t (ms) 65 82 43 171 122 52 76 t (ms) 80 106 50 228 165 62 90 t (ms) 77 104 49 230 161	0.5 1.1 4.3 3.3 3.0 η (%) 0.6 1.7 4.5 1.5 2.5 3.3 4.8 η (%) 0.4 0.0 0.5 1.7 3.9 3.1 1.5 η (%) 0.00 0.00 0.00 0.00 0.00	0.051 0.129 0.180 0.127 0.075 MEE 0.205 0.208 0.202 0.188 0.185 0.210 0.183 MEE 0.283 0.306 0.252 0.260 0.261 0.279 0.303 MEE 0.049 0.052 0.046 0.052 0.078	0.08 0.08 0.11 0.10 0.24 ρ (%) 0.16 0.17 0.20 0.17 0.13 0.21 0.16 ρ (%) 0.42 0.42 0.42 0.25 0.24 0.47 0.33 0.54 ρ (%) 0.018 0.017 0.018 0.019 0.018 0.019 0.019 0.019	A	FAST SIFT SURF STAR MSER Method GFT FAST SIFT SURF STAR MSER Method GFT FGFT FAST SIFT SURF STAR MSER Method GFT FAST SIFT SURF STAR MSER Method GFT FAST SIFT SURF STAR MSER	4 414 237 18 93 3tD (ms) 20 40 4 267 218 62 12 62 1D (ms) 27 57 51 18 89 1tD (ms) 27 56 41 375 247	63 476 299 74 148 t (ms) 76 97 57 319 276 60 108 t (ms) 93 124 68 484 324 80 151 t (ms) 92 122 62 438 310	2.2 1.9 3.3 2.0 2.3 η (%) 6.6 7.1 4.1 5.3 4.9 4.2 5.6 η (%) 4.7 3.6 2.6 5.7 4.6 3.1 3.0 η (%) 0.5 0.6 0.1 1.0 0.4	0.050 0.057 0.066 0.057 0.066 0.057 0.051 MEE 0.225 0.235 0.204 0.202 0.202 0.202 0.227 0.189 MEE 0.091 0.117 0.1102 0.105 0.260 MEE 0.138 0.138 0.058 0.085	$\begin{array}{c} \textbf{1.25} \\ 0.78 \\ 1.06 \\ 0.94 \\ \hline \rho  (\%) \\ 1.40 \\ 1.14 \\ \textbf{2.28} \\ 0.83 \\ 1.67 \\ 0.75 \\ 0.67 \\ \hline \rho  (\%) \\ 1.24 \\ 1.27 \\ \textbf{3.30} \\ 1.51 \\ 1.20 \\ 1.34 \\ 2.70 \\ \hline \rho  (\%) \\ \textbf{0.23} \\ 0.21 \\ 0.19 \\ 0.16 \\ 0.21 \\ \end{array}$

**PGFT.** The PGFT improves the GFT in some sequence. E.g. *Urban3*, *RubberWhale* and *Hydrangea*, there the tracking efficiency is decreased and the cov-

erage is increased. However, the benefit results in an increased detection runtime.

**STAR.** Due to the efficient implementation the STAR method reaches the runtime ranking two. In some special sequences as *Venus* or *Urban3* it gets good covering performance with a low feature set. But generally the performance of the STAR is below average.

**SIFT.** As shown in Figure 2 the SIFT detector runtime depends on the number of features. It is the slowest of the evaluation. But it shows good performance within a low feature set. This method reaches the best MEE results at *Grove2* and *Grove3* and the best tracking performance at the difficult *Urban2* and *Urban3*. In our experiments the scale space analysis of the DoG of the SIFT tends to detect less features at object boundaries. Almost homogeneous regions are also selected, e.g. the sky of the *Grove3* sequence where tracking is still applicable. Though the set of objects are not covered uniformly, this results into low coverage. Summarizing the SIFT detector is a slow feature detector with a high tracking performance at sequences with few objects.

**SURF.** In our experiments the improved runtime performance regarding the SIFT could be confirmed, but  $t_d$  is still high compared to the other detectors. Related to SIFT the SURF shows some improvements at large sets of features in terms of tracking performance and accuracy. But FAST and GFT are still superior at large feature sets.

**MSER.** The MSER is the only method based on segmentation instead of finding features using first or second order derivatives. In our experiments we could observe that features are less likely detected at object boundaries e.g. in the *RubberWhale* sequence features are detected in the center of the fence holes instead of their corners. Considering the generalized aperture problem this is an important benefit. But it is not reflected in the results of the whole dataset, where the MSER detector achieve average results. Even at the *Venus* sequence it performs the best MEE results.

This sequence is also a challenging sequence for the GFT because it mainly consists of homogeneous objects. Most of the cornerness regions are distributed at the object boundaries. Thus MSER and also the scale space detector SIFT and SURF achieve good results. That leads to the conclusion that a region based or a scale space based approach would be attractive to improve the GFT method.

## 6 CONCLUSIONS

In this paper we evaluate different feature detectors in conjunction with the RLOF local optical flow method. While the state-of-the-art KLT-Tracker operates with

the GFT detector, our goal is to provide a set of baseline results for alternative feature detectors to allow researchers to get a sense of which detector to use for a good performance on their specific problem. To compare the resulting sparse motion fields we propose a methodology based on accuracy, efficiency and covering measurements. The benchmark is performed on the Middleyburry dataset, which provides a set of consecutively captured images and the corresponding dense motion ground truth.

We observe that the efficient performing algorithm is the FAST approach. With a runtime of about 3 ms for a VGA sequence and an overall good performance for the tracking efficiency, median endpoint error and coverage it outperforms the standard GFT detector. For standard scenarios i.e. uniform texture distribution the GFT is a fast and reliable feature detector. From the results given by the evaluations we conclude that for specific sequences, e.g. sequences including homogeneous objects, where the texture distribution concentrates on object boundaries, there is still room for improvements. Limited advantages shows the PGFT but also SIFT and MSER shows enhanced performance under these conditions. Furthermore an improved GFT method could benefit from the scale space analysis of the SIFT or the region based approach of the MSER.

## **ACKNOWLEDGEMENTS**

The research leading to these results has received funding from the European Community's FP7 under grant agreement number 261743 (NoE VideoSense).

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