

# Alias-Free GAN for 3D-Aware Image Generation

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**Abstract:** In this work we build a 3D-aware generative model that produces high quality results with fast inference times. A 3D-aware model generates images and offers control over camera parameters to the user, so that an object can be shown from different viewpoints. The model we build combines the best of two worlds in a very direct way: alias-free Generative Adversarial Networks (GAN) and a Neural Radiance Field (NeRF) rendering, followed by image super-resolution. We show that fast and high-quality image synthesis is possible with careful modifications of the well designed architecture of StyleGAN3. Our design overcomes the problem of viewpoint inconsistency and aliasing artefacts that a direct application of lower-resolution NeRF would exhibit. We show experimental evaluation on two standard benchmark datasets, FFHQ and AFHQv2 and achieve the best or competitive performance on both. Our method does not sacrifice speed, we can render images at megapixel resolution at interactive frame rates.

## 1 INTRODUCTION

3D-aware image generative models aim to generate 2D images in a way that the viewpoint is controllable by the user, the camera parameters can be specified at inference time. Generative Adversarial Networks (GANs) (Goodfellow et al., 2014) can be used to solve this task, where a generator is combined with a renderer to produce an image. GAN training can be unsupervised, only an image collection of unrelated samples and no ground truth labels are required. However, there is no out-of-the-box solution, the task is very challenging. The details of the GAN architecture, the renderer and the 3D representation and the interplay between these modules matter a lot. In this work we propose a novel design for a 3D-aware GAN that combines the best practices of modern 2D and 3D models. It is alias-free, produces high-resolution results, is 3D-aware and has fast inference time.

The first 3D-aware GANs build on explicit 3D representations, for example voxels (Gadelha et al., 2017) and meshes (Szabó et al., 2019). More recent work (Chan et al., 2021), (Chan et al., 2022) then used volumetric rendering and a Neural Radiance Field (NeRF) (Mildenhall et al., 2022) renderer.

Compared to voxel- and mesh-based methods,

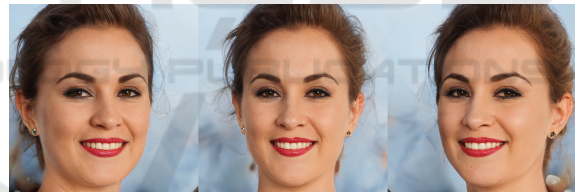


Figure 1: An example result of our model, three images rendered under three different viewpoints that are manually chosen. The images are of high-quality with no visible artefacts and high-resolution. Our 3D model is trained using unlabelled 2D images without any knowledge of viewpoints at training time. In contrast to previous work, it does not employ any task-specific priors or regularization.

NeRF parameterisations offer more flexibility and produce higher-quality images. Ideally, one would just run a vanilla NeRF at a high resolution with dense depth sampling. In principle, this could work very well, but the computational cost and memory requirements make this naive approach infeasible. Thus, recent approaches were proposed to reduce the requirements on computation and memory, e.g. GIRAFFE (Niemeyer and Geiger, 2021b), where a NeRF is used to render a feature map at a low resolution, followed by 2D super-resolution.

Rendering features at low resolution, however, creates images artefacts. A slight change in the cam-

era viewpoint creates an *wobbling* effect in the image. This *wobbling* effect is caused by aliasing effects that stem from the design of 2D convolution networks. This aliasing effect motivated the work of StyleGAN3 (Karras et al., 2021a), that was specifically designed to be alias-free. In our work we take the idea of (Karras et al., 2021a) and lift it to 3D. We show that alias-free network can be lifted to 3D, thus we can avoid the image artefacts. The empirical results show that our model performs better or on par with previous 3D-aware methods, that tried to address the shortcomings with more complex components, such as extra regularization terms.

Putting the ideas together, our model generates images in three stages. First, we sample points on a 3D grid and apply alias-free convolutions on it, which produces 3D feature grid. Second, the features are processed with volumetric rendering, which technically is a weighted sum along the depth axis of the 3D grid. The result of the rendering is a low resolution 2D grid (image) of a feature map. Finally, the 2D feature grid is supplied to the super-resolution network, which is an alias-free 2D convolution network. An example result can be seen in Figure 1, a sample from our model using three different viewpoints.

The key contributions of this work are:

- We design and implement a novel alias-free 3D-aware generative model that combines state of the art NeRF and GAN components.
- Quantitative results show that our approach achieves state-of-the-art (SOTA) and competitive results on FFHQ and AFHQv2 on high resolutions, while having interactive frame rates.
- Qualitatively we show viewpoint consistency when we control variables such as appearance, horizontal and vertical translation and rotation.

## 2 RELATED WORK AND MODEL PRELIMINARIES

Different types of 3D-aware generative models exist, prominent examples are autoencoders (Shi et al., 2021), diffusion models (Poole et al., 2022) (Kim and Chun, 2022) (Wang et al., 2022) and GANs. The GAN architecture (Szabó et al., 2019) (Kwak et al., 2022) (Chan et al., 2022) (Xue et al., 2022) (Sun et al., 2022) remains a strong contender in this space and is the model of choice for our construction. In this section we quickly review the main ingredients for this model and in Section 3 explain our 3D extension.

### 2.1 GAN

A GAN consists of a pair of neural networks, a generator  $G$  and a discriminator  $D$  that compete during training. The generator network produces novel images and the discriminator network is trained to distinguish between real and generated images. The original loss function from (Goodfellow et al., 2014) is a min-max objective

$$\min_G \max_D \mathbb{E}_{\mathbf{x}_{\text{real}}} [\log(D(\mathbf{x}_{\text{real}}))] + \mathbb{E}_{\mathbf{z}} [\log(1 - D(G(\mathbf{z})))] \quad (1)$$

where the training images are drawn from the real image distribution  $\mathbf{x}_{\text{real}} \sim p_{\text{real}}$ , the latent vectors are usually drawn from a Normal distribution  $\mathbf{z} \sim \mathcal{N}(0, I)$ . In theory, with perfect training, the generator learns to create samples  $\mathbf{x}_{\text{fake}} = G(\mathbf{z})$  from the data distribution that are indistinguishable from real data points. In practice, however, quite some engineering and network design is required to train the models to achieve good performance, e.g. trading off learning rates of the generator and discriminator.

Several GAN variants have been proposed since the inception and the Alias-Free GAN (Karras et al., 2021a) is a modern variant that produces high-quality images and includes equivariance properties (especially, the StyleGAN3-R variant). Intuitively, StyleGAN3-R emulates an implicit representation, similar to a neural network applied to each pixel location separately, which gives the RGB pixel color. StyleGAN3-R operates on a band limited continuous signals, but represents them as a discrete 2D grid based on the Nyquist–Shannon sampling theorem (Shannon, 1949). When a nonlinear function is applied to a band limited signal, the result is not necessarily band-limited. Thus, one can define an alias-free non linear function by filtering the result of the vanilla non-linear function  $f$  with a low-pass filter. In the discrete domain the alias-free  $F$  function is

$$F(Z) = s^2 \cdot \text{III} \odot (\phi_s * f(\phi_s * Z)), \quad (2)$$

where  $Z$  is the sampling grid,  $s$  is the sampling rate,  $\phi_s$  is the ideal low-pass filter with band limit  $s/2$ ,  $\text{III}$  is the Dirac comb,  $\odot$  denote element-wise multiplication and  $*$  is continuous convolution. StyleGAN-R uses radially symmetrical jinc filters to achieve rotational equivariance. Notice, that this operation can only be performed by entering temporarily the continuous domain. However, in practice it is enough to approximate it by first upsampling, then applying the vanilla function  $f$ , and finally downsampling.

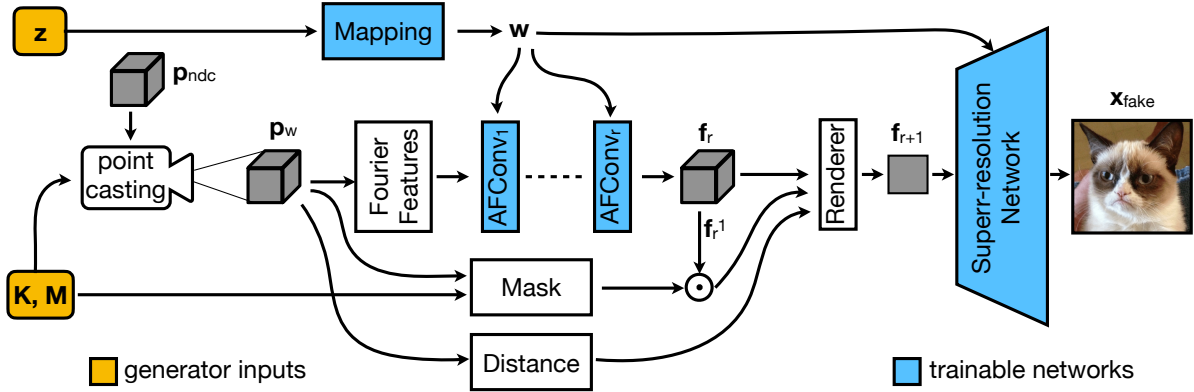


Figure 2: Our generator takes the latent  $\mathbf{z}$  and the intrinsic and extrinsic camera parameters  $\mathbf{K}$  and  $\mathbf{M}$ . 3D points are sampled on a grid, then Fourier features are computed on them, which go through the alias-free 3D convolutional layers. Then the features are rendered and passed to the super-resolution network to get the image as an output.

## 2.2 3D-Aware GAN

A 3D-aware GAN (Szabó et al., 2019) can control camera viewpoints by means of generator conditioning. More precisely, it takes the intrinsic and extrinsic camera parameters  $\mathbf{K}$  and  $\mathbf{M}$ , respectively, as inputs. The training objective now includes terms of camera parameters and reads

$$\min_G \max_D \mathbb{E}_{\mathbf{x}_{\text{real}}} [\log(D(\mathbf{x}_{\text{real}}))] + \mathbb{E}_{\mathbf{z}, \mathbf{K}, \mathbf{M}} [\log(1 - D(G(\mathbf{z}, \mathbf{K}, \mathbf{M})))] \quad (3)$$

The camera parameters  $\mathbf{K}, \mathbf{M}$  are either sampled from a fixed distribution (as in our work) or a viewpoint distribution can be learned alongside the networks (Niemeyer and Geiger, 2021a).

An image generator is now composed of a neural network  $NN$  that produces a 3D representation (e.g. a mesh), followed by a renderer  $R$  that takes the 3D representation and camera parameters and produces the image. As for all GAN models, optionally, a super-resolution network can be used to upscale the image:

$$\begin{aligned} \mathbf{x}_{\text{fake}} &= G(\mathbf{z}, \mathbf{K}, \mathbf{M}) \\ &= \text{SuperRes}(R(NN(\mathbf{z}), \mathbf{K}, \mathbf{M})). \end{aligned} \quad (4)$$

In order to train a generative model of 3D shapes from natural 2D images, 3D GANs exploit the idea that a realistic 3D object should yield a realistic rendering from any plausible viewpoint. By randomizing the choice of the viewpoint, model training forces the generator network to learn a 3D representation disentangled from the viewpoint. The work of (Szabó et al., 2019) provides a theory for such systems, which is a special case of a general theory of Ambient-GAN (Bora et al., 2018).

This design then offers several possibilities regarding the choice of the 3D representation. One

can use meshes (Szabó et al., 2019), voxels (Gadelha et al., 2017) (Schwarz et al., 2022), multi-plane images (Kumar et al., 2023), radiance manifolds (Deng et al., 2022b) (Xiang et al., 2022) (Deng et al., 2022a), signed distance functions (Or-Eli et al., 2022) (Burkov et al., 2022) (Liu and Liu, 2022); each of these representations are paired with their corresponding differentiable renderer. Arguably, the most popular representation for modern 3D GANs is the Neural Radiance Fields (Chan et al., 2021) (Gu et al., 2022) (Zhou et al., 2021) (Kaneko, 2022) (Tang et al., 2022).

## 2.3 Volumetric Rendering

Volumetric rendering techniques (Max, 1995) (Meetz et al., 1991) (Rushmeier and Torrance, 1987) (Williams and Max, 1992) (Kajiya, 1986) are modelling the physical process of image formation and are capable of representing the scene unambiguously and accurately. A popular formulation is the radiance field equation

$$C(\mathbf{r}) = \int_{t_n}^{t_f} T(t) \sigma(\mathbf{r}(t)) \mathbf{c}(\mathbf{r}(t), \mathbf{d}) dt, \quad (5)$$

$$\text{where } T(t) = \exp\left(-\int_{t_n}^t \sigma(\mathbf{r}(s)) ds\right). \quad (6)$$

Here,  $T$  is the transmittance,  $\sigma$  is the density and  $\mathbf{c}$  is the color at the locations  $\mathbf{r}(t) = \mathbf{o} + t\mathbf{d}$ ,  $\mathbf{o}$  is the camera center and  $\mathbf{d}$  is the direction of a ray. The integral bounds are the distances to the near and far plane,  $t_n$  and  $t_f$  respectively. In practice, Eq. 5 is approximated by numerical integration, where, for each pixel, points are sampled along the corresponding ray. Recently Neural Radiance Fields (NeRF) (Mildenhall et al., 2022) proposed to use a volumetric rendering, where the volume is parameterised by a Multi-layer Perceptron (MLP): it takes 3D coordinates as inputs,

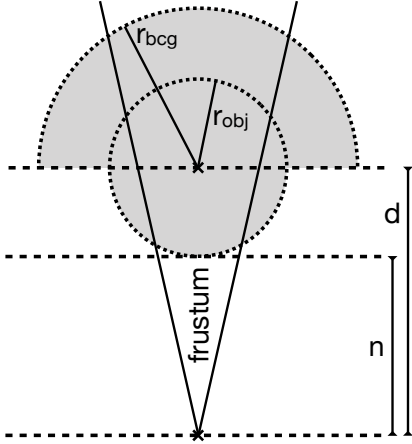


Figure 3: The grey region shows the part of the scene that are part of the object mask, i.e. potentially visible. We render the part that is both masked and inside the frustum.

and outputs the corresponding density and color. In our work instead of an MLP we use a 3D convolutional network, which calculates the features for the rendering on a 3D point grid of points.

For 3D-aware GANs, the NeRF is conditioned on the latent variables  $\mathbf{z}$ , so the neural network takes both the 3D locations and  $\mathbf{z}$  as inputs. The neural network is not always an MLP. Their computational cost is high, and with the current hardware it is not feasible to use them in high-resolution image synthesis as is. Thus, more efficient architectures were introduced. VoxGRAF (Schwarz et al., 2022) uses a sparse voxel grid to speed up computation by skipping empty space. Tri-plane representations (Chan et al., 2022) (Skorokhodov et al., 2022) (Xu et al., 2023) run standard 2D convolutional networks, then rearrange their outputs as three planes that are perpendicular to each other, then features are sampled by projecting the 3D points onto them. This is much faster than having to compute a full MLP forward pass for each point.

GIRAFFE (Niemeyer and Geiger, 2021b) proposed to render scenes using a low-resolution NeRF model, followed by a super-resolution module. The MLP in their case does not directly compute RGB pixel values, but instead creates a high-dimensional feature map.

In our work, we build upon StyleGAN3-R and NeRF rendering. As they both produce and use implicit representations, StyleGAN3-R can be naturally modified to allow 3D viewpoint control. Similar to GIRAFFE, we render a low-resolution feature map, and then upsample it to produce high-resolution images.

### 3 APPROACH

In this section we present the construction of our model, and show how we combine the alias free properties of (Karras et al., 2021a) with a 3D NeRF rendering. For this we need to equip the generator with an explicit rendering function that ensures geometry and viewpoint consistency across different samples. We will explain every steps in detail in this section, the main flow are generation of the 3D representation, alias free convolutions, rendering followed by a final super-resolution step to map to the target resolution. An overview of this method is shown in Figure 2.

The training procedure remains the same as before, we optimize the minimax objective w.r.t. the generator  $G$  and discriminator  $D$  parameters as in Eq. 3. The discriminator is taken as is from the vanilla StyleGAN3 implementation. During training we need to sample viewpoints and camera parameters and we will explain the choices in the respective sections.

#### 3.1 Viewpoint Sampling

Viewpoints are parameterised by polar coordinates. The horizontal and vertical angles are sampled independently within the ranges of  $\pm 80^\circ$  and  $\pm 20^\circ$  respectively, while the radius is sampled within  $[5, 25]$ . The camera center is placed according to the polar coordinates and it points at the origin. The focal length is set to be equal to the radius, thus the unit ball around the origin always fits tightly to the rendered square image. Once these parameters are given, they determine the camera parameters  $\mathbf{K}$  and  $\mathbf{M}$  as described below. Note we use dimensionless units for the focal length and the 3D coordinates, as we do not have any ground truth sizes in meters.

#### 3.2 Camera Parameters

The cameras are parameterised with intrinsic  $\mathbf{K}$  and extrinsic  $\mathbf{M}$  matrices:

$$\mathbf{K} = \begin{pmatrix} f & 0 & 0 \\ 0 & f & 0 \\ 0 & 0 & 1 \end{pmatrix}, \quad \mathbf{M} = \begin{pmatrix} \mathbf{R} & \mathbf{t} \\ \mathbf{0} & 1 \end{pmatrix}, \quad (7)$$

where  $f \in \mathbb{R}^+$  is the focal length,  $\mathbf{R} \in \mathbb{R}^{3 \times 3}$  is a rotation matrix and  $\mathbf{t} \in \mathbb{R}^3$  is a translation, thus  $\mathbf{M} \in \mathbb{R}^{4 \times 4}$  is the (world-to-camera) matrix that describes a rigid movement.

#### 3.3 Normalised Device Coordinates

We use Normalised Device Coordinates (NDC) for sampling points during the volumetric rendering.



The points in this coordinate system are  $\mathbf{p}_{\text{ndc}} = (x_{\text{ndc}}, y_{\text{ndc}}, z_{\text{ndc}}) \in \mathbb{R}^3$  and they relate to the points in the camera frame by a perspective transformation

$$\mathbf{p}_{\text{ndc}}^h \sim \mathbf{P}\mathbf{p}_{\text{cam}}^h, \quad (8)$$

where the superscript denotes homogeneous coordinates,  $\mathbf{p}_{\text{cam}}^h = (x_{\text{cam}}, y_{\text{cam}}, z_{\text{cam}}, 1)$ . The perspective transformation matrix is given by:

$$\mathbf{P} = \begin{pmatrix} f & 0 & 0 & 0 \\ 0 & f & 0 & 0 \\ 0 & 0 & a & b \\ 0 & 0 & 1 & 0 \end{pmatrix}, \quad (9)$$

where  $f \in \mathbb{R}$  is again the focal length from  $\mathbf{P} \in \mathbb{R}^{4 \times 4}$  and  $a, b \in \mathbb{R}$ . To remain consistent with  $\mathbf{K}$ , only the entries  $a$  and  $b$  are free parameters. We set them in such a way that applying the transformation would bring the near plane  $n > 0$  of the camera to zero in NDC, and at depth  $d > 0$  the Jacobian of the transformation becomes proportional to the identity matrix,

$$a = f \cdot d / n, \quad b = -f \cdot d. \quad (10)$$

This way,  $\mathbf{P}$  is designed to produce the least amount of distortion in the rendered volume.

### 3.4 Scene

In our setting, we assume that the object is located at the origin in the world coordinate frame inside a sphere with radius  $r_{\text{obj}} = 1.5$  (which is slightly bigger than  $\sqrt{2}$ , so the sides of the frustums we use for rendering can fit inside it). We also set a background radius  $r_{\text{bkg}} = 2.0$ , to allow the model to put some background behind the object. Figure 3 shows which part of the scene is visible. The distance between the camera and the object center is  $d$ . If a point is closer to the camera than  $d$  and is inside the sphere with  $r_{\text{obj}}$ , it is considered for rendering. Points further than the distance  $d$  are rendered, if they are inside the sphere with  $r_{\text{bkg}}$ . For calculating  $\mathbf{P}$  in Eq. 9, we set the near plane  $n = d - r_{\text{obj}}$ .

### 3.5 Point Casting

We first generate points in NDC space in a regular 3D grid. The size of the grid is  $D \times H \times W$ , denoting the grid sizes for depth, height and width, respectively. We chose  $H = W = 52$ , which corresponds to a  $32 \times 32$  pixel grid plus a 10-point margin on each side. We do not use margins for the depth axis, we set  $D = 32$ . Excluding the margin, the ranges are  $x_{\text{ndc}} \in [-1, +1]$ ,  $y_{\text{ndc}} \in [-1, +1]$  and  $z_{\text{ndc}} \in [0, +4]$ . Note that the neighboring points are  $2 \times$  less dense along the depth axis. We denote the point grid with

an overloaded notation  $\mathbf{p}_{\text{ndc}}$ , where a single point  $\mathbf{p}_{\text{ndc}}[k, j, i]$  is indexed by  $k, j$  and  $i$ , which correspond to the depth and  $v, u$  pixel coordinates, respectively. To make the notation succinct, we omit indices if they are not necessary, e.g.  $\mathbf{p}_{\text{ndc}}[k]$  is a 2D slice of the 3D grid.

Next, we back-project the points to the world coordinate frame by applying the inverse perspective transformation by the matrix  $(\mathbf{PM})^{-1}$ . We get a 3D grid of points  $\mathbf{p}_{\text{w}}$  in the world coordinate frame:

$$\mathbf{p}_{\text{w}}^h \sim (\mathbf{PM})^{-1} \mathbf{p}_{\text{ndc}}^h, \quad (11)$$

where, as before, the superscript denotes homogeneous coordinates.

### 3.6 Fourier Features

Similarly to StyleGAN3-R, we first compute Fourier features (Tancik et al., 2020), to supply the network with input, except in our case we compute them for 3D points instead of 2D pixel locations. The Fourier features are the input to the first layer, so we denote them  $\mathbf{f}_0$ .

$$\mathbf{f}_0 = [\cos(\omega_1^T \mathbf{p}_{\text{w}}), \sin(\omega_1^T \mathbf{p}_{\text{w}}), \dots, \cos(\omega_L^T \mathbf{p}_{\text{w}}), \sin(\omega_L^T \mathbf{p}_{\text{w}})], \quad (12)$$

Fourier features are a concatenation of  $2L$  sine and cosine waves. The  $\omega_l \in \mathbb{R}^3$  parameters are randomly sampled from a uniform 3D ball and fixed at the beginning of the training. We choose  $2L = 128$ .

### 3.7 Alias-Free Convolutions

Next, we apply the StyleGAN3-R rotation-invariant alias-free convolutional layer  $AFConv_1$  for all of the 2D slices along the depth axis of the 3D grid. In order to make the features alias-free, we apply a low pass filter on them and downsample by  $2 \times$  for every slice.

$AFConv_1$  is conditioned on  $\mathbf{w} = \text{Mapping}(\mathbf{z})$ , where  $\text{Mapping}$  is an MLP, which enable conditioning on the latents  $\mathbf{z}$ , thus,

$$\mathbf{f}_1[k] = AFConv_1(\text{down}2x(\mathbf{f}_0[k]), \mathbf{w}). \quad (13)$$

$AFConv_1$  contains a convolution with a  $1 \times 1$  kernel and a leaky ReLU activation. The nonlinearity of the leaky ReLU function is handled via Eq. 2, first upsampling the features, then applying the nonlinearity, then downsample with a low pass filter. The next layers then depend on the one before them,

$$\mathbf{f}_m[k] = AFConv_m((\mathbf{f}_{m-1}[k]), \mathbf{w}) \quad (14)$$

for a total of  $r$  layers. The last features  $\mathbf{f}_r$  are then then input to the renderer. Please note that the down-sampling is necessary only for the Fourier features

Table 1: Quantitative evaluation results using Fréchet Inception Distance (FID) ↓ for FFHQ and AFHQv2-Cats datasets. The resolution of the generated images is given next to the dataset’s name. Scores for the compared approaches are taken from the corresponding papers, † scores taken from (Xue et al., 2022). The best and second-best scores are coloured in red and orange, respectively.

	FFHQ-256	FFHQ-512	FFHQ-1024	AFHQv2-256	AFHQv2-512
GIRAFFE (Niemeyer and Geiger, 2021b)	32	-	70.08 <sup>†</sup>	33.39 <sup>†</sup>	-
Lift. SG (Shi et al., 2021)	29.81	-	-	-	-
GRAM (Deng et al., 2022b)	17.9	-	-	14.6	-
GRAM-HD (Xiang et al., 2022)	13.00	-	12.0	7.05	7.67
GIRAFFE-HD (Xue et al., 2022)	11.93	-	10.13	12.36	-
VoxGRAF (Schwarz et al., 2022)	9.6	-	-	9.6	-
CIPS-3D (Zhou et al., 2021)	6.97	-	12.26	-	-
GMNR (Kumar et al., 2023)	9.20	6.81	6.58	-	6.01
OmniAvatar (Xu et al., 2023)	-	5.70	-	-	-
EG3D (Chan et al., 2022)	4.80	4.70	-	3.88	2.77
SURF-GAN (Kwak et al., 2022)	4.72	-	-	-	-
IDE-3D (Sun et al., 2022)	-	4.60	-	-	-
<b>Ours</b>	<b>3.94</b>	<b>4.10</b>	<b>3.14</b>	<b>4.66</b>	<b>4.57</b>

and not for the rest of the intermediate layers ( $m > 1$ ). The perspective transformation may cause aliasing artefacts during the sampling process, which are handled by a denser sampling and down-sampling the Fourier features. The number of layers  $r = 3$  before rendering is set such that they correspond to the number of convolutional layers in StyleGAN3 with resolution  $16 \times 16$ . We set the number of channels to 128.

### 3.8 Rendering

Now that the 3D features are computed, we use them to render the 2D image. For each point on the 3D grid, we calculate the corresponding distance and density. The distance of a 3D point to the camera is

$$\delta[k] = \|\mathbf{p}_w[k+1] + \mathbf{p}_w[k-1]\|/2, \quad (15)$$

where negative indices correspond to the points on the margin.

The densities  $\sigma$  at a 3D point are chosen to be the first channel of  $\mathbf{f}_r$ . Let *Mask* denote a masking function associated with the scene, it determines whether a point should be used during rendering. The mask will then remove points from the rendering process by setting their densities to zero, further we clip any negative values that may exist.

$$\sigma = \max(0, \text{Mask}(\mathbf{p}_w, \mathbf{M}) \odot \text{up2x}(\mathbf{f}_r^1)), \quad (16)$$

where the superscript denotes the index of the channel. Note that the mask computation requires the extrinsic camera parameters and also up-sampling for the features so that they match the sampling rate of the 3D points.

Given the densities and the distances from the camera we can perform volumetric rendering. We sum along the depth axis and numerically integrate

the points  $k$  along the ray

$$\mathbf{f}_{r+1} = \sum_{k=1}^D T[k](1 - \exp(-\delta[k]\sigma[k]))\text{up2x}(\mathbf{f}_r[k]), \quad (17)$$

where  $T$  are the transmittance values,

$$T[k] = \exp\left(-\sum_{m=1}^{k-1} \delta[m]\sigma[m]\right). \quad (18)$$

The result  $\mathbf{f}_{r+1}$  is a 2D feature map.

Notice that full 3D equivariance with the perspective camera model and the volumetric rendering is hard to define. Thus throughout the paper we only use alias-free operations along the width and height axes and not along the depth. This is an approximation, that we found to work well in practice.

### 3.9 Super-Resolution

The super-resolution part is then borrowed from the StyleGAN3-R architecture. It is the convolutional network comprising of the higher-resolution 2D convolutional layers. The output of the super-resolution network is then the generated RGB image

$$\mathbf{x}_{\text{generated}} = \text{SuperRes}(\mathbf{f}_{r+1}). \quad (19)$$

## 4 EXPERIMENTS

We evaluate our approach in the task of unconditional multi-view image generation on two real-world image datasets that allow a comparison with prior work. The first dataset is FFHQ (Karras et al., 2021b), a set of 70,000 human face images at  $1024^2$  pixels resolution. FFHQ exhibits considerable variation in terms of age,



Figure 4: Sample images generated by our model trained on FFHQ-1024<sup>2</sup> and AFHQv2-Cats-512<sup>2</sup> datasets.

ethnicity and image background. Because of its high resolution we can test generation results on different results, namely 256, 512, and 1024<sup>2</sup>. To test the generalization capability of the proposed approach, we also conduct experiments on AFHQv2 (Choi et al., 2020; Karras et al., 2021a), a collection of 15,000 images of animal faces at a resolution of 512<sup>2</sup> pixels. AFHQv2 includes three domains (cats, dogs, wildlife), each consisting of  $\approx 5,000$  images. We follow previous work and use the 5,065 cat image subset of this dataset to evaluate our method and compare it to the most recent SOTA image synthesis methods: GMNR (Kumar et al., 2023), OmniAvatar (Xu et al., 2023), IDE-3D (Sun et al., 2022), GIRAFFE-HD (Xue et al., 2022), GRAM-HD (Xiang et al., 2022), SURF-GAN (Kwak et al., 2022),

VoxGRAF (Schwarz et al., 2022), EG3D (Chan et al., 2022), Lift. SG (Shi et al., 2021), pi-GAN (Chan et al., 2021), and GIRAFFE (Niemeyer and Geiger, 2021b). We adapt the same training setup as in previous work; we also augment both datasets with horizontal flips. In contrast to other methods, e.g. EG3D, we do not use any additional pose estimators, adaptive data augmentation or transfer learning techniques.

#### 4.1 Quantitative Results

In terms of metric-based evaluation, we assessed image quality with the FID (Heusel et al., 2017), a common metric used to estimate the distance between generated and real images. To compute the FID scores for the proposed approach, we used 50,000 images





Figure 5: Qualitative comparison between our approach and recent SOTA methods on the FFHQ-256<sup>2</sup> dataset.

generated by a trained model and all real images from the respective dataset. As can be seen from Table 1, the proposed approach demonstrates competitive FID performance on both datasets, surpassing prior work on all FFHQ variants and being the second best on AFHQ. The results on AFHQv2 are behind those achieved by the best approach EG3D. We attribute this to the difference in pose distribution between FFHQ and AFHQv2 where AFHQv2 is much more complex and diverse. For EG3D a pose estimator is used so that a pose distribution is known at training time, for simplicity we choose the same distribution for both FFHQ and AFHQv2.

Following (Chan et al., 2022), we evaluate multi-view facial identity consistency (ID) by calculating the mean ArcFace (Deng et al., 2019) cosine similarity score between pairs of views of the same synthesized face rendered from random camera poses. As can be seen from Table 2, our approach compares favourably with the current SOTA contenders.

Table 2: Multi-view identity consistency (ID) for FFHQ. We indicated the image resolution used for training and evaluation.

	resolution	ID↑
GIRAFFE	256 <sup>2</sup>	0.64
$\pi$ -GAN	128 <sup>2</sup>	0.67
Lift. SG	256 <sup>2</sup>	0.58
EG3D	256 <sup>2</sup>	0.76
EG3D	512 <sup>2</sup>	0.77
SURF-GAN	128 <sup>2</sup>	0.66
IDE-3D	512 <sup>2</sup>	0.76
Ours	256 <sup>2</sup>	0.73
Ours	512 <sup>2</sup>	0.76
Ours	1024 <sup>2</sup>	0.78



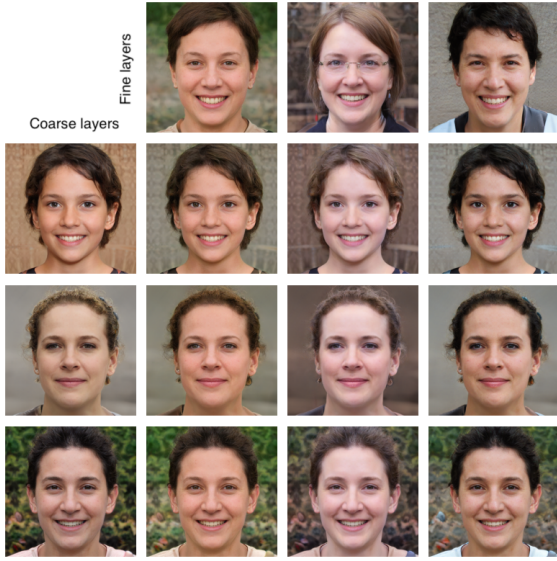


Figure 6: Style-mixing with our approach on FFHQ-1024 with mixing regularization. We take the coarse layers (0-7) from the images in the first column and the fine layers (8-15) from the images in the first row. Coarse layers determine the facial traits, hair length and hairstyle. Fine layers are influence the skin tone and hair colouring.

## 4.2 Qualitative Results

In Figure 4 we show some sample images generated by our approach on both datasets with the highest available resolution, FFHQ-1024 and AFHQv2-512. Manual examination of the images verifies the high quality, viewpoint consistency and diversity of the outputs.

To put the results into context, we follow previous work and compare the image samples generated by the competing approaches side-by-side, shown in Figure 5. Some of the methods have clearly visible artefacts. For example, the faces generated by GIRAFFE exhibit a halo around the hair region, the hair strands are also inconsistently positioned when looked at from different viewpoints.  $\pi$ -GAN generates overly-smoothed faces, making them look unrealistic. Lifting StyleGAN generates well-formed faces, but struggles with capturing details (note the blur around the hair regions). Our method, on the other hand, synthesizes high-quality images which are viewpoint-consistent, detailed and realistic: note the correct positioning and lack of artefacts when generating fine details, like hair strands or earrings. Qualitatively, both ours, GIRAFFE-HD and EG3D are photorealistic. Many images have the effect that the eyes of the person look directly into the camera from all viewpoints. This is not an error in viewpoint consistency, but a well known ambiguity. When the

Table 3: Rendering speed in images/second at three different rendering resolutions. All compared approaches were evaluated on a single GPU but the corresponding numbers are taken from the original papers, so they serve as a reference, not a fair speed comparison.

resolution	256 <sup>2</sup>	512 <sup>2</sup>	1024 <sup>2</sup>
EG3D	36	35	-
GIRAFFE	181	161	-
GMNR	313	78.9	17.6
GRAM-HD	-	-	90
Lift. SG	51	-	-
pi-GAN	5	1	-
SURF-GAN	72	-	-
VoxGRAF	64	-	-
Ours	30	26	23

geometry of the eye is inverted, it causes an illusion that the eye looks at the camera all the time. As most images look directly towards the camera in FHHQ, it is natural for the network to learn the inverted geometry, and all 3D-aware methods suffer from this.

## 4.3 Speed

In Table 3 we list the inference speed of our approach and other methods we compared against. Since we used standard components we achieve a high throughput rate of the trained models of about 23 frames per second for the highest tested resolution on a single V100 GPU.

The numbers are given as a rough reference: the approaches were benchmarked by the respective authors on different hardware and with different requirements. For example, while our method performs end-to-end image synthesis, GRAM-HD (Xiang et al., 2022) caches the manifold surfaces and HR radiance maps as textured 3D meshes, and then runs fast free-view synthesis with an efficient mesh rasterizer from (Laine et al., 2020). Our method is capable of real-time inference even at 1024<sup>2</sup> resolution, without sacrificing image quality.

## 4.4 Style Mixing

The ability to modulate image style by feeding two or more different latent code vectors to different layers of the generator at inference time is known as style mixing (Karras et al., 2021a; Karras et al., 2020; Karras et al., 2021b). Given the fact that our approach is based on the StyleGAN3 architecture, it is reassuring that the style mixing abilities are preserved. In Figure 6 we can observe that there is a clear separation of the roles the coarse and fine layers of the model take on: coarse layers are responsible for the overall head

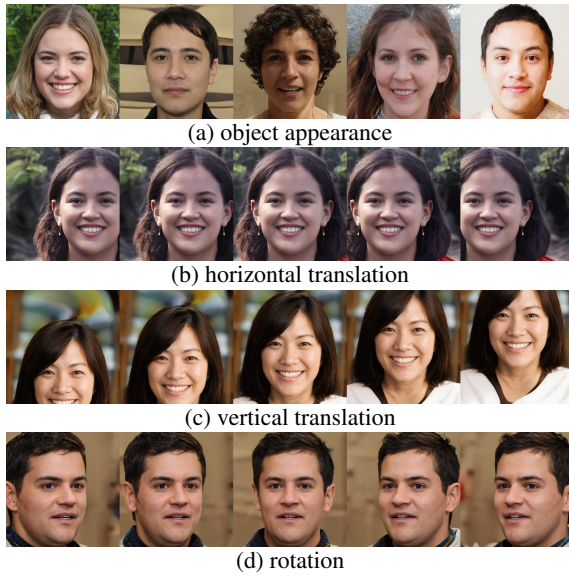


Figure 7: Conditioning and control: varying **a)** the latent  $\mathbf{z}$  that controls appearance, **b)** the camera matrix  $\mathbf{M}$  for horizontal translation, **c)** vertical translation and **d)** rotation.

pose, coarse face details and hairstyle, while fine layers perform appropriate skin tone and hair colouring.

#### 4.5 3D Controllability

In Figure 7 we visually demonstrate that our method is capable of generating 3D controllable images which is a feature that emerges naturally from volume rendering of input Fourier features. To explore this capability, we decompose our camera into individual components of (1) vertical translation, (2) horizontal translation and (3) spherical rotation. For vertical translation, Figure 7 (a) shows the object identities are preserved while the viewpoints are consistent. Our qualitative results for horizontal translation and spherical rotation show compelling evidence that our method provides multi-view consistency, in terms of subject identities and backgrounds.

## 5 DISCUSSION

In this paper we constructed a 3D-aware generative model that is able to render images both of high quality and high resolution, while maintaining fast inference and gain viewpoint control for the user. We have demonstrated these capabilities both qualitatively and quantitatively, while we kept the design as simple as possible.

We argue that a benefit of the proposed construction is the avoidance of extra regularization terms,

dual discriminators or specialized data-augmentation strategies. The model retains the respective advantages of its ingredients “simply” by a careful combination of NeRF and the alias-free StyleGAN3-R. The training protocol follows the standard procedure of StyleGAN3-R which is what we hoped for when starting the investigation since specialized protocols are hard to attain and prone to be sub-optimal.

There are several limitations that we plan to address as future work. Currently our method does not provide 3D depth or normals as output, as they can only be extracted at a very low  $16 \times 16$  pixel resolution. It would require specialized depth up-sampling for any usable resolution.

Another interesting direction could be to learn the viewpoint distribution similar to CAM-PARI (Niemeyer and Geiger, 2021a). Training a 3D-aware GAN requires a good match of the viewpoint distribution used to sample and present in the training data. Mismatch, either wider or narrower viewpoints can lead to instability and incorrect geometry. We expect that learning the viewpoint distribution would lead to better performance e.g. on the AFHQ dataset.

We understand the presented model and result as a promising step to more complete 3D generation. In particular we are interested in full 3D human generation and our model contains some necessary features such as alias-free, high-quality, 3D-aware to move into this more challenging domain.

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