Geographical Self-Organizing Map Clustering in Large-Scale Urban Networks for Perimeter Control

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Abstract: Traffic congestion in urban areas presents a major challenge to efficient transportation systems. Recent advancements in traffic management provide promising solutions, with perimeter control emerging as a technique to tackle network-wide congestion. However, it is crucial to identify geographically connected homogeneously congested areas for effective implementation. This research explores the application of clustering techniques, particularly geographical self-organizing maps (GeoSOM), to identify spatially connected and homogeneously congested areas within transportation networks. While GeoSOM has found applications across various domains, its adaptation to transportation networks for congestion clustering is novel. This study introduces and implements an adaptation of the GeoSOM algorithm tailored for the large-scale urban environment of downtown Los Angeles. Its performance is assessed through a comparative evaluation with two other clustering algorithms, namely DBSCAN and K-means. The results demonstrate that GeoSOM surpasses other clustering algorithms, exhibiting improvements of up to 43% in traffic density variance, up to 61% in the spatial quantization error, and 15% in the quantization error. This finding demonstrates that the proposed clustering algorithm is effective in identifying a spatially homogeneous congested area within a large-scale transportation network.

1 INTRODUCTION

Traffic congestion has become a prevalent issue in many urban areas. Recent advances in traffic management and control techniques have proven effective in addressing this issue and increasing the efficiency of urban transport systems. Evaluating traffic congestion patterns across metropolitan road networks is critical for effective traffic management. This assessment allows researchers to accurately determine the operational status of network traffic, such as congested routes. Perimeter control is a promising technique for reducing traffic congestion across networks rather than considering individual routes (Bichiou et al., 2020). Identifying geographically connected homogeneously congested regions within transporta-

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referred to as self-organizing feature maps (SOFM), was introduced by Kohonen (Kohonen, 2013). SOM involves the mapping of an input space onto a lower-dimensional output space composed of units known as neurons, forming the basis of this idea. The input space’s topology is maintained by this mapping. This implies that neurons nearby are mapped to inputs nearby as well, and vice versa. Particularly in high-dimensional spaces, it is an extremely helpful tool for understanding the data structure (Pires et al., 2007). SOM is essentially a data-driven technique for data compression and dimensionality reduction. It is frequently utilized for data clustering and graph mining. Numerous applications use SOM including object recognition, learning a motion map, image segmentation, density modeling, gene expression analysis, object classification, skin detection, robot behavior learning, text mining, and information management (Le Thi and Nguyen, 2014).

Although SOM is extensively utilized in clustering tasks, it typically does not consider geographic location. In clustering geo-referenced data, Baccao et al. (Baçao et al., 2005) emphasized how crucial it is to take physical locations into account. “Everything is related to everything else, but near things are more related than distant things,” according to the first law of geography, which they referenced (Waters, 2017). This implies that even if two parts are identical in every other way, they shouldn’t be grouped if they are far apart geographically. To incorporate geographical features into the SOM clustering, two approaches were investigated by Baccao et al. With one approach, they added geographic coordinates to the input vectors and assigned them a high weight to indicate their significance. With the second approach they created a new architecture called Geographical SOM (GeoSOM) (Baçao et al., 2004).

SOM and GeoSOM are used in various clustering applications including forest management (Kim et al., 2023), illness spreading patterns (Melin et al., 2020), tourism patterns (Provenzano and Giambrone, 2023), and water quality studies (Feng et al., 2023). However, as far as we are aware, they have never been applied to transportation network clustering, where the deployment of traffic controllers to alleviate congestion requires spatially connected and homogeneously congested clusters.

Therefore, in this research, the objective is to identify a homogenously congested area using the GeoSOM algorithm within a large-scale network, specifically the Los Angeles (LA) downtown. Additionally, the effectiveness of the proposed GeoSOM algorithm will be evaluated through comparison with two well-known clustering algorithms, namely, DBSCAN and K-means (Wulandari et al., 2024).

The paper is structured as follows: Section 2 describes the GeoSOM algorithm. Section 3 presents the LA case study and the simulation configuration. Section 4 performs a sensitivity analysis of the GeoSOM algorithm to determine the best set of parameters. Section 5 evaluates the effectiveness of GeoSOM by comparing it to DBSCAN and K-means clustering algorithms. Finally, Section 6 discusses the conclusions drawn from the study and future work.

2 GeoSOM ALGORITHM

The SOM is a competitive learning-based artificial neural network (Kohonen, 2013). It operates by computing the degree of similarity between the weights of each neuron and the input vector. The neuron whose weights most closely resemble the input vector is designated as the winning neuron, often referred to as the best matching unit (BMU). Subsequently, the neighborhood of the winning neuron is adjusted closer to the input vector through the updating of neuron weights.

The primary distinction between GeoSOM and SOM lies in their two-stage BMU search process. In GeoSOM, a geographical BMU (geoBMU) is initially identified, where the search relies solely on the geographic locations of neurons (Baçao et al., 2004). The geoBMU is the neuron closest to the input vector in terms of geography. In the subsequent stage, non-geographical features are considered to select the final BMU, which is located within a defined radius (R) of the geoBMU. This radius, denoted as the geographical tolerance, limits the neighboring units within physical proximity to the input vector as the only contenders for becoming a BMU.

The set of N input vectors is represented as X. Each input vector X is structured as X = [xgeo, xatt], where xgeo represents the non-geographical attributes of the input, and xatt denotes the geographical coordinates. In our specific context, the non-geographical attribute refers to the densities (k) of roads, indicating the number of vehicles per unit distance and serving as a metric for road congestion.

Let G denote a grid consisting of Ngeo neurons with weights W, where W = [wgeo, watt] represents the weight of each neuron. Here, watt represents the non-geographical weights, while wgeo represents the geographical weights. Initially, W is randomly selected. The GeoSOM algorithm, outlined in Algorithm 1, comprises three stages:

- Competition. Neurons compete to determine the best matching unit (BMU), striving to be the clos-
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3 CASE STUDY: NETWORK DESCRIPTION AND SIMULATION SETUP

The real-life Los Angeles (LA) downtown network shown in Figure 1 is a large-scale network composed of 3,556 links (Abdelghaffar and Rakha, 2019). It is characterized by congested traffic, long travel times, and frequent delays. To alleviate the congestion, our ultimate goal is to apply the network perimeter control strategy in the congested region (Elouni et al., 2021). For the control system to function properly, the area where it will be implemented must exhibit homogeneous congestion. In other words, a densely homogeneous area that is geographically connected must be located. Therefore, the GeoSOM algorithm is deployed across the network, considering both the link densities and their geographic locations, to achieve this objective.

Throughout the simulation, the neuron weights are updated until they converge to a state where either the change becomes minimal or ceases altogether. Then, the distances between each neuron and its neighboring neurons are computed using the unified distance matrix, commonly referred to as the U-matrix (Hamel and Brown, 2011). Neurons are grouped into the same clusters when the distances between them are relatively small, while cluster boundaries are delineated by larger distances between neurons. To define a color code for each network link, the U-matrix results are projected and interpolated into the input space. Based on these colors, the clusters are then visually identified.

4 SENSITIVITY ANALYSIS

The objective of this research is to identify a heavily congested homogeneous area to manage congestion within it. In evaluating GeoSOM’s effectiveness, our emphasis was on identifying a specific area characterized by a high volume of vehicles, i.e., high traffic.
density. The peak density observed in the LA real traffic volume during rush hour is represented by the yellow zone in Figure 2.

GeoSOM operates on artificial neural networks and encompasses multiple parameters that necessitate fine-tuning. These parameters include the number of neurons, the learning rate, and geographical tolerance. The best configuration is determined through a sensitivity analysis, as presented below.

4.1 Number of Neurons

GeoSOM was executed with varying numbers of neurons, ranging from a $5 \times 5$ to a $25 \times 25$ grid, on the LA network. Figure 3 depicts three cases, corresponding to grid sizes of $5 \times 5$, $15 \times 15$, and $25 \times 25$, respectively, from left to right.

Figure 3a illustrates the neurons' grid at the end of the simulation, following Algorithm 1. Meanwhile, Figure 3b displays a color-coded interpolation of the neurons' weights onto the network links. Blue indicates similar densities among the links, implying they could potentially be clustered together, whereas yellow indicates a notable disparity in densities, implying they should not be clustered together. The leftmost plot in Figure 3a shows that the neurons did not adequately cover the map, implying that a $5 \times 5$ neuron configuration is inadequate. Furthermore, the outcome for the $25 \times 25$ neuron configuration, as depicted in Figure 3b, reveals that all the links are grouped into only a single large cluster. Therefore, $25 \times 25$ neurons are ineffective. Figure 3 shows that the best number of neurons is $15 \times 15$. The neuron grid efficiently covers the network, as evidenced by the middle plot in Figure 3a, and it also effectively achieves homogeneous clusters, as indicated by the dark blue color with clear light color boundaries in the middle plot of Figure 3b.

4.2 Learning Rate

In this section, various learning rates ($\alpha$) were experimented within the GeoSOM algorithm. As $\alpha$ falls between 0 and 1, the tested values ranged between 0.05 to 0.8. Figure 4 shows GeoSOM results for three different $\alpha$ values. It is evident that for small $\alpha$ values (e.g., $\alpha = 0.05$), the homogeneous regions, characterized by a dark blue color, are quite small, which may not be optimal for the control objective. Conversely, with a high $\alpha$ value (e.g., $\alpha = 0.8$), the network is consolidated into a single cluster. The best $\alpha$ value appears to be 0.4, where a well-defined homogeneous dark blue area is discernible with clear distinct borders, exhibited by yellow and green colors, making it more suitable for control purposes.

4.3 Geographical Tolerance

This section investigates the impact of geographical tolerance ($R$) on GeoSOM results, with low $R$ values indicating that geographical attributes are prioritized and higher $R$ values indicating a preference for non-geographical attributes over geography. The $R$ values tested with the GeoSOM algorithm ranged between 0 and 8.

Figure 5 illustrates that for $R = 0$, the clustering results did not yield a homogeneous dark blue area. As $R$ increases, the dark blue area expands. A well-defined cluster emerged when $R = 5$. However, as the geographical tolerance increases to $R = 8$, cluster borders start to blur, and all links are grouped into a single cluster.

4.4 Sensitivity Analysis Conclusion

The best configuration for the GeoSOM clustering algorithm is identified as $15 \times 15$ neurons, $\alpha = 0.4$, and $R = 5$. Within the various homogeneous areas depicted by the dark blue color in Figure 6, the area of primary interest is the one with the highest mean density, representing the most congested area, as illustrated in Figure 2, and depicted by the black contour in Figure 6.

5 COMPARING GeoSOM TO OTHER CLUSTERING ALGORITHMS

In this Section, the GeoSOM algorithm is compared with two other widely used clustering techniques: DBSCAN and K-means, to evaluate its performance.
While these two methods have been employed in the literature for clustering transport networks, they lack the explicit incorporation of geographical data, a feature inherent in GeoSOM (Lopez et al., 2017; Lin and Xu, 2020).

5.1 DBSCAN

The density-based spatial clustering algorithm (DBSCAN) (Sahu et al., 2023) clusters points based on their proximity to neighboring points. It relies on two key parameters: \( \epsilon \), representing the radius of a neigh-
Figure 6: GeoSOM cluster identification using best configuration.

Figure 7: K-distance graph for DBSCAN.

Figure 8: DBSCAN.

Figure 9: Calinski Harabasz for K-means.

The clustering outcomes are displayed in Figure 10, where cluster 12 corresponds to the most congested area, as inferred from the data presented in Figure 2.

5.2 K-Means

K-means is a clustering algorithm that partitions data points into \( k \) clusters and assigns each point to the cluster with the nearest mean. Often, it serves as a benchmark to assess the performance of other clustering algorithms (Lopez et al., 2017; Saeedmanesh and Geroliminis, 2016). Unlike DBSCAN, K-means only requires the determination of one parameter, which is the number of clusters.

The Calinski-Harabasz method (Aik et al., 2023) is employed to identify the best number of clusters. The results obtained using this method for \( k_m \) values ranging from 2 to 30 indicate that \( k_m = 12 \) is the best number of clusters, i.e., the maximum value in Figure 9.

5.3 Performance Metrics

To evaluate the performance of the GeoSOM algorithm, we compare it to the DBSCAN and K-means algorithms using the following metrics:

- **Quantization Error (QE):**
  
  \[
  QE = \frac{||k(cluster) - \bar{k}(cluster)||}{\text{length(cluster)}}
  \]
where $\bar{k}(cluster)$ represents the cluster’s mean density, and $\text{length}(cluster)$ represents the cluster’s number of elements.

- **Spatial Quantization Error (SQE):**
  \[
  \text{SQE} = \frac{||xy(cluster) - \bar{xy}(cluster)||}{\text{length}(cluster)}
  \]
  where $xy(cluster)$ represents the $x$ and $y$ coordinates of the cluster’s centre.

- **Density Variance (DV):** It refers to the density variance within the cluster, reflecting how much the densities of individual points within the cluster deviate from the mean density.

Table 1 illustrates the three performance metrics for the three clustering algorithms. The performance is improved when QE, SQE, and DV are minimized. Table 1 demonstrates that GeoSOM outperforms the other two algorithms.

<table>
<thead>
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<th></th>
<th>QE</th>
<th>SQE</th>
<th>DV</th>
</tr>
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<tbody>
<tr>
<td>DBSCAN</td>
<td>0.0396</td>
<td>0.0095</td>
<td>0.1241</td>
</tr>
<tr>
<td>K-means</td>
<td>0.0333</td>
<td>0.0055</td>
<td>0.1494</td>
</tr>
<tr>
<td>GeoSOM</td>
<td>0.0336</td>
<td>0.0037</td>
<td>0.0837</td>
</tr>
</tbody>
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Table 2 presents the percentage improvements of GeoSOM over DBSCAN and K-means across various performance metrics. The most significant enhancements are observed in SQE and DV, aligning with GeoSOM’s objectives of fostering spatially connected links within clusters (yielding the best SQE) and achieving clusters with minimal density variance.

<table>
<thead>
<tr>
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<th>GeoSOM over DBSCAN</th>
<th>GeoSOM over K-means</th>
</tr>
</thead>
<tbody>
<tr>
<td>QE</td>
<td>15.15</td>
<td>-0.9</td>
</tr>
<tr>
<td>SQE</td>
<td>61.05</td>
<td>32.72</td>
</tr>
<tr>
<td>DV</td>
<td>32.55</td>
<td>43.98</td>
</tr>
</tbody>
</table>

The results reveal that the GeoSOM approach successfully achieved the research goal of identifying highly congested and geographically compact clusters with low-density variance, surpassing DBSCAN and K-means with improvement percentages reaching up to 43% in DV, up to 61% in SQE, and up to 15% in QE. These findings could ultimately be used for the development of traffic control systems aimed at alleviating congestion within the network.

6 CONCLUSION

In this research, a novel clustering algorithm is proposed (GeoSOM) to identify densely congested and spatially compact areas within transportation networks. This study provides valuable insights for developing effective traffic control strategies to alleviate traffic congestion. The proposed clustering algorithm is evaluated on a large-scale urban network in downtown Los Angeles, and its performance is compared to two other clustering algorithms, namely: DBSCAN and K-means. The results demonstrated enhancements across all three performance metrics when using GeoSOM compared to DBSCAN and K-means. Specifically, there was a 15% reduction in the quantization error, a reduction of up to 43% in the traffic stream density variance within the cluster, and a reduction of up to 61% in the spatial quantization error. The results also demonstrate GeoSOM’s effectiveness in accurately delineating spatially homogeneous, congested areas within a large-scale network. This research establishes a framework for harnessing advanced clustering algorithms to tackle intricate traffic management challenges, thereby paving the way for more efficient urban mobility solutions. Future research will involve leveraging this study’s findings to develop network perimeter control strategies targeting congested areas to reduce congestion and improve the overall efficiency of urban transport systems.
ACKNOWLEDGEMENTS
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