

On Some Artificial Intelligence Methods in the V-Model of Model-Based Systems Engineering

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Abstract: The enhancement of the standard V-Model of Model-Based Systems Engineering (MBSE) with methods from Artificial Intelligence (AI) is currently in the research focus of many universities and engineering companies. In the need to find new means to deal with the steadily increasing complexity in modern systems engineering and design of complex systems, traditional MBSE methods, most notably the standard V-Model of MBSE, is a candidate to be enriched with several AI methods. The work presented summarizes the experience gained with several AI methods in a machine-executable version of the V-Model of MBSE based on an graph-based design language approach to design automation and tries to summarize the resulting shift in the engineering burden and effort as well as the observed gains in design time and quality. Based on the results from engineering practice and some theoretical foundations underlying engineering as a branch of the natural sciences per se, an outlook is attempted on some necessary aspects in future developments of AI for engineering applications.

1 ENGINEERING BACKGROUND

As necessary background knowledge and engineering context for the work presented hereafter, the standard V-Model of MBSE is shown in figure 1.

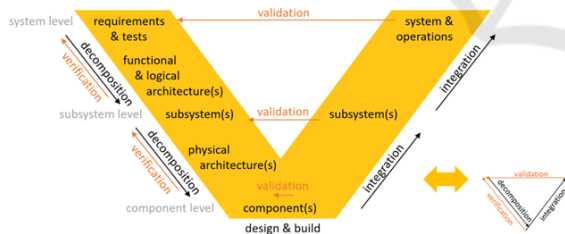


Figure 1: The standard-V-Model of MBSE.

The standard V-Model of MBSE starts on its left side with a three-fold mapping sequence of the design requirements onto the three intermediate design representations via a subsequent mapping of the requirements onto the functional system architecture model onto the logical system architecture model onto the physical system architecture model. At the end of this decomposition procedure, components design and build occurs and in the subsequent integration phase the components are integrated to system modules. Finally, the system modules are integrated to the system on the right side of the V-Model, according to the devised system architecture.

Dedicated procedures for verification and validation (V&V) intend hereby to guarantee in the V-model in figure 1 that the original system design intent is maintained (by selected verification methods, often by formalisms) and that the design requirements are met at the devised (sub-)system levels (by selected validation methods, often by simulation or experiment). Human systems engineering experts usually “know”¹ how to decompose, structure, manage and steer the flow of information of the dedicated design teams for subsystems, components, simulations and the like, as shown in figure 1. The underlying patterns of *decomposition and verification* and *decomposition, integration and validation* can hereby occur at various levels of detail, showing that the design process may be of fractal nature with repeating patterns at all relevant scales of detail.

Humans seem to have no general problem with the aforementioned, apparently weak scientific nature of *knowing*, since humans switch easily back and forth between textual, graphical and symbolical representations and their appropriate reasoning mechanisms. If

¹The scientific nature of this “*know(ing)*” is key to the application of AI methods to engineering, since this is not a pure, deductive process but resembles more an individual, intuitive search process. Mimicking this process later by AI methods seems thus straightforward and has led in the past to the famous paradigm “*design is search*” (Simon, 1969).

however a machine or an algorithm needs to mimic or replace these human capabilities, first an appropriate formalization step is mandatory. In this required formalization, an appropriate mathematical model which provides an adequate mapping of the real-world problem into a machine-readable form of representation² has to be provided.

1.1 Formalization of Data and Processes

To formalize an engineering problem mathematically, the concept of models and transformations between the models³ needs to be introduced. The models M_0 and M_N represent hereby a formal and machine-readable representation of an object or space. The transformation $T_{(0,N)}$ describes how the model M_0 is transformed into the model M_N , as shown in figure 2 (Hahn and Rudolph, 2023).

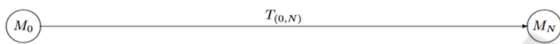


Figure 2: Definition of the model transformation $T_{(0,N)}$.

The transformation $T_{(0,N)}$ can be further splitted and decomposed into a sequence of smaller transformations $T_{(0,I)}$ and $T_{(I,N)}$ with $0 < I < N$. However, the smallest possible transformation is the transformation $T_{(I,I+1)}$ which transforms (i.e. modifies) at least one atomic element of the model representation M_I into M_{I+1} . An atomic element of a model is hereby a representational element which is not further decomposable in the chosen representation. The shown transformation $T_{(I,I+1)}$ corresponds to such a smallest possible level of detail of modification in the engineering model concept, as shown in figure 3 (Hahn and Rudolph, 2023).



Figure 3: Decomposition of $T_{(0,N)}$ down into $T_{(I,I+1)}$.

The digital modeling of engineering data and processes is therefore straightforward possible using the above introduced concept of models and transformations. As a first flavor how this is used in the following section to formalize the V-Model serves the following statement: Supposed M_0 in figure 2 represents the re-

²This formal representation needs to fulfill furthermore the “closed-world assumption”, in order to guarantee that the still unknown solution can be in fact found by a search procedure, leading otherwise the concept of the paradigm “design is search” ad absurdum (Simon, 1969).

³The terms *model*, *transformation* and later even *model transformation* are used in mathematics, engineering and computer science in slightly different settings. In this work it is taken special care to make clear in the context which of the multiple meanings is intended.

quirements model, and M_N represents the final product or system model, then the transformation $T_{(0,N)}$ represents the philosophy of *requirements-driven engineering*, stating that the final product M_N should be designed with the intention in mind to exactly fulfill the requirements M_0 .

In the sense of the research question of finding an adequate decomposition of meaningful transformations according to figure 3, a requirements-driven engineering means to find an explicit solution sequence of transformations which models the design process as a sequence of intermediate steps. In consequence, model transformations may therefore be few in numbers during the early concept design phase, during the later detailed design phase hundreds, thousands or even more model transformations maybe used to digitally encode the design process knowledge.

1.2 Digital Machine-Executable V-Model

All the engineering models and engineering tasks in the standard V-Model of MBSE shown in figure 1 can now be formalized as (sequences of) transformations which transform one state of a model into another. These transformations are ideally suited for such a formalisation, digital programming and, as a direct consequence, to obtain in consequence a machine-executable V-Model (Walter et al., 2019; Walter et al., 2018), of which the intermediate model states are shown in figure 4 (Hahn and Rudolph, 2023).

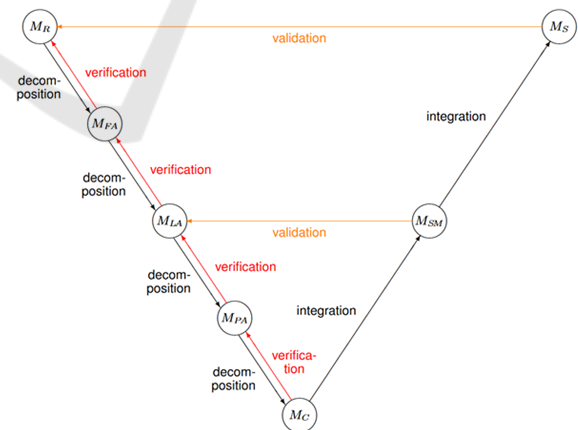


Figure 4: Digital machine-executable V-Model.

The legend for figure 4 is as follows: requirements model (M_R), functional architecture model (M_{FA}), logical architecture model (M_{LA}), physical architecture model (M_{PA}), component models (M_C), subsystem module models (M_{SM}) and system model (M_S), transformations shown as directed arrows.

1.3 Properties of Model Spaces

Two different digital and mathematical properties are most interestingly to note in the digital machine-executable V-Model shown in figure 4.

Firstly, the emphasis in the visual representation lies on the models, which are usually implemented as digital data structures in the form of linked data objects, lists, trees or graphs thereof. Figure 4 resembles therefore much of a static data flow graph visualization, which may be dynamically updated incrementally by the transformation $T_{I,J}$ with $(0 < I < J < N)$ from model M_I into the new model M_J .

Secondly, the different models M_I, M_J do not necessarily exist in the same model spaces. As mentioned in the introduction, humans are very good to mix or switch easily back and forth between textual, graphical and symbolical representations and their appropriate reasoning mechanisms. Usually algorithms don't possess this easiness of representation changes and must therefore specifically adapted to such different spaces. It is therefore important to check and know the different nature of model spaces involved when digitizing the V-Model.

From common general engineering experience, the following different spaces can be identified:

- **Verbal Spaces.**

Design requirements are either expressed in human languages textually or already expressed formally. In languages such as English and German, each noun (i.e. vocabulary defined in a dictionary) is the name of a concept. A mathematical formalization by means of formal concept analysis allows the formal definition of super- and sub-concepts as well as the formal definition of characteristic dependencies between the concepts expressed in the form of links.

The digital encoding of the concept properties in an object-oriented programming language (such as JAVA) or a modern visual modeling language (such as UML) yields an object-oriented model of that domain, i.e. an ontology. Using the aforementioned graph-based representation allows to model such domain ontologies by means of abstract nodes and specialized links.

- **Logical Spaces.**

Customers can typically choose from a huge variety of product options in order to configure their future product. These are often expressed as Boolean constraints and can be handled and processed efficiently by dedicated algorithms for specialized types of binary trees.

Again, the processed results can be represented in the form of abstract nodes with specialized links.

- **Real-valued Spaces.**

Mathematics, physics and most other natural sciences make heavy use of this space in which a large variety of functional relationships in the form of linear, nonlinear, integral, and differential equations etc. as well as even systems of such equations and many more other useful mathematical operands and operations exist. Fortunately, in this case the formalization in form of a formal language (i.e. mathematics itself) already exists and has led to the availability of many algorithms, toolboxes and solvers for processing typical (differential) equations and equation systems occurring in engineering (e.g., solvers for FEM, MBS, CFD, etc.).

Once again, the results can be represented in the form of abstract nodes with specialized links.

- **Functional, Logical, and Physical System Architecture Spaces.**

Many widely used engineering design methods, ranging from the more traditional systematic German design methodology (Pahl and Beitz, 1996) up to the more modern machine-executable V-Model of MBSE in figure 4, advice to map the design requirements subsequently via the intermediate design representations of the functional system architecture model to the logical system architecture design model to the physical system architecture design model.

Functional architecture representations are often represented as graphs and so are logical architectures in the form of block diagrams also representable as graphs. Physical architectures are typically represented in 3D metric spaces, often in the form of parametric CAD models, internally represented as graph-based data structures as well.

From the above analysis of the properties of the different spaces, it can be stated that a graph-based design representation is the common denominator to represent design information. Such graph-based representations are capable to model *parametrical as well as topological design information* in a *unified representation and graph transformation processing mechanisms*. The design information can come from various and heterogeneous spaces, with different levels of abstraction and detail. If such a generic graph-based data representation is freely accessible inside a performant digital modeling and processing framework and can be mapped to open standards (such as UML or SysML) in order to exchange information with other engineering modeling and analysis tools, this can be summarized as the key concept of *graph-based design languages* (Riestenpatt gen. Richter and Rudolph, 2019).

1.4 Graph-Based Design Languages

The core mechanism of graph-based design languages consists of the encoding of any engineering concept of interest as an abstract graph node and to express any existing dependencies or couplings, either disciplinary or multi-disciplinary, by dedicated links between the graph nodes. The traditional terminology in design languages is the *vocabulary* (for the building blocks of the *models*), the *rules* (for the *transformations*) and the *production system* for the rule sequence embedded in the control structures to define a *program* for compilation (Riessenpatt gen. Richter and Rudolph, 2019).

The effort of programming in graph-based design languages consists thus of writing down a sequence of graph transformations (Voss et al., 2023) which may be intermixed with conventional control structures known from other programming languages to guarantee that in a certain moment at the end of a design computation a certain result is obtained or another computational iteration loop is triggered to achieve the desired result, see figure 5.

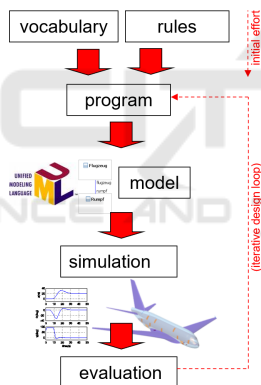


Figure 5: Model generation, simulation and evaluation loop by compilation of design languages (Rudolph, 2011).

Like any other formal programming language in computer science, graph-based design languages need a language compiler to translate the design language (i.e. the source-code) into an executable engineering model (i.e. a CAD-model). In the work here, the commercial software product *Design Cockpit 43*[®] (IILS mbH, 2023) is used as a compiler to translate graph-based design languages into executable models for the purpose of design automation (Rudolph, 2011; Schmidt and Rudolph, 2016).

The automation of a design loop of a complex system in modules of graph-based design languages opens the horizon to substitute selected design language modules by modules with *artificial intelligence* exhibiting the same input-output relation.

2 ARTIFICIAL INTELLIGENCE IN ENGINEERING DESIGN

In the following three paragraphs, several artificial intelligence search strategies are used to create a physical architecture from a given logical architecture. Since all three problems of packing, piping and routing are known to be *NP-complete* (Sahni and Bhatt, 1980; Leung et al., 1990; Cagan et al., 2002), no global optimum solution can be expected in reasonable run-time for industry-size problems.

This bottleneck opens the window for all kinds of *search heuristics* to reduce the run-time at the expense of optimality. In most real-world industrial applications, the notion of *optimality* seems mostly to be an illusion anyway, since the often mandatory design constraints (i.e. internal design codes and external standards and norms) are observed to dominate the solutions found. In AI exists a wide range of algorithms with divers setups and with different mathematical properties and search characteristics, ranging from stochastic to deterministic behaviors.

In a *particle multiple swarm optimization* (PMSO) algorithm exist several sets of design solution candidates in parallel, while in an *simulated annealing* (SA) algorithm (Kirkpatrick et al., 1983) only a single set of design solutions exists. Such algorithms also possess a set of parameters to modify the algorithmic behavior and need therefore some experience in customizing the algorithm to a specific search problem. If one or several parameters in these algorithms are randomized, the behavior of the algorithm becomes stochastic. In other cases when the design problem can be mapped to a graph representation, in which a shortest path connection problem needs to be solved, several graph search algorithms are available as solutions, and the *A**-algorithm (Eheim et al., 2021) is known to be optimal, complete and deterministic.

In the following sections three applications of AI search algorithms (PMSO, SA and *A**) are used for the automated packing, piping and routing in arbitrary complex 3D CAD-geometries.

2.1 AI in Packing Automation

In the V-Model in figure 4 the logical architecture defines the list of system components and their interconnections. This serves as input for a packing algorithm which defines the boundary conditions for the subsequent piping and routing algorithms inside a certain design space. The AI algorithm used is a *particle multiple swarm optimization* (PMSO) algorithm (Schopper, 2023), which allows to consider constraints of all kinds to be included in the optimization.

The optimization goal is the overall minimization of the layout area, and as additional constraint, only straight connections between the components are allowed, see figure 6. While in figure 6 the optimization

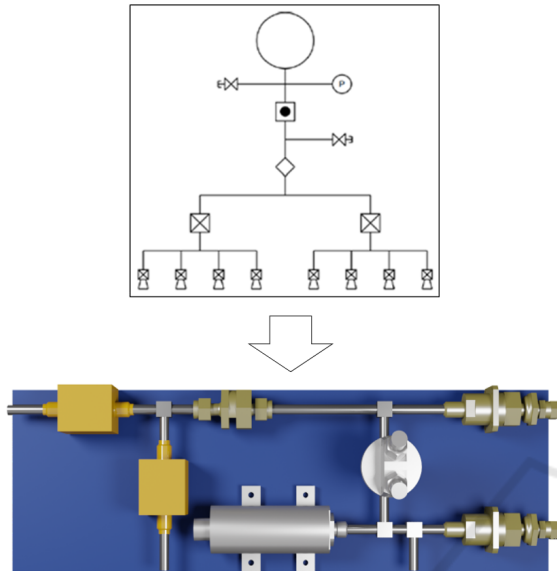


Figure 6: Automated PMSO packing (Schopper, 2023).

goal was the layout minimization under the constraint of only straight connections between the components, the layout can be further compacted if bends of 90° between the components are allowed, see figure 7.

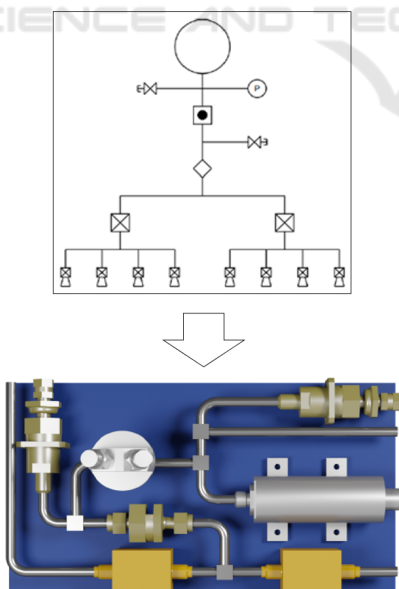


Figure 7: Automated PMSO packing (Schopper, 2023).

The difference of the two bending conditions in figures 6 and 7 results in a 21% area saving from 457 cm² to 361 cm² for the generated packages.

2.2 AI in Piping Automation

The following pipings stem from a comparison of an Airbus A320 landing gear bay, which was manually designed, and was now compared in an industrial case study with pipings obtained by a *simulated annealing* (SA) algorithm (Neumaier et al., 2022).

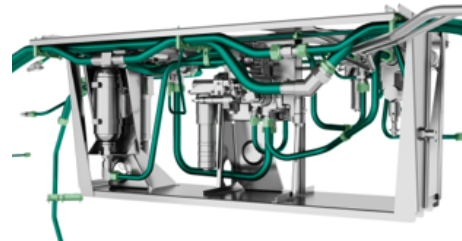


Figure 8: Manual Airbus A320 series piping with total pipe length 22.6m and 107 bends) (Neumaier et al., 2022).

The comparison of the manually designed A320 series solution in figure 8 and the generated piping in figure 9 yields a 8,4% length and weight saving at the expense of a surplus of 43 bends.

Since the number of bends drives the cost for manufacturing, a second industrial case study showed that the algorithm could be further improved to yield an

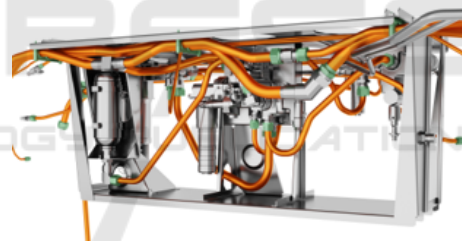


Figure 9: Automated *Design Cockpit 43*[®] piping with total pipe length 20.7m and 150 bends) (Neumaier et al., 2022).

even more reduced total pipe length of 20.4m and reduced number of only 95 bends, resulting in a combined saving of 9,7% in total length and weight and a 11,2% saving in bends (Rudolph, 2023).

2.3 AI in Routing Automation

While the previous showcases of packing and piping were from aerospace, the following routing automation application is taken from the automotive industry. Routing comes in industry usually after the piping, since wires are more flexible than pipes and previously no software system could handle both problems in a common framework simultaneously. Figure 10 shows a routing generated with a modified version of an A*-algorithm (Eheim et al., 2021).

The challenge of wire harness design in industry is hereby not the only the overall length and cost of copper, but due to the mass customization a huge number of customer options become possible and need to be manufactured. This means that the wire harness in the premium segment of the automotive industry mutated to a wire harness design with “lot-size 1”.

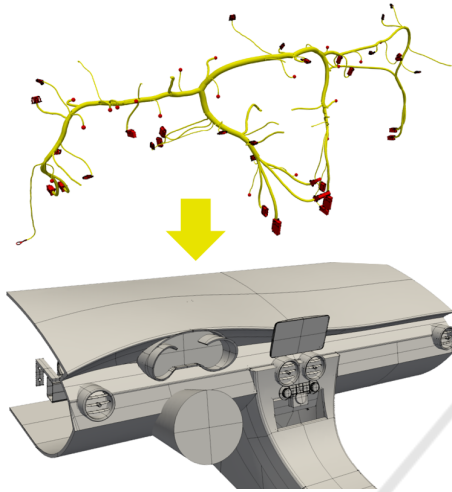


Figure 10: Automated harness routing with navigation system and round air outlets (Eheim et al., 2021).

The first harness shown in figure 10 differs to the second harness shown in figure 11 by the two different electric components (navigation system versus radio) which results in a subset of different connections

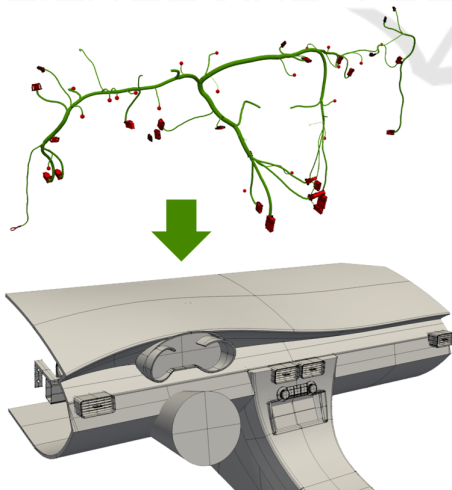


Figure 11: Automated harness routing with radio instead navigation and square air outlets (Eheim et al., 2021).

(with positions and tangents) for the harness and due to the different CAD-modeling (round versus square air outlets) the permissible design space for the harness might be slightly different. This shifts the goal

of the shortest length of the harness more and more towards the optimal harness module size and the optimization of harness manufacturing constraints such cost and manufacturing integration issues (Karlsson et al., 2023).

The examples of packing, piping and routing have been shown here as isolated capabilities. However, due to the encoding of packing, piping and routing as software modules inside a graph-based design language approach, packing, piping and routing are now available as engineering services, which is reflected by the concept of *Engineering as a Service* (EaaS) in analogy to the concept of *Software as a Service* (SaaS). The combination of such services allows the creation of complete automated process chains for a quite complex design process automation.

In most of these automated engineering process chains, the synthesis power of these algorithms to create a solution under the current boundary conditions is much more important than the knowledge whether the global optimum of the most lightweight network connection is in fact achieved, since due to the aforementioned *NP-completeness* of the engineering task this global optimum is out of reach for industry-sized problems anyway.

2.4 AI in Innovation

So far, the presented three search algorithms (PMSO, SA and A^*) used the *design is search* paradigm based on the *closed-world assumption*. This means that all three algorithms have used a predefined vocabulary and a predefined set of rules. In consequence, the scientific question arises to what an extent unconventional “creative” and new “innovative” solutions may be generated. In (Riestenpatt gen. Richter and Rudolph, 2019) these questions are answered as follows: An

- *innovation* may be achieved through an unorthodox instantiation of an already available vocabulary. As a necessary condition, the parameter value mutation must be useful in some sense of the set of employed design goal criteria.
- *innovation* may be achieved through the extension of the design language in form of a new vocabulary which brings in and describes some new, formerly unknown physical behavior.

This means that similarly to the first possibility, all three algorithms have used a predefined vocabulary and a predefined set of rules and all potential instantiations thereof remain in the syntactically permissible hull of the vocabulary. The solutions belong in this respect to a *closed system*.

There may occur a very special effect in case the syntactical hull of a vocabulary is larger than its permissible semantical hull (Riestenpatt gen. Richter and Rudolph, 2019). In such a case, the occurring unconventional instantiation is either meaningless or gives birth to a new semantic meaning by the mechanism of *emergence*. The second possibility of innovation above by adding a new vocabulary to the known vocabulary set has in this respect the very same effect, but relies on the enlargement of the vocabulary from the outside in an *open system*.

Large Language Models (LLMs) represent in this respect a new AI technique which opens new perspectives. However, at least for the near future, the underlying method of *word embeddings* (Gomez-Perez et al., 2020) in LLMs is however not yet well understood nor stable (Arseniev-Koehler, 2022), but the potential to have an information processing system which is capable to be permanently extended offers a clear research perspective and shows a huge potential for future industrial applications of all kinds.

2.5 The Potential of AI in Design

Beyond the three above show-cases of AI techniques shown in the design of the physical architectures of aerospace or automotive systems and products, AI techniques possess a huge potential in design applications. The fact that the currently known state of AI doesn't represent a theory in closed form but looks more like a dispersed and fragmented set of different methods and divers tools is hereby not necessarily a disadvantage. This is due to the fact that the activity of engineering design as it is performed by humans, follows a pattern of *divergence and convergence*.

In the phase of *divergence*, a set of multiple to many design alternatives is created. In this phase, it is most important to increase the number of potential design solutions in order to "widen the solution space". This search for alternative design solutions seems to be quite opportunistic, since the true source of these new alternatives doesn't really matter, even blind search using randomized algorithmic elements are accepted as long as it serves the purpose of creating something new and potentially useful.

In the phase of *convergence*, the emphasis is on the simulation, analysis and evaluation of the design alternatives in order to establish a ranking to select the best. In this phase, first principles play a central role in order to be capable to compute and prove the correct behavior of the design in order to justify the evaluation and selection of the chosen design solution despite the fact that the origin of this design alternative might be the result of a stochastic algorithm.

In reference to the already explained and digital machine-executable V-model of MBSE shown in figure 4 the potential for AI techniques in design becomes now fully apparent, since the subsequent creation of the functional system architecture, the logical system architecture and the physical system architecture marks the presence of three subsequent divergent and convergent design phases for the creation, synthesis, simulation, analysis, evaluation and final selection of one design alternative out of many in order to proceed to the next design phase. In each of these three system architecture design phases, AI techniques of various kinds might be useful.

There exists a huge interest in design to make also the divergent phase accessible to methods based on first principles to minimize the effort of creating new designs. This means as a consequence, that the better these AI methods and tools are mathematically analyzed and understood, the more they lose their original character as AI black boxes and become a member in the methods repertoire of the natural sciences.

3 CONCLUSIONS

An AI-enhanced machine-executable V-Model for MBSE for the "intelligent" automation of packing, piping and routing in real-world engineering design tasks is shown. The integration of artificial intelligence search techniques is achieved by means of graph-based design languages.

Graph-based design languages consist of a vocabulary which form ontologies, a set of rules and a production systems which contains the definition of the rule sequence. Graph-based design languages can be automatically compiled by a compiler into various executable domain-specific language models such as the CAD-models shown. Three different AI search methods (PMSO, SA and A*) have been illustrated with industrial examples such as the automated packing, piping and routing of subsystems during the physical system architecture design phase. Due to the fact that the behavior of these AI techniques is often not fully understood, their use is often driven by opportunism as long as it serves the purpose.

Furthermore, the notion of closed and open systems has been shortly introduced and discussed to understand the different underlying assumption of emergence, which differentiates a closed system from an open system. The most recent implementations of such open systems in the form of LLMs are however far too little understood to entirely understand their behavior, despite the fact that LLMs seem to be capable to push AI to the next level of open systems.

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