USING EXPANDED MARKOV PROCESS AND JOINT DISTRIBUTION FEATURES FOR JPEG STEGANALYSIS

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Abstract: In this paper, we propose a scheme for detecting the information-hiding in multi-class JPEG images by

combining expanded Markov process and joint distribution features. First, the features of the condition and joint distributions in the transform domains are extracted (including the Discrete Cosine Transform or DCT, the Discrete Wavelet Transform or DWT); next, the same features from the calibrated version of the testing images are extracted. A Support Vector Machine (SVM) is applied to the differences of the features extracted from the testing image and from the calibrated version. Experimental results show that this

approach delivers good performance in identifying several hiding systems in JPEG images.

1 INTRODUCTION

To enable covert communication, steganaography is the technique of hiding data in a digital media. Digital image is currently one of the most popular digital media for carrying covert messages. The innocent image is called carrier or cover; and the adulterated image carrying some hidden data is called stego-image or steganogram. In image steganography, the common information-hiding information-hiding techniques implement modifying the pixel values in space domain or modifying the coefficients in transform domain. Some other information hiding techniques include spread spectrum steganography (Marvel et al., 1999), statistical steganography, distortion, and cover generation steganography (Katzenbeisser and Petitcolas, 2000), etc.

The objective of steganalysis is to discover the presence of hidden data. To this date, some steganographic embedding methods such as LSB embedding, spread spectrum steganography, and LSB matching, etc. (Fridrich et al., 2002), (Harmsen and Pearlman, 2004), (Harmsen and Pearlman, 2003), (Ker, 2005), (Liu and Sung, 2007), (Liu et al., 2006; Liu et al., 2008a, 2008b) have been success-

fully steganalyzed.

JPEG image is one of the most popular media on the Internet and easily used to carry hidden data; many information-hiding methods and/or tools on the Internet implement hiding message in JPEG images, therefore, it's important for many purposes to design a reliable algorithm to decide whether a JPEG image found on the Internet carries hidden data or not. There are a few methods for detecting JPEG steganography. One of them is Histogram Characteristic Function Center Of Mass (HCFCOM) for detecting noise-adding steganography (Harmsen and Pearlman, 2003) another well-known method is to construct the high-order moment statistical model in the multi-scale decomposition using wavelet-like transform and then apply learning classifier to the high order feature set (Lyu and Farid, 2005). Fridrich et al. presented a method to estimate the coverimage histogram from the stego-image (Fridrich et al., 2002). Another new feature-based steganalytic method for JPEG images was proposed where the features are calculated as an L1 norm of the difference between a specific macroscopic functional calculated from the stego-image and the same functional obtained from a decompressed, cropped, and recompressed stego-image (Fridrich,

2004). Harmsen and Pearlman implemented a detection scheme using only the indices of the quantized DCT coefficients in JPEG images (Harmsen and Pearlman, 2004). Recently, Shi et al. proposed a Markov process based approach to effectively attacking JPEG steganography, which have remarkably better performance than general purpose feature sets (Shi et al., 2007). By applying calibration to Markov features, Pevny and Fridrich merged their DCT features and calibrated Markov features to improve the steganalyis performance in JPEG images (Pevny and Fridrich, 2007).

Based on the Markov process based approach (Shi et al., 2007) and the calibration version (Pevny and Fridrich, 2007), in this article, we expand the Markov features to inter-blocks of the DCT domain and to the wavelet domain, and design the features of the joint distribution on the DCT domain and the wavelet domain, and calculate the difference between the features from the testing images and the same features from the calibrated ones. We successfully improve the detection performance in multi-class JPEG images.

The rest of this article is organized as follows: the second section expands the Markov features; the third presents the features of joint distribution of the transform domains; the forth explains the calculation of the calibrated version of the images and the feature extraction; the fifth introduces experiments and compares the detection performances of the different feature sets; and followed by our conclusions in the sixth.

2 EXPANING MARKOV PROCESS

2.1 Introduction to Markov Approach

Shi *et al.* proposed the Markov process by modeling the differences between absolute values of neighboring DCT coefficients as a Markov process (Shi et al., 2007). The matrix F (u, v) stands for the absolute values of DCT coefficients of the image. The DCT coefficients in F (u, v) are arranged in the same way as pixels in the image by replacing each 8 \times 8 block of pixels with the corresponding block of DCT coefficients. Four difference arrays are calculated along four directions: horizontal, vertical, diagonal, and minor diagonal, denoted F_h (u, v), F_v (u, v), F_d (u, v), and F_m (u, v), respectively.

$$F_{k}(u,v) = F(u,v) - F(u+1,v)$$
 (1)

$$F_{v}(u,v) = F(u,v) - F(u,v+1)$$
 (2)

$$F_d(u, v) = F(u, v) - F(u+1, v+1)$$
(3)

$$F_m(u,v) = F(u+1,v) - F(u,v+1)$$
 (4)

Here we just utilize F_h (u, v) and F_v (u, v). The four transition probability matrices $M1_{hh}$, $M1_{hv}$, $M1_{vh}$, and $M1_{vv}$ are set up as

$$M1_{hh}(i,j) = \frac{\sum_{u=1}^{S_u-2} \sum_{v=1}^{S_v} \delta(F_h(u,v) = i, F_h(u+1,v) = j)}{\sum_{u=1}^{S_u-2} \sum_{v=1}^{S_v} \delta(F_h(u,v) = i)}$$
(5)

$$M1_{hv}(i,j) = \frac{\sum_{u=1}^{S_u-1} \sum_{v=1}^{S_v-1} \delta(F_h(u,v) = i, F_h(u,v+1) = j)}{\sum_{u=1}^{S_u-1} \sum_{v=1}^{S_v-1} \delta(F_h(u,v) = i)}$$
(6)

$$M1_{vh}(i,j) = \frac{\sum_{u=1}^{S_u-1} \sum_{v=1}^{S_v-1} \delta(F_v(u,v) = i, F_v(u+1,v) = j)}{\sum_{u=1}^{S_u-1} \sum_{v=1}^{S_v-1} \delta(F_v(u,v) = i)}$$
(7)

$$M1_{vv}(i,j) = \frac{\sum_{u=1}^{S_u} \sum_{v=1}^{S_v-2} \delta(F_v(u,v) = i, F_v(u,v+1) = j)}{\sum_{u=1}^{S_u} \sum_{v=1}^{S_v-2} \delta(F_v(u,v) = i)}$$
(8)

Where S_u and S_v denote the dimensions of the image and $\delta = 1$ if and only if its arguments are satisfied. Due to the range of differences between absolute values of neighboring DCT coefficients could be quite large, the range of i and j is limited [-4, +4]. Thus, all Markov features consist of $4 \times 81 = 324$ features.

2.2 Expanding Markov Process

From our standpoint, the original Markov features utilize the relation of neighboring DCT coefficients in the intra-DCT-block. Actually, the neighboring DCT coefficients on the inter-block have the similar relations; we expand the original Markov features to the neighboring DCT coefficients on the inter-blocks.

2.2.1 Inter-DCT block Markov Process

In addition to the transition matrices constructed on the intra-difference, we also construct the transition matrices based on the inter-DCT blocks.

First, the horizontal and vertical difference arrays on the inter-block are defined as follows:

$$D_{b}(u,v) = F(u,v) - F(u+8,v)$$
 (9)

$$D_{u}(u,v) = F(u,v) - F(u,v+8)$$
 (10)

The four transition probability matrices $M2_{hh}$, $M2_{hv}$, $M2_{vh}$ and $M2_{vv}$ are constructed as follows.

$$M2_{hh}(i,j) = \frac{\sum_{u=1}^{S_u-16} \sum_{v=1}^{S_v} \delta(D_h(u,v) = i, D_h(u+8,v) = j)}{\sum_{v=1}^{S_u-16} \sum_{v=1}^{S_v} \delta(D_h(u,v) = i)}$$
(11)

$$M \, 2_{hv}(i,j) = \frac{\sum_{u=1}^{S_u-8} \sum_{v=1}^{S_v-8} \delta(D_h(u,v) = i, D_h(u,v+8) = j)}{\sum_{u=1}^{S_u-8} \sum_{v=1}^{S_v-8} \delta(D_h(u,v) = i)}$$
(12)

$$M2_{vh}(i,j) = \frac{\sum_{u=1}^{S_u-8} \sum_{v=1}^{S_v-8} \delta(D_v(u,v) = i, D_v(u+8,v) = j)}{\sum_{u=1}^{S_u-8} \sum_{v=1}^{S_v-16} \delta(D_v(u,v) = i)}$$
(13)

$$M2_{vv}(i,j) = \frac{\sum_{u=1}^{S_{u}} \sum_{v=1}^{S_{v}-16} \delta(D_{v}(u,v) = i, D_{v}(u,v+8) = j)}{\sum_{u=1}^{S_{u}} \sum_{v=1}^{S_{v}-16} \delta(D_{v}(u,v) = i)}$$
(14)

Similar to the original version of Marko feature, the range of i and j is [-4, +4].

2.2.2 DWT Approximate Sub-band Markov **Process**

We also construct the transition matrices on the DWT approximate sub-band. Let WA denote the DWT approximation sub-band. The horizontal and vertical difference arrays are defined as follows:

$$WA_{k}(u, v) = WA(u, v) - WA(u+1, v)$$
 (15)

$$WA_{u}(u, v) = WA(u, v) - WA(u, v+1)$$
 (16)

The four transition probability matrices M3_{hh}, M3_{hv}, M3_{vh}, and M3_{vv} are constructed as follows. Let S_u and S_v denote the size of the WA.

$$M3_{hh}(i,j) = \frac{\sum_{u=1}^{S_u-2} \sum_{v=1}^{S_v} \delta(WA_h(u,v) = i, WA_h(u+1,v) = j)}{\sum_{v=1}^{S_u-2} \sum_{v=1}^{S_v} \delta(WA_h(u,v) = i)}$$
(17)

$$M3_{hh}(i,j) = \frac{\sum_{u=1}^{S_u-2} \sum_{v=1}^{S_v} \delta(WA_h(u,v) = i, WA_h(u+1,v) = j)}{\sum_{u=1}^{S_v-2} \sum_{v=1}^{S_v} \delta(WA_h(u,v) = i)}$$

$$M3_{hv}(i,j) = \frac{\sum_{u=1}^{S_u-1} \sum_{v=1}^{S_v-1} \delta(WA_h(u,v) = i, WA_h(u,v+1) = j)}{\sum_{u=1}^{S_u-1} \sum_{v=1}^{S_v-1} \delta(WA_h(u,v) = i)}$$

$$(18)$$

$$M3_{vh}(i,j) = \frac{\sum_{u=1}^{S_u-1} \sum_{v=1}^{S_v-1} \delta(WA_v(u,v) = i, WA_v(u+1,v) = j)}{\sum_{u=1}^{S_u-1} \sum_{v=1}^{S_u-1} \delta(WA_v(u,v) = i)}$$
(19)

$$M3_{vh}(i,j) = \frac{\sum_{u=1}^{S_{u}-1} \sum_{v=1}^{S_{v}-1} \delta(WA_{v}(u,v) = i, WA_{v}(u+1,v) = j)}{\sum_{u=1}^{S_{u}-1} \sum_{v=1}^{S_{v}-1} \delta(WA_{v}(u,v) = i)}$$

$$M3_{vv}(i,j) = \frac{\sum_{u=1}^{S_{u}} \sum_{v=1}^{S_{v}-2} \delta(WA_{v}(u,v) = i, WA_{v}(u,v+1) = j)}{\sum_{u=1}^{S_{u}} \sum_{v=1}^{S_{v}-2} \delta(WA_{v}(u,v) = i)}$$

$$(20)$$

Similar to the original version of Marko feature, the range of i and j is [-4, +4].

JOINT DISTRIBUTION 3 **FEATURES**

Besides the Markov features, we also design the following joint distribution matrices U1, U2 and U3 in the DCT and DWT domains, corresponding to the previous Markov features. We modified the definitions in (5)-(8), (11)-(14), and (17)-(20), and described as follows.

$$U1_{hh}(i,j) = \frac{\sum_{u=1}^{S_u-2} \sum_{v=1}^{S_v} \delta(F_h(u,v) = i, F_h(u+1,v) = j)}{(S_u-2)S_v}$$
(21)

$$U1_{hv}(i,j) = \frac{\sum_{u=1}^{S_u-1} \sum_{v=1}^{S_v-1} \delta(F_h(u,v) = i, F_h(u,v+1) = j)}{(S_u-1)(S_v-1)}$$
(22)

$$U1_{vh}(i,j) = \frac{\sum_{u=1}^{S_u-1} \sum_{v=1}^{S_v-1} \delta(F_v(u,v) = i, F_v(u+1,v) = j)}{(S_u-1)(S_v-1)}$$
(23)

$$U1_{vv}(i,j) = \frac{\sum_{u=1}^{S_u} \sum_{v=1}^{S_v-2} \delta(F_v(u,v) = i, F_v(u,v+1) = j)}{S_u(S_v-2)}$$
(24)

$$U2_{hh}(i,j) = \frac{\sum_{u=1}^{S_u-16} \sum_{v=1}^{S_v} \delta(D_h(u,v) = i, D_h(u+8,v) = j)}{\left(S_u - 16\right)S_v}$$
 (25)

$$U2_{hv}(i,j) = \frac{\sum_{u=1}^{S_u-8} \sum_{v=1}^{S_v-8} \delta(D_h(u,v) = i, D_h(u,v+8) = j)}{(S_u-8)(S_v-8)}$$
 (26)

$$U2_{vh}(i,j) = \frac{\sum_{u=1}^{S_u-8} \sum_{v=1}^{S_v-8} \delta(D_v(u,v) = i, D_v(u+8,v) = j)}{(S_u-8)(S_v-8)}$$
(27)

$$U2_{vv}(i,j) = \frac{\sum_{u=1}^{S_u} \sum_{v=1}^{S_v-16} \delta(D_v(u,v) = i, D_v(u,v+8) = j)}{S_u(S_v-16)}$$
 (28)

$$U3_{hh}(i,j) = \frac{\sum_{u=1}^{S_u-2} \sum_{v=1}^{S_v} \delta(WA_h(u,v) = i, WA_h(u+1,v) = j)}{(S_u-2)S_v}$$
(29)

$$U3_{hv}(i,j) = \frac{\sum_{u=1}^{S_u-1} \sum_{v=1}^{S_v-1} \delta(WA_h(u,v) = i, WA_h(u,v+1) = j)}{(S_u-1)(S_v-1)}$$
(30)

$$U3_{vh}(i,j) = \frac{\sum_{u=1}^{S_u-1} \sum_{v=1}^{S_v-1} \delta(WA_v(u,v) = i, WA_v(u+1,v) = j)}{\left(S_u-1\right)\left(S_v-1\right)}$$
(31)

$$U3_{vv}(i,j) = \frac{\sum_{u=1}^{S_u} \sum_{v=1}^{S_v-2} \delta(WA_v(u,v) = i, WA_v(u,v+1) = j)}{S_u(S_v-2)}$$
(32)

CALIBRATED FEATURES AND FEATURE SELECTION

Considering the variation of the statistics of the features from one image to another, besides extracting the joint distribution features, Markov features in the DCT and DWT domains and the features of EPF, we also extract these features from the calibrated version. The calibrated version is produced in this way:

- 1. Uncompress the JPEG image
- 2. Crop the pixels, and the distance of these pixels to the boundary is in the range of 0 to 3
- 3. Compress the cropped image in JPEG with the same compression ratio

After we extract the features from the calibrated version, then we compute the difference between the features from the pre-calibrated version and the features from the calibrated version. After that, we apply support vector machine recursive feature elimination (Guyon et al., 2002) to the identification of the detector of the feature set.

5 EXPERIMENTAL RESULTS

5.1 Experimental Setup

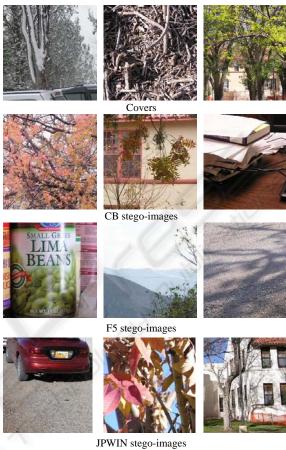
The original images are TIFF raw format digital pictures taken during 2003 to 2005. These images are 24-bit, 640×480 pixels, lossless true color and never compressed. According to the method in the references (Liu et al, 2008), (Lyu and Farid, 2005), we converted the cropped images into JPEG format with the default quality 75. In our experiments, besides the original 5000 JPEG covers, five types of steganograms are incorporated, described as follows:

- 1. 3950 CryptoBola (CB) stego-images. CryptoBola is available at http://www.cryptobola.com/.
- 2. 5000 stego-images produced by using F5 (Westfeld, 2001).
- 3. 3596 JPHS (JPHIDE and JPSEEK) stego-images. JPHS for Windows (JPWIN) is available at: http://digitalforensics.champlain.edu/download/jphs_05.zip/.
- 4. 4504 stego-images produced by steghide (Hetzl and Mutzel, 2005).
- 5. 5000 JPEG Model Based steganography without deblocking (MB1) (Sallee, 2004).

Figure 1 lists some samples of these five types of steganograms as well as some cover samples.

5.2 Steganalysis Performance

In our experiments, besides the features set consisting of the differences of the features from the pre-calibrated versions and the features from the calibrated versions, we also tested the combination of the differences and the features from the precalibrated versions. The first type of feature set is denoted DIFF and the second type of feature set is denoted as COMB. The original Markov approach, denoted Markov, as well as a sub-set of Markov features, chosen by ANOVA (the same standard to determine the features of DIFF and COMB), are also compared. In each experiment, 50% samples are chosen randomly to form a training data set and the remaining samples are tested. A Support Vector Machine with a Radial Basis kernel Function (RBF) (Duda et al., 2001), (Vapnik, 1998) is employed for training and testing. In testing each type of feature set, we do the experiment 10 times. Tables 1-1 to 1-4 lists the average testing accuracy for each type of feature set. Table 2 lists the testing accuracy values of GA and WA of different feature sets.







Steghide stego-images







MB1 stego-images

Figure 1: Some samples of the six types of JPEG images.

Generally, for an N-class classification problem, the testing samples are $m_1, m_2, ..., m_N$, respectively, corresponding to class 1, class 2, ..., and class N. The numbers of the correct testing samples are t_1 for class 1, t_2 for class 2, ..., and t_N for class N. The

general testing accuracy (GA) and weighted testing accuracy (WA) are defined as follows:

$$GA = \frac{\sum_{i=1}^{N} t_{i}}{\sum_{i=1}^{N} m_{i}}$$

$$WA = \sum_{i=1}^{N} (w_{i} \times \frac{t_{i}}{m_{i}})$$
(33)

$$WA = \sum_{i=1}^{N} (w_i \times \frac{t_i}{m_i})$$
 (34)

and $w_i = 1/6$, i = 1, 2, ..., 6.

Table 1.1: The testing results of the feature set of DIFF.

Image type		JPWIN	F5	СВ	Steg hide	MB1	Cover
	JPWIN	69.6	0.0	0.0	0.9	0.1	8.0
	F5	1.3	100	0.1	0.0	1.1	0.9
Testing	CB	0.0	0.0	99.9	0	0.0	0.0
accuracy	steghide	2.0	0.0	0.0	89.7	2.1	3.5
(%)	MB1	0	0.0	0.0	0.7	96.7	0.0
	cover	27.1	0.0	0.0	8.7	0.0	87.5

Table 1.2: The testing results of the feature set of COMB.

Image type		JPWIN	F5	СВ	Steg hide	MB1	Cover
	JPWIN	69.8	0	0	0.7	0	5.6
T:	F5	2.1	100	0.1	0.1	1.8	1.8
Testing	CB	0	0	99.9	0	0	0
accuracy (%)	steghide	3.2	0	0	92.3	0.7	4.0
(70)	MB1	0.1	0	0	1.2	97.5	0
	cover	24.8	0	0	5.7	0	88.6

Table 1.3: The testing results of the subset of Markov features that is chosen by ANOVA.

Image type		JPWIN	F5	СВ	Steg hide	MB1	Cover
	JPWIN	54.8	0.0	0.0	1.6	0.0	8.8
Testing	F5	0.3	99.8	0.0	0.0	0.6	0.5
	CB	0.3	0.0	100	0.1	0.0	0.1
accuracy (%)	steghide	5.8	0.0	0.0	80.5	1.2	9.7
, ,	MB1	0.9	0.2	0.0	5.2	97.9	1.0
	cover	38.0	0.0	0.0	12.7	0.3	79.9

Table 1.4: The testing results of the whole Markov features.

Imag <mark>e</mark> type		JPWIN	F5	СВ	Steghi de	MB1	Cover
	JPWIN	74.3	1.4	0.1	4.3	0.3	24.0
Testing accuracy (%)	F5	0.0	94.7	0.0	0.0	0.1	0.0
	СВ	0.0	0.0	99.9	0.1	0.0	0.0
	steghide	2.9	0.1	0.0	85.5	5.3	11.7
	MB1	0.0	1.9	0.0	0.4	93.4	0.3
	cover	22.9	1.9	0.0	9.8	0.9	64.0

Table 2: Average Testing accuracy (%) of GA and WA.

Feature Set	GA	WA
DIFF	91.3	90.6
COMB	92.1	91.4
Markov-subset	86.6	85.5
Markov	85.1	83.9

5.3 **Comparison of Binary Classification Performances**

According to the results shown in table 1, the detection performances of Markov features and the COMB features are both close to or reach 100% in detecting F5 and CB. We focus on the comparison of the binary testing accuracy in detecting JPWIN, steghide, and MB1. Since the feature selection of support vector machine recursive feature elimination (SVMRFE) performs well and it is applied to several kinds of feature selection (Guyon et al., 2002), (Liu et al. 2008a). Here we apply SVMRFE to choose feature sets from Markov features and COMB feature, respectively, and then apply support vector machine to the chosen features sets. Fig. 2 compares the detection performances.

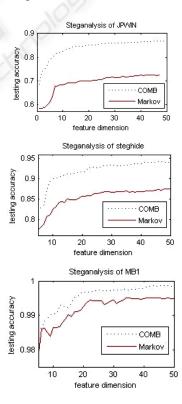


Figure 2: Comparison of detection performances with Markov and COMB features.

Apparently, the detection performances on the feature sets with COMB features are better than the corresponding feature sets with Markov features.

6 CONCLUSIONS

In this paper, we expand the well-known Markov features into the neighboring on the inter-blocks of the DCT domain and the wavelet domain. We also propose the joint distribution features of the differential neighboring in the DCT domain and the DWT domain, and calculate the difference of these features from the testing image and the calibrated version. We successfully improve the blind steganalysis performance in multi-class JPEG images. Since different hiding systems show different sensitivities to the same feature set, a method for selecting the optimal feature set is critical to maximize detection performance, and this topic is being addressed and it is possible to come out in the final version of this manuscript.

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