On the Formal Robustness Evaluation for AI-based Industrial Systems

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Abstract: The paper introduces a three-stage evaluation pipeline for ensuring the robustness of AI models, particularly neural networks, against adversarial attacks. The first stage involves formal evaluation, which may not always be feasible. For such cases, the second stage focuses on evaluating the model's robustness against intelligent adversarial attacks. If the model proves vulnerable, the third stage proposes techniques to improve its robustness. The paper outlines the details of each stage and the proposed solutions. Moreover, the proposal aims to help developers build reliable and trustworthy AI systems that can operate effectively in critical domains, where the use of AI models can pose significant risks to human safety.

1 INTRODUCTION

Over the last decade, there has been a significant advancement in Artificial Intelligence (AI) and, notably, Machine Learning (ML) has shown remarkable progress in various critical tasks. Specifically, Deep Neural Networks (DNN) have played a transformative role in machine learning, demonstrating exceptional performance in complex applications such as cybersecurity (Jmila and Khedher, 2022) and robotics (Khedher et al., 2021).

Despite the capacity of Deep Neural Networks to handle high-dimensional inputs and address complex challenges in critical applications, recent evidence indicates that small perturbations in the input space can lead to incorrect decisions (Bunel et al., 2018). Specifically, it has been observed that DNNs can be easily misled, causing their predictions to change with slight modifications to the inputs. These carefully chosen modifications result in what are known as adversarial examples. These discoveries underscore the critical challenge of ensuring that machine learning systems, especially deep neural networks, function as intended when confronted with perturbed inputs.

Adversarial examples are specially crafted inputs that are designed to fool a machine learning model into making a wrong prediction. These examples are not randomly generated but created with precise calculations. There are various methods for generating adversarial examples, but most of them focus on minimizing the difference between the distorted input and the original one while ensuring the prediction is incorrect. Some techniques require access to the entire classifier model (white-box attacks), while others only need the prediction function (black-box attacks).

Adversarial attacks pose a significant threat to critical industrial applications, particularly in sectors such as manufacturing, energy, and infrastructure, where precision and reliability are paramount. These attacks, carefully crafted to exploit vulnerabilities in machine learning models, introduce subtle modifications to input data. In critical industrial processes, the consequences of misclassification or data manipulation by adversarial attacks can result in operational failures, compromised safety, and potentially catastrophic outcomes.

To illustrate the severity of adversarial attacks in crucial applications like anomaly detection in the cybersecurity domain, consider Figure 1. An attacker, possessing malicious traffic, can manipulate the traffic by adding imperceptible perturbations, making it appear benign to the cybersecurity system, allowing it to pass undetected. Such attacks can severely compromise the system’s ability to identify and mitigate threats, posing significant security risks.

In this paper, we recommend a three-stage pipeline (Khedher et al., 2023) to industrialists to investigate the robustness of their models and, if possi-
An adverse sample is generated by adding a small perturbation to the original sample. Thus, malicious perturbed traffic can be misclassified as benign and thus bypass the intrusion detection system. This can have serious consequences for the system (Jmila and Khedher, 2022).

ble, obtain a formal guarantee of robustness. The first stage is formal evaluation, which consists of evaluating all possible inputs of the model and formally verifying its output. This stage is very complex, or even impossible, if the model is complex or the data is of very high dimensionality. In this last case, we propose a second stage that consists of evaluating the robustness of the AI model against a set of adversarial attacks. If the model fails against adversarial attacks, we recommend the third stage, which consists of improving robustness using techniques called defenses or adversarial training.

In the rest of the paper, in section 2, the need for Formal methods for AI-based critical systems is detailed. Then, in sections 3, 4 and 5, we describe each of the three stages of robustness evaluation pipeline and describe the popular solutions proposed in the state of the art. Finally, the section 6 concludes the paper.

2 THE NEED FOR TRUSTWORTHY AI-BASED CRITICAL SYSTEMS

The use of Artificial Intelligence techniques is becoming increasingly popular in various applications (Miglani and Kumar, 2019), as the technologies mature and become more affordable (Boardman and Butcher, 2019). These techniques can be physically embodied as in the case of safety-critical systems such as electricity grids or on-board aircraft networks or exist only as software agents that autonomously process data at speeds or for durations that humans are not capable of.

Applying AI techniques can confer a competitive advantage to the industry by providing both high value-added products and services and support to decision-makers (Mattioli et al., 2023). In this sense, production efficiency, product quality, and service level will be improved by artificial intelligence (Li et al., 2017). However, while AI has much potential for innovative applications (advanced automation and autonomous systems), it raises several concerns such as security and safety (El-Sherif et al., 2022). These concerns are even more salient when it comes to AI-based critical systems, where the integration of AI technologies can pose significant risks to human safety.

AI-based critical systems are defined as those systems containing AI-based components alongside traditional software components and whose failure leads to unacceptable circumstances such as loss of human lives (Mwadulo, 2016). Such systems are not only safety-critical but also complex. Consequently, they impose strict certification requirements and high safety standards (Ferrari and Beek, 2022). In this sense, the integration of AI technologies in those systems is constrained by the need for verification, extensive testing, and certification.

When employing verification in the engineering process, trust in the safety of the resulting system will to a large extent be deduced from trust in the integrated AI/ML models. Therefore, such models need to be robust and the results of the verification process need to be trustworthy. To achieve the highest levels of trustworthiness, one might proceed by formally verifying the robustness of AI/ML models. Indeed, formal robustness evaluation helps developers build reliable and trustworthy AI systems that can operate effectively in critical domains. Thus, it is essential for AI safety-critical systems for several reasons including:

- **Identifying vulnerabilities**: AI systems are susceptible to various vulnerabilities, including adversarial attacks, data distribution shifts, and model biases. Formal robustness evaluation helps identify these vulnerabilities by subjecting the system to rigorous testing and analysis. By understanding the system’s weaknesses, developers can take appropriate measures to mitigate risks and improve the system’s robustness.

- **Safety assurance**: AI systems are increasingly being deployed in safety-critical domains such
as autonomous vehicles, healthcare, and finance. These systems must operate reliably and safely, as failures can have severe consequences, including loss of life or significant financial losses. Formal robustness evaluation helps ensure that the system behaves as intended and can handle unexpected scenarios or adversarial attacks.

- **Adversarial robustness**: Adversarial attacks involve intentionally manipulating inputs to deceive or mislead AI systems. Formal robustness evaluation helps assess the system’s resilience against such attacks. By analyzing the system’s response to adversarial inputs, developers can identify vulnerabilities and develop defenses to ensure the system remains robust in the face of potential attacks.

- **Compliance with regulations and standards**: Many safety-critical domains have regulations and standards that govern the deployment of AI systems. Formal robustness evaluation helps demonstrate compliance with these requirements by providing evidence of the system’s reliability, safety, and ability to handle unexpected situations. It allows developers to provide a rigorous and systematic assessment of the system’s performance, which is crucial for gaining regulatory approvals and ensuring public trust.

- **Handling edge cases**: AI systems often encounter edge cases or scenarios that are not well-represented in the training data. These cases can lead to unexpected behavior or errors. Formal robustness evaluation involves testing the system with a wide range of inputs, including edge cases, to ensure it can handle them appropriately. By identifying and addressing potential issues in edge cases, developers can improve the system’s overall reliability and safety.

### 3 FORMAL METHODS FOR NEURAL NETWORK VERIFICATION

Formal methods are a set of techniques that use logic and mathematics to rigorously prove that software meets specific requirements. These methods were initially developed in the 1960s and involved hand-written proofs for small programs (Floyd, 1967; Hoare, 1969). However, recent advancements have led to the creation of automated software verification tools.

These tools focus on the semantic properties of programs, which are concerned with how the program behaves when it runs. Unlike syntactic properties, which can be determined by simply looking at the code, semantic properties cannot be fully automated due to the undecidability of Rice’s theorem. This means that verification tools must make some trade-offs between automation, generality, and completeness. While they cannot always provide a complete answer, formal methods ensure that any property proven by a tool is indeed true.

Formal methods are widely used in the hardware and software industries, and are mandated by safety standards for critical embedded systems like avionics software. Their adoption is expanding into less critical domains, such as Facebook and Amazon’s use cases (Newcombe et al., 2015). This demonstrates the maturity and scalability of formal methods for software verification.

#### 3.1 Formal Methods Categories

Different approaches to verify neural networks can be categorized into three categories based on the formulation of the problem:

- **Reachability**: This method aims to identify inputs that lead to specific states or properties within the network. It approximates around selected representative inputs, propagates the over approximation along the layers.

- **Optimization**: This method employs optimization techniques to find instances that violate the given property. The network’s function is incorporated as a constraint in the optimization process. Due to the non-convex nature of the optimization problem, various techniques have been developed to represent nonlinear activation functions as linear constraints.

- **Search**: This method systematically explores the input space to find inputs that contradict the property. It often utilizes heuristics or probabilistic search strategies to guide the exploration.

In the following sections, we will discuss formal methods for verifying neural networks. We will present a variety of solutions that have been proposed in the literature.

#### 3.2 Reachability Approaches

In the verification of neural networks, the Reachability approach involves computing the reachable set for a specific output, meaning finding the set $X$ such that every element in that set produces a predefined output $y$ when propagated through the network:
\( \mathcal{R}(X, f) := y : y = f(x), \forall x \in X \) (1)

The straightforward task of verifying all outputs produced by a set of inputs can already be expensive, depending on the size of the input set. This indicates that the reverse problem of finding the sets for which a property on the output holds is not scalable and is infeasible in practice. For this reason, most work in this domain uses over-approximations of the sets, for example, employing abstract domains instead of exact sets, as defined in Abstract Interpretation.

Two main approaches to reachability analysis for neural networks are proposed in the literature: exact and approximate reachability. Below, we outline formal methods associated with each type of reachability approach. The choice between exact and approximate reachability depends on the specific application and the desired balance between accuracy and computational efficiency. For safety-critical applications where precise results are required, exact reachability may be the preferred method. However, for applications where speed is more critical, approximate reachability can be a valuable alternative.

### 3.2.1 Exact Reachability

This approach aims to determine the precise set of outputs associated with a given set of neural network inputs. It is particularly well-suited for piece-wise linear networks, where the reachable set can be computed by dividing the network into smaller segments and analyzing each segment individually. However, this method becomes computationally demanding as the network grows in size due to the exponential growth of linear segments.

**ExactReach.** Exact reachability analysis for neural networks using either linear or ReLU activations is achieved in (Xiang et al., 2017b) by precisely representing input sets as unions of polyhedra. ExactReach, a specialized tool designed for this purpose, utilizes polyhedron manipulation tools for computing the reachable set at each network layer. For ReLU activation functions, ExactReach demonstrates a key property: the reachable set of outputs can also be represented as a union of polyhedra if the input set is represented in the same manner. This property enables ExactReach to thoroughly explore the reachable set for networks with ReLU activations, ensuring precise determination of the exact boundaries of the reachable set, considering all possible combinations of input values and activation functions. As a result, ExactReach provides comprehensive insights into the network’s behavior and helps identify output ranges associated with specific input regions.

### 3.2.2 Approximate Reachability

Approximate reachability provides an over-approximation of the reachable set, meaning that it estimates the set that is guaranteed to contain all possible outputs, even if it may not be the exact set. This method is more efficient than exact reachability as it does not require dividing the reachable set into smaller pieces, but it sacrifices some accuracy.

**Abstract Interpretation.** Abstract interpretation (Cousot and Cousot, 1977) is a powerful technique for computing sound approximations of the reachable set of a given function, expressed as specific sets of properties that can be automatically determined. Originally developed for analyzing program semantics, abstract interpretation provides a systematic approach to relating an often-intractable concrete function with a more manageable abstract function, also known as an abstract transformer. This abstraction enables conservative over-approximations of the reachable set, allowing for efficient reasoning about complex functions. Crucially, proving that the computed over-approximation is safe implies that the concrete reachable set is also safe.

An abstract transformer operates on abstract elements, which are typically logical properties representing sets of corresponding concrete elements within the actual function. These abstract elements collectively form an abstract domain. The design of effective abstract transformers and domains involves a delicate balance between accuracy and efficiency. These abstractions must be sufficiently precise to identify erroneous cases as unreachable while maintaining computational tractability and scalability to handle large and complex functions.

Abstract interpretation, a technique for analyzing program semantics, has found a new application in analyzing neural networks. In the paper (Gehr et al., 2018), the authors introduce a method for proving properties of neural networks using abstract transformers constructed from CAT (Conditional Affine Transformation) functions. This approach offers a promising avenue for formally verifying the behavior of neural networks.

**MaxSens.** In (Xiang et al., 2017a), the authors conducted a study on the estimation of reachable sets by focusing on the computation of maximal sensitivity in neural networks. They treated this problem as a series of convex optimization problems within a simulation-based framework that utilizes interval arithmetic. This approach is scalable and supports monotonic activation functions, making it applicable.
3.3 Optimization Approaches

Optimization techniques are applied to challenge the assertion, treating the neural network’s function as a constraint in the optimization process. Consequently, the optimization problem becomes non-convex. In primal optimization, several approaches have emerged to represent nonlinear activation functions as linear constraints. Methods like NSVerify (Lomuscio and Maganti, 2017a), MIPVerify (Tjeng et al., 2019), Big-M (Ibn-Khedher et al., 2021), and ILP (Bastani et al., 2016) are instances of techniques that simplify constraints through primal optimization. Alternatively, dual optimization techniques provide another avenue for simplifying constraints. Lagrangian dual methods, including Duality (Dvijotham et al., 2018) and ConvDual (Kolter and Wong, 2017), as well as semidefinite programming methods such as Certify (Raghunathan et al., 2018) and SDP (Fazlyab et al., 2022), represent representative approaches for dual optimization.

3.3.1 Primal Optimization

Primal optimization methods tackle the verification task by embedding the network structure as a constraint in the optimization problem. However, these methods are currently limited to networks with ReLU (Rectified Linear Unit) activations. To address this, researchers have developed techniques to encode the network using linear or mixed integer linear constraints, taking advantage of the piece-wise linear-ity of ReLU activations. This approach allows for a more focused exploration of optimization solutions tailored to the specific characteristics of ReLU-based networks.

Big-M. In the work presented in (Ibn-Khedher et al., 2021), the authors advocate for utilizing the bigM technique as an automated encoder for linearizing the ReLU, a non-linear activation function. This technique involves a mixed-integer linear programming transformation that precisely converts non-linear constraints into linear inequalities.

To illustrate, considering the example depicted in Eq.2 where neurons $H_1$ and $H_2$ are activated with ReLU, employing Big-M for the verification problem results in formulating it as a maximization problem: $\max \ Z = \text{Constant}$, subject to a set of constraints that delineate the relationships between neurons across different layers. The core of this approach lies in the linearization of the ReLU function, achieved by replacing it with a set of constraints. For instance, the relationship between neuron $H_1$ and inputs $x_1$ and $x_2$ is expressed as the following system of equations.
\[
\begin{align*}
\text{out}(H_1) & \geq (\theta_1 - 1)M + (x_1 + x_2) \\
\text{out}(H_1) & \leq (1 - \theta_1)M + (x_1 + x_2) \\
\text{out}(H_1) & \leq \theta_1 \times M \\
x_1 + x_2 & \geq (\theta_1 - 1) \times M \\
x_1 + x_2 & \leq \theta_1 \times M \\
\theta_1 & \in \{0, 1\}
\end{align*}
\]  

MIPVerify. The authors of (Tjeng et al., 2019) similarly encode the neural network using mixed integer linear constraints. However, there are two key distinctions between MIPVerify and NSVerify (Lomuscio and Maganti, 2017b). Firstly, MIPVerify employs node bounds to refine the constraints. Secondly, MIPVerify addresses an adversarial problem that aims to estimate the maximum permissible perturbation on the input side. Like NSVerify, MIPVerify is also recognized as a complete method, ensuring that it can successfully handle and analyze all feasible scenarios. Formally, MIPVerify computes maximum allowable disturbance using mixed integer linear programming. Mathematically, MIPVerify optimizes for the adversarial bound \( \min_{x, y} \| y - x \|_p, s.t. y \notin \mathcal{F}, y = f(x) \) using mixed integer encoding (with lower and upper bounds) and returns adversarial bounds.

ILP. The authors of ILP (Iterative Linear Programming) (Bastani et al., 2016) represents the neural network as a series of linear constraints by linearizing it around a reference point. In ILP, the optimization problem addresses an adversarial scenario aiming to determine the maximum permissible perturbation on the input side. The optimization is performed iteratively. However, it is important to note that ILP is not considered a complete method as it only considers a single linear segment of the network, thus potentially overlooking certain aspects of the overall network behavior.

\section*{3.3.2 Dual Optimization}

While various techniques have been developed for encoding constraints in primal optimization methods, dual optimization offers an alternative approach by simplifying the constraints within the primal problem. This simplification typically leads to fewer and more manageable constraints in the dual problem. However, the corresponding objectives in dual optimization tend to be more complex than those in the primal problem. The construction of the dual problem often involves incorporating relaxations, which means that these approaches are considered incomplete due to the approximation inherent in the relaxation process.

Duality. (Dvijotham et al., 2018) addressed various challenges associated with SMT-based, branch-and-bound, or mixed-integer programming methods, particularly concerning scalability and restrictions linked to specific piece-wise linear activation functions. They introduced a universal approach capable of accommodating any activation function and specification type. The key concept involves formulating the verification property as an optimization problem, aiming to identify the most substantial violation of the specification. Their strategy entails solving a Lagrangian relaxation of the optimization problem to derive an upper bound on the maximum potential violation of the specification. While the approach is sound, indicating that if the largest violation is less than or equal to zero, the property holds, it is also incomplete. A positive largest violation does not conclusively establish that the property does not hold in reality. Moreover, the process can be halted at any point to obtain the current valid bound on the maximum violation.

ConvDual. ConvDual (Wong and Kolter, 2018) follows a dual approach to estimate output bounds. It begins by performing a convex relaxation of the network within the primal optimization framework to simplify the dual problem. Unlike explicit optimization, ConvDual heuristically computes the bounds by selecting a fixed, dual feasible solution. This heuristic approach allows ConvDual to achieve computational efficiency compared to Duality. While the original ConvDual approach utilizes the obtained bounds for robust network training, this survey primarily concentrates on the method’s capability to compute these bounds accurately.

\section*{3.4 Search Approaches}

Reluplex. In (Katz et al., 2017), the authors propose Reluplex. Reluplex is the abbreviation of ReLU for the simplex algorithm. The simplex algorithm is an algorithm for solving linear optimization problems. Its objective is to minimize a function on a set defined by inequalities. Reluplex’s principle consists in formalizing the neural network by a set of equations. To solve this system of equations, starting from an initial assignment, it tries to correct some constraints violated at each step. The specification of this approach is that, from one iteration to another, the constraints between the variables can be violated.

PLANET. In (Ehlers, 2017), the authors propose PLANET, "a Piece-wise LineAr feed-forward NEural network verification Tool". Its principle consists first
of replacing non-linear neural network functions by a set of linear equations. It tries then to find a solution to the system of equations. The approach supports both types of nodes: ReLU and Max Pooling.

**BaB.** BaB (Bunel et al., 2017) employs the branch and bound technique to calculate the output bounds of a network. Its modular design allows it to function as a comprehensive framework that can accommodate other methods like Reluplex and Planet. This versatility enables BaB to serve as a unified platform for various approaches within the field.

**Fast-Lin.** Fast-Lin (Weng et al., 2018) adopts a layer-by-layer approach and utilizes binary search within the input domain to determine a certified lower bound on the allowable input disturbance for ReLU networks. This methodology enables efficient computation and offers a dependable estimation of the maximum permissible input perturbation.

**Fast-Lip.** Fast-Lip (Weng et al., 2018) builds upon the foundation of Fast-Lin for calculating activation function bounds while also estimating the local Lipschitz constant of the network. Fast-Lin excels in terms of scalability, being more efficient in this regard. However, Fast-Lip provides enhanced solutions specifically for 'L1 bounds,' offering improved performance in that specific context.

While we present a rough overview of the different techniques developed in each field, it is important to note that more often than not, state of the art tools leverage more than one kind of method. They rely on reachability approaches for their scalability, adding some optimization to improve the precision and make their tool complete through search based approaches. One can look at the performances of state of the art approaches through the VNN-COMP (Brix et al., 2023), which brings together and evaluate tools such as α-β-CROWN (Zhang et al., 2018), Marabou (Katz et al., 2019), nnenum (Bak et al., 2020) or PyRAT (Lemesle et al., 2023).

## 4 ROBUSTNESS TESTING

In some cases the formal evaluation of a neural network is costly in terms of computation time. To get an idea about the new robustness of the neural network, it is recommended to start by analyzing the behavior of the neural network in front of adversary attacks. A network that is already vulnerable to adversarial attacks needs to improve its robustness using state-of-the-art adversarial training techniques and it is very early to formally evaluate its robustness.

### 4.1 Adversarial Attacks Types

There are two main types of adversarial attacks (White-box attacks and Black-box attacks) that aim to fool neural networks into making incorrect predictions. The key difference between the two lies in the amount of knowledge the attacker has about the target neural network.

White-box Attacks assume that the attacker has full knowledge of the neural network, including its architecture, weights, and training data. This allows the attacker to comprehensively analyze the network’s vulnerabilities and design targeted adversarial attacks that exploit its specific weaknesses. In contrast, Black-box Attacks operate with limited or no knowledge of the target network’s internal structure or parameters. The attacker can only interact with the network by making input queries and observing the corresponding output predictions. This poses a significant challenge, as the attacker must infer the network’s vulnerabilities and design attacks without direct access to its inner workings.

In the industrial context, the two type of attacks serve distinct purposes. Organizations typically employ white-box Attacks internally to enhance their systems and detect potential vulnerabilities before they can be exploited by external actors. By gaining comprehensive knowledge of their neural networks’ architectures, weights, and training data, organizations can thoroughly analyze their networks’ robustness and identify areas where adversarial attacks could be successful. This proactive approach helps organizations to detect the weakness of their models and mitigate risks.

On the other hand, Black-Box Attacks play a crucial role in testing and evaluating neural networks before they are deployed in real-world applications. By simulating the actions of an external attacker, Black-Box Attacks assess the network’s resilience against unknown or obfuscated threats. This helps organizations identify potential vulnerabilities that may arise from limited knowledge of the network’s internals.

### 4.2 Adversarial White-Box Attacks

**Fast Gradient Sign Method (FGSM).** (Goodfellow et al., 2015) have developed a method for generating adverse sample based on the gradient descent method. Each component of the original sample $x$ is modified by adding or subtracting a small perturbation $\epsilon$. The adverse function $\psi$ is expressed as fol-
\[ \psi : X \times Y \longrightarrow X \]
\[(x, y) \mapsto -\varepsilon \nabla_x L(x, y) \]
Thus, the loss function of the classifier will decrease when the class of the adverse sample is chosen as \( y \).
We then wish to find \( x' \) adverse sample of \( x \) such as:
\[ \|x' - x\|_p \leq \varepsilon. \]
It is clear that the previous formulation of FGSM is related to targeted attack case where \( y \) corresponds to the target class that we wish to impose on the original input sample. However, this attack can be applied in the case of untargeted attack, by considering the following perturbation:
\[ \rho : X \longrightarrow X \]
\[ x \mapsto -\psi(x, C(x)) \]
Thus, the original input \( x \) is modified in order to increase the loss function \( L \) when the classifier retains the same class \( C(x) \). This attack only requires the computation of the loss function gradient, which makes it a very efficient method. On the other hand, \( \varepsilon \) is a hyperparameter that affects the \( x' \) class: if \( \varepsilon \) is too small, the \( \rho(x) \) perturbation may have little impact on the \( x' \) class.

**Basic Iterative Method (BIM).** (Kurabin et al., 2017) proposed an extension of the FGSM attack by iteratively applying FGSM. At each iteration \( i \), the adverse sample is generated by applying FGSM on the generated sample at the \( (i - 1) \)th iteration. The BIM attack is generated as the following:
\[
\begin{aligned}
x_0' &= x \\
x_{i+1}' &= x_i' + \psi(x_i', y)
\end{aligned}
\]
where \( y \) represents, in the case of a targeted attack, the class of the adverse sample and \( y = C(x_{i}') \) in the case of an untargeted attack. Moreover, \( \psi \) is the same function defined in the case of FGSM attack.

**Projected Gradient Descent (PGD).** The PGD (Madry et al., 2017) attack is also an extension of the FGSM and similar to BIM. It consists in applying FGSM several times. The major difference from BIM is that at each iteration, the generated attack is projected on the ball \( B(x, \varepsilon) = \{z \in X : \|x - z\| \leq \varepsilon\} \). The adverse sample \( x' \) associated with the original one \( x \) is then constructed as follows:
\[
\begin{aligned}
x_0' &= x \\
x_{+1}' &= \Pi_k (x_i' + \psi(x_i', y))
\end{aligned}
\]
where \( \Pi_k \) is the projection on the ball \( B(x, \varepsilon) \) and \( \psi \) is the perturbation function as defined in FGSM. Likewise, \( y \) refers to the target label you wish to reach, in the case of targeted attack, or it refers to \( C(x_{i}') \) in the case of an untargeted attack.

**DeepFool.** DeepFool is a non-targeted attack proposed by (Moosavi-Dezfooli et al., 2015). The main idea of DeepFool is to find the closest distance from the original input to the decision boundary. To overcome the non-linearity in high dimension, they performed an iterative attack with a linear approximation. For an affine classifier \( f(x) = w^T x + b \), where \( w \) is the weight of the affine classifier and \( b \) is the bias, the minimal perturbation of an affine classifier is the distance to the separating affine hyperplane \( \mathcal{f} = x: w^T x + b = 0 \). Given the example of a linear binary classifier, the robustness of the classifier \( f \) for an input \( x_0 \) is equal to the distance of \( x_0 \) to the hyperplane separating the two classes. In fact, the minimal perturbation to change the classifier’s decision corresponds to the orthogonal projection of \( x_0 \) onto the hyperplane, given by:
\[ \eta^*(x) = \frac{-f(x)}{\|w\|^2_2} \cdot w. \]
For a general differentiable classifier, DeepFool assumes that \( f \) is linear around \( x \) at each iteration. The minimal perturbation is expressed as follows:
\[
\arg \min_{\eta_i} \|\eta_i\|_2 \\
\text{subject to } f(x_i) + \nabla f(x_i)^T \eta_i = 0.
\]
This process runs until \( f(x_i) \neq f(x) \), and the minimum perturbation is eventually approximated by the sum of \( \eta_i \). This technique can also be extended to a multi-class classifier by finding the closest hyperplanes. It can also be extended to a more general \( \ell_p \) norm, \( p \in [0, \infty) \). As mentioned in (Yuan et al., 2019), DeepFool provides less perturbation compared to FGSM.

**4.3 Adversarial Black-Box Attacks**

**ZOO.** Zeroth Order Optimization (ZOO) is proposed by (Chen et al., 2017) to estimate the gradients of target DNN in order to produce an adversarial input. ZOO is suitable for problems where gradients are unavailable, uncomputable or private. The threat model assumed by the authors is that the target model can only be queried to obtain the probability scores of all the classes. The authors then use symmetric difference quotient method to estimate the gradient \( \frac{\partial f(x)}{\partial x_i} \), where \( f \) is the loss function:
\[
\hat{g} := \frac{\partial f(x)}{\partial x_i} \approx f(x + he_i) - f(x - he_i)
\]
(3)

The naïve solution above requires querying the model \( 2p \) times, where \( p \) is the dimension of the in-
put. So the authors propose two stochastic coordinate methods: ZOO-Adam and ZOO-Newton in which a gradient is estimated for a random coordinate and the update formula is obtained using ADAM and Newton’s Method until it reaches convergence. The authors also discuss the generation of noise in a lower dimension to improve efficiency and specify its advantages and disadvantages (Bhambri et al., 2019).

Boundary. Boundary Attacks are decision-based adversarial attacks that are based on a model’s decision. This was the first time that decision-based attacks were introduced that focus on deep learning models using real-life data sets such as ImageNet. The proposed algorithm initializes by taking a random distribution of pixels for an image in the range of [0, 255]. Using this image, the algorithm traverses the decision boundary of the class to which the sample input image belongs to. The initialized image is then able to reduce its distance w.r.t. the input image besides staying inside the adversarial region.

5 DEFENSE TECHNIQUE FOR IMPROVING ROBUSTNESS

Defense techniques aim to strengthen a model’s resilience against adversarial attacks. The literature distinguishes three categories of defense techniques, specifically those based on: i) Modifying the input data, ii) Modifying the classifier, and iii) Adding an external model. These categories are elaborated upon below.

5.1 Modifying the Input Data

Instead of directly altering the network architecture or training process, data modification techniques focus on manipulating the input data itself. These techniques aim to make the input data less susceptible to adversarial perturbations, thereby improving the network’s overall robustness. One such technique, Gaussian data augmentation (Zantedeschi et al., 2017), involves adding copies of the original data points with Gaussian noise. This approach trains the network to recognize the same class for both the original instance and its slightly perturbed version, enhancing its ability to generalize and withstand adversarial modifications. The simplicity, ease of implementation, and effectiveness of Gaussian data augmentation have made it a widely adopted technique for mitigating adversarial attacks.

5.2 Modifying the Classifier

Classifier modifications involve altering the neural network architecture or training process to enhance its resilience to adversarial attacks. One such approach is gradient masking, which aims to conceal or mask the network’s gradient information from potential attackers. While many adversarial attacks rely on knowledge of the gradient, gradient masking aims to obscure this information, making it more difficult for attackers to manipulate the network.

Gradient masking techniques work by manipulating the gradients during the training process, effectively hiding the network’s internal workings from external observers. This makes it challenging for attackers to craft effective adversarial examples based on gradient information.

5.3 Adding an External Model

Instead of directly modifying the primary network, external model integration utilizes additional models to augment the system’s defenses against adversarial attacks. This approach introduces an extra layer of protection, making it more challenging for attackers to manipulate the network’s output.

One such technique, introduced in (Lee et al., 2017), employs generative adversarial networks (GANs) to enhance the network’s resilience. A separate generator network actively generates adversarial perturbations that aim to fool the primary network. By incorporating this adversarial training process, the system becomes more adept at identifying and countering adversarial inputs. The integration of external models alongside the primary network during testing provides a robust and effective defense strategy. This approach demonstrates the potential of combining different models and techniques to strengthen the overall security of neural networks against adversarial attacks.

6 CONCLUSION AND PERSPECTIVES

Machine learning models are, ultimately, software artefacts. And as such, there must be adequate consideration and effort devoted to the characterization of its safety and robustness aspects when it is used in sensitive environments, particularly critical systems. However, ML models come with their own challenges, demanding new methods and tools to be devised. While this task seems arduous, the goal of this paper is to offer a broad range of avenues for trust, to show the first
steps in these paths, and to inspire the conviction that the research community is advancing on this topic and making greater strides every year, expanding the toolbox needed by the industrial sector to enforce trust in their models.

In future work, we propose the application of the suggested pipeline in real industrial use cases. Given that the methods mentioned in this survey depend on types of data (images, time series, tabular data), we have observed that the approaches proposed for time series are not sufficiently advanced. Therefore, we suggest investigating the adaptability of this pipeline for temporal data.

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