Aggregating Predicted Individual Hospital Length of Stay to Predict Bed Occupancy for Hospitals

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Abstract: This paper addresses the important issue of optimizing hospital bed management by integrating machine learning-based length of stay (LoS) predictions with bed occupancy forecasting. The study primarily utilizes the MIMIC-IV dataset to compare actual bed occupancy against predictions derived from estimated LoS. A novel approach is adopted to translate individual patient LoS predictions into bed occupancy forecasts for the entire hospital. Through various simulations, the paper evaluates the effects of different error margins and patterns in LoS predictions on bed occupancy forecasting accuracy. Key findings reveal that a more symmetric error distribution in LoS predictions significantly enhances the accuracy of bed occupancy forecasts compared to merely reducing the overall prediction error. The paper makes significant contributions to the field. The paper introduces a practical translation scheme from LoS prediction to bed occupancy, which is crucial for hospital administrators in resource planning and management. Also the paper illuminates how various improvements in state-of-the-art LoS prediction models can directly impact the accuracy of bed occupancy forecasts, thereby setting clear objectives for future machine learning research.

1 INTRODUCTION

The efficient management of hospital resources, particularly bed allocation, remains a critical challenge for healthcare providers worldwide. In recent years, a considerable body of research has focused on predicting hospital length of stay (LoS) as a means to optimize patient flow and resource utilization (Baek et al., 2018; Buttigieg et al., 2018; Gentimis et al., 2017; Mak et al., 2012; Rocheteau et al., 2021; Stone et al., 2022; Lequerterier et al., 2021; Winter et al., 2023). With the advance of data science applications in the healthcare sector, researchers have used machine learning techniques to forecast LoS for individual patient’s at different points in patient’s hospital life-cycle.

For hospitals the patient’s LoS has a direct impact on the occupancy rates (Majeed et al., 2012). Other studies have examined the opposite effect that for example a high occupation in the hospital leads to longer length of stay for emergency department (ED) patients (Forster et al., 2003). Overall the relation is very straight-forward, when a patient has a longer LoS a bed in the hospital is blocked for a longer period of time. Therefore an overall lower LoS across multiple patients decreases the occupancy rates of the hospital and allows the treatment of more patients.

Currently the work on forecasting or simulating bed occupancies in hospitals is detached from the LoS prediction performed with classic machine learning methods. This gap in research presents a significant opportunity for improving hospital bed management strategies. In this paper, we focus on translating the LoS prediction for individual patients into a prediction of bed occupancy for the whole clinic. Therefore we look at state-of-the-art hospital length of stay prediction research on the MIMIC-IV data set and compare calculated bed occupancy based on the actual LoS to the calculated bed occupancy based on predicted LoS. We conduct several simulations to better understand the impact of different error margins and error curves of LoS predictions on prediction of bed occupancy. By establishing a clear linkage between
these two predictive domains, we endeavor to present a model that not only anticipates patient flow but also serves as a tool for strategic planning, ultimately contributing to improved patient care and hospital efficiency.

One core finding is that a more symmetric error distribution in state-of-the-art LoS prediction would have higher impact on predicting a bed occupancy than halving the error for all predictions in the dataset. Another finding is that in use case where we predict a bed occupancy three days in advance, using an average number of admissions and average LoS for the patients does result in poor prediction underlying the need for detailed patient by patient LoS prediction.

The remainder of the paper is structured as follows. Section 2 covers the related work on LoS prediction and bed occupancy in hospitals. Section 3 describes the used data set and the methodology to calculate occupancy. Section 4 contains experiments. Section 5 discusses the results. Section 6 concludes and provides ideas for further research directions.

2 RELATED WORK

The related work for this paper consists of research on hospital length of stay and of research on bed occupancy in hospitals. As mentioned in the introduction there has been various research using machine learning for predicting hospital length of stay. For us the main related work is the work from Winter et al. (2023) where the authors predict the stationary LoS after a patient moves from the ED to the stationary hospital units. This work also uses the MIMIC-IV data set, uses state-of-the-art machine learning models and allows an aggregation of the predicted LoS versus the actual LoS of patients. The authors also provide the model for us in order to look at the error curve and make several adjustments in our experiment.

There are of course other papers focusing on related machine learning tasks that predict LoS in different scenarios. Gentimis et al. (2017) predict the LoS after a patient leaves the intensive care unit (ICU) and Rocheteau et al. (2021) predict the remaining days in the ICU. Regarding bed occupancy there have been different research streams that can be related to our work. First, model the decisions which patients to take into the hospital and assign a bed as a queuing problem. Examples are the work from Gorunescu et al. (2002) who formulated a queuing model that can be used to schedule patients to reduce delay and the work from Belciug and Gorunescu (2015) who included an evolutionary optimization approach in their queuing. Second, using compartment models to describe the flow of patients through compartments within the total number of patients. Examples are the work from Harrison (1994) and Mackay and Lee (2005). Third, using classical time-series forecasting methods. Examples are the early work from Farmer and Emami (1990) who used ARMA models and the work of Kutafina et al. (2019) who used RNN models. Notably, Mackay and Lee (2005) has already mentioned critique on using average LoS to calculate occupancy and therefore introduced compartment modeling. Since 2005 the work on machine learning for predicting individual LoS for patient has advanced a lot. In this paper we therefore address a very important conceptual gap that combines thoughts from early research on occupancy with the power of machine learning on individual patients.
3 DATA SET AND BED OCCUPANCY

In this section, we describe the underlying dataset created from the MIMIC-IV collection and the methodology for calculating bed occupancy.

3.1 MIMIC-IV

MIMIC-IV is a centralized medical information mart, containing real-world electronic health records (EHRs) about roughly 300k patients, who visited in a total of 430k times the Beth Israel Deaconess Medical Center in Boston between the years 2008 and 2022 (Johnson et al., 2023). All data is stored separately into four different modules, namely the core, hosp, icu, and recent published ED module. Patients were de-identified according to Health Insurance Portability and Accountability Act (HIPAA) in order to ensure patient data privacy. Among others, for each patient, all dates where shifted by a randomly selected offset. Hence, dates are not real anymore, however the interval between dates for each patient is still preserved. We describe in the following selected features, how to extract these and which outliers were removed for first predicting LoS as described by Winter et al. (2023). Only data is extracted at when a patient is located at the ED, as otherwise we would consider too many information for predicting the LoS of a patient in the hospital. By removing outliers, the following statistics about selected features may differ from those listed in Johnson et al. (2023). We distinguish between demographic, medical, and triage features extracted from the MIMIC-IV database and selected four demographic ones:

- **Gender.** The gender is of type binary and extracted from the patient's relation. It is either “F” or “M”.
- **Age.** The age of a patient is extracted as well as the gender from the patients relation and is rounded to whole numbers. The distribution is depicted in Figure 1.
- **Ethnicity.** Eight different ethnicities where extracted from the admissions relation.
- **Insurance.** The insurance is extracted from the admissions relation. Approximately 15k are “medicaid”, 66k are “medicare”, and 90k are “other”.

We extracted nine different medical features from the database:

- **ICD Code.** The International Statistical Classification of Diseases and Related Health Problems (ICD) code is extracted from the diagnosis relation within the ED module. It encodes the primary diagnose of the patient that entered the ED. Within the data, 50% are ICD-9 and 50% are ICD-10 codes.
- **Admission Location.** The location of a patient prior being submitted to the hospital is extracted from the admissions relation. Patients were submitted from eleven different locations in our dataset from, among others, “walk-in/self referral” or the “physician referral”.
- **Diagnosis Count.** The total count of diagnoses were made at when a patient is located in the ED.
- **Medicine Count.** Patients are asked to provide a list of medications they currently take. We extract the count of different medications as a feature from the medrecon relation within the ED module.
- **Previous Admissions.** The total count of admissions of a patient in the past to the hospital extracted from the admissions relation.
- **Average LoS of Previous Stays.** The average LoS of previous stays extracted from the admissions relation.
- **ED LoS.** The LoS of a patient in the ED extracted from the edstays relation within the ED module.
- **LoS.** The LoS of a patient in the hospital is the target feature we aim to predict, has as well as the ED LoS an accuracy of minutes and its distribution is depicted in Figure 5.

Finally, we extracted seven different features from the triage relation within the ED module:

- **Resprate.** The patient’s respiratory rate per minute.
- **Temperature.** Measured temperature of the patient.
Figure 4: Actual Occupancy.

O2sat. Oxygen saturation of the patients blood.
SBP. Systolic blood pressure.
DBP. Diastolic blood pressure.
Pain. The pain felt during the admission. Measured between one and ten.
Acuity. The priority between one and five of how urgently the patient needs treatment.

In total, MIMIC-IV contains EHRs of 299,712 patients from which 180,733 where admitted to the hospital with 431,231 individual admissions, from which 205,504 patients entered the ED. From these patients, who entered the ED, 93,114 patients with 171,606 individual admissions are used in the final training dataset after extracting features and removing outliers. Outliers are filtered out by removing patients under the age of 18 and admissions with a LoS of more than 50 days. For us the 171,606 admissions will be the basis for all further analyses.

3.2 Bed Occupancy

Although predicting the LoS with an EHR is useful, it does not directly help hospital staff to know how many patients may be occupying the hospital within the next days. Hence, given the predicted LoS of a patient, we aim to predict the total bed occupancy for the next days. Predicting the total bed occupancy of a hospital requires access to exact dates at when a patient was admitted to a hospital. However, due to the anonymization process applied to the MIMIC-IV database, only a range of anchor years is available to indicate when a patient was admitted in the hospital as illustrated in Figure 2.

Exact dates are shifted consistently for each patient by a randomly selected offset. For instance, a patient is 50 years old in the year 2150, visited the ED in 2160-01-14 08:14:02, and visited the hospital ED somewhere in reality between the years 2008 and 2010, then the anchor_year is 2150, anchor_age is 50, anchor_year_group is 2008 – 2010, and the intime is 2160-01-14 08:14:02. Hence, it is known that at 2160-01-14 08:14:02 the patient is 60 years old when visiting the ED, however the real date at when the patient visited the ED is completely unknown. In this paper, we use the shifted the admission date to have a relative even spread over the years and map all admission dates to the real data collection period of twelve years between 2008 and 2019.

With the patients spread over the time we can calculate a corresponding bed occupancy by counting all patients that are in the hospital on that day. It is important to understand that this method implies that the individual patients LoS and the occupation are not independently measured. We cannot make any claims that say the LoS of ED patients is driving the hospital bed occupancy because we directly calculate the occupancy using the LoS. But those claims are not in focus of this paper. Instead we want to analyse how different accuracy or shapes of error curves of predicting LoS effect the accuracy or the shape of predicting bed occupancy in the process of aggregation.

The bed occupancy for one artificial year (after the shift) in the mimic database is depicted in 3 and aggregated over all years in Figure 4. It can be seen that the spread is relatively even throughout the year with occupancy ranging from 8 to 338 patients. The mean is 208.6 and the standard deviation through the year is 88.54.

4 GENERATING LOS PREDICTIONS

As described by Winter et al. (2023) and in Subsection 3.1, we approximate the LoS of a patient, given
4.1 Scenario 1 (Basis)

The basis scenario just uses the CatBoost model architecture with the hyperparameter, as listed in Table 1, and training regime from Winter et al. (2023) to generate LoS predictions. The corresponding distribution of the LoS error can be found in 6a. The mean absolute error is 2.34. The distribution has a skew resulting in an overall underestimation of the LoS.

4.2 Scenario 2 (Simulation, Symmetry)

The second scenario is a simulation that enforces the error distribution to be more symmetric. The main skew is introduced by the patients with long stay that are not predicted by the model resulting in a long tail of positive errors (errors were the actual is larger than the predicted value). To enforce symmetry, we calculate the difference in number of admissions between a positive error bucket (e.g. 5) and its corresponding negative bucket (e.g. -5) and shift half of the difference in the negative bucket by overriding the prediction with the corresponding value. Because the center is already relative symmetric we start this shift beginning at an LoS error of 3. This shift does not affect the mean absolute error of the prediction because for each admission the absolute error stays the same (only the sign has changed). The LoS error distribution can be found in Figure 6b.

4.3 Scenario 3 (Simulation, Narrow)

The third scenario is a simulation that assumes a better prediction of the LoS. It is simply taking the original LoS prediction and the actual LoS for each admission and takes the average of both values as a new prediction, thus halving the error for each admission. The resulting mean absolute error is 1.17. The LoS error distribution can be found in Figure 6c.
Figure 7: Occupancy error distributions for all four scenarios.

4.4 Scenario 4 (Simulation, Narrow, Symmetric)

The last scenario is a simulation that combines both changes. The errors are made symmetric and then halved. The resulting mean absolute error is again 1.17. The LoS error distribution can be found in Figure 6d.

5 ANALYSIS OF BED OCCUPANCY

In this section, we describe two analyses of the bed occupancy in a hospital, given four different scenarios for the predicted LoS of an admission, as described in Chapter 4. The first analysis takes an outside perspective and compares a fully predicted vs. a fully actual view. The second more realistic analysis takes a hospital administrator view and takes the time at which the prediction is made into account.

5.1 Overarching View

First we take an overarching view where we just aggregate the actual and the predicted LoS into a bed occupancy respectively and then compare the two numbers day by day. Of course that analysis reflects not how a real hospital provider would actually use the data, because at everyday there would be already some information of the patient and for the following days there would be data missing but this gives an idea about the direct relation of the two different error types.

Using the predicted LoS of a patient in Scenario 1 underestimates the bed occupancy as can be seen in the error curve in Figure 7a. This behavior is expected, as the LoS of a patient is underestimated as well. The MAE (the average daily error for bed occupancy) is 42.10 whereas the mean is 42.05 showing the skew towards underestimation.

In Scenario 2 where we enforced the symmetry, the MAE is reduced to 9.82 whereas the mean is even slightly negative. The resulting error curve in bed occupancy can be seen in Figure 7b. The view over time in 8b shows that the bed occupancy errors are now less one-sided and even slightly negative.

In Scenario 3 where the prediction was made significantly better in the simulation, the MAE is reduced to 22.20 but the skew is still present (even if it is of course also scaled down). The resulting error curve in bed occupancy can be seen in Figure 7c. The view over time in 8c shows that the bed occupancy errors have still a skew to the underestimation even though it is smaller.

In Scenario 4 where both improvements were in the simulation, the MAE is reduced to 5.78. The re-
Considering error curve in bed occupancy can be seen in Figure 7d. The view over time in 8d shows the most balanced errors in both directions.

### 5.2 Time-Dependent View

The more realistic scenario involves a hospital administrator using a LoS prediction in real-world conditions. At a fixed point in time, $t_n$, the administrator seeks to forecast hospital occupancy for a specific future date, $t_{n+i}$, $i$ days ahead.

In practice, predictions can only utilize data within the time range $(t_0, t_n)$. The LoS is calculated for patients admitted between $(t_0, t_n)$ who have not yet been discharged. By summing the estimated number of patients likely to be in the hospital at $t_{n+i}$, one can approximate the bed occupancy for that date. This estimation can be refined by considering the average number of patients admitted post $t_n$ and their likelihood of remaining in the hospital at $t_{n+i}$.

In the following example, at each $t_n$, the hospital administrator aims to predict the patient count for $t_{n+3}$, i.e., three days later. This involves forecasting the LoS for patients currently in the hospital at $t_n$ and estimating the average admissions between $(t_{n+1}, t_{n+3})$, including those likely to stay at least until $t_{n+3}$, as illustrated in Figure 10.

On average, 40.85 patients are admitted daily, and their LoS distribution is shown in Figure 5. As indicated in Figure 10, of the daily 40.85 average admissions, 22.05 are expected to remain in the hospital at least until $t_{n+3}$. By $t_{n+2}$, an average of 29.00 patients will likely stay for at least one more day, thus still present at $t_{n+3}$. Additionally, 40.85 patients are projected to be admitted on $t_{n+3}$ itself. Therefore, the forecasted patient count at $t_{n+3}$ is the sum of these figures, plus the number of patients in the hospital at $t_n$ expected to stay until $t_{n+3}$.

Scenario 1’s predicted LoS tends to overestimate bed occupancy at $t_{n+3}$, with a mean error of $-5.99$, as depicted in Figure 9a. Scenario 2, shown in Figure 9b, demonstrates a slightly improved mean absolute error (MAE) compared to Scenario 1, but with a higher mean error of $-13.44$. In Scenarios 3 and 4, illustrated in Figure 9c and Figure 9d respectively, the mean error is lower, although the MAE is marginally worse than in Scenarios 1 and 2.

Overall, the error across all four scenarios is
(a) Occupancy error with a forecast of three days with filling from LoS distribution with Mean = $-5.99$ and MAE = 29.87.

(b) Occupancy error with a forecast of three days with filling from a symmetric LoS distribution with Mean = $-13.44$ and MAE = 28.30.

(c) Occupancy error with a forecast of three days with filling from a narrowed LoS distribution with Mean = 4.13 and MAE = 34.08.

(d) Occupancy error with a forecast of three days with filling from a symmetric and then narrowed LoS distribution with Mean = $-2.74$ and MAE = 31.57.

Figure 9: Time dependent occupancy error distribution with a forecast of three days.

Figure 10: Occupancy filling at $t_0$ for predicting bed occupancy at $t_3$ with $22.05 + 29.00 + 40.85 = 92$ patients being in average additionally at the hospital at $t_3$ nearly identical, stemming from the assumption that the number of patients admitted post $t_n$ and present at $t_n+3$ is a constant, estimated at 92. An overview of all four scenarios, including the overarching and time-dependent view, can be found in Table 2.

6 DISCUSSION OF THE RESULTS

When we examine the MAE across the four scenarios from an overarching perspective, it becomes evident that reducing the skew in predicting hospital LoS has a more significant impact on the accuracy of bed occupancy forecasts than halving the distance between all predictions and actual values. Although this general effect might have been anticipated, its extent is quite remarkable. For hospital providers, managing occupancy is more crucial than predicting individual LOS for patients. Hence, focusing on these real-world aggregations and their improvement is essential. In a generalized view, it is clear that more emphasis should be placed on creating a more symmetric error curve rather than solely enhancing accuracy. This symmetry also affects the occupancy error over time, as illustrated in Figure 8. A more balanced error curve, with equal under- and overprediction, could facilitate hospital administrators in optimally scheduling elective procedures during periods of lower-than-expected bed occupancy.

In the time-dependent analysis, the errors appear relatively consistent across all scenarios. Due to the large number of patients with short LoS, using the average number of patients with average LoS significantly impacts bed occupancy predictions for the following three days, proving this method to be an inadequate predictor. These findings highlight the importance of using individual patient-based LoS predictions for accurate bed occupancy forecasting. Relying solely on averages omits crucial information. For future predictions, where upcoming patient admissions are unknown, additional research should consider seasonal or other factors to better estimate the number and types of incoming patients.
Table 2: Overview of all four scenarios including the overarching as well as the time dependent view (*actual LoS of 0 left out).  

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<tr>
<th>Scenario</th>
<th>Mean</th>
<th>MAE</th>
<th>MAPE</th>
<th>Mean</th>
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7 CONCLUSION

Overall we made three major contributions in the paper. First, we introduced a translation scheme from well-researched LoS prediction to the bed occupancy that is needed for a hospital administrator to work with. Second, we show-cased how different improvements in the state-of-the-art LoS prediction would impact the accuracy of the bed occupancy prediction and thus gave clear tasks for further research in the machine learning community. Third, we discussed a time-depended hospital administrator view, that showed the importance of individual information about patients for adequately predicting a realistic bed occupancy.

There are a couple of further research questions that can be tackled based on this paper. One future research direction is to include more intelligent handling of the time-depended view, i.e. a better way of including yet unknown patients based on seasonal or other time-depended patterns. Another research direction would be to validate the approach in a clinic where patient’s LoS is recorded independently from bed occupation. There might be effects (e.g. blockings, room dependencies, etc.) that lead to a more noisy relationship between LoS and bed occupancy than assumed in this paper which could be interesting to research. Additionally, not only CatBoost should be considered as a model to predict the LoS of a patient’s admission and it would be interesting to test different models on different datasets. Many factors have a high impact on the LoS of a patient’s admission, as shown by Winter et al. (2023), where some are directly available in the dataset and others are engineered from available features in the dataset. However, some are hidden in the hospitals policies, staffing levels, etc. which are not available in the data. In the future, we aim to collaborate with an hospital on an interdisciplinary level, ensuring these factors are thoroughly considered and addressed.

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