

Vehicle Pose Estimation: Exploring Angular Representations

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Abstract: This paper addresses the challenge of azimuth estimation in the context of car pose estimation. Our research utilizes the PASCAL3D+ dataset, which offers a diverse range of object categories, including cars, with annotated azimuth estimations for each photograph. We introduce two architectures that approach azimuth estimation as a regression problem, each employing a deep convolutional neural network (DCNN) backbone but diverging in their output definition strategies. The first architecture employs a sin-cos representation of the car's azimuth, while the second utilizes two directional discriminators, distinguishing between front/rear and left/right views of the vehicle. Our comparative analysis reveals that both architectures demonstrate near-identical performance levels on the PASCAL3D+ validation set, achieving a median error of 3.5°, which is a significant advancement in the state of the art. The minimal performance disparity between the two methods highlights their individual strengths while also underscoring the similarity in their practical efficacy. This study not only proposes effective solutions for accurate azimuth estimation but also contributes to the broader understanding of pose estimation challenges in automotive contexts. The code is available at https://github.com/vani-or/car_pose_estimation.

1 INTRODUCTION

Pose detection revolves around the process of determining the position and orientation of specific parts or features of an object or entity in images or videos. Historically, the primary motivation for developing pose detection algorithms was to detect and analyze human body parts and their relative positions. Over time, these methodologies have evolved and have been adapted to cater to various objects, including cars, enabling applications in fields as varied as animation, augmented reality, sports analytics, and vehicle damage assessment.


Early techniques employed to estimate pose made use of part-based models, where individual parts of an entity (like limbs in humans) were detected and then assembled to deduce the overall pose (Felzenszwalb and Huttenlocher, 2005).


Feature-based methods like Scale-Invariant Feature Transform (SIFT) (David, 2004) marked a significant advancement in the field, moving beyond ba-


sic image processing techniques. In this era, geometric problems like the Perspective-n-Point (PnP) were critical, where the objective was to deduce an object's pose from 2D-to-3D point correspondences (Lepetit et al., 2009).

The rise of deep learning, and particularly CNNs, brought a paradigm shift in pose detection methodologies. Unlike traditional methods, where features had to be meticulously crafted, CNNs allowed for automatic feature learning from data. Deep learning models, such as PoseNet (Kendall et al., 2015) and Mask R-CNN (He et al., 2017), are representative examples that have showcased the potential of CNNs in pose estimation tasks.

This paper focuses on improving azimuth estimation in car pose detection. Using the PASCAL3D+ dataset, it presents two architectures based on deep convolutional neural networks, differing in their treatment of azimuth: one uses a sin-cos representation, and the other employs directional discriminators. Both demonstrate advanced performance in pose estimation. The paper is structured to first provide background, followed by a problem definition, detailed methodology, evaluation of results, and concludes with discussions and future work.

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2 RELATED WORKS

Deep learning, particularly CNNs, has significantly advanced car pose estimation. Models like those in (Mousavian et al., 2017) accurately predict 3D car bounding boxes from 2D images. (Prokudin et al., 2018) introduced a probabilistic model for angular regression, enhancing accuracy and handling varying image qualities. MonoGRNet (Qin et al., 2019) provides a unified approach for 3D vehicle detection and pose estimation using monocular RGB images, while (Xiao et al., 2019) developed a generic, flexible deep pose estimation method.

Addressing training data scarcity and feature extraction, (Su et al., 2015) combined image synthesis and CNNs, and (Grabner et al., 2018) focused on 3D pose estimation and model retrieval. Innovative techniques like the characteristic view selection model (CVSM) by (Nie et al., 2020) and a CNN-based monocular orientation estimation integrating Riemannian geometry by (Mahendran et al., 2018) have been proposed.

Car pose estimation is vital in autonomous driving and insurance sectors, essential for understanding vehicle orientation and assessing damages. It's also crucial in scenarios lacking direct sensor data, where visual cues are pivotal (Geiger et al., 2012).

2.0.1 The PASCAL3D+ Dataset

Selecting an apt dataset is pivotal in guiding the research process and ensuring the derived outcomes are reflective of the research objectives. Previous work (Buzzelli and Segantin, 2021) highlighted the importance of training data that faithfully model the application scenario, specifically for the case of vehicle analysis. For our investigation into car pose estimation, with a particular focus on azimuth estimation, the PASCAL3D+ (Xiang et al., 2014) dataset emerged as a front-runner. A driving factor behind this choice was the detailed annotations the dataset offers for each image, notably the azimuth values. Azimuth estimation, a critical facet of pose detection, provides insights into an object's orientation within a 3D space, as detailed later on in section 3. PASCAL3D+ alleviates the complexities of deriving these angles by offering direct data for azimuth estimation, ensuring a more precise and streamlined research methodology.

The PASCAL3D+ dataset, an extension of the PASCAL VOC dataset, augments the original images with intricate 3D annotations, laying the foundation for 3D object detection and pose estimation tasks. A prominent feature of this dataset is its compilation of 5,475 car images, sourced directly from

ImageNet, presenting a myriad of scenarios for researchers to explore. Each car in this dataset is meticulously annotated with a corresponding 3D CAD model, which enables researchers to juxtapose pose estimations against a standardized 3D reference. For cars, the annotations delve deep, offering viewpoints, bounding boxes, and crucially, azimuth angles.

Several nuances make PASCAL3D+ a challenging yet rewarding dataset. The presence of occluded objects simulates real-world complications that algorithms need to account for. Furthermore, the dataset showcases a wide variance in car makes and models, capturing the diversity of the automotive world. However, it is essential to note that while the dataset offers this diversity, it does not explicitly label the specific makes or models.

3 DEFINING AND VISUALIZING AZIMUTH

In the domain of vehicle pose detection, one of the paramount tasks is the precise estimation of the vehicle's orientation in a given image or frame. The key orientation parameter being focused upon in this research task is the azimuth, often denoted as ϕ .

The azimuth, ϕ , is defined as the angle in the range $[-\pi, \pi]$ that represents the orientation of a vehicle with respect to the viewer. Originating from the front of the car, this angle describes how much the vehicle has rotated from this frontal viewpoint. For instance, $\phi = 0$ would indicate a car directly facing the viewer, while $\phi = \frac{\pi}{2}$ would signify the car turned 90° to the right. This definition is depicted in Figure 1.

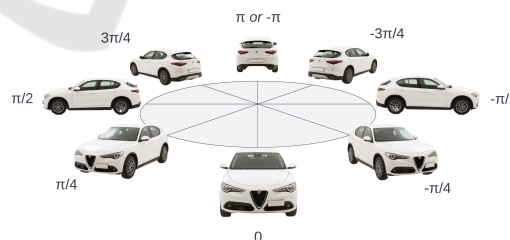


Figure 1: Azimuth ϕ definition for car pose estimation. In this image, an azimuth of $\phi = -\pi/4$ corresponds to the car slightly turned to present its right side (passenger side) towards the viewer. Angle 0 represents the reference axis for this calculation.

It is noteworthy to mention the deliberate exclusion of other viewpoint characteristics from this study, such as elevation, distance, and the roll equivalent from roll pitch and yaw. While these parameters can offer further granularity to pose detection, the primary

focus here remains the continuous estimation of azimuth. When distilled to its essence, the problem tackled in this research is one of regression. Instead of the conventional classification-based approach where discrete classes represent different poses or orientations, the goal here is continuous azimuth estimation. This involves predicting a specific value of φ for a given vehicle image. The advantage of this method is that it allows for a much finer granularity of orientation prediction.

4 PROPOSED APPROACH

Vehicle pose estimation, especially focusing on the azimuthal angle, is a multifaceted challenge. While most regression tasks in deep learning provide continuous values within a predictable range, the angular nature of azimuth presents cyclic constraints that require special consideration. Traditional regression models would in fact treat angles such as $\varphi = \pi$ and $\varphi = -\pi$ as distinct, ignoring their equality due to the cyclic nature of angles.

In the context of this research, two distinct methodologies have been adopted. The common architecture is presented in Figure 2, with two different heads corresponding to the two distinct methodologies, described in the following.

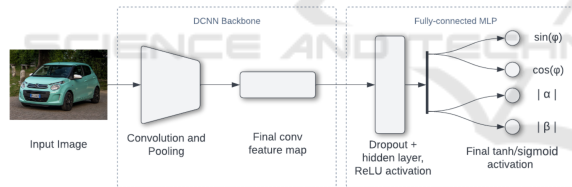


Figure 2: Proposed architecture, with Sin-Cos output representation (top head) and Directional Discriminators output representation (bottom head).

4.1 Sin-Cos Representation

One of the pivotal tasks in vehicle pose estimation is to represent the azimuthal angle, φ , in a format that can be effectively estimated using deep convolutional neural networks (DCNNs). In addressing this, our first proposed architecture adopts what is referred to in (Beyer et al., 2015) as the “biternion” representation, a two-dimensional vector format comprising the sine and cosine of φ . This format effectively addresses the challenge of azimuth representation as a periodic variable in DCNNs.

Model Construction. The designed DCNN architecture is partitioned into two primary segments. Initially, a *backbone* is utilized as an image feature de-

scriptor. This backbone captures intricate patterns and details from the input images, converting them into a condensed feature map. Following this feature extraction phase, a custom multi-layer perceptron (MLP) is stacked atop the backbone. This MLP consists of a hidden layer comprising 100 neurons, activated by the Rectified Linear Unit (ReLU) function. To enhance generalization and curtail overfitting, a dropout layer with a rate of 10% is integrated into the architecture (Srivastava et al., 2014).

Output Mechanism. The crux of this architecture lies in its output mechanism. The network culminates in two output neurons that are activated by the hyperbolic tangent (tanh) function. The tanh activation ensures that the output values lie within the range $[-1, 1]$, which aligns with the natural range of sine ($\sin(\varphi)$) and cosine ($\cos(\varphi)$) functions. Thus, these neurons are adeptly designed to predict the sine and cosine values of the azimuthal angle. Consequently, the estimated azimuth φ can be derived using the inverse tangent function as:

$$\varphi = \text{atan2}(o_1, o_2), \quad (1)$$

where o_1 and o_2 correspond to the outputs of the sine and cosine neurons respectively.

Loss Function. The training process aims to optimize the mean squared error (MSE) between the predicted values and the true sine and cosine values. Mathematically, the loss L is represented as:

$$L = \frac{1}{N} \sum_{i=1}^N ((o_{1i} - y_{1i})^2 + (o_{2i} - y_{2i})^2), \quad (2)$$

where N is the number of samples, o_{1i} and o_{2i} are the predicted sine and cosine values respectively, and y_{1i} and y_{2i} are the true sine and cosine values.

Azimuth Calculation from Sine and Cosine. To estimate the azimuth φ from the predicted sine and cosine outputs, the inverse tangent function, typically represented as atan2 , is employed. Given the nature of this function, it is capable of determining the correct quadrant for the resulting angle based on the signs of the sine and cosine values. Specifically:

$$\varphi = \text{atan2}(y_{\sin}, y_{\cos}). \quad (3)$$

Drawbacks. While the Sin-Cos representation offers a unique approach to tackle the cyclic nature of azimuth angles, it is not devoid of challenges. The most significant is that the predicted sine and cosine values, when considered in isolation, do not guarantee a resultant unit vector. Specifically, when reconstructing the azimuth using $\text{atan2}(y_{\sin}, y_{\cos})$, only one of the sine or cosine values dominantly determines the resultant angle, while the other mainly influences the sign and quadrant determination. Thus, even if one value

is significantly off, it might not significantly affect the angle’s magnitude but can change its direction. This can lead to errors, especially when the predicted values drift away from forming a unit vector.

4.2 Directional Discriminators

To introduce more nuance and precision in the estimation of the azimuthal angle, φ , the second architecture employs a distinctive double-discriminator approach. While it retains the same backbone as the first architecture, it refines its head to present an innovative mechanism for pose determination.

Output Interpretation. In contrast to the previous architecture, the network culminates in two output neurons activated by the sigmoid function. This choice ensures that the predictions are bounded within $[0, 1]$. These outputs correspond to the normalized absolute values of two novel angles: α and β .

Alpha Discriminator ($|\alpha|$). The α angle represents the azimuthal view from the car’s front position. Specifically:

- $\alpha = 0$ depicts a direct frontal view of the car.
- $\alpha = \pi$ corresponds to a direct rear view.
- $\alpha = \pi/2$ represents the left side view.
- $\alpha = -\pi/2$ equates to the right side view.

Given the absolute interpretation $|\alpha|$, it inherently serves as a front/rear discriminator. However, this absolute representation also forfeits its ability to distinguish between the car’s left and right sides.

Beta Discriminator ($|\beta|$). The β angle complements α and serves a similar function but with different reference points:

- $\beta = 0$ signifies the car’s left side (driver’s seat) view.
- $\beta = \pi$ corresponds to the car’s right side (passenger seat) view.
- $\beta = \pi/2$ indicates the car’s rear view.
- $\beta = -\pi/2$ represents the direct frontal view.

Being an absolute representation $|\beta|$, it naturally acts as a left/right discriminator, but similarly loses distinction between front and rear views.

A visualization is provided to elucidate these angles and their orientation in Figure 3.

Loss Function. The network optimizes a composite loss function derived from the binary cross-entropy (BCE) loss for both α and β predictions. Formally, the loss L is given by:

$$L = \text{BCE}(\alpha_{\text{pred}}, \alpha_{\text{true}}) + \text{BCE}(\beta_{\text{pred}}, \beta_{\text{true}}), \quad (4)$$

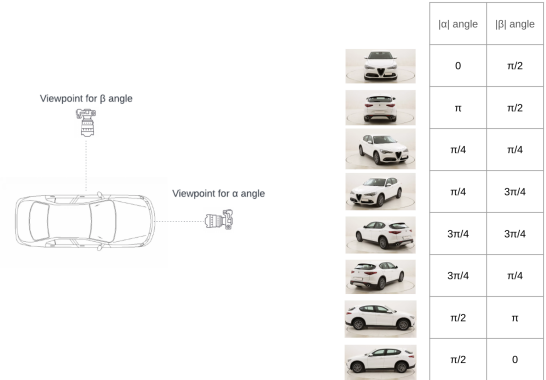


Figure 3: On the left: viewpoints visualization for the α and β angles. On the right: Viewpoint of a car and corresponding values of $|\alpha|$ and $|\beta|$.

where the binary cross-entropy (BCE) is defined as:

$$\text{BCE}(y, \hat{y}) = -\frac{1}{N} \sum_{i=1}^N [y_i \log(\hat{y}_i) + (1 - y_i) \log(1 - \hat{y}_i)], \quad (5)$$

where y represents the true labels (ground truths), \hat{y} denotes the predicted values from the network, and N is the total number of samples.

Azimuth Calculation from the Sigmoid Predictions. To estimate the azimuth φ from the sigmoid outputs, it is necessary to transform these outputs to angles within the range $[0, \pi]$.

$$\alpha_{\text{abs}}, \beta_{\text{abs}} = y_{\text{sigmoid}} \times \pi \quad (6)$$

Here, α_{abs} and β_{abs} represent the absolute angles corresponding to the front/rear and left/right discriminators, respectively. The next step is to determine the specific quadrant of the azimuth angle based on the values of α_{abs} and β_{abs} :

$$Q_1 \leftrightarrow \alpha_{\text{abs}} < \frac{\pi}{2} \wedge \beta_{\text{abs}} < \frac{\pi}{2}, \quad (7)$$

$$Q_2 \leftrightarrow \alpha_{\text{abs}} \geq \frac{\pi}{2} \wedge \beta_{\text{abs}} < \frac{\pi}{2}, \quad (8)$$

$$Q_3 \leftrightarrow \alpha_{\text{abs}} \geq \frac{\pi}{2} \wedge \beta_{\text{abs}} \geq \frac{\pi}{2}, \quad (9)$$

$$Q_4 \leftrightarrow \alpha_{\text{abs}} < \frac{\pi}{2} \wedge \beta_{\text{abs}} \geq \frac{\pi}{2}. \quad (10)$$

Having determined the quadrant, it is necessary to compute the secondary angle, $\alpha_{2,\beta}$, based on the quadrant and the value of α_{abs} and β_{abs} :

$$\alpha_{2,\beta} = \begin{cases} \frac{\pi}{2} - \beta_{\text{abs}}, & \text{if } Q_1. \\ \frac{\pi}{2} + \beta_{\text{abs}}, & \text{if } Q_2. \\ 3\frac{\pi}{2} - \beta_{\text{abs}}, & \text{if } Q_3. \\ -\frac{\pi}{2} + \beta_{\text{abs}}, & \text{if } Q_4. \end{cases} \quad (11)$$

The mean angle, $\bar{\alpha}$, is then computed by averaging α_{abs} and $\alpha_{2,\beta}$:

$$\bar{\alpha} = \frac{\alpha_{\text{abs}} + \alpha_{2,\beta}}{2}. \quad (12)$$

Lastly, the azimuth φ is obtained by adjusting the sign of $\bar{\alpha}$ based on the quadrant:

$$\varphi = \bar{\alpha} \times (-1)^{\delta(Q_3 \vee Q_4)}, \quad (13)$$

where δ is the Kronecker delta function, which assigns a value of 1 if either condition Q_3 or Q_4 is true, and 0 otherwise.

Drawbacks. The introduction of two discriminators for azimuth representation can make the network's prediction mechanism less intuitive and more intricate than the more direct sin-cos representation. Moreover, by utilizing absolute values and confining outputs to the range $[0, \pi]$, there is potential for a loss of precision in angle estimation, especially when the real angle hovers near the defined boundaries.

4.3 Evaluation Method

Viewpoint estimation, especially for automobile orientation, distinguishes itself from traditional classification tasks by predicting a continuous variable instead of categorical outputs. In this work, by decomposing the target into two variables (e.g., sin/cos or alpha/beta), it is possible to employ classical regression error metrics for evaluation. Therefore, besides the commonly used Median Error (MedErr) and Accuracy within $\pi/6$ ($\text{Acc}_{\pi/6}$), regression evaluation metrics like Mean Absolute Error (MAE), Root Mean Square Error (RMSE), and the coefficient of determination (R^2) have been incorporated, given their significance in assessing models yielding continuous predictions.

4.4 Training

4.4.1 Data Preparation

Dataset Split. The PASCAL3D+ dataset, which was employed for this research, inherently provides a train/validation split. The total number of images in the dataset amounts to 5,475. Of these, 2,763 belong to the training set, while 2,712 are earmarked for validation, representing a nearly even 50/50 split.

Data Augmentation. To boost the robustness of the trained models and to mitigate overfitting, an array of data augmentation techniques was integrated into the pipeline:

- Rotation. Images were rotated with a random angle constrained to a maximum of 10° .
- Barrel/Pincushion Distortions. These were introduced to simulate lens distortions.

- Brightness and Contrast Adjustments. Random adjustments were made to image brightness and contrast levels.
- Horizontal Flips. Images were horizontally flipped. It is essential to note that the azimuth angle needs adjustment when flipping.

Azimuth Adjustment for Horizontal Flips. When an image is flipped horizontally in the Sin-Cos approach, the sine value of the azimuth changes its sign while the cosine value remains the same. Given the original pose $[\sin(\varphi), \cos(\varphi)]$, the adjusted pose after a horizontal flip becomes:

$$[-\sin(\varphi), \cos(\varphi)]. \quad (14)$$

In the Directional Discriminators approach, the value for α remains unchanged after the horizontal flip, but the value for β is subtracted from 1. Given the original pose $[\alpha, \beta]$, the adjusted pose post horizontal flip becomes:

$$[\alpha, 1 - \beta]. \quad (15)$$

Network Backbone. For the neural network backbone, the EfficientNetB0 architecture (Tan and Le, 2019) was chosen, pre-trained on ImageNet dataset (Russakovsky et al., 2015). EfficientNetB0 is acknowledged for delivering state-of-the-art performance while maintaining a relatively compact model size. Its design philosophy makes it an ideal choice for this research, ensuring efficient training without compromising accuracy.

4.4.2 Training Parameters & Hardware Configuration

The training process was governed by the following parameters:

- Learning Rate: 5×10^{-3} ;
- Optimizer: Adam;
- Learning Rate Decay: 0.96;
- Batch Size: 32.

The models were trained for a maximum of 50 epochs. However, an early stopping mechanism was integrated to halt training if the validation performance did not improve for 7 consecutive epochs (patience parameter).

The training was facilitated on a hardware setup powered by an Nvidia Tesla T4 GPU, ensuring swift and efficient computation throughout the training process.

5 RESULTS

5.1 Quantitative Results

The quantitative assessment of the viewpoint estimation performance comprises two tables. Table 1 provides a detailed performance evaluation of the proposed methods using all five metrics—Median Error, Accuracy within $\pi/6$, Mean Absolute Error (MAE), Root Mean Square Error (RMSE), and R^2 . In contrast, Table 2 exclusively compares the proposed methodologies on the PASCAL3D+ category-specific viewpoint estimation for cars with several state-of-the-art methods using the two metrics that are widely reported in existing literature.

Table 1: Comprehensive Performance Metrics for Viewpoint Estimation Methods.

Approach	MAE	RMSE	R^2	$Acc_{\pi/6}$	MedErr
Sin-Cos	7.3	14.8	0.95	0.97	3.5
Directional Discriminators	7.2	14.5	0.95	0.97	3.4

- Comprehensive Performance Assessment.** Table 1 showcases the full breadth of performance metrics for both of the described methodologies. The Directional Discriminators approach demonstrates a slightly superior performance with an MAE of **7.2**, RMSE of **14.5**, and R^2 of **0.95**. In comparison, the Sin-Cos representation achieves an MAE of **7.3**, RMSE of **14.8**, and an equivalent R^2 score of **0.95**.
- Benchmark Achievement.** Both of the presented methodologies—the Sin-Cos representation and the Directional Discriminators approach — surpass all the prior methods documented. Remarkably, both of the described methods reach an $Acc_{\pi/6}$ score of **0.97**, which stands as the top performance among the evaluated techniques. Further emphasizing the accuracy of the proposed methods, the MedErr metric—which gauges the median error—registers its lowest values for the discussed approaches. The Directional Discriminators leads with a MedErr of **3.4**, closely followed by the Sin-Cos representation at **3.5**.
- Intra-Comparison of the Two Approaches.** A side-by-side examination of the two techniques reveals closely aligned results. The Directional Discriminators slightly outperforms the Sin-Cos representation in terms of MedErr. Nonetheless, the difference is a mere 0.1, which, in practical applications, might fall within an acceptable margin of error. This tight competition underscores the robustness and reliability of both approaches.

- Residuals Analysis.** One powerful diagnostic tool to assess the accuracy and reliability of the viewpoint prediction model is to inspect the distribution of residuals — the differences between the observed orientations and their predicted values. For a given true orientation φ and its predicted orientation $\hat{\varphi}$, the residual r is given by:

$$r = \varphi - \hat{\varphi}. \quad (16)$$

The histogram of residuals for the Directional Discriminators, shown in Table 4 approach reveals a compellingly centered distribution around 0, indicating a generally accurate prediction by the model.

However, the presence of non-zero residuals in extreme intervals such as $r < -150^\circ$ and $r > 150^\circ$ signifies occasional outlier predictions. These outliers emphasize that, despite the model’s overall strong performance, there remains room for further refinement. Such sporadic, significantly erroneous predictions underscore the need for ongoing research to perfect the model and minimize these anomalies.

Table 2: Results on PASCAL3D+ category-specific viewpoint estimation (car). $Acc_{\pi/6}$ measures accuracy (the higher the better) and MedErr measures error (the lower the better).

Method	$Acc_{\pi/6}$	MedError
(Prokudin et al., 2018)	0.91	4.5
(Su et al., 2015)	0.88	6.0
(Mousavian et al., 2017)	0.90	5.8
(Tulsiani and Malik, 2015)	0.90	8.8
(Pavlakos et al., 2017)	-	5.5
(Grabner et al., 2018)	0.94	5.1
3DPoseLite (Dani et al., 2021)	0.92	-
(Xiao et al., 2019)	0.91	5.0
(Klee et al., 2023)	-	4.9
(Nie et al., 2020)	0.92	5.1
(Mahendran et al., 2018)	0.95	4.5
Ours (Sin-Cos)	0.97	3.5
Ours (Directional Discriminators)	0.97	3.4

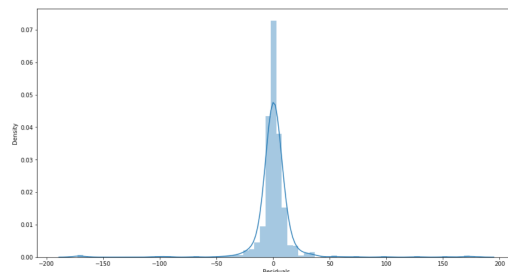


Figure 4: Residuals distribution for the Directional Discriminators approach.

5.2 Qualitative Results

PASCAL3D+ Validation Set. Figure 5 presents a 5×5 grid showcasing predictions made on the validation set of the PASCAL3D+ dataset. Each image in this grid is accompanied by an azimuth diagram situated at the right top corner, in which the predicted azimuth is marked with a red line while the ground truth is indicated by a green line. A closer inspection of the images reveals the striking proximity between the predicted and actual orientations across the majority of samples, highlighting the model’s effectiveness.

However, it is essential to recognize instances like the sample in the second row and third column where the divergence between the prediction and the ground truth is nearly 30° . Contrary to initial impressions, this deviation does not necessarily reflect an inaccuracy in the model. Upon closer inspection, it becomes evident that the ground truth provided for this particular image does not align seamlessly with the actual orientation of the car, hinting at occasional noise and inconsistencies in the PASCAL3D+ dataset. Such observations underline the importance of maintaining a critical approach when evaluating predictions, especially in the context of potentially noisy datasets.

Internet-Sourced Images. The versatility and generalizability of the proposed model are further demonstrated in Figure 6. This figure showcases a 5×5 grid of car images sourced from the internet, beyond the boundaries of the PASCAL3D+ dataset. As these images come without any associated ground truth, only the predicted azimuth, denoted by a red line, is illustrated on the azimuth diagrams. Notably, even in the absence of ground truth for comparison, the predictions appear highly plausible, resonating well with the visual orientations of the cars.

An intriguing observation from this set is the image located in the first column and fourth row, where a car is obscured by a car cover. Despite this blanket obscuring the intricate details and distinctive features of the vehicle, the model still manages to deduce the azimuth quite accurately. This exemplifies the model’s ability to generalize and make predictions based on broad contextual cues, even when faced with unconventional scenarios.

Model Interpretability and Utility. Visual results, as presented in the aforementioned figures, are vital for offering an intuitive sense of model performance. They not only establish confidence in the model’s quantitative metrics but also showcase its utility in real-world, diverse scenarios. Moreover, such qualitative results facilitate potential troubleshooting and re-

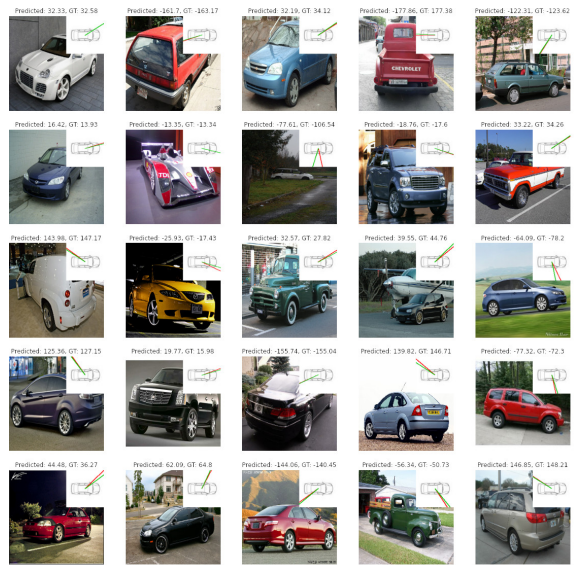


Figure 5: Sample predictions on the PASCAL3D+ validation set. Red and green lines on the azimuth diagrams correspond to predicted and ground truth azimuths, respectively.

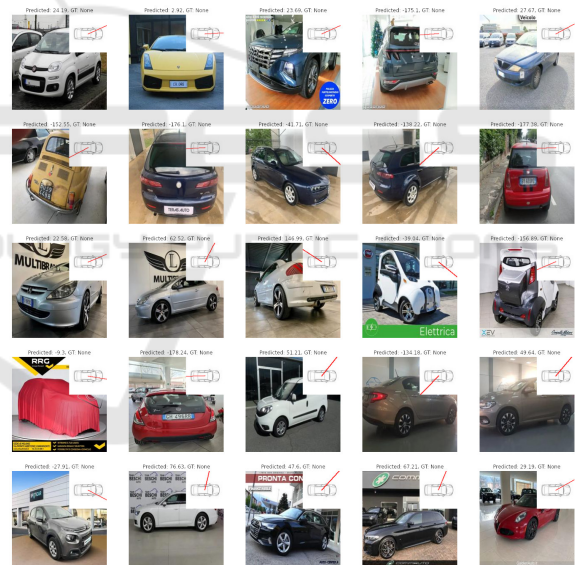


Figure 6: Sample predictions on car images sourced from the internet. Only the predicted azimuth (red line) is depicted due to the absence of ground truth.

finement strategies by revealing situations where the model might underperform or when external factors, like dataset noise, come into play.

6 CONCLUSIONS

This study has introduced two methods for car azimuth estimation, utilizing the sinusoidal properties

of orientations and directional discriminators. Both methods demonstrated state-of-the-art performance on the PASCAL3D+ dataset, with minimal performance differences under certain conditions, highlighting their practical applicability.

In terms of potential improvements, exploring a range of data augmentation techniques could enhance model robustness, particularly in real-world scenarios. Additionally, accuracy might be further refined by employing model ensembling to combine predictions from various models or iterations, thereby reducing the impact of outlier predictions.

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