

# THE MASKLE: AUTOMATIC WEIGHTING FOR FACIAL ANIMATION

## *An Automated Approach the Problem of Facial Weighting for Animation*

Alun Evans, Marco Romeo, Marcelo Dematei and Josep Blat

*Barcelona Media – Centre d'Innovació / Universitat Pompeu Fabra, Av. Diagonal 177, planta 9, 08018 Barcelona, Spain*

**Keywords:** Facial animation, Automated animation, Weighting.

**Abstract:** Facial animation of 3D characters is frequently a time-consuming and repetitive process that involves either skeleton-rigging or pose-setting for morph targets. A major issue of concern is the necessity to repeat similar tasks for different models, re-creating the same animation system for several faces. Thus there is a need for reusable methods and tools that allow the introduction of automation into these processes. In this paper we present such a method to assist in the process of facial rigging: the Maskle. Based upon the standard bone-weight linear skinning animation technique, the desired distribution of vertex-movement weights for facial animation is pre-programmed into a low-resolution, generic facial mask. This mask, or 'Maskle', is then semi-automatically overlaid onto a newly created face model, before the animation-weight distribution is automatically transferred from the Maskle to the model. The result is a weight-painted model, created semi-automatically, and available for the artist to use for animation. We present results comparing Maskle-weighted faces to those weighted manually by an artist, which were treated as the gold standard. The results show that the Maskle is capable of automatically weight-painting a face to within 1.58% of a manually weighted face, with a maximum error of 3.82%. Comparison with standard professional automatic weighting algorithms shows that the Maskle is over three times more accurate.

## 1 INTRODUCTION

The goal of facial animation for 3D models is to enable the representation of emotions and expressions in a plausible manner. Since pioneering work in the field was first published over 25 years ago (Parke, 1982), a large amount of research has been carried out on the development of computational models of the human face. The ultimate goal for this research is a system that 1) creates convincing animation, 2) operates in real time, 3) is automated as much as possible and 4) adapts easily to individual faces. While there has been significant progress towards solving each of these four matters individually, there has been relatively little progress in developing techniques that succeed in solving all four of the problems simultaneously. It is with this goal in mind that we present the first results of a novel method for automatic bone-weight facial rigging, called the Maskle. The motivation for the development of the Maskle has two sources. The first is the amount of

time it can take an experienced artist to create a simple animation on a 3D face model, even using a powerful tool such as Autodesk's Maya or 3DS Max. The second is the multimedia industry's increasing need for reusable tools to assist in production work, reflected by current research being carried out by several EU-funded projects, for example SALERO (SALERO, 2006). The concept of the Maskle is a result of direct contact of academic researchers with multimedia production companies, and the results of the research are being directly funnelled into the professional sector.

The main contribution of this paper is in the area of facial animation, specifically towards automation of the facial animation process. We show the results of our initial tests which are designed to ascertain whether the Maskle is a viable concept for use within a professional production. The results obtained show a mean error of only 2.63%, and have led to the Maskle system being used already by our production partners.

## 2 RELATED WORK

The techniques used for the rigging of 3D characters to create convincing facial animation can be broadly divided into two distinct areas. The first are those that focus on mimicking the movement of the face surface only, attempting only to replicate facial poses using surface deformations (Guenter et al., 1998; Kalra et al., 1992). The second are those that model the anatomy of the face, attempting to replicate the movement of bones and muscles within a virtual framework (Lee et al., 1995; Platt and Badler, 1981; Waters and Frisbie, 1995). Some of the earliest work in facial animation represents this split, with Parke's work on the parameterisation of faces balanced by Waters' (Waters, 1987) attempt to replicate facial movement by modelling the movement of muscles. In the decades since this pioneering work there has been considerable research effort put into to generating realistic facial animation, much of it reviewed in detail by Noh and Neumann (1998) and Ersotelos (2008).

Of particular relevance are Lee et al.'s (1995) efforts at digitising facial geometries and automatically animating them through the dynamic simulation of facial tissues and muscles. Their approach was to construct functional models of the heads of human subjects from laser-scanned range and reflectance data. These models were then extended with contractile muscles embedded within a dynamic skin model. The result was automatic animation of a human face from a scanned subject.

Noh and Neumann (Noh and Neumann, 2001) made considerable advances within the field of automatic character animation with their work on the cloning of expressions. Their technique was one of the first to directly address the problem of reusing existing animations, and transferring them to newly created virtual characters. After letting users select a set of points of the surface of a model, their method was able to transfer vertex motion vectors from a source character to a target character, with the aid of an automated heuristic correspondence search.

Orvalho et al. (Orvalho et al., 2006) extend this concept by attempting to adapt a generic facial rig to different facial models. The technique required considerable labelling effort yet was able to find corresponding points between source and target faces. This point matching was then used as a basis for the transfer of a complex, muscle-based facial rig system, to enable the target face to replicate the expressions provided by the base rig. Although this technique is of some interest, the authors do not present quantitative results, and only a few

qualitative images to prove the validity of their method.

Despite these efforts, there is still substantial gap in the state of the art that remains to be filled before we reach a facial modelling system that fulfils all four points mentioned above in section 1. In this paper we present our efforts at addressing this gap, with a highly automated system that is capable of enabling artists to quickly create suitable facial animation for a wide variety of face models.

## 3 THE MASKLE

### 3.1 Overview

The concept of the Maskle is to allow artists to create a facial animation system once, yet be able to re-apply it to as many characters as they desire. In this sense, the keyword is that the system is *reusable*. Unlike some of the related research presented above, the goal of the system is not to transfer an animation system from one face to another; neither is it to automatically animate a face based on a scan or photograph. Rather, it is designed such that an artist can develop their own system of facial animation and, once designed, quickly apply this system to any number of characters that they create.

The type of facial animation system that the Maskle is based around is a standard bone-weight system, where the deformation of the set of vertices that form the skin of a model is controlled by the movement of an underlying skeleton; the exact movement of each vertex (proportional to the bones of the skeleton) is represented by a set of numeric proportions, or *weights*, assigned to each vertex. The justification for basing our algorithm on a bone-weight system, as opposed to other animation systems such as blend shapes, is that the bone-weight system can be abstracted to a number of control points (representing the locations of the bones); this abstraction facilitates the organisation of weight-transfer algorithm presented below, and allows rapid testing to ensure the results are satisfactory.

Once an artist has created a character, bone-weight animation of a face usually requires extensive effort in accurately assigning, or *painting*, the weights for each vertex and for each bone. This can be done automatically, and many 3D design packages such Autodesk Maya and 3DS Max have such functionality, frequently based around using envelope systems (Autodesk, 2007). However,

despite being generally successful at automatically painting body areas where the skin can be tightly bound to the bone (such as the arms or legs), these existing systems are less suitable for facial rigs, where the ‘bones’ of the face are rarely modelled on the real-life bones of a skull. Thus, weight-painting a newly designed character to fit an existing facial rig becomes a labour intensive and time consuming process, as there is little existing automation that can be used.

The Maskle system directly addresses this problem by using a pre-painted, low resolution mask to automatically weight-paint a newly created face. The initial step is for an artist to create a facial rig, (according to individual requirements) for the Maskle itself. Given this rig, the overall process occurs as follows. After the user has marked a total of ten specific marker points around the areas of the lips and the eyes, the structure of the Maskle is loaded. This structure consists of a low-resolution facial ‘mask’, designed so that it will be able to wrap around areas of a 3D face that are commonly used for animation. The Maskle is then adjusted semi-automatically so that it shrinks around the shape of the face; a collision detection algorithm detects when the Maskle has contacted the face and prevents its further movement. Once the Maskle has wrapped around the face, ray-face collision algorithms find, for each vertex of the face model, the nearest point on the surface of the mask, which is then used to calculate the animation weight for each vertex of the face mesh. The Maskle can then be deleted, leaving the face surface bound to the bone rig, ready for animation.

The mesh used to represent the Maskle can vary in terms of its actual structure. However, for the work presented in this paper, the Maskle structure consists of a 90-vertex, 82-face, symmetrical triangle/quad mesh. While it is designed to cover the areas surrounding the lips and eyebrows; the precise details of topology and dimensions are less relevant due to the changes that it undergoes during the process of fitting it to a target face (as explained in section 3.2 below). The techniques presented in sections 3.2 and 3.3 were developed using C++ and Maya Scripting Language (MEL) to create a plug-in for Autodesk Maya, due to it being one of the most popular 3D modelling packages available. It has also been ported to Autodesk 3DS Max, and the design of the system is such that it would be straightforward to transfer it to other modelling and animation tools such as Blender, or proprietary software. The facial models used for testing and evaluation are triangle/quad vertex-face models,

consisting of between 757 and 6603 vertices. Each facial model must have a small gap between the upper and lower lips to ensure correct weighting in these areas (see below).

## 3.2 Automatic Fitting

To ensure that the animation weights for each vertex are transferred as accurately as possible, it is important that the Maskle fits closely over the face model. More importantly, it is vital that the equivalent areas of the mask and face model are in close proximity; for example, the upper lip of the Maskle must be in close proximity to the upper lip of the face model. Failure to ensure this proximity frequently results in errors in the transferring of weights, for example, the upper lip of the face model acquiring the weights from the lower lip of the mask.

### 3.2.1 Initial Placement

Due to the wide variety of facial shapes and sizes that can exist, for each face it is necessary to pre-programme the Maskle with some figures that relate to the scale of the model in question. Thus, the fitting of the Maskle to the face is initialised by the user manually marking ten vertices of the face: two at the lateral boundaries of the lips; four along the central axis of the face, marking the highest and lowest vertices of both the upper and lower lip, and four marking the inner and outer lateral points of both eyes. While it is unfortunate that the user should have to manually mark locations, the number is substantially less than that required by similar techniques (Orvalho et al. 2006).

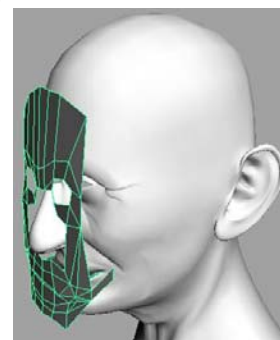


Figure 1: View of the Maskle system post-initialisation step.

Once the vertices have been marked, the respective distances between them are used to scale the basic Maskle shape so that it has the same

dimensions (e.g. the distance between nose and mouth) as the face. The Maskle mesh is then loaded and placed in front of the face model. It is almost entirely flattened to a 2D plane, with only a ‘tongue’ extending into the mouth. This ‘tongue’ is present to ensure that the Maskle will correctly cover the lips of the face model; if it is not present the probability of either lip being assigned the animation weight of the other is much higher. The final placement of Maskle is decided by the user, to ensure that the ‘tongue’ of the Maskle enters the mouth at the correct angle. Figure 1 shows the position of Maskle post-initialisation.

### 3.2.2 Automatic Shrinking

Following the initial placement, the Maskle undergoes an automatic movement/shrinking process which allows the shape of the Maskle mesh to hug closely the shape of the target face mesh. The basic system of movement is a curtailed version of the dynamic force formulation for active surface models (Sonka and Fitzpatrick, 2000). An iterative process applies a combination of forces to each vertex, the direction and magnitude of each force contributing to the overall movement. This method was preferred over direct correspondence techniques as it allows the structure of the Maskle to change dynamically as it is laid over the face model; also it is very fast.

The location,  $\mathbf{x}_i$ , of each vertex,  $v_i$ , moving through time  $t$  can be calculated as

$$\mathbf{x}_i(t+1) = \mathbf{x}_i(t) + \mathbf{F}_i(t) \quad (1)$$

The total force,  $\mathbf{F}$ , applied to each vertex at each iteration is dependent on two forces;  $\alpha$  and  $\beta$ .

$$\mathbf{F}_i(t) = a\alpha_i(t) + b\beta_i(t) \quad (2)$$

$a$  and  $b$  are factors used to control the influence of  $\alpha$  and  $\beta$  respectively.  $\alpha_i(t)$  is calculated according to:

$$\alpha_i(t) = c_i - \mathbf{x}_i(t) \quad (3)$$

where  $c_i$  is the average coordinate location of the set of vertices adjacent to  $v_i$  (i.e. the set of vertices that are connected to  $v_i$  by a single edge).  $\beta_i(t)$  is equivalent to the normalised vector representing the initial (i.e. when  $t=0$ ) direction of the ‘tongue’ of the Maskle (as mentioned above in 3.2.1) and is calculated using the relative locations of the relevant vertices of the Maskle mesh. The effect of iteratively

applying equation (1) to the vertices of the Maskle is that each vertex moves (in Euclidean space) according to the direction and magnitude of the resulting vector. Thus, the mesh moves towards the face model (due to the influence of  $\beta$ ) and wraps around it (due to the influence of  $\alpha$ ). The termination condition for the movement is partially applied when the Maskle mesh collides with the face model mesh (alternatively, the user may choose to manually terminate the movement phase). Specifically, if a Maskle triangle/quad collides with the face model, the constituent vertices of the Maskle are flagged and prevented from further movement. Once all the vertices of the Maskle have been flagged, the algorithm stops. Collision detection is carried out by Moller’s triangle-triangle intersection test algorithm (Moller, 1997), optimised by a standard axis-aligned octree (Ericson, 2005), and run at each movement iteration. Quad faces are split into two constituent triangles for the purposes of collision detection. Figure 2 shows an example of the result of the completed movement.

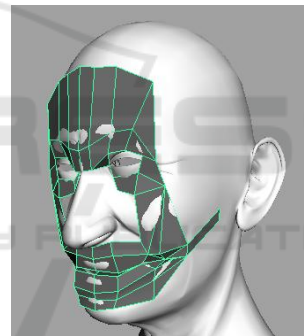


Figure 2: Final position of the Maskle for weight transfer.

It is important to note that the results of the automatic shrinking algorithm are dependent on the accuracy of the initial placement (described above in section 3.2.1). If the initial placement is incorrect, the overall dimensions of the Maskle structure will be incorrect, and the automatic shrinking algorithm will not hug the face model correctly.

### 3.3 Weight Transfer

Now that the Maskle mesh has been placed adjacent to the face model, its location can be used to recreate an existing rig on the model (as mentioned in section 3.1 above, such a rig will have been already created by the artist and applied to the Maskle). Firstly the system of bones of the facial rig is re-created. Given the location of a manually created ‘base’ bone, a simple script recreates the bones of the rig, using the

locations of the vertices of the Maskle to ensure correct placement. The exact form of this script will depend on the number of bones that form part of the facial rig which the Maskle is applying. The animation weights for each vertex and for each bone can now be set for the face model. For each vertex of the face model, an infinite bi-directional ray is projected along the axis of the Normal vector of the model surface at that vertex. An intersection test (Ericson, 2005) is carried out between this ray and the faces of the Maskle. If successful, this test defines an intersection point,  $p_I$ , which lies on the plane of a quad/triangle face of the Maskle. This face is labelled  $f_I$ . Recalling that the Maskle vertices have been already weighted by the artist during the creation of the original facial rig, the coordinates of  $p_I$  on the surface of the Maskle are then used to interpolate the animation weights associated with the constituent vertices of  $f_I$ . The method used for this interpolation is the Inverse Distance Weighting, or ‘‘Shepard’’, method, where the interpolated value is a weighted average of the values of the surrounding points (Amidror, 2002). The interpolated weight values for  $p_I$  are then assigned the vertex of the face model from which  $p_I$  was created. To increase computational speed, the process is carried out for only those vertices of the face model that lie within the largest possible circumsphere that can be created using the vertices of the Maskle mesh. The result is that the weights for each bone are interpolated from the vertices of the Maskle to the vertices of the face model. The final step is to run a smoothing algorithm (Autodesk, 2007) that ensures even distribution of weights over the area of the face. The artist is now free to animate the face as desired.

## 4 EVALUATION

An evaluation of the Maskle was carried out to prove that the concept of the weight-transfer system had validity. The difficulty in designing such a test is increased due to the very nature of the work that the Maskle is designed to facilitate i.e. animating a face. Such work can be highly subjective, and it is important to try and remove or negate any influences that may introduce such subjectivity. For example, the Maskle is designed to work with a variety of facial rig designs, and any evaluation procedure should be as independent as possible from these or other variable elements that exist in the animation pipeline.

To this extent we designed an evaluation procedure that tests *only* the capability of the Maskle

to transfer the weights for the correct regions of the face. An artist created a very simple, seven-bone facial rig, and applied it manually to the Maskle and to four different face models. We then commenced the evaluation process by using the Maskle to automatically transfer its associated rig to unrigged copies of same four face models. The values assigned to variables  $a$  and  $b$  in equation (1) were deduced according to visual inspection of the movement path of the Maskle mesh, and were set to 0.005 and 0.05 respectively. They were kept constant for all tests. Such low values ensure slow movement of the Maskle mesh and thus more accurate collision detection.

The success of the Maskle weighting was measured by comparing the animation weight distribution of manually weighted face-model (the gold standard) and the Maskle-weighted face model (the test candidate). However, doing this for every single vertex in the face model could have introduced bias into the procedure. This is because neither artist nor Maskle will have applied animation weights to immovable facial features (e.g. the ear) and so these vertices should not be allowed to bias any mean comparison towards smaller error. Thus, we isolated the set of vertices of the face model whose Normal vector rays intersect with the Maskle (as described in section 3.3) and label this set  $M$ , where  $M = \{m_i\}$ ,  $i = 1, \dots, I$ . The difference between the manually weighted set,  $M_{Manual}$  and the Maskle-weighted set  $M_{Maskle}$ , for each of the seven bones in the rig, can now be calculated thus:

$$diff_{bone} = \frac{\sum_0^I abs(m_{i_{Manual}} - m_{i_{Maskle}})}{I}$$

where  $m_{i_{Manual}}$  is the weight of the  $i^{\text{th}}$  vertex of set  $M_{Manual}$  and  $m_{i_{Maskle}}$  is the weight of the  $i^{\text{th}}$  vertex of set  $M_{Maskle}$ .

The total average difference between  $M_{Manual}$  and  $M_{Maskle}$  is then calculated by averaging  $diff_{bone}$  over each of the seven bones in the test rigs. As the goal was to test the weight distribution (i.e. the spread of weights for each joint across the mesh), the differences between manual and automatic were normalised according to the difference in maximum weight spread.

As a comparison, an industry standard envelope-based automatic skinning algorithm (Autodesk, 2007) was applied to the same four faces, and the differences calculated in the same way (using the same set of vertices). Figure 6 shows a table with the

results as percentage of the total possible weight (weight values range from 0 – 1, thus an average weight difference of 0.5 means there is a gap between the sets of 50% of the possible weight). The face models have been labelled according to their appearance.

Table 1 shows that the Maskle weighted face achieves lower error rates in weighting all the test models. When considering the mean figures, the table shows that the Maskle is over three times more accurate than the standard envelope algorithm. Visual analysis of the results for each face shows an even greater difference that the data in the table illustrates, as the envelope based method deals very poorly with the area of the lips, incorrectly associating vertices of the upper lip to the bone of the lower lip, and vice versa. The error can be seen visually in Figure 4(c). Due to the nature of the Maskle (specifically, the ‘tongue’ that divides the upper and lower lips, this error is completely removed.

Table 1: The mean differences between manually weighted faces and automatically weighted faces. A sample of each model is shown in Figures 4, 5 and 6.

Model	Maskle difference as % of possible weight	Envelope difference as % of possible weight
Realistic Human	1.58	8.43
Cartoon Human	2.49	7.40
Cartoon Devil	2.61	7.17
Venetian Mask	3.82	11.92
<b>Average</b>	<b>2.63</b>	<b>8.73</b>

To illustrate this, Figure 3 consists of two graphs that show the weight distribution profile for the weights of the lower lip bone of one of the models used in the study (the ‘Realistic Human’ model in Table 1 and illustrated in Figure 4). Figure 3 (a) shows a comparison between the manually weighted face and the Maskle weighted face. The graph shows that there the two sets of data overlap and that there are very few vertices that are weighted in only one of the sets. Figure 3 (b) shows a comparison between the manually weighted face and the envelope-algorithm weighted face. In this graph there is less correlation between the datasets, and the envelope algorithm has incorrectly weighted several vertices which remain unweighted by the manual

operator. Further examples of animated faces generated successfully using the Maskle can be seen in Figures 4(b), 5 and 6.

## 5 DISCUSSION AND FUTURE WORK

In this paper we have presented the concept of the Maskle system and the results of a study on the validity of using such a system. The novel contribution is in the area of automation of facial animation, with specific contribution in the automated animation of areas of the face that are time-consuming to animate manually, such as the lips. The results show that the system used for this study is capable of creating a facial rig that is, on average, within 2.63% of being identical to that created manually. This error rate is over three times less than that obtained by carrying out the same tests on a standard envelope-based weighting algorithm.

The Maskle is a novel idea of automatically recreating a facial animation system on a variety of face models, and addresses this issue in a way that is different to work previously published; thus, it is difficult to compare the obtained error rates with the results published by other researchers. Perhaps the most similar previous work is Orvalho et al.’s (2006) efforts in transferring a facial animation system, yet their work focuses strongly on transferring a rather complex generic facial rig, and involves the user manually marking 44 points landmark points. The Maskle system is more flexible in that it can be used with a variety of facial rigs, and only requires the marking of ten landmark points. Unfortunately, Orvalho et al. do not provide numerical results for their technique, showing their results only in graphical format, thus it is difficult to directly compare the accuracy of the Maskle with their results. Noh and Neumann (Noh and Neumann, 2001) presented statistics comparing the results of the motion vectors for cloned expressions (i.e. expression that are copied from a ‘source’ face to a ‘destination’ face). Again, this is difficult to compare to the results in this paper, as the Maskle does not attempt to directly transfer expressions, rather it is directly transferring movement weights to allow artists to animate as they desire.

Due to the low error rates, analysis of graphs of the type shown in Figure 3, and visual analysis of the face models, our interpretation of the results obtained in the study is that the Maskle is a tool that can greatly aid the process of creating facial

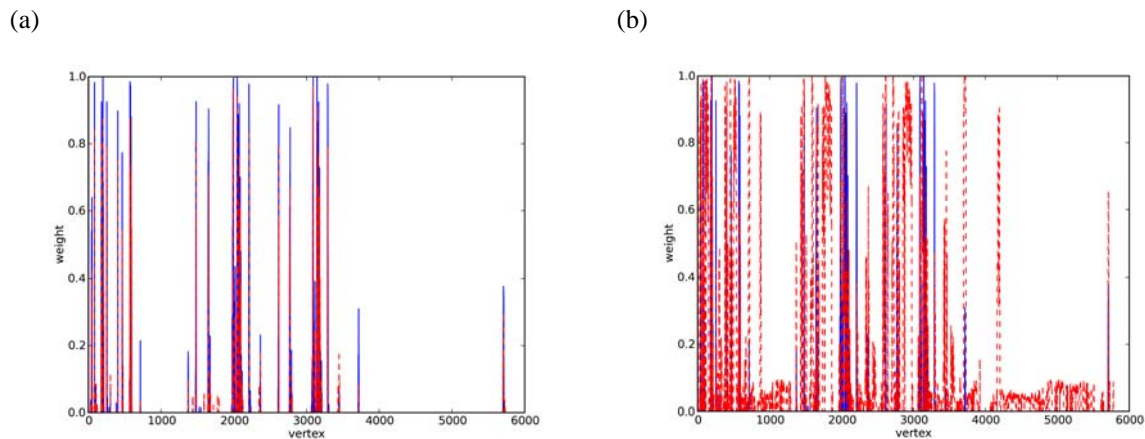


Figure 3: Sample weight profiles for one bone of a manually-weighted face (blue line) and automatically weighted face (red dashed line). Figure (a) shows the results for the Maskle, Figure (b) for the envelope algorithm. The envelope algorithm shows a much greater level of noise and erroneous calculations.

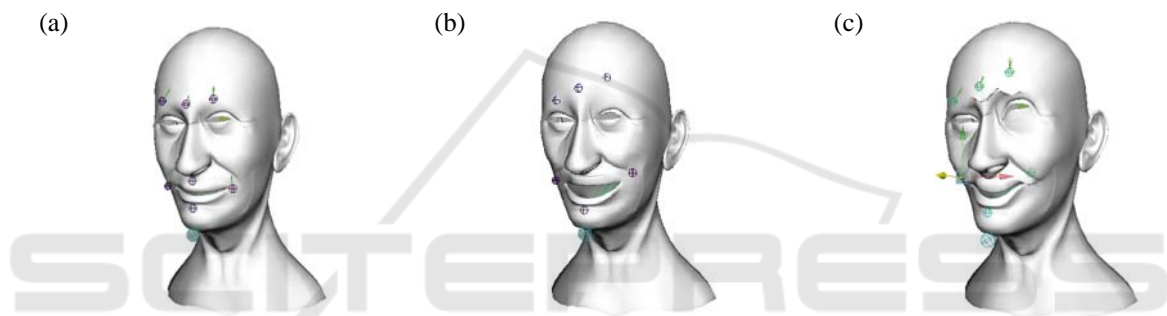


Figure 4: Visual differences between Maskle-weighted and envelope-weighted faces, comparing a simple expression created by moving the bones of the rig. (a) shows the unanimated face; (b) shows the expression applied to the Maskle-weighted face; (c) shows the same expression applied to the envelope-weighted face.

animation for 3D characters. This being said, the technique does have several limitations. The first is that in its current state, the Maskle does not cover certain areas of the face that are usually used in animation e.g. the chin. The reason for this is that, in practice, such areas are straightforward for even a non-experienced artist to animate, and thus there is little need for an automated tool to assist in this area. By contrast the area around the lips is difficult and time-consuming to animate, and it is this and other similar areas in which the Maskle is of most use. Nevertheless, in the interest of creating a more comprehensive tool, our future work will involve expanding the Maskle to cover other areas of the face. A further limitation is in situations where the face shape is very different to the structure of the Maskle. The system works well with humanoid faces, but has not yet been tested with animal, fantasy, or highly abstract faces. There is also scope for technical improvement by investigating different

methods of Maskle-face correspondence. While the current method is adequate and fast, it does require manual fine adjustment. Several other correspondence techniques exist, and a study could be carried out to see if using any of these improves the system. Our immediate future work is to conduct a more comprehensive evaluation study to measure the impact of the use of the Maskle in real-life animation situations, possibly recording the time that it takes several artists to create a facial rig on several characters, with and without the Maskle.

Finally we also intend to combine the Maskle with other facial animation work that is being currently being conducted within our group, which involves automatic creation of facial emotions across a wide range of facial models. It is expected that this further work will lead to a considerable breakthrough in the field of automatic facial animation, in which the Maskle system will play a major role.

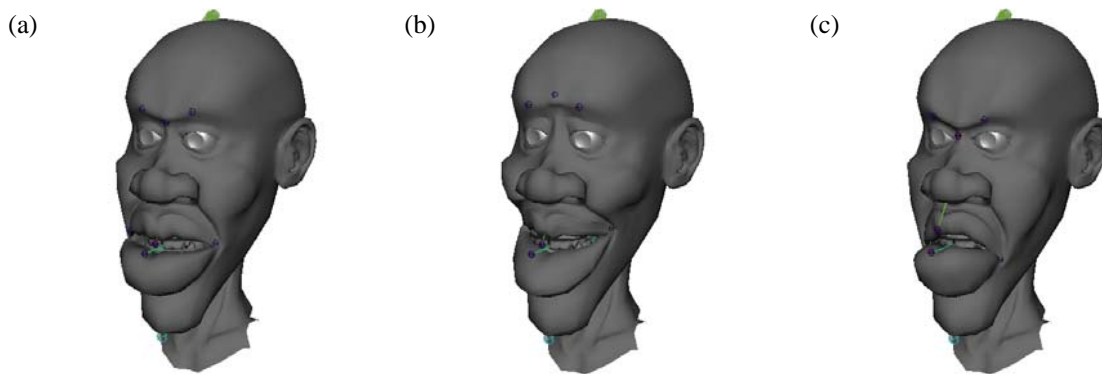


Figure 5: Example of expressions successfully created using the Maskle on a cartoon character with pronounced features. (a) is the unanimated face, (b) and (c) are expressions created after the Maskle has weighted the face.



Figure 6: Examples of expressions created on 3D models animated using the Maskle (images © Merja Nieminen, Crucible Studio / University of Art and Design Helsinki 2008).

## ACKNOWLEDGEMENTS

The authors would like to acknowledge the support of the SALERO project <http://www.salero.info>.

## REFERENCES

- Amidror, I. 2002. Scattered data interpolation methods for electronic imaging systems, a survey, *Journal of Electronic Imaging*, 11, 2, 157-176.
- Autodesk Maya Press. 2007. *Learning Autodesk Maya 2008: The Modeling & Animation Handbook*. Sybex.
- Ericson, C. 2005. *Real-time Collision Detection*. Morgan Kaufmann.
- Ersotelos, N. and Dong, F. 2008. Building highly realistic facial modeling and animation: a survey, *The Visual Computer*, 24, 13-30.
- Guenter, B., Grimm, C., Wood, D., Malvar, H., and Pighin, F. 1998. Making Faces, In *Proceedings of ACM SIGGRAPH 1998*, 55-66.
- Kalra, P., Mangili, A., Thalmann, N., and Thalmann, D. 1992. Simulation of Facial Muscle Actions Based on Rational Free From Deformation. *Eurographics*, 11, 3, 59-69.
- Lee, Y., Terzopoulos, D., and Waters, K. 1995. Realistic Modeling for Facial Animation. In *Proceedings of ACM SIGGRAPH 1995*, 55-62.
- Lee, Y., Terzopoulos, D., and Waters, K. 2002. Realistic Face Modelling for Animation. In *Proceedings of ACM SIGGRAPH 1995*, 55-62.
- Möller, T. 1997. A fast triangle-triangle intersection test, *Journal of Graphics Tools*, 2, 2, 25-30.
- Noh, J. and Neumann, U. 2001. Expression Cloning, In *Proceedings of ACM SIGGRAPH 2001*, 277-288.
- Noh, J. and Neumann, U. 1998. A survey of facial modeling and animation techniques, USC Technical Report.
- Orvalho, V., Zacur, E., and Susin, A. 2006. Transferring a Labeled Generic Rig to Animate Face Models, *Lecture Notes in Computer Science 4069*, 223-233.
- Parke, F. 1982. A parameterized Model for Facial Animation, *IEEE Computer Graphics and Applications*, 2, 9, 61-68.
- Platt, S., and Badler, N. 1981. Animating Facial Expressions. *Computer Graphics*, 15, 3, 245-252.
- SALERO. 2006. <http://www.salero.info/>.
- Sonka, M and Fitzpatrick, J. 2000. *Handbook of Medical Imaging, Vol. 2 Medical Image Processing and Analysis*. SPIE Press.
- Waters, K. 1987. A Muscle Model for Animating Three-Dimensional Facial Expression, *Computer Graphics*, 21, 4, 17-24.
- Waters, K., and Frisbie, J. 1995. A coordinated Muscle Model for Speech Animation, *Graphics Interface*, 163-170.