

FEATURE SELECTION FOR IDENTIFICATION OF SPOT WELDING PROCESSES

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Abstract: Process identification in the field of resistance spot welding can be used to improve welding quality and to speed up the set-up of a new welding process. Previously, good classification results of welding processes have been obtained using a feature set consisting of 54 features extracted from current and voltage signals recorded during welding. In this study, the usability of the individual features is evaluated and various feature selection methods are tested to find an optimal feature subset to be used in classification. Ways are sought to further improve classification accuracy by discarding features containing less classification-relevant information. The use of a small feature set is profitable in that it facilitates both feature extraction and classification. It is discovered that the classification of welding processes can be performed using a substantially reduced feature set. In addition, careful selection of the features used also improves classification accuracy. In conclusion, selection of the feature subset to be used in classification notably improves the performance of the spot welding process identification system.

1 INTRODUCTION

Resistance spot welding is one of the most important methods for joining metal objects. It is in widespread use in, for example, the automotive and electrical industries, where more than 100 million spot welding joints are produced daily in European vehicle industry only (TWI, 2004).

In resistance spot welding, two or more metal sheets are joined together by passing an electrical current through them. The current is conducted through two electrodes pressed against the metal surfaces to hold the parts to be welded tightly together. The heat produced by the flowing current melts the metals, and a welding spot is formed. The amounts of current, pressure and time are all carefully controlled and matched to the type and thickness of the material.

After cooling, the quality of the welding joint can be estimated by measuring its diameter. In general, the bigger the diameter is, the firmer is the welding joint. Some other factors, such as faults and embrittlement in the welding joint, also affect its strength. The most reliable and commonly used method to verify the quality of a welding joint is to tear the welded parts apart and to measure the spot diameter. However, the welding joint is thereby destroyed. Some nondestructive methods for estimating the spot diam-

eter also exist, but so far, no real-time, nondestructive method for online use on production lines has been developed. The two most common methods of nondestructive testing are radiographic and ultrasonic weld inspection (Anderson, 2001). These methods can also be used to detect discontinuities within the internal structure of a weld. Another example of nondestructive quality control methods of spot welding is the method based on primary circuit dynamic resistance monitoring by (Cho and Rhee, 2002).

Different combinations of welding machines used and materials welded constitute distinctive welding processes. In other words, welding processes could also be called production batches. In this study, the properties of welding experiments that distinguish different processes are the type of welding machine used, the materials welded, the thicknesses of the materials and the welding time. However, changes in current, electrode force and electrode wear are thought to be internal changes of processes. Recognition of the most similar process from a pool of previously stored processes is called process identification.

This study is a follow-up on a previous article by the authors, in which different classification methods were evaluated for use in the identification of spot welding processes (Haapalainen et al., 2005). That study showed that welding processes can be reliably

identified by extracting certain statistical and geometrical features of current and voltage signals measured during welding and performing classification based on these features. The k -nearest neighbour classifier (k NN) with the parameter value $k = 3$ was found to be the most suitable method for the classification of spot welding processes.

Process identification is needed to be able to utilise information collected from previously run processes to produce new welding spots of good quality. The characteristics of a sample from a new welding process can be compared to information collected from previously run processes to find a similar process. After that, the process parameters of the previous process already proven to lead to high-quality welding joints can be applied to the new process. With this approach, good welding results are achieved right from the beginning, and the time needed for the set-up of a new process can be significantly reduced. In addition, if a similar process is found, the quality control methods that proved viable for that process can also be used for the new process.

In the previous study by the authors, classification of welding processes was performed using altogether 54 distinctive features extracted from the signal curves recorded during welding. The aim of this study was to reduce the dimension of the feature space by eliminating features with less classification-relevant information and to consider the usefulness of the individual features. This was expected to cut down the time needed for classification and, most importantly, to further improve the classification accuracy. Various feature selection methods were tested to find the minimal feature set yielding good classification results.

Previously, feature selection in the field of spot welding has been studied by (Stoppiglia et al., 2003). In that study, however, only one process was considered at a time, and the study concentrated exclusively on nondestructive estimation of the diameter of the welding spot. The existing feature selection methods have been extensively reviewed in the studies (Dash and Liu, 1997) and (Kudo and Sklansky, 2000). Especially, in (Kudo and Sklansky, 2000) and (Jain and Zongker, 1997), the Sequential Floating Feature Selection methods used in this study have been shown effective and suitable for feature selection problems with the dimension of the feature data of the same magnitude as the data used in this study.

2 THE DATA

The data used in this study were supplied by two welding equipment manufacturers. There were altogether 20 processes, of which 11 had been welded at Harms+Wende GmbH & Co.KG and 9 at Stanz-

biegetechnik. A total of 3879 welding experiments were covered. The experiments were done by welding two metal objects together using a resistance spot welding machine. Each of the observations contained measurements of current and voltage signals recorded during welding.

The raw signal curves contained plenty of oscillatory motion and a pre-heating section, and they were therefore pre-processed. The pre-heating parts of the curves were cut off, so that all that remained was the signal curves recorded during the actual welding phase. In addition, the curves were smoothed using the Reinsch algorithm (Reinsch, 1971). An example of a signal curve before and after pre-processing is shown in Figs. 1 a) and b).

3 THE FEATURES

Altogether 54 geometrical and statistical features were extracted from the two signal curves relating to a single welding experiment. The geometrical features were chosen to locate the transition points of the curves as precisely as possible. The statistical features included the median of the signal and the arithmetic means of the signal values calculated on four intervals based on the transition points. In addition, the signal curve was divided into ten intervals of equal length, and the means of the signal values within these intervals were used as features. There were altogether 12 geometrical and 15 statistical features extracted from both signal curves. The features are demonstrated in Figs. 2 a) and b).

In practice, it often happens that some of the geometrical features overlap, and that the overlapping features vary from one curve to another. However, this can also be regarded as a characteristic of the curve. In Fig. 2 a), all the geometrical features are demonstrated on an artificial curve simulating the real data. On this curve, the features do not overlap, but the curve is otherwise notably similar to genuine signal curves. Figure 2 b) shows an example of the features calculated on a real signal curve.

The ten means of a signal curve have earlier been used as features in the articles (Junno et al., 2004a), (Junno et al., 2004b), (Junno et al., 2005) and (Haapalainen et al., 2005). It has been discovered that they present the main characteristics and differences of the curves very well and are therefore suitable to be used in the quality control and identification of welding processes.

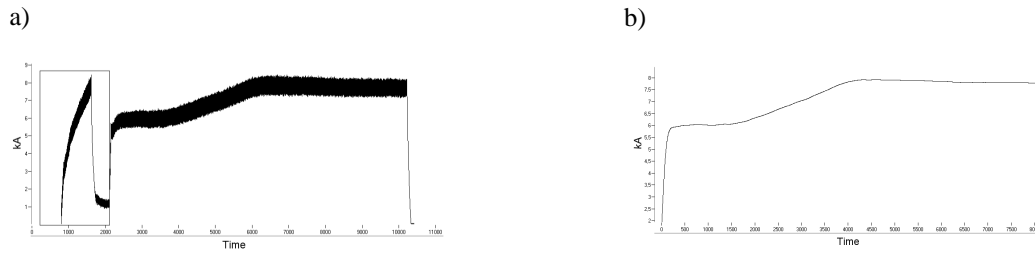


Figure 1: a) A raw signal curve. The pre-heating section is outlined with a rectangle. b) The same curve after pre-processing.

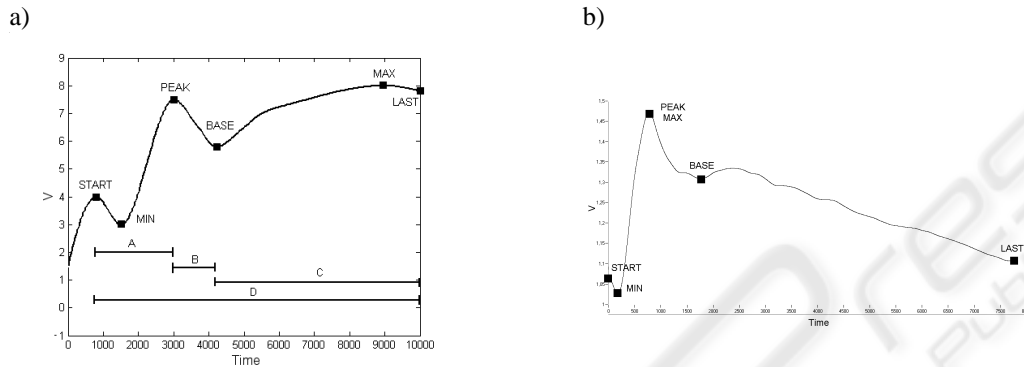


Figure 2: a) The geometrical features on an artificial voltage curve. The line segments A-D below the curve demonstrate the intervals based on the transition points on which means were calculated. b) An example of how the geometrical features often partially overlap in practice. On this voltage curve, the features named 'peak' and 'max' overlap.

4 FEATURE SELECTION

Of the classification methods evaluated in the previous article by the authors (Haapalainen et al., 2005), the k -nearest neighbour classifier proved to be optimal for the identification of spot welding processes. The parameter value $k = 3$ was selected based on the comparative study. The classification was performed using alternatively either all the 54 features extracted from the curves or only the ten mean values calculated on both signal curves (altogether 20 features). The best results were obtained using the ten means. In that case, a classification accuracy of 98.53 percent was obtained, while the classification based on all the 54 features yielded notably inferior results with a classification accuracy of only 84.13 percent.

Although good classification results were obtained using the ten means as features, there was still an interest to study the usability of the other features. Also, the amount of classification-related information carried by each of the ten means was unknown. Therefore, various feature selection methods were applied to the entire feature set to find the optimal feature subset to be used in classification. It was studied whether classification accuracy could be further improved by discarding redundant features. Since dimension reduction of the feature set also reduces the computational time required for classification, a minimal sub-

set was searched for.

Five different feature selection methods were tested: *Sequential Forward Selection* (SFS), *Sequential Backward Selection* (SBS), *Sequential Forward Floating Selection* (SFFS), *Sequential Backward Floating Selection* (SBFS) and *n Best Features Selection*.

SFS is a simple bottom-up search procedure in which one feature at a time is added to the current feature set. At each stage, the feature to be included is selected from the set of remaining available features, so that the new extended feature set yields a maximum value of the criterion function used (Devijver and Kittler, 1982). The SBS method is the top-down counterpart of the SFS algorithm.

The Floating Forward and Backward Feature Selection methods, SFFS and SBFS, introduced in (Pudil et al., 1994), are based on the *plus l-take away r* method (Stearns, 1976), in which the feature set is alternately enlarged by l features using the SFS method and reduced by discarding r features applying the SBS algorithm. In the Floating Feature Selection methods, however, the number of forward and backward steps is dynamically controlled instead of being fixed in advance. The conditional inclusion and exclusion of features is controlled by the value of the criterion function. In the bottom-up algorithm, SFFS, after each forward step, a number of backward steps

are applied as long as the resulting subsets yield better values of the criterion function than the previously evaluated ones of the same dimension. In the top-down counterpart, SBFS, an exclusion of a feature is followed by a series of successive conditional inclusions if an improvement to the previous sets can be made. The feature to be included into the current feature set or excluded from it is always the one that improves the set most or degrades the value of the criterion function least (Pudil et al., 1994).

The n Best Features Selection method simply means selection of the n individually best features in the sense of maximizing the criterion function. It is the simplest alternative for feature subset selection, but also the most unreliable since the features may correlate with each other. Therefore, it was only used for comparison in this study.

The best possible way to design the process identification system would have been to select the feature set and the classification method used simultaneously. However, because the k NN classifier had previously been found suitable for the process identification task (Haapalainen et al., 2005), the effectiveness of the different feature subsets produced by the feature selection methods were evaluated using the classification accuracy of the $3NN$ classifier as the criterion function. In addition, the k -nearest neighbour method has been used to measure the goodness of a feature set also in the studies (Jain and Zongker, 1997) and (Kudo and Sklansky, 2000).

The SFS, SBS and n Best Features methods were selected to be used in this study because of their easy application and relatively short calculation time. Compared to the basic sequential feature selection methods, the main advantage of the floating methods is that the resulting feature sets of different dimensions are not necessarily nested, as in the case of the SFS and SBS methods. This is because the floating methods are able to correct the erroneous decisions made at the previous steps of the algorithm. Therefore, these methods provide a close to optimal solution to the problem of feature subset selection (Pudil et al., 1994). Because of this characteristic, they are also highly applicable to problems involving nonmonotonic feature selection criterion functions, which was the case in this study. In addition, even though the floating feature selection methods are only nearly optimal, they are much faster than the optimal but computationally prohibitive *Branch and Bound* algorithm (Narendra and Fukunaga, 1977).

In order to evaluate classification accuracy when using different feature sets, the data were divided into training and test data sets, which consisted of 2/3 and 1/3 of the data, respectively. The training data set was used to train the $3NN$ classifier, and the test data set was used to evaluate the classification accuracy.

5 RESULTS

The best possible feature subsets for maximizing the $3NN$ classifiers classification accuracy were searched for. The feature selection methods were applied to both the original and a normalized feature set. The latter was formed by normalizing the feature values of the original feature set to have an average of zero and a standard deviation of one. The results of the classification using feature subsets constructed by the various feature selection methods are presented in Tables 1 a) and b).

The tables show the best classification accuracy obtained using feature sets formed by each of the feature selection methods. The feature subsets of all dimensions between 1 and 54 (dimension of the original feature set) were formed with each of the feature selection methods. Classification using each of these sets was performed, and the best classification accuracy obtained was recorded in the tables. The percentages in the middle row indicate the ratios of correctly classified processes and the numbers in the bottom row stand for the dimension of the feature set used in classification. It should be noted that the best feature subsets produced by the different feature selection methods are composed of unequal numbers of features.

The classification results of feature subsets formed from the unnormalized features are presented in Table 1 a), and the results of the subsets constructed from the normalized features are shown in Table 1 b). It can be seen that the subsets of the set of normalized features are notably larger than the subsets of the set of original features. However, the dimensions and classification accuracies of the different feature subsets are difficult to compare since only the subsets yielding the best classification results were considered at this point. Only the backward methods, SBS and SBFS, seem to yield better feature subsets when applied to normalized data. Nevertheless, the dimensions of these sets, 17 and 29, are much larger than those of the subsets formed from the unnormalized feature data, which are both of dimension 7. For comparison, it can be studied what the classification accuracies would be for smaller subsets of the set of normalized features formed with the backward methods. These results are presented in Table 2. It can be seen that quite good classification results are also obtained by using the smaller feature sets. However, these results do not compare with the classification results of the subsets produced from the unnormalized feature set by the forward methods, SFS and SFFS.

From the point of view of this study, it was considered more important to find a moderately small feature set that yields excellent classification results than to reduce the dimension of the feature set used to the absolute minimum. It can be stated, however, that the best classification results are obtained with small fea-

Table 1: Classification results of the 3NN classifier using different feature subsets formed by the feature selection methods together with the number of features included in each feature set. a) Subsets formed from the original feature set. b) Subsets formed from normalized feature data.

a)	Feature selection method	SFS	SBS	FFFS	SBFS	nBEST
	Classification accuracy	98.92	84.67	99.30	84.75	95.28
	Number of features used	6	7	11	7	10
b)	Feature selection method	SFS	SBS	FFFS	SBFS	nBEST
	Classification accuracy	98.30	97.14	98.45	97.45	95.12
	Number of features used	18	17	19	29	52

Table 2: Classification accuracies of subsets of different dimensions formed by the SBS and SBFS methods from the normalized feature set.

Method/Dim.	6	7	8	10	15	20
SBS	95.74	96.28	96.44	96.83	96.75	97.06
SBFS	95.67	96.21	96.52	96.90	97.14	97.21

ture subsets formed from the original feature set. The best of all feature subset with a classification accuracy of 99.30 percent was produced by the SFFS method. The dimension of this set was 11. The SFS method also yielded a feature subset with almost equally good classification accuracy of 98.92 percent. And what is remarkable about this result is that this set consists of only 6 features.

The observation that, in general, the subsets generated from the set of original features yield better classification results than the subsets formed from the normalized data alludes that the measurements of current contain more information related to process identification than the measurements made of voltage. This is because the original range of current measurement values was wider than the range of voltage values. Therefore, in the case of the original data, the features extracted from the current signals affect the classification more than the features calculated from the voltage signals. Since the influence of the two signals is equalized in normalized data, this implies that the features calculated from current signals are more significant to process identification than the features extracted from the voltage signals. From experience, however, it is known that only a rough classification of welding processes can be made based on the current signals alone, and the information carried by the voltage signals is also needed to get more precise results.

The significance of the features extracted from the current signals can also be established by comparing the amount of classification-related information contained in each of the features individually. Table 3 a) presents the 20 individually best features of the normalized feature set. The column in the middle shows the accuracy of classification based on only one feature. The classification results of the feature subsets formed with the n Best Features Selection method are

presented in the column on the right. It can be seen that all the 20 individually best features are extracted from the current curves. (The first feature extracted from voltage signals would be the 22th on this list.) However, the individual goodness of the features is not a sufficient criterion for feature selection since the features may correlate with each other. Because of this, the feature subsets produced by the n Best Features Selection method are generally inferior to the subsets formed by the other methods. The best subset formed from the normalized feature set yielded a classification accuracy of 95.12 percent, and the subset consisting of unnormalized features yielded an accuracy of 95.28 percent as seen in Table 1.

It should also be noted in Table 3 that all of the ten means calculated on the current signal (called interval means) are among the 18 individually best features. After this, it only seems logical that remarkably better classification results were obtained in the previous study using a feature subset consisting of the ten means than using the entire feature set in classification.

In Table 4, the features selected by the SFS, SFFS and n Best Features Selection methods are presented. These feature subsets of the dimensions 6, 7 and 10 were formed from the unnormalized feature set. It can be seen that several of the features have been selected by two or all three of the methods. Again, the ten means are well represented in the set of features selected. It should also be noted that the SFS and SFFS methods have selected approximately evenly features extracted from the current and the voltage signals. As the best classification results are obtained using feature subsets formed by these methods, it can be concluded that the use of features extracted from both the signals is necessary to obtain excellent classification results.

Table 3: The 20 individually best features of the normalized feature set. A *c* at the end of a feature name means that the feature has been extracted from the current signal, while a *v* stands for voltage signal.

Feature	%	n
median_c	72.45	72.45
start_value_c	72.29	89.47
mean_C_c	71.67	90.40
interval_mean_5_c	71.36	92.57
mean_D_c	69.51	92.57
interval_mean_6_c	69.20	92.26
interval_mean_4_c	68.65	92.57
interval_mean_2_c	68.50	94.58
interval_mean_7_c	68.19	94.74
mean_A_c	66.33	94.97
interval_mean_8_c	65.87	94.58
interval_mean_9_c	65.71	94.50
interval_mean_10_c	64.94	94.35
interval_mean_3_c	64.63	94.43
peak_value_c	62.38	94.50
mean_B_c	61.84	94.50
max_value_c	61.77	93.96
interval_mean_1_c	61.53	94.43
last_value_c	60.06	94.81
min_value_c	59.68	94.66

6 CONCLUSION

In this study, various feature selection methods were discussed with an aim to improve the performance of a spot welding process identification system. The methods were applied to a set of features extracted from current and voltage signals recorded during welding. The classification accuracy of the 3NN classifier found suitable for the process identification task in a previous study was used as the criterion function for the feature subsets produced by the methods. Altogether five different feature selection methods were tested on both the original and a normalized feature set. These methods were the *Sequential Forward Selection* (SFS), the *Sequential Backward Selection* (SBS), the *Sequential Forward Floating Selection* (SFFS), the *Sequential Backward Floating Selection* (SBFS) and the *n Best Features Selection*. In general, the subsets generated from the set of original features yielded better classification results than the subsets formed from the normalized data.

It was discovered that classification accuracy can be improved from the 84.13 percent obtained previously to 99.30 percent simultaneously reducing the dimension of the feature set from 54 to 11. This reduction in the feature set size facilitates both the extraction of features and the actual process identification. The best feature subset (classification accuracy of 99.30 percent) was obtained using the SFFS

Table 4: The features selected by the SFS, SFFS and n Best Features Selection method from the original feature set.

Feature	SFS	SFFS	nB
start_value_c	x	x	x
interval_mean_2_c	x	x	x
interval_mean_1_v	x	x	
interval_mean_5_v	x	x	
median_c	x		x
interval_mean_5_c		x	x
interval_mean_6_c		x	x
interval_mean_10_v	x		
last_value_v		x	
peak_value_v		x	
median_v		x	
interval_mean_3_v		x	
interval_mean_6_v		x	
mean_A_c			x
mean_C_c			x
mean_D_c			x
interval_mean_4_c			x
interval_mean_7_c			x

method. The feature subset produced by the SFS method also yielded a very good classification result. The classification accuracy obtained using this set was 98.92 percent. And what is most important about this result is that the dimension of this set was notably smaller than the dimension of the set produced by the SFFS method being only 6. Hence, it was shown, that the dimension of the feature subset used in classification can be significantly reduced and the performance of the spot welding process identification system notably improved.

By considering the amount of classification-related information contained in each of the features individually, it was confirmed that the ten means calculated on intervals of equal length of a signal curve are indeed very good features to be used in classification. In addition, it was discovered that the features extracted from current signals contain more information related to process identification than those calculated from voltage signals. Nevertheless, the use of both of these is necessary to obtain excellent classification results.

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