

# TABU SEARCH STRATEGIES IN SCHEDULING PROBLEM IN FLEXIBLE MANUFACTURING SYSTEM

## *Considering tool switches and number of setups*

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Abstract: In this paper it's investigated the impact of the Tabu List size, neighborhood generation approach and the managing of the decision variables of the Objective Function in the quality of a Tabu Search solution to the Scheduling Problem applied to a Flexible Manufacturing System. It was used a Part Scheduling Model, which starts with qualitatively different initial solutions that yields experiments in which it's observed the Tabu List size influence in the results quality, according to the pre-defined Objective Function variables contribution. This Model creates a schedule in a Flexible Manufacturing System, considering resident tooling concepts, production turns, Part Selection, Machine Magazine Constraints and Due-dates. Numerical results show relations among neighborhood strategies and the Tabu List size behavior considering initial solutions and contribution managing of the Objective Function variables.

## 1 INTRODUCTION

In this paper the impact of the *Tabu List* size is analyzed in the solution's quality in the Scheduling Problem applied to a Flexible Manufacturing System (FMS). Its considered initials solutions approaches, neighborhood generation and the managing of the decision variables of a Objective Function. In order to do so, two classic problems are studied: the Part Selection Problem and the Scheduling Problem.

The FMS is the highest degree in automation of a manufacturing system (Kaighobadi and Venkatech, 1993). Among several definitions, it can be said the FMS possesses high degree of distributed data processing and automated material flow, using computer-controlled CNC/DNC machines, assembly cells, robots and inspection machines (Dorf and Kusiak, 1994; Kusiak, 1992).

The studied problems are solved with Cluster Analysis techniques (Kusiak and Chow, 1986), Dispatching rules (Kusiak, 1992) and Tabu Search (Glover and Laguna, 1997).

Based in these techniques, a Part Scheduling Model was developed, with which experiments were accomplished.

The Problems and the contemplated techniques are presented in the section 2. In the section 3 it is described the Part Scheduling Model. The

accomplished experiments are described in section 4 and the conclusions are showed section 5.

## 2 PROBLEMS AND TECHNIQUES CONTEMPLATED

The Part Selection Problem can be defined as a technique in which similar parts are grouped according to similar attributes of design and production processes (Groover, 2001), respecting environmental and machining constraints (Kusiak and Chow, 1986; Bedworth *et al.*, 1991). Similar parts are grouped in Part Families, where each Part Family possesses similar design/process characteristics. In this work, the type of tool that processes a part is the attribute used to generate the Part Families (*PF*).

To solve this problem it's used a Part Selection Model (Rodrigues *et al.*, 1999) which is based in the Cluster Identification Algorithm created by Kusiak and Chow (Gómez, 1993). This model uses a binary part-tool incidence matrix formulation to create *PFs* and considers the tool sharing among *PFs* (Gómez, 1993). For the model's performance improvement, dynamic programming approach was used.

The Scheduling Problem (Kusiak and Chow, 1986) can be defined in scheduling parts in processing machines respecting its due dates. Other objectives can be considered, such as minimizing throughput, minimizing work in process and so on (Kusiak and Chow, 1986). In this paper, the Scheduling Problem approach concerns to the production batch processing time reduction, through the minimization of the number of machine stops for tool switching (*setup*). The schedule generated should respect the production turn time, or, it cannot have in processing

without improvement occurrence in the best solution found (*nbmax*) (Glover,1989; Gómez et al,2002).

### 3 MODEL ARCHITECTURE

The Part Scheduling Model (Gómez et al,2002) deals to generate a schedule of a part set in a flexible machine (Hwang e Shogan, 1987) considering productions turns, minimizing the setup number.

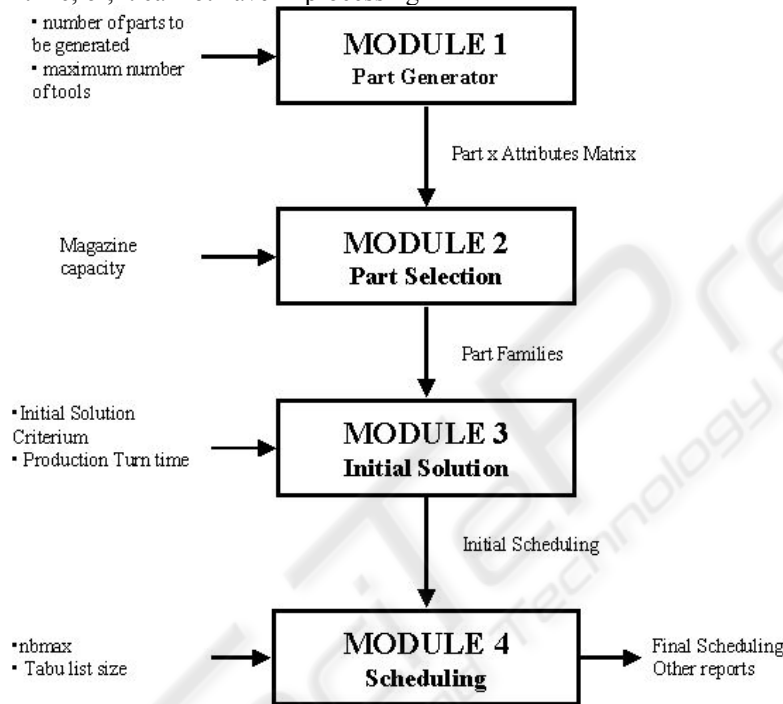


Figure 1: Part Scheduling Model architecture.

after the end of each turn.

To solve the Scheduling Problem, a Tabu Search approach was proposed (Hertz, 1991; Glover, 1989). This technique has been applied in combinatorial optimisation problems, such as Travel Salesman Problem, Time Tabling Problem, Job Shop Scheduling Problem (Hertz, 1991; Glover, 1989; Widmer, 1991). Tabu Search deals to find a better solution exploring the feasible solution space. Starting with an initial solution, Tabu Search successively generates a set of feasible solutions by well-defined moves approaches, in which a local optimal is found. This local optimal becomes the starting point for a new iteration. Among the iterations, the best result found is stored. Each move that leads to a local optimal is stored in a circular list of forbidden (or tabu) moves, called *Tabu List*. The stop criterion is defined as a number of interactions

The model's representation is showed in Figure 1.

Each module in Figure 1 represents a specialized algorithm and the flow among the modules shows the execution sequence. The modules are described following:

*Part Generator Module*: this module creates data for experiments. These data are part-tool incidence matrixes, which are the Part Selection Module input.

*Part Selection Module*: it applies the Part Selection Algorithm (Kusiak e Chow,1986) in the parts that it receive as input. These parts are grouped in *PFs* according to the tool-type (Rodrigues and Gómez, 2000), taking in account the tool sharing among *PFs*. An example of *PF* generation is shown in the Figure 2;

*Dispatching Rules Module*: starting with a set of parts grouped in *PFs*, this module generates a initial scheduling of parts in the machine based in the following criterions: Random, Part Family Sorting,

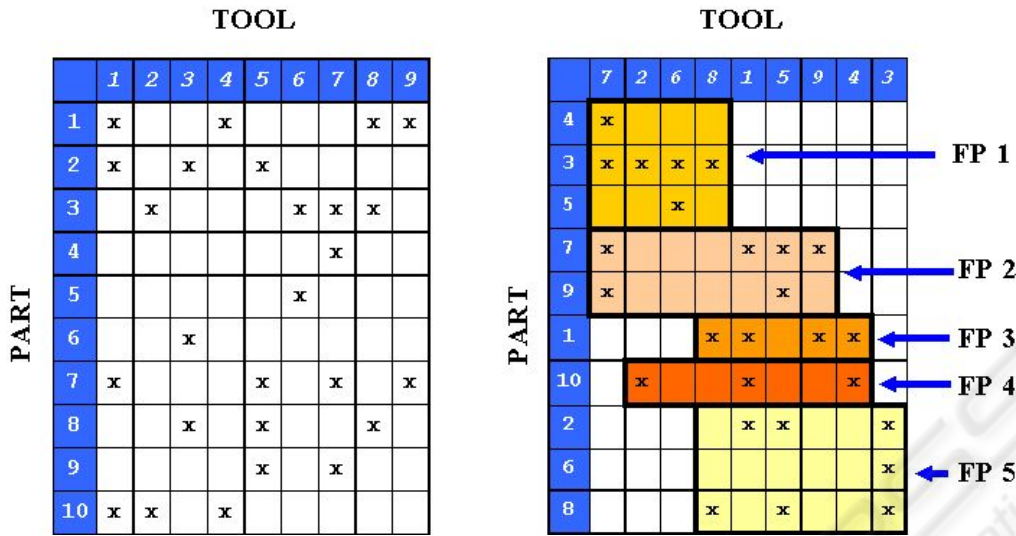


Figure 2: Part-tool incidence Matrix and Part Selection.

Most dissimilar Resources, Most Similar Family Resources and Larger Process-time First (Gómez et al, 2002);

*Tabu Search Module:* starting with a initial solution, the Tabu Search Algorithm generates a schedule that reduces the production time through minimizing the number of setups and the number of tool switches. Its considered part batching and production turn time. The Objective Function considered is the following:

$$\min f(x) = \sum_{i=1}^{n-1} TSwt_i + \sum_{i=1}^{n-1} Set_i + \sum_{i=1}^n BTime_i$$

Where:

- $TSwt_i$ : tool switches in batch  $i$ ;
- $Set_i$  : number of setups;
- $BTime_i$ : processing time of the batch  $i$ ;
- $n$  = total of batches;

The neighborhood generation approaches considered are *batch swap* (where the two batches are shifted from its turns) and *batch insertion* (where a batch is removed from its turn and inserted into another) (Rodrigues and Gómez, 2001). The Tabu Search Algorithm implemented is shown following.

```

Begin
  Initialise TList empty;
  Initialise niter;
  Initialise biter;
  Initialise nbmax;

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Load Initial Solution s;
Upload bs with init;

While (niter - biter < nbmax) do
  Generate neighborhood V(s)
  starting with s;
  Calculate F(s) for each s
  generated;
  Find s* of V(s) that minimizes
  F(s);
  If (s* is not in TList) then
    Bs = s*;
    Biter = niter;
  End_if
  s = s*;
  increment niter;
End_while;
End

```

- Where:
- TList: tabu list;
  - Niter: iteration counter;
  - Bs: best solution found;
  - Biter: iteration when a better solution was found;
  - Nbmax: number of iterations with no improvement of bs;
  - F(s) parts processing time calculus;
  - V(s): neighborhood of solutions;
  - s: a solution in V;
  - s\*: better solution in V;

#### 4 EXPERIMENTS

The model's implementation was made in C++ language, using GCC compiler in a GNU-Linux operational system. A Pentium III 833Mhz 128MB RAM was used to perform the experiments batches. A experiment batch consists that follows: the Part Generator Module starts creating 10 par-tool incidence matrixes with 90 parts *versus* 10 tools dimension, respecting the 4 tools magazine constraints. Each one of the five dispatching rules receives as input the 10 matrixes and it generates a set of initial solutions. All those initial solutions are used by the Tabu Search Module, witch is executed considering independently the two neighborhood generation approaches and the *Tabu List* size variation. The *nbmax* number was set in 120 iterations without improvement in the global result and the *Tabu List* size were varied in 10, 50 and 100 positions. For each batch of experiments, the analysis of the number of tool switches and the number of setups is done separately.

In the following tables the statistics obtained with the experiments are presented. Those statistics are referring to the averages of setups number and tool switches number of the initial solutions (generated by Dispatching Rules) and final solutions (generated by Tabu Search) and to the variation of the *Tabu List* size. The tables 1,2 and 3 refer to the accomplished experiments being considered the number of setups and the tables 4, 5 and 6 consider the number of tool switches.

The initial solutions are shown briefly: RAN (Random Initial Solution), FAM (Part Family Initial Solution Based), PMSR (Part Family Most Similar Resources), MDR (Most Dissimilar Resources) and LPTF (Larger Process Time First).

Table abbreviations:

*istn* = number of tool switches of the initial solution;  
*fstn* = number of tool switches of the final solution;  
*issn* = number of setups of the initial solution;  
*fssn* = number of setups of the final solution;  
*std* = stander deviation;

Table 1: Average of the initial and final number of setups and number of tool switches for the dispatching rules, with Tabu List size set in 10 position and considering only the machine setup.

	Initial Solutions				Batch swap				Batch insertion			
	Istn	std	issn	std	fstn	std	fssn	std	fstn	std	fssn	std
FAM	40,4	4,22	21,9	2,23	39,8	4,92	20,2	2,66	39,8	4,92	20,2	2,66
LPTF	198,1	13,16	82,9	2,47	53,1	7,74	21,3	2,75	51,5	6,82	20,6	2,72
MDR	214,5	15,57	86,6	1,17	50,2	6,46	21,2	3,01	49,2	8,79	19,7	3,02
PMSR	28,1	2,64	20,5	2,55	27,9	3,21	19,6	3,03	27,7	3,40	19,7	2,98
RAN	200,5	13,54	77,7	20,39	51,1	5,86	20,8	2,57	50	8,26	20,1	2,77

Table 2: Average of the initial and final number of setups and number of tool switches for the dispatching rules, with Tabu List size set in 50 position and considering only the machine setup.

	Initial Solutions				Batch swap				Batch insertion			
	Istn	std	issn	std	fstn	Std	fssn	std	fstn	std	fssn	std
FAM	40,4	4,22	21,9	2,23	39,5	5,05	19,8	2,74	39,8	4,92	20,2	2,66
LPTF	198,1	13,16	82,9	2,47	52,4	8,22	20,8	2,90	50,8	7,21	20,4	2,59
MDR	214,5	15,57	86,6	1,17	50,1	6,38	21,1	2,96	49	8,87	19,6	3,03
PMSR	28,1	2,64	20,5	2,55	27,9	3,21	19,6	3,03	27,7	3,40	19,7	2,98
RAN	200,5	13,54	77,7	20,39	49,6	8,47	20,5	2,59	49,8	8,07	20	2,62

Table 3: Average of the initial and final number of setups and number of tool switches for the dispatching rules, with Tabu List size set in 100 position and considering only the machine setup.

	Initial Solutions				Batch swap				Batch insertion			
	Istn	std	issn	std	fstn	std	fssn	std	fstn	std	fssn	std
FAM	40,4	4,22	21,9	2,23	39,5	4,99	20	2,75	39,8	4,92	39,8	4,92
LPTF	198,1	13,16	82,9	2,47	52,4	8,13	20,7	2,83	50,8	7,21	50,8	7,21
MDR	214,5	15,57	86,6	1,17	50,1	6,38	21,1	2,96	49	8,87	49	3,03
PMSR	28,1	2,64	20,5	2,55	27,9	3,21	19,6	3,03	27,9	3,40	27,9	3,35
RAN	200,5	13,54	77,7	20,39	49,6	8,47	20,4	2,67	49,8	8,07	49,8	2,62

Table 4: Average of the initial and final number of setups and number of tool switches for the dispatching rules, with Tabu List size set in 10 position and considering only the tool switches.

	Initial Solutions				Batch swap				Batch insertion			
	istn	std	issn	std	fstn	Std	fssn	std	fstn	std	fssn	std
FAM	40,4	4,22	21,9	2,23	34,8	3,77	20	2,79	32,7	2,31	20,1	2,69
LPTF	198,1	50,41	82,9	2,47	40,8	7,83	23,1	5,00	32,3	2,11	20,4	2,41
MDR	214,5	15,57	86,6	1,17	38,7	3,92	22,2	3,16	32,3	2,58	20,2	2,86
PMSR	28,1	2,64	20,5	2,55	26,9	3,11	19,8	2,86	26,6	2,88	19,6	3,03
RAN	200,5	13,54	84	2,21	41,1	7,02	22,5	3,72	33,6	2,55	20,2	2,82

Table 5: Average of the initial and final number of setups and number of tool switches for the dispatching rules, with Tabu List size set in 50 position and considering only the tool switches.

	Initial Solutions				Batch swap				Batch insertion			
	istn	std	issn	std	fstn	std	fssn	std	fstn	std	fssn	std
FAM	40,4	4,22	21,9	2,23	34,1	3,45	20	2,79	31,5	2,59	19,9	2,69
LPTF	198,1	50,41	82,9	2,47	37,9	5,09	21,6	2,80	31,9	2,56	20,1	2,81
MDR	214,5	15,57	86,6	1,17	37,7	4,06	21,7	3,16	30,7	2,91	19,7	2,98
PMSR	28,1	2,64	20,5	2,55	26,9	3,11	19,8	2,86	26,3	2,87	19,6	3,03
RAN	200,5	13,54	84	2,21	37,8	6,11	21,3	2,75	33	2,49	20,2	2,82

Table 6: Average of the initial and final number of setups and number of tool switches for the dispatching rules, with Tabu List size set in 100 position and considering only the tool switches.

	Initial Solutions				Batch swap				Batch insertion			
	Istn	std	issn	std	fstn	std	fssn	std	fstn	std	fssn	std
FAM	40,4	4,22	21,9	2,23	34,2	3,46	20	2,79	30,9	3,28	19,9	2,69
LPTF	198,1	50,41	82,9	2,47	37,1	3,51	21,2	2,44	31,8	2,57	20,1	2,81
MDR	214,5	15,57	86,6	1,17	37,4	4,01	21,3	3,16	31	2,49	19,8	2,82
PMSR	28,1	2,64	20,5	2,55	26,9	3,11	19,7	2,98	26,7	3,23	20,3	3,40
RAN	200,5	13,54	84	2,21	37,9	7,19	21,1	2,69	33,2	2,49	20,2	2,82

Can be noticed in these experiments that the approach of neighborhood generation based on *batch insertion* moves promotes a better Tabu Search performance compared to the approach *batch swap* based. That is due to the fact the move type accomplished in the *batch insertion* generates a richer neighborhood than the one generated by *batch swap* approach, taking to a better result. The *batch insertion* approach needs a larger number of moves to find a qualitatively superior result (according to the number of tool switches) to the result found by *batch swap* approach (Rodrigues and Gómez, 2001). For the Dispatching rules RAN, MDR and LPTF, which generate worse initial solutions, the increase of the *Tabu List* size has positive impact in the Tabu Search performance, therefore it extends the search in the solutions space.

The initial solutions approaches that present better results were the PMSR and FAM, which as it can be seen in previous works (Gómez et al,2002). The *Tabu List* size increasing did not bring significant performance improvements in Tabu Search that have as initial solutions those approaches, independent of used neighborhood generation approach. Those Dispatching Rules generate a result very close to the better solution, so the necessary number of iterations to find it becomes smaller. To the Dispatching rules RAN, MDR and LPTF, which generates worse initial schedules (faraway from the better solution), the increase of the *Tabu List* has a positive impact, therefore it extends the search, escaping from local optima.

It is also noticed in the experiments that the contribution of the decision variable of the Objective Function *tool switches* is more significant in the reduction of the batch processing time, generating better results than the ones generated for the setups number variable contribution. The variable change of tools considers the resource sharing among *PFs*, factor that relieve in the setup time reduction, assuring better solutions.

## 5 CONCLUSIONS

In this paper it was developed a Part Scheduling Model in which it was observed the *Tabu List* size variation and its influence in the Tabu Search performance. In the Tabu Search Algorithm, two approaches of neighborhood generation were used: (the *batch insertion* and the *batch swap* approaches). The initial solutions were based in five Dispatching rules (RAN, MDR, PMSR, FAM, LPTF). In the accomplished experiments, the *Tabu List* size was varied.

It could be observed that the *batch insertion* approach promotes better Tabu Search Performance due to generation of a richer neighborhood in comparison to the *batch swap* approach. That leads to a larger number of iterations to find the better result. The *Tabu List* variation has positive impact in the *batch swap* approach, doing with its performance went as good as the one of the *batch insertion* approach.

The initial solutions that more contribute to the Tabu Search performance improvement are PMSR and FAM, therefore these rules take into account the resource sharing among *PFs*. The *Tabu List* size variation has positive impact in dispatching rules that generates worse initial solutions (RAN, MRD, LPTF), because with the search diversification, a larger number of solutions in the neighborhood is visited, escaping of the local optimum.

To solve the Scheduling Problem, can be opted by the use of a more flexible approach of neighborhood generation (*batch insertion* approach), having as initial solution a Dispatching Rule that takes into account the resource sharing among *PFs* (PMSR and FAM), which is important factor for the batch processing time minimization. The *batch swap* approach needs a larger number of iterations to reach a better result like the one found by the *batch insertion* approach. To this approach, the *Tabu List* would not need to store a larger number of forbidden moves.

In case the approach of neighborhood generation cannot be flexible and the initial solution cannot take into account the resource sharing, a larger *Tabu List* will act diversifying the space search, leading to a better result.

## REFERENCES

- Bedworth, D. D., Henderson, M. R., Wolfe, P.M., 1991. *Computer Integrated Design and Manufacturing*, McGraw-Hill.
- Dorf, R., Kusiak, A., 1994. *Handbook of Design, Manufacturing and Automation*, John Wiley and Sons.
- Glover, F., 1989. Tabu Search: Part I, ORSA Journal of Computing.
- Glover, F., Laguna, M., 1997. *Tabu Search*, Kluwer Academic, Boston.
- Gómez, A. T., 1993. Aplicação de Otimização Combinatória em Sistemas de Manufatura Flexíveis, INPE, São Paulo, Brazil.
- Gómez, A. T., Rodrigues, A. G., Hoffmann, L. T., 2002. Análise da Performance de um Modelo de Escalonamento Baseado em Pesquisa Tabu aplicado a um Sistema de Manufatura Flexível. In *LAPTEC 2002, 3rd Congress of Logic Applied to Technology*.

- Hertz, A., 1991. Tabu Search for large Timetabling Problems, *European Journal of Operational Research*.
- Kaighobadi, M., Venkatesh, K., 1993. Flexible Manufacturing Systems: An Overview, *International Journal of Operations & Production Management*.
- Kusiak, A., Chow, W. S., 1986. Efficient Solving of Group Technology Problem, University of Manitoba, Winnipeg.
- Kusiak, A., 1992. *Intelligent Design and Manufacturing*, John Wiley and Sons.
- Rodrigues, A. G., Araújo, R. S., 1999. Modelagem de Sistemas de Manufatura Flexíveis considerando restrições físicas e temporais. In *CRICTE'99, Congresso Regional de Iniciação Científica e Tecnológica em Engenharia*, Santa Maria, Rio Grande do Sul, Brazil.
- Rodrigues, A. G., Gómez, A. T., 2000. Utilização de metaheurísticas para a modelagem de Problemas de Seleção de Partes e Scheduling em um Sistema de Manufatura Flexível, *Scientia*, São Leopoldo, Rio Grande do Sul, Brazil.
- Rodrigues, A. G., Gómez, A. T., 2001. Utilização de Pesquisa Tabu no Escalonamento de um Sistema de Manufatura Flexível. In *CRICTE'2001, Congresso Regional de Iniciação Científica e Tecnológica em Engenharia*, Ijuí, Rio Grande do Sul, Brazil.
- Widmer, M., 1991. Job Shop Scheduling with Tooling Constraints: a Tabu Search Approach. *Journal of Manufacturing*.

