# Error Analysis of Aerial Image-Based Relative Object Position Estimation 

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#### Abstract

This paper presents a thorough analysis of precision and sensitivity in aerial image-based relative object position estimation, exploring factors such as camera tilt, 3D projection error, marker misalignment, rotation and calibration error. Our unique contribution lies in simulating complex 3D geometries at varying camera altitudes ( $20-130 \mathrm{~m}$ ). The simulator has a built-in unique mathematical model offering an extensive set of error parameters to improve reliability of aerial image-based position estimation in practical applications.


## 1 INTRODUCTION

Over the last decade, the development of safer transportation has become an important endeavour. New requirements were imposed on manufacturers to improve safety, increase comfort, and optimize energy consumption. Therefore, the need for further traffic analysis has increased, focusing on traffic participants. However, using conventional methods like radar- or LiDAR-based approaches, the analysis is an expensive and time-consuming process.

Computer Graphics (CG) is often applied to simulate the urban environment for the testing of autonomous vehicles. A popular open-source tool is the CARLA simulator (Dosovitskiy et al., 2017) that uses the Unreal Engine. Although CG-based tools can generate specious pictures and videos, they do not produce realistic recordings in many cases, especially for range sensors like LiDAR or radar devices.

Traffic analysis, including relative object position estimation, can be solved by a new aerial image-based approach as well, which is a less expensive solution since one downward looking camera is enough to have a broad view of the traffic.

This paper collects and analyzes the different er-

[^0]ror factors of aerial image-based relative object position estimation by simulating their effect on accuracy. We determine the theoretical accuracy of this new approach and whether aerial imagery could replace or complete the classical methods. Our results can foster the development and validation of aerial image-based relative object position estimation.

## 2 RELATED WORK

The task of object pose estimation in aerial imagery has gained attention in recent years due to its wide range of applications, i.e., autonomous navigation and surveillance (Krajewski et al., 2018; Nguyen et al., 2022; Nieuwenhuisen et al., 2016; Organisciak et al., 2022; Patoliya et al., 2022). Thus, evaluating the limitations, accuracy, and sensitivity of ADAS systems is essential to ensure their effective and responsible deployment in real-world scenarios.

Most pose estimation methods rely on a multimodal sensor input that provides 3D information of the surroundings. (Kucharczyk et al., 2018) showed that utilizing LiDAR point clouds, 2 and 8 cm horizontal and vertical class-level accuracy can be achieved while mapping a static environment. However, various scenarios require continuous localization of dynamic objects over time. This can be resolved only by using data with high temporal granularity. Apart from the data quality, high energy con-
sumption of 3D sensing devices cannot be neglected either (Wang, 2021). In this paper, we present accuracy analysis on aerial imagery, hence considering only high-resolution, energy-efficient solutions.

While there are several works on the sensitivity and accuracy of image-based aerial pose estimation, considering perspective mapping (Collins, 1992; Hartley and Zisserman, 2003), motion prediction (Dille et al., 2011) and uncertainty in sensor position (Nuske et al., 2010). The work that served as a solid reference for this report was written by (Babinec and Apeltauer, 2016), who studied the errors caused by the real world elevation, the positional inaccuracy of the landmarks, and the distortion caused by the camera.
Contributions. Beyond these factors, we analyze the errors caused by the 3D geometry of the target objects, possible camera tilts, and the uncertainty of camera position. This allows a more realistic approach for dynamic scenarios. Finally, unlike other works, we consider a wide range in altitudes (20130 m ), enabling a much wider field of view and a comprehensive comparison in projection errors.

## 3 OUR METHOD

This section outlines the basic virtual environment and the working principles of the simulator.

First, we model a 3D environment: a traffic participant and a marker (e.g. checkerboard) are defined by their 3D model and 3D position. The camera is modelled by its intrinsic and extrinsic parameters, see Eqs. 1-4.

Second, the image capturing is modelled by a 2 D projection using a pinhole camera model. This step projects the corner points of the original 3D object to the 2D image plane, i.e. to pixel coordinates based on the defined camera parameters (Figure 2). Also considering camera distortion and/or camera tilt.

The third step is the simulation of the object detection within the image, i.e., the determination of the 2 D rotated bounding box, defined as the minimal-area rectangle that covers the contour points of the object.

Finally, the simulator maps the objects back to the original world coordinate system and compares their original and new position. The Euclidean distance between their center points gives the error.

### 3.1 Initialization of 3D Environment Camera and Vehicle Models

In the initialization phase, the parameters and positions of the camera, the traffic participants and the
marker are defined as well as the the world scene topography.

A general camera model is given by its intrinsic and extrinsic parameters. The intrinsic parameters are the focal length $f_{x}, f_{y}$ and the principal point $c_{x}, c_{y}$, which can be written in the form of the camera matrix.

$$
K=\left[\begin{array}{ccc}
f_{x} & 0 & c_{x}  \tag{1}\\
0 & f_{y} & c_{y} \\
0 & 0 & 1
\end{array}\right] .
$$

The extrinsic parameters are represented by the 3D rotation matrix $\mathbf{R}_{c}$ and the 3D translation vector $t_{c}$. For the 3D-2D projection, a pinhole camera model is used, described by the following equation:

$$
\left[\begin{array}{c}
u  \tag{2}\\
v \\
1
\end{array}\right]=K\left[\mathbf{R}_{c} \mid t_{c}\right]\left[\begin{array}{c}
x \\
y \\
z \\
1
\end{array}\right],
$$

where $\left[\begin{array}{ll}u & v\end{array}\right]^{T}$ and $\left[\begin{array}{lll}x & y & z\end{array}\right]^{T}$ are the pixel and spatial coordinates, respectively. Radial and tangential distortions were also assumed which can be given with five parameters. The related equations are as follows:

$$
\begin{array}{r}
u_{d i s t}=u\left(1+\kappa_{1} r^{2}+\kappa_{2} r^{4}+\kappa_{3} r^{6}\right)+ \\
2 p_{1} u v+p_{2}\left(r^{2}+2 u^{2}\right) \tag{3}
\end{array}
$$

$$
\begin{array}{r}
v_{d i s t}=v\left(1+\kappa_{1} r^{2}+\kappa_{2} r^{4}+\kappa_{3} r^{6}\right)+ \\
p_{1}\left(r^{2}+2 v^{2}\right)+2 p_{2} u v \tag{4}
\end{array}
$$

where $r=\|\mathbf{u}-\mathbf{c}\|, \mathbf{u}=\left[\begin{array}{ll}u & v\end{array}\right]^{T}, \mathbf{c}=\left[\begin{array}{ll}c_{x} & c_{y}\end{array}\right]^{T}$, the $\kappa$ and p coefficients are the radial and tangential components of the distortion model, respectively.

By default, the camera is looking downwards from altitude $h_{c}$ in bird's-eye view (Figure 3). If this is not the case, and the camera has a tilt (pitch $\mathbf{R}_{y}(\beta)$ or roll $\mathbf{R}_{x}(\gamma)$ ), then the projection error will increase in most of the cases due to the perspective view.

In the simulation, the virtual environment has a flat surface, elevated topography was not modelled yet.

The traffic participants are defined by their 3D model and 3D position. Thus, cars are represented not only by one rectangular cuboid, but by a more complex car-like design - based on a commercial vehicle, with different shapes on different z levels (Figure 1). The lowest point of the vehicle, i.e. the wheel, should always be on the ground. Therefore, its position can be represented by 2D rotation $\mathbf{R}_{o}$ and 2D translation $t_{o}$ on the $\mathrm{x}-\mathrm{y}$ plane. In this paper a single car is used as traffic participant, but any object (pedestrian, twowheeler) can be used assuming an approximate 3D model.

The ideal marker is a 2D planar object, which has an altitude $h_{m}$ and a pattern definition. Ideally, its


Figure 1: Abstract 3D representation of the vehicle.
center point should be placed in the origin, its edges should be parallel with axes $x$ and $y$, and its plane should be perpendicular to axis $z$ (Figure 6). Bias can occur while installing the marker, so it can be tilted, rotated and translated.
The rotation around axis $z$ is called yaw and it can be described by $\mathbf{R}_{z}(\alpha)$ (Eq. 5). Rotation biases around axes $y$ and $x$ are called pitch $\mathbf{R}_{y}(\beta)$ and roll $\mathbf{R}_{x}(\gamma)$, respectively (Eqs. 6 and 7).

$$
\begin{align*}
& \mathbf{R}_{z}(\alpha)=\left[\begin{array}{ccc}
\cos (\alpha) & -\sin (\alpha) & 0 \\
\sin (\alpha) & \cos (\alpha) & 0 \\
0 & 0 & 1
\end{array}\right]  \tag{5}\\
& \mathbf{R}_{y}(\beta)=\left[\begin{array}{ccc}
\cos (\beta) & 0 & \sin (\beta) \\
0 & 1 & 0 \\
-\sin (\beta) & 0 & \cos (\beta)
\end{array}\right]  \tag{6}\\
& \mathbf{R}_{x}(\gamma)=\left[\begin{array}{ccc}
1 & 0 & 0 \\
0 & \cos (\gamma) & -\sin (\gamma) \\
0 & \sin (\gamma) & \cos (\gamma)
\end{array}\right] \tag{7}
\end{align*}
$$

### 3.2 Simulator Working Principles, Applied Camera and Vehicle Models

After the parameter initialization of the environment, the image creation has to be simulated. This is done by applying the central projection camera model, so the simulator program projects the 3D metric coordinates of the traffic participant onto the 2D image plane pixel coordinates (Eqs. 2-4). The projection is visualized in Figure 2. Its accuracy depends on the type of the camera lens and its parameters.

After detection in the image, the objects can be represented by minimum area rectangular boxes on the image, also known as rotated bounding boxes. This object representation is shown with a blue


Figure 2: Projection from the 3D world (left side) to the 2D image plane (right side) using the central projection camera model. Vehicle and marker feature points are visualized by filled circles. Best viewed in color.
bounding box in Figure 4. It can be observed that the original (red) and the projected (yellow) bounding boxes does not completely coincide. This is caused by the projection error, which is dependent on the camera altitude, the distance between the traffic participant and the camera, the shape of the traffic participant (height and angularity), and the camera tilt.

Even though the traffic participant is represented by a bounding box on the image plane, the position of this box is unknown in the original "real-world", metric coordinate system. Therefore it cannot be compared to the original object position. The current and the following paragraphs will explain the pixel to meter conversion and the backmapping, based on the marker pattern and position. It allows to determine the position of the traffic participants in the original coordinate system. To perform the pixel to meter conversion, the pixel per meter ratio has to be calculated, based on the original and projected marker pattern. However this calculation is not enough in itself, because the marker could lay higher than the ground level. In this case the pixel per meter ratio will define only the ratio on the marker level, not on the ground level, where the distance between the real and projected object (i.e., the error) is calculated. Section 3 highlights that the final error-distance measurement is done on the ground level on $z=0$ because during the projection all object points were projected there. Thus, the pixel per meter ratio needs to be adapted accordingly by the compensation of the pattern altitude. This can be done by the following equation:

$$
\begin{equation*}
\lambda_{z}=\frac{h_{c}-h_{m}}{h_{c}} \lambda_{m}, \tag{8}
\end{equation*}
$$

where $\lambda_{m}$ is the pixel per meter ratio on the marker level, $h_{m}$ is the marker height, $h_{c}$ is the camera height, and $\lambda_{z}$ is the pixel per meter ratio on the ground level. Equation 8 is based on similar triangles as Figure 3 shows. The accuracy of the pixel per meter ratio cal-


Figure 3: Adaptation of the pixel per meter ratio to the ground level.
culation depends on the accuracy of the pattern recognition, the marker altitude positioning, and marker horizontality. Thus, uncertainty in any of these factors introduces pixel per meter ratio error, which in turn results in center point distance error. The pixel per meter ratio error $\lambda_{e}$ can be defined by the difference between the real $\lambda_{r}$ and calculated pixel per meter ratio $\left(\lambda_{z}\right)$ (Eq. 9).

$$
\begin{equation*}
\lambda_{e}=\lambda_{z}-\lambda_{r}, \tag{9}
\end{equation*}
$$

After the pixel per meter ratio on plane $z=0$ is calculated $\left(\lambda_{z}\right)$, the coordinates of all object points can be converted from pixels to meters (Eq. 10).

$$
\left[\begin{array}{c}
u^{\prime}  \tag{10}\\
v^{\prime}
\end{array}\right]=\lambda_{z}\left[\begin{array}{l}
u \\
v
\end{array}\right] .
$$

The next step is backmapping, which will determine the position of the new bounding box in the original coordinate system. It is important to note that the detected marker position is not necessarily in the origin of the picture, as it was in the original coordinate system, because the camera is not necessarily above the origin or because the marker could be translated and rotated as well. The difference between the real and the detected marker positions define the backmapping transformation. This is shown in the following equation:

$$
\left[\begin{array}{c}
u^{\prime \prime}  \tag{11}\\
v^{\prime \prime} \\
w^{\prime \prime}
\end{array}\right]=-\left(\mathbf{R}_{m z}(\alpha) \mathbf{R}_{m y}(\beta) \mathbf{R}_{m x}(\gamma)\right)\left[\begin{array}{c}
u^{\prime}-m_{c p x} \\
v^{\prime}-m_{c p y} \\
0
\end{array}\right],
$$

where $m_{c p x}$ and $m_{c p y}$ are the center point coordinates of the detected marker and $\mathbf{R}_{m z}(\alpha) \mathbf{R}_{m y}(\beta) \mathbf{R}_{m x}(\gamma)$ represents the initial rotation bias of the marker.

The backmapping is shown in Figure 4, where the real-world coordinate system is marked with dashed red arrows, with origin $[0,0,0]$, and the red bounding box represents the real position of the traffic participant. Figure 4 demonstrates a setup where initially a marker rotation bias occurred, demonstrated with an orange $\alpha$ angle. This caused a rotation bias in the position of the new (blue) bounding box during backmapping (blue $-\alpha$ angle) on top of the already existing projection error. The orange arrows represent the coordinate system of the initially wrongly placed


Figure 4: Center points distance error caused by marker rotation bias during backmapping.


Figure 5: Simulation of center points distance error caused by projection error and marker-rotation bias.
marker, with $\alpha$ rotation bias compared to the correct orientation, and the orange bounding box shows the position of the projected traffic participant. Due to the initial marker placement bias, a rotation error with $-\alpha$ angle occurs on the orange bounding box, while it is backmapped to the original coordinate system. The result is the blue boundig box. The precision of the backmapping depends on the precision of the initial marker placement, as marker translation and rotation bias can introduce an elementary error to the system.

Finally, the positions of the bounding boxes can be compared and the difference can be calculated. It is important to highlight that the comparison has to be done on ground level, because all object points were previously projected there and hereby lost their 3D representation. The error is defined by the distance between the center point of the the real and measured bounding boxes as

$$
\text { Error }=\left\|\left[\begin{array}{l}
u  \tag{12}\\
v \\
0
\end{array}\right]-\left[\begin{array}{c}
u^{\prime \prime} \\
v^{\prime \prime} \\
0
\end{array}\right]\right\|_{2} .
$$

Figure 5 shows the visual output of the simulator in a similar scenario as Figure 4, simulating a projection error and an initial marker rotation bias.


Figure 6: The visualization of error types.
The most important error factors influencing the position estimation accuracy are collected in Section 4. Their effects are analysed in Section 5 by using the simulator program.

## 4 ERROR TYPES

There are two main considerations behind the choices: (1) focus exclusively on factors relevant to visual sensors, (2) maintaining a level of generality that keeps our approach more widely usable within the visual sensing domain. The studied error types and their effect on position estimation accuracy are pictured in Figure 6.
Uncertainty of the Marker Altitude. If there is a difference between the real and the hypothetical marker altitudes, where the altitude is measured from the ground level, it leads to an error in the pixel per meter adaption algorithm, which causes a biased pixel per meter ratio, which finally causes the center point distance error (unless the center point of the car is directly in the origin).
Marker positioning bias may occur during marker installation and calibration. A wrongly calibrated marker directly causes an error during the mapping of the coordinate system, and results an elementary center point distance error.
Non-parallel planes can be caused by a not directly downward looking camera (non $90^{\circ}$ ), by a steep scene topography, by a tilted marker installation, or by the combinations of these factors. This paper focuses on the simulation of camera and marker tilt, which causes the same error as a plane with a slope.
Unknown 3D Structure of the Projected Objects. Traffic participants are modelled in 3D (Figure 1), causing a projection error. In the absence of a precise model, this error cannot be compensated, thus leading to misalignment (Figure 4 red - orange boxes). This error increases with larger perspective angle, i.e.,

Table 1: Experiment parameters.

| Parameter | $\mathrm{x} / \gamma$ | $\mathrm{y} / \beta$ | $\mathrm{z} / \alpha$ |
| :--- | :---: | :---: | :---: |
| Camera pos. | $0-50 \mathrm{~m}$ | $0-50 \mathrm{~m}$ | $0-130 \mathrm{~m}$ |
| Camera tilt | $0-180^{\circ}$ | $0-180^{\circ}$ | $0-180^{\circ}$ |
| Object pos. | $0-50 \mathrm{~m}$ | $0-50 \mathrm{~m}$ | - |
| Marker pos. bias | $0-1 \mathrm{~cm}$ | $0-1 \mathrm{~cm}$ | $0-1.5 \mathrm{~cm}$ |
| Marker rot. bias | $0-3^{\circ}$ | $0-3^{\circ}$ | $0-3^{\circ}$ |

when the object is at the edge of the image, or when its height relative to the camera altitude is larger.
Camera distortion depends on the camera lens type and quality. It leads to wrong pixel per meter ratio and to distorted object outlines, especially on the edge of the image. It can be compensated by camera calibration methods.

## 5 EXPERIMENTAL RESULTS

In this section, the previously collected error types are simulated and their effects on the position estimation accuracy are visualized and evaluated.

The error of accuracy is measured in two ways, applying the pixel per meter error (Eq. 9) and the distance of the original and back-projected-back-mapped traffic participant center points (Eq. 12), where the center point is defined in a way that it means the center point of the minimum area rectangle around the traffic participant outermost corner points.

The experimental parameters and ranges are summarized in Table 1.

### 5.1 Error due to the Uncertainty of the Marker Altitude

In this section, the center points distance error and the error of pixel per meter ratio are simulated and analysed, caused by the marker-altitude uncertainty. All other error factors are zero.
Marker Below the Camera. The marker altitude uncertainty causes a linear pixel per meter ratio error, but does not cause any center point differences errors. Even tough the outline increases, it increases centrally, therefore the center point remains in position.
Marker Not below Camera. In the next setup, we fixed the marker altitude uncertainty to 0.06 m . The camera and the traffic participants are moving together along axis x . Thus, no projection error occurs. In this case, the constant marker-altitude uncertainty causes constant pixel per meter ratio error, regardless of the distance between the marker and the camera. However, the center points difference error increases linearly as the camera distance increases.

### 5.2 Error due to Marker Positioning

In this section we analyse the center points distance error and the pixel per meter ratios error, caused by the marker positioning biases, while keeping other error factors zero.

### 5.2.1 Marker Translation Bias

Three different marker translation biases were studied. Based on the simulator results, translation applied to the marker separately or combined into directions $x$ and $y$ does not affect the pixel per meter ratio. However, increasing its distance from the center point causes a linear growth in the error.

### 5.2.2 Marker Rotation Bias

Five different marker-rotation biases are simulated. They are visualized with different graph colors, yaw blue, pitch - orange, roll - green, yaw and pitch at the same time - red, yaw and pitch and roll at the same time - purple.
Close to Camera. The following figures show the simulation of errors caused by marker-rotation bias, where the marker is laying in position [ $0,0,0.2$ ] but the camera and the vehicle position is not above the origin, but in $[2,0]$.

(a) ppm. ratio error

(b) cp. dist. error

Figure 7: Pixel per meter ratio error (a), center points distance error (b) caused by marker rotation bias, close to cam.

Figure 7a highlights the pixel per meter ratio error w.r.t marker-rotation biases around the $x ; y ; z ; x y$; $x y z$ axes. Whereas Figure 7b shows the center point differences w.r.t. same rotation biases.
Far from Camera. Figure 8 shows the errors caused by marker-rotation biases, where the marker is originally laying in position $[0,0,0.2$ ], while the camera and the vehicle position is not in origin, but in $[10,0]$.

(a) ppm . ratio error

(b) cp. dist. error

(c) cp. dist. error

Figure 8: Pixel per meter ratio error (a) and center points distance error (b,c) caused by marker rotation biases.

Figure 8a shows the pixel per meter ratio error tendency depending on the marker-rotation around the $x ; y ; z ; x y ; x y z$ axes. Figure 8b shows the center point differences tendency regarding the same rotations. Figures 8a and 8b show that the most significant error is caused by the rotation bias around $z$ axis (yaw). Figure 8 c shows the center points distance error tendency in a wider rotation angle range.

Two conclusions can be drawn from Figures 7 and 8. First, the center points distance error increases when the marker-rotation bias increases. Second, this error is even greater when increasing the distance between the vehicle and the origin. At a distance of 30 m from camera, even a one-degree marker yaw deviation adds another 31 cm error. This happens because the distant objects move on a longer arc.

### 5.2.3 Marker Rotation Bias with Fixed Translation

The following section shows the simulation of errors caused by marker-rotation bias with fixed 0.02 m marker translation bias along axis $x$.

The marker is laying in position $[0.02,0,0.2]$ and the marker rotation biases around axes $x ; y ; z ; x y ; x y z$ are swept, the camera position is in $[10,0,100]$, the vehicle is directly below the camera. All of the other error factors are zero.

(a) ppm . ratio error

(b) cp. dist. error

Figure 9: Pixel per meter ratio error (left) and center points distance error (right) caused by marker rotation bias by axis with a fixed marker translation bias, far from the camera.

Figure 9 shows similar behavior as Figure 7. It is important to note that the most significant error is caused by rotation, not by the translation bias, which has a large effect on accuracy of distant objects.

### 5.3 Error due to Non-Parallel Planes

In this section the errors caused by non-parallel planes will be presented that occurs due to different tilts.
Marker Tilt. Marker pitch and roll tilts cause nonparallel plane problem. These errors are already simulated in Section 5.2.2.
Camera Tilt. The experiments include camera tilt on the roll, pitch and yaw axes. Figure 11 shows that


Figure 10: Center points distance error caused by the 3D-2D perspective projection, from different camera altitudes.


Figure 11: Center points distance error caused by different camera tilts, directly above the marker.
the final center points distance error increases with increasing angle values.

### 5.4 Error due to Unknown 3D Structure

In this section the bounding box center points distances are analysed, depending on the vehicle position and camera (lowered) altitude.

Since the traffic participants are modelled in 3D, see in Figure 1, it affects their position estimation from perspective view (because of projection error). In the absence of a precise 3D model, this error cannot be compensated by back-projection and leads to bounding box misalignment. In order to demonstrate it, the vehicle is moved around the scene with fixed camera position above the origin. By applying a lower camera altitude, the perspective view increases, leading to a growth for projection and center point difference error. This is showed on Figure 10 with camera altitudes of $130 \mathrm{~m}, 90 \mathrm{~m}, 40 \mathrm{~m}$ and 20 m .

### 5.5 Error due to Camera Distortion

Two types of camera distortion are analyzed in this section, that are barrel and pincushion distortions. They occur by non calibrated cameras, depending on the camera lens type and quality.

Figure 12 shows the applied camera distortions in the simulator. Note its comparison with the second plot in Figure 10, where no distortion was applied. They have the same scaled color bars and they are simulating the same scenario from 100 m altitude. It can be concluded that the camera distortions increase


Figure 12: Center points distance error due to barrel (left) and pincushion (right) camera distortions across the scene.
the error, especially on the edges, highlighting the importance of the proper calibration of the camera.

### 5.6 Complex Scenarios

In this section, the bounding boxes center points distance error are simulated in real, complex scenarios, defined by the parameters listed in Table 1.

Several scenarios are covered in order to form the final conclusions. Three scenarios are highlighted in Table 2 which demonstrates: (a) the robustness of the system in close camera range with huge biases (visualised in Figure 13a), (b) perspective distortion from low camera altitude (visualised in Figure 13b), (c) close camera range, with realistic biases.

Table 2: Complex scenarios parameters.

| no. | cam. <br> pos. <br> $[x, y, z]$ | veh. <br> pos. <br> $[\mathrm{x}, \mathrm{y}]$ | cam. <br> rot. <br> $[\alpha, \beta, \gamma]$ | marker <br> transl. bias <br> $[\mathrm{x}, \mathrm{y}, \mathrm{z}] 10^{-2}$ | marker <br> rot. bias <br> $[\alpha, \beta, \gamma]$ | cp. <br> distortion <br> error |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| a) | $[0,0,100]$ | $[3,0]$ | $[0,0.7,0]$ | $[1,1,1.5]$ | $[3,0,0]$ | 17.2 cm |
| b$)$ | $[0,0,30]$ | $[10,0]$ | $[0,0,0]$ | $[0,0,0]$ | $[0,0,0]$ | 21.19 cm |
| c) | $[0,0,100]$ | $[3,0]$ | $[0,0.7,0]$ | $[1,0,0]$ | $[1,1,0]$ | 4.82 cm |



Figure 13: Center point distance error in complex scenarios.

## 6 CONCLUSION AND FUTURE WORK

Through a systematic experimental setup, covering diverse scenarios, we identified key factors influencing the accuracy of aerial image-based relative object position estimation, including plane misalignment, 3D structure uncertainties and calibration errors. We developed mathematical models, and used them in a unique simulator that allowed us to conclude the followings.

Our main contribution is the evaluated projection error of 3D-modelled traffic participants. We showed that the distortion originating from this factor is minimal, when the object is below the camera (nadir) and increases as the object moves away from the camera.

We also demonstrated that, the initial angular misalignment of the marker and camera causes a significant error. Thus, a precise calibration is crucial for aerial image-based positioning, especially for longrange applications.

Setting the distortion and bias parameters to values that correspond to practically relevant use cases, we found that in near range, the error of aerial imagebased relative object position estimation is less than 10 cm . Thus, under the aforementioned circumstances, the novel approach can achieve a precision comparable to other, more complex, radar or LiDARbased methods. To reach a better precision, or a similar precision for a wider range, one can use, for instance, complex camera systems.
Future Work. In this stage, the simulator is ready to build up a simple 3D world-model and simulate basic error factors. Further developments can lead to a more realistic simulated environment, including topography; different weather conditions (rain/fog); random noise. More realistic camera models can be implemented, considering resolution, field of view, and gimbal stabilization biases. Finally, more sophisticated error metrics can be developed for further analysis.

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