

SUMMARIZING SETS OF CATEGORICAL SEQUENCES

Selecting and Visualizing Representative Sequences

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Keywords: Categorical sequence data, Representativeness, Dissimilarity, Discrepancy of sequences, Summarizing sets of sequences, Visualization.

Abstract: This paper is concerned with the summarization of a set of categorical sequence data. More specifically, the problem studied is the determination of the smallest possible number of representative sequences that ensure a given coverage of the whole set, i.e. that have together a given percentage of sequences in their neighborhood. The goal is to yield a representative set that exhibits the key features of the whole sequence data set and permits easy sounded interpretation. We propose an heuristic for determining the representative set that first builds a list of candidates using a representativeness score and then eliminates redundancy. We propose also a visualization tool for rendering the results and quality measures for evaluating them. The proposed tools have been implemented in TraMineR our R package for mining and visualizing sequence data and we demonstrate their efficiency on a real world example from social sciences. The methods are nonetheless by no way limited to social science data and should prove useful in many other domains.

1 INTRODUCTION

Sequences of categorical data appear in many different scientific fields. In the social sciences, such sequences are mainly ordered list of states (employed/unemployed) or events (leaving parental home, marriage, having a child) describing individual life trajectories, typically longitudinal biographical data such as employment histories or family life courses.

One widely used approach for extracting knowledge from such sets consists in computing pairwise distances by means of sequence alignment algorithms, and next clustering the sequences by using these distances. This method has been applied to various data since the pioneering work of (Abbott and Forrest, 1986). A review can be found in (Abbott and Tsay, 2000). The expected outcome of such a strategy is a typology, with each cluster grouping cases with similar patterns (trajectories).

An important aspect of sequence analysis is also to compare the patterns of cases grouped according to the values of covariates (for instance sex or socio-economic position in the social sciences).

A crucial task is then to summarize groups of sequences by describing the patterns that characterize

them. This could be done by resorting to graphical representations such as sequence index plots, state distribution plots or sequence frequency plots (Müller et al., 2008). However, relying on these graphical tools suffers from some drawbacks. Sequence index plots give a (sorted) view of all the sequences in each subset and assigning them a meaning is mainly a subjective task. State distribution plots are aggregated transversal views that occult individual sequences and their interpretation can be misleading. Sequence frequency plots that focus on the most frequent sequences provide only a partial view especially when there is a great number of distinct sequences.

Hence, we need more appropriate tools for extracting the key features of a given subset or data partition. We propose an approach derived from the concept of representative set used in the biological sciences (Hobohm et al., 1992; Holm and Sander, 1998). The aim in this field is mainly to get a reduced reference base of protein or DNA sequences for optimizing the retrieval of a recorded sequence that resembles to a provided one. In this setting, the representative set must have “maximum coverage with minimum redundancy” i.e. it must cover all the spectrum of distinct sequences present in the data, including “outliers”.

Our goal is similar regarding the elimination of re-

Table 1: List of states in the mvad data set.

1	EM	Employment
2	FE	Further education
3	HE	Higher education
4	JL	Joblessness
5	SC	School
6	TR	Training

dundancy. It differs, however, in that we consider in this paper representative sets with a user controlled coverage level, i.e. we do not require maximal coverage. We thus define a representative set as a set of non redundant “typical” sequences that largely, though not necessarily exhaustively covers the spectrum of observed sequences. In other words, we are interested in finding a few sequences that together summarize the main traits of a whole set.

We could imagine synthetic — not observed — typical sequences, in the same way as the mean of a series of numbers that is generally not an observable individual value. However, the sequences we deal with in the social sciences (as well as in other fields) are complex patterns and modeling them is difficult since the successive states in a sequence are most often not independent of each other. Defining some virtual non observable sequence is therefore hardly workable, and we shall here consider only representative sets constituted of existing sequences taken from the data set itself.

Since this summarizing step represents an important data reduction, we also need indicators for assessing the quality of the selected representative sequences. An important aspect is also to visualize these in an efficient way.

Such tools and their application to social science data are presented in this paper. These tools are new features of our TraMineR library for mining and visualizing sequences in R (Gabadinho et al., 2009).

2 DATA

To illustrate our purpose we consider a data set from (McVicar and Anyadike-Danes, 2002) stemming from a survey on transition from school to work in Northern Ireland. The data contains 70 monthly activity state variables from July 1993 to June 1999 for 712 individuals. The alphabet is made of 6 states detailed in Table 1.

The three first sequences of this data set represented as distinct states and their associated durations (the so called State Permanence Format) look as follows

Sequence

- [1] EM/4-TR/2-EM/64
- [2] FE/36-HE/34
- [3] TR/24-FE/34-EM/10-JL/2

We consider in this paper the outcome of a cluster analysis of the sequences based on Optimal Matching (OM). The OM distance between two sequences x and y , also known as edit or Levenshtein distance, is the minimal cost in terms of indels — insertions and deletions — and substitutions necessary to transform x into y . We computed the distances using a substitution cost matrix based on transition rates observed in the data set and an indel cost of 1. The clustering is done with an agglomerative hierarchical method using the Ward criterion. A four cluster solution is chosen. Table 2 indicates some descriptive statistics for each of the clusters.

The sequence frequency plots in Fig. 1 displays the 10 most frequent sequences in each cluster and give a first idea of their content. The bar widths are proportional to the sequence frequencies. The 10 most frequent sequences represent about 40% of all the sequences in cluster 1 and 2, while this proportion is 27% and 21% for clusters 3 and 4 due to a higher diversity of the patterns.

3 METHODS

Our aim is to find a small subset of non redundant sequences that ensures a given coverage level, this level being for instance defined as the percentage of cases that are within a given neighborhood of at least one of the representative sequences. We propose an heuristic for determining such a representative subset.

It works in two main steps. In the first stage it prepares a sorted list of candidate representative sequences without caring for redundancy and eliminates redundancy within this list in a second stage. It basically requires the user to specify a representativeness criterion for the first stage and a similarity measure for evaluating redundancy in the second one.

Table 2: Number of cases, distinct sequences and discrepancy within each cluster.

	N	Dist. seq.	Discr.
Cluster 1	265	165	18.3
Cluster 2	153	88	23.5
Cluster 3	194	148	27.9
Cluster 4	100	89	37.2

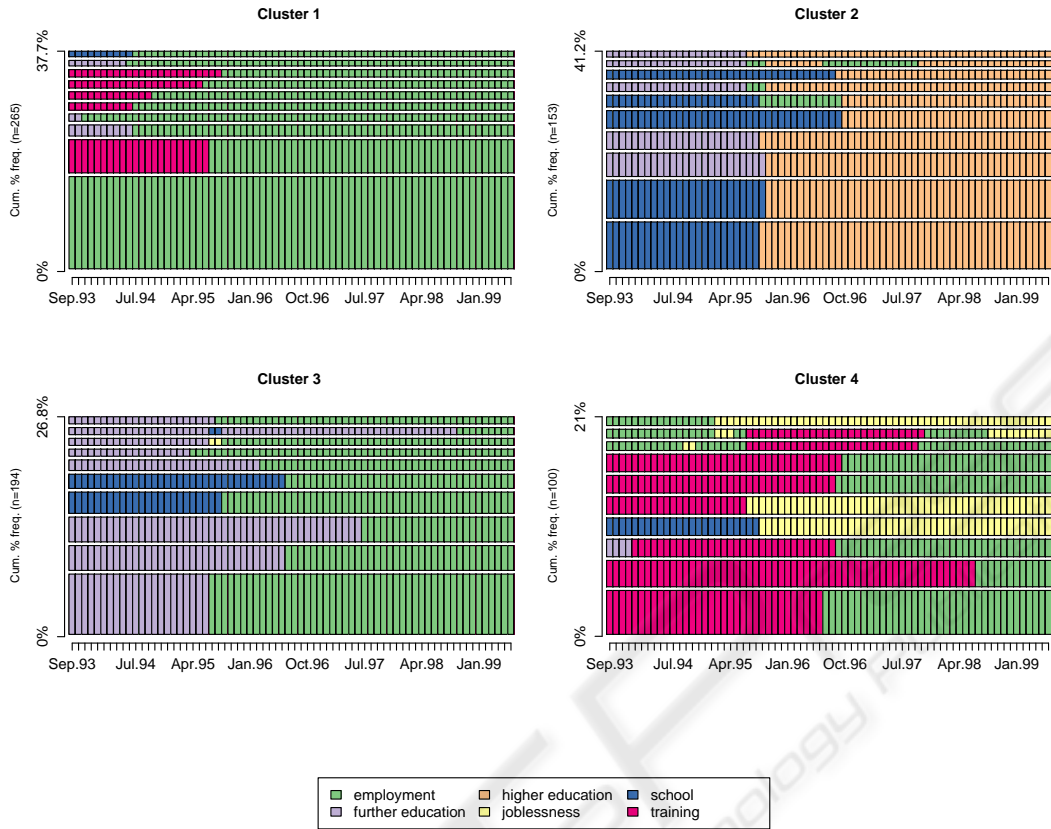


Figure 1: 10 most frequent sequences within each cluster.

3.1 Sorting Candidates

The initial candidate list is made of all distinct sequences appearing in the data. Since the second stage will extract non redundant representative sequences sequentially starting with the first element in the list, sorting the candidates according to a chosen representativeness criterion ensures that the “best” sequences given the criterion will be included. We present here five alternatives for measuring the sequence representativeness.

Sequence Frequency. A first simple criterion is to sort the sequences according to their frequency. The more frequent a sequence the more representative it is supposed to be. Hence, sequences are sorted in decreasing frequency order.

Neighborhood Density. A second criterion is the number — the density — of sequences in the neighborhood of each candidate sequence. This requires indeed to set the neighborhood diameter. We suggest to set it as a given proportion of the maximal theoretical distance between two sequences. Sequences are sorted in decreasing density order.

Mean State Frequency. A third criterion is the mean value of the transversal frequencies of the successive states. Let $s = s_1 s_2 \dots s_\ell$ be a sequence of length ℓ and $(f_{s_1}, f_{s_2}, \dots, f_{s_\ell})$ the frequencies of the states at time $(t_1, t_2, \dots, t_\ell)$. The mean state frequency is the sum of the state frequencies divided by the sequence length

$$MSF(s) = \frac{1}{\ell} \sum_{i=1}^{\ell} f_{s_i}$$

The lower and upper boundaries of MSF are 0 and 1. MSF is equal to 1 when all the sequences in the set are the same, i.e. when there is a single distinct sequence. The most representative sequence is the one with the highest score.

Centrality. A classical representative of a data set used in cluster analysis is the medoid. It is defined as the most central object, i.e. the one with minimal sum of distances to all other objects in the set (Kaufman and Rousseeuw, 1990). This suggests to use the sum of distances to all other sequences, i.e. the centrality as a representativeness criterion. The smallest the sum, the most representative the sequence. It may be mentioned that the most central observed sequence

is also the nearest from the ‘virtual’ true center of the set (Studer et al., 2009).

Sequence likelihood. The sequence likelihood $P(s)$ is defined as the product of the probability with which each of its observed successive state is supposed to occur at its position. Let $s = s_1 s_2 \dots s_\ell$ be a sequence of length ℓ . Then

$$P(s) = P(s_1, 1) \cdot P(s_2, 2) \dots P(s_\ell, \ell)$$

with $P(s_t, t)$ the probability to observe state s_t at position t . The question is how to determinate the state probabilities $P(s_t, t)$. One commonly used method for computing them is to postulate a Markov model, which can be of various order. Below, we just consider probabilities derived from the first order Markov model, that is each $P(s_t, t)$, $t > 1$ is set to the transition rate $p(s_t | s_{t-1})$ estimated across sequences from the observations at positions t and $t - 1$. For $t = 1$, we set $P(s_1, 1)$ to the observed frequency of the state s_1 at position 1. The likelihood $P(s)$ being generally very small, we use $-\log P(s)$ as sorting criterion. The latter quantity is minimal when $P(s)$ is equal to 1, which leads to sort the sequences in ascending order of their score.

3.2 Eliminating Redundancy

Once a sorted list of candidates has been defined, the second stage consists in eliminating redundancy since we do not want our representative set to contain similar sequences. The procedure is as follows:

- Select the first sequence in the candidate list (the best one given the chosen criterion);
- Process each next sequence in the sorted list of candidates. If this sequence is similar to none of those already in the representative set, that is distant from more than a predefined threshold from all of them, add it to the representative set.

The threshold for sequence similarity is defined as a proportion of the maximal theoretical distance. For the OM distance this theoretical maximum is for two sequences (s_1, s_2) of length (ℓ_1, ℓ_2)

$$D_{max} = \min(\ell_1, \ell_2) \cdot \min(2C_I, \max(S)) + |\ell_1 - \ell_2| \cdot C_I$$

where C_I is the indel cost and $\max S$ the maximal substitution cost.

3.3 Size of the Representative Set

Limiting our representative set to the mere sequence(s) with the best representative score may lead to leave a great number of sequences badly represented. Alternatively, proceeding the complete list of

candidates to achieve a full coverage of the data set is not a suitable solution since we look for a small set of representative sequences.

To control the size of the representative set, we limit the size of the candidate list so that the cumulated frequency of the retained distinct candidates reaches a threshold proportion $trep$ of the whole data set. Setting for instance $trep = 25\%$ ensures that at least 25% of the sequences will have a representative in their neighborhood and that the final representative set will contain at most 25% of the distinct sequences in the whole set. Thus $trep$ defines also a minimum coverage level.

There are indeed other possible ways of controlling the size of the representative set such as fixing a) the number or the proportion of sequences in the final representative set, or b) the desired coverage level.

3.4 Measuring Quality

A first step to define quality measures for the representative set is to assign each sequence to its nearest representative according to the considered pairwise distances. Let $r_1 \dots r_{nr}$ be the nr sequences in the representative set and $d(s, r_i)$ the distance between the sequence s and the i th representative. Each sequence s is assigned to its closer representative. When a sequence is equally distant from two or more representatives, the one with the highest representativeness score is selected. Hence, letting n be the total number of sequences and na_i the number of sequences assigned to the i th representative, we have $n = \sum_{i=1}^{nr} na_i$. Once each sequence in the set is assigned to a representative, we can derive the following quantities from the pairwise distance matrix.

Mean distance. Let $SD_i = \sum_{j=1}^{na_i} d(s_j, r_i)$ be the sum of distances between the i th representative and its na_i assigned sequences. A quality measure is then

$$MD_i = \frac{SD_i}{na_i}$$

the mean distance to the i th representative.

Coverage. Another quality indicator is the number of sequences assigned to the i th representative that are in its neighborhood, that is within a distance dn_{max}

$$nb_i = \sum_{j=1}^{na_i} \left(d(s_j, r_i) < dn_{max} \right) .$$

The threshold dn_{max} is defined as a proportion of D_{max} . The total coverage of the representative set is the sum $nb = \sum_{i=1}^{nr} nb_i$ expressed as a proportion of the number n of sequences, that is nb/n .

Distance gain. A third quality measure is obtained by comparing the sum SD_i of distances to the i th rep-

representative to the sum $DC_i = \sum_{j=1}^{na_i} d(s_j, c)$ of the distances of each of the na_i sequences to the center of the complete set. The idea is to measure the gain of representing those sequences by their representative rather than by the center of the set. We define thus the quality measure Q_i of the representative sequence r_i as

$$Q_i = \frac{DC_i - SD_i}{DC_i}$$

which gives the relative gain in the sum of distances. Note that Q_i may be negative in some circumstances, meaning that the sum of the na_i distances to the representative r_i is higher than the sum of distances to the true center of the set. A similar measure can be used to assess the overall quality of the representative set, namely

$$Q = \frac{\sum_i^{nr} DC_i - \sum_i^{nr} SD_i}{\sum_i^{nr} DC_i} = \sum_{i=1}^{nr} \frac{DC_i}{\sum_j DC_j} Q_i .$$

Discrepancy. A last quality measure is the sum $SC_i = \sum_{j=1}^{na_i} d(s_j, c_i)$ of distances to the true center c_i of the na_i sequences assigned to r_i , or the mean of those distances $V_i = SC_i/na_i$, which can be interpreted as the discrepancy of the set (Studer et al., 2009).

4 RESULTS

A graphical tool for visualizing the selected representative sequences together with information measures is included in the TraMineR package. A single function produces a “representative sequence plot” (Figure 2) where the representative sequences are plotted as horizontal bars with width proportional to the number of sequences assigned to them. Sequences are plotted bottom-up according to their representativeness score. Above the plot, two parallel series of symbols associated to each representative are displayed horizontally on a scale ranging from 0 to the maximal theoretical distance D_{max} . The location of the symbol associated to the representative r_i indicates on axis *A* the (pseudo) variance (V_i) within the subset of sequences assigned to r_i and on the axis *B* the mean distance MD_i to the representative.

4.1 Key Patterns

The set of representative sequences found with the sequence frequency criterion is displayed in Figure 2 for each of the four clusters of our example. The plots give clearly a more readily interpretable view of the content of the clusters than the frequency plots displayed in Figure 1. Detailed statistics about these sets are presented in Table 3.

Table 3: Representative sequences by cluster, frequency criterion, $trep=25\%$.

	<i>na</i>	(%)	<i>nb</i>	(%)	<i>MD</i>	<i>V</i>	<i>Q</i>
Cl. 1							
r_1	116	43.8	66	24.9	12.5	9.9	14.5
r_2	101	38.1	34	12.8	17.3	13.3	17.0
r_3	48	18.1	21	7.9	19.2	14.5	11.5
r_{1-3}	265	100.0	121	45.7	15.6	18.3	15.0
Cl. 2							
r_1	62	40.5	35	22.9	11.9	9.0	30.5
r_2	63	41.2	24	15.7	20.4	13.9	30.6
r_3	28	18.3	10	6.5	18.3	12.1	24.5
r_{1-3}	153	100.0	69	45.1	16.6	23.5	29.4
Cl. 3							
r_1	54	27.8	41	21.1	10.3	8.3	41.3
r_2	47	24.2	21	10.8	22.8	17.1	-11.6
r_3	56	28.9	18	9.3	31.0	22.1	8.9
r_4	22	11.3	10	5.2	31.7	20.1	22.9
r_5	15	7.7	4	2.1	28.1	19.0	38.7
r_{1-5}	194	100.0	94	48.5	23.1	27.9	17.0
Cl. 4							
r_1	28	28.0	15	15.0	15.0	10.9	50.4
r_2	12	12.0	4	4.0	17.8	12.7	53.3
r_3	7	7.0	4	4.0	20.6	14.4	63.9
r_4	15	15.0	7	7.0	21.3	15.3	31.7
r_5	2	2.0	2	2.0	6.8	3.4	81.7
r_6	5	5.0	2	2.0	20.7	12.0	48.4
r_7	4	4.0	1	1.0	41.0	24.2	-6.9
r_8	13	13.0	1	1.0	29.4	13.2	39.0
r_9	3	3.0	1	1.0	24.3	15.1	35.3
r_{10}	6	6.0	1	1.0	41.7	24.3	-19.9
r_{11}	5	5.0	1	1.0	37.4	20.1	-6.0
r_{1-11}	100	100.0	39	39.0	22.7	37.2	39.0

The representative sequences were extracted from a list of candidates sorted in decreasing order of their frequency. The number of candidates was limited by setting the *trep* threshold for the cumulated frequency of the candidates to 25%. The pairwise distances used are the optimal matching distances that we used for the clustering. The threshold dn_{max} for similarity (redundancy) between sequences was set as 10% of the maximal theoretical distance D_{max} . The sequence length being $\ell = 70$, the indel cost 1 and the maximal substitution cost 1.9995, we get $D_{max} = 70 \cdot \min(2, 1.9995) = 139.96$.

The first cluster is represented by three sequences. The first one, employment during the whole period represents 116 (44%) sequences of the cluster (Table 3), and its neighborhood (within 10% of D_{max}) includes 66 (25%) sequences. The second representative sequence, a spell of training followed by employment represents 101 (38%) additional cases and counts 34 (13%) sequences in its neighborhood. The

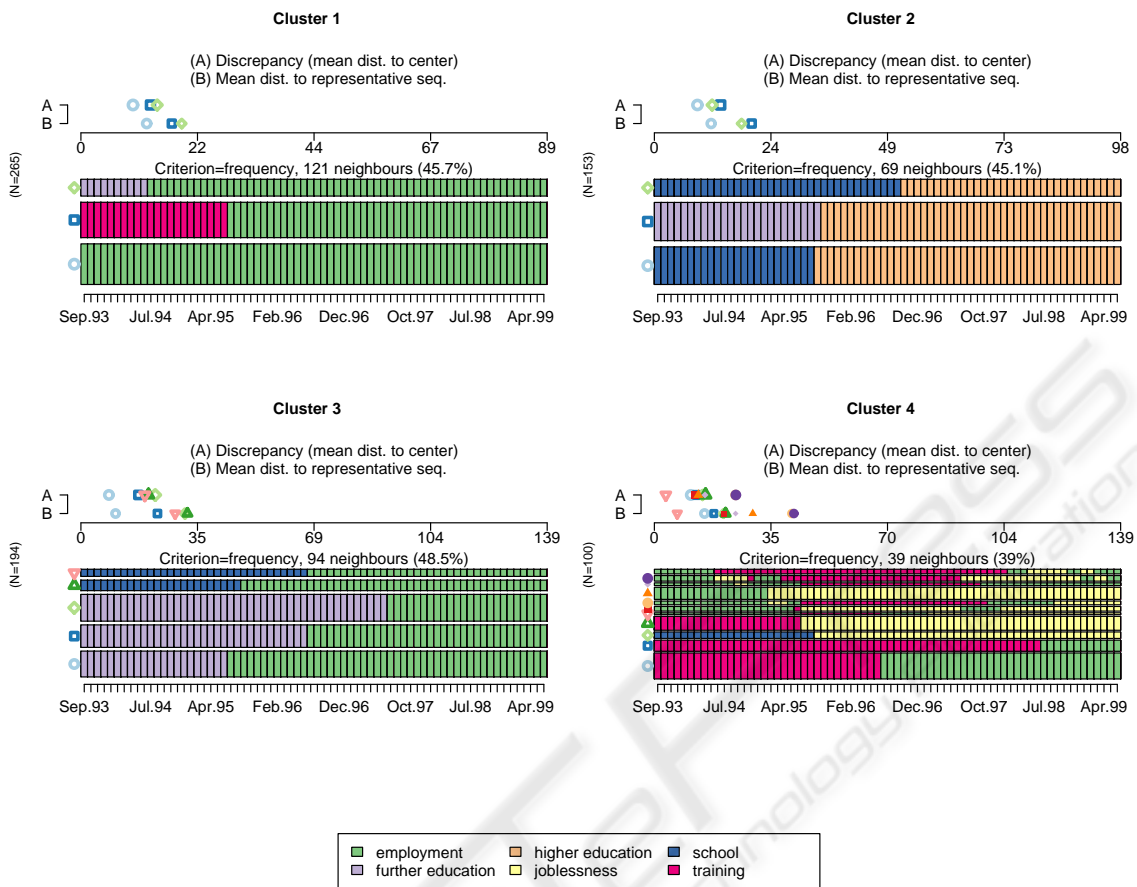


Figure 2: Representative sequences selected with the Frequency criterion, within each cluster (mvad data).

third and last representative sequence exhibits a short spell of further education followed by employment. Hence, this cluster is characterized by patterns of rapid entry into employment. Overall, the distance to the representative is within 10% of D_{max} for 121 (46%) sequences of the cluster. The quality measure Q (see Section 3.4) is respectively 11.5%, 17% and 14.5% for the three sequences in the set and reaches 15% for the whole set.

The second cluster is described by three patterns leading to higher education, either starting with a spell of further education or with school. These three patterns cover together (have in their neighborhood) 45% of the sequences and the overall quality measure for the representative set is 29%.

The number of selected representative sequences in cluster 3 and 4 is higher due to a lesser redundancy in the candidate list. In cluster 3, the pattern is a transition to employment preceded by long (compared to Cluster 1) spells of school and/or further education. In this cluster, the five representative sequences cover together 48.5% of the sequences, which is the highest

attained value.

The key patterns in cluster 4 was less clear when looking at the sequence frequency plot (Figure 1). This group is dominated by long spells of training leading to employment or joblessness and by disrupted patterns containing spells of joblessness. Hence these trajectories can be characterized as less successful transitions from school to work. The diversity of the patterns is high in this cluster which leads to the extraction of eleven non redundant sequences from the candidate list. The selected representative set covers nonetheless 39% of the cases in the cluster while the quality measure reaches its highest level ($Q = 39\%$). Indeed the discrepancy is high in this group ($V = 37.2$) and representing the sequences with their assigned representative rather than by the center of the set significantly decreases the sum of distances.

4.2 Comparing Sorting Criteria

Table 4 summarizes the outcome obtained with each of the five proposed criteria. The Frequency, Density

and Likelihood criteria provide results of quite equivalent quality while the Mean State Frequency (MSt-Freq) and Centrality criteria are clearly less satisfactory.

Table 4: Comparing criterions with $trep=25\%$.

	<i>nr</i>	<i>nb</i>	(%)	<i>MD</i>	<i>Q</i>
Cluster 1					
Frequency	3	121	45.7	15.6	15.0
Density	3	121	45.7	15.6	15.0
Likelihood	3	121	45.7	15.6	15.0
MStFreq	2	82	30.9	25.2	-37.6
Centrality	7	104	39.2	18.1	1.4
Cluster 2					
Frequency	3	69	45.1	16.6	29.4
Density	3	69	45.1	16.6	29.4
Likelihood	2	59	38.6	18.7	20.5
MStFreq	4	62	40.5	18.4	21.5
Centrality	3	39	25.5	29.9	-27.2
Cluster 3					
Frequency	5	94	48.5	23.1	17.0
Density	6	100	51.5	19.3	30.6
Likelihood	8	105	54.1	18.2	34.8
MStFreq	3	81	41.8	31.2	-12.0
Centrality	4	67	34.5	31.3	-12.4
Cluster 4					
Frequency	11	39	39.0	22.7	39.0
Density	11	37	37.0	23.8	35.9
Likelihood	7	42	42.0	26.5	28.8
MStFreq	12	36	36.0	29.3	21.3
Centrality	15	36	36.0	29.8	19.9

Selecting the representative sequences in a candidate list sorted according to the distance to the center yields poor results in many cases. Indeed selecting representatives close from the center of the group leads to poor representation of sequences that are far from it. The sometimes bad results yielded with the Mean State Frequency criterion is attributable to the nature of this criterion, which focuses on the total of position-dependant scores while completely ignoring the sequence structure.

From Table 4, it seems that among the three winners, Density that is always ranked 1st or 2nd is the best compromise. We may notice, however, that no criterion yields systematically the smallest number of representatives.

4.3 Size of the Candidate List

Table 5 presents the results obtained after increasing the $trep$ threshold for the size of the candidate list to 75%. As a consequence the proportion of well represented sequences is now at least 75%. This gain

comes however at the cost of a considerable increase in the number nr of selected representative sequences. With this high $trep$, the results obtained with the Density criterion get the best scores with any of the three considered quality measures for all four clusters. With Likelihood and Frequency we get results of a quality close to that yielded by Density, while the Mean State Frequency and Centrality give again poorer results.

Table 5: Comparing criterions with $trep=75\%$.

	<i>nr</i>	<i>nb</i>	(%)	<i>MD</i>	<i>Q</i>
Cluster 1					
Frequency	58	224	84.5	4.4	76.0
Density	58	230	86.8	3.7	79.6
Likelihood	44	216	81.5	5.2	71.6
MStFreq	39	201	75.8	9.1	50.2
Centrality	40	202	76.2	9.4	48.5
Cluster 2					
Frequency	27	129	84.3	5.0	78.9
Density	26	132	86.3	4.6	80.3
Likelihood	18	123	80.4	6.1	74.2
MStFreq	23	122	79.7	7.1	69.6
Centrality	23	119	77.8	8.5	64.0
Cluster 3					
Frequency	50	158	81.4	8.2	70.7
Density	58	171	88.1	5.5	80.3
Likelihood	42	157	80.9	8.5	69.6
MStFreq	41	148	76.3	12.3	55.9
Centrality	52	156	80.4	10.4	62.6
Cluster 4					
Frequency	48	87	87.0	5.6	84.9
Density	48	87	87.0	5.2	85.9
Likelihood	35	76	76.0	10.1	72.8
MStFreq	41	77	77.0	10.8	71.0
Centrality	46	76	76.0	10.1	72.8

5 CONCLUSIONS

We have presented a flexible method for selecting and visualizing representatives of a set of sequences. The method attempts to find the smallest number of representatives that achieve a given coverage. Different indicators have been considered to measure representativeness and the coverage can be evaluated by means of different sequence dissimilarity measures. The heuristic can be fine tuned with various thresholds for controlling the trade-off between size and quality of the resulting representative set. The experiments demonstrated how good our method is for extracting in an readily interpretable way the main features from sets of sequences. The proposed tools

are made available as functions of the TraMineR R-package and are awaiting to be tested with other data sets.

ACKNOWLEDGEMENTS

This work is part of the Swiss National Science Foundation research project FN-1000015-122230 “Mining event histories: Towards new insights on personal Swiss life courses”.

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