A Toolset for Constraint Programming

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Keywords: Tools, Constraint Programming, Solver Interface, Remote Control.

Abstract: Constraint Programming (CP) allows solving combinatorial problems across various domains. Numerous solvers and tools have been developed in this area. However, their interoperability is often limited. This paper presents a suite of tools for constraint programming, consisting of a solver interface and a remote control application. The solver interface offers a unified API for interacting with different solvers of various programming languages. Based on this API, we present a remote control system enabling to configure the solver and to observe and analyze its behaviour while it is running.

1 INTRODUCTION

Constraint Programming (CP) is a powerful paradigm to solve complex combinatorial problems across various domains. In this paper, we consider CP in a broad sense, including the Boolean satisfiability problem (SAT) (Biere et al., 2021), its generalization to pseudo-Boolean (PB) problems (Roussel and Manquinho, 2021), and general constraint programming as defined for instance in (Rossi et al., 2006) (Lecoutre, 2009).

For these different paradigms, numerous solvers have been proposed such as Kissat (Biere and Fleury, 2022), Glucose (Audemard and Simon, 2018), RoundingSat (Ellmers and Nordström, 2018), Sat4j (Le Berre and Parrain, 2010), ACE (Lecoutre, 2023), Choco (Narendra Jussien, 2008), or Picat (Zhou et al., 2015). These solvers often have very different programming interfaces. Choosing one solver or another thus imposes to follow this particular interface when using the solver as a library. To face this issue, generic interfaces like IPASIR or IPAMIR have been developed to provide a simple common interface for incremental SAT and MaxSAT solvers, especially in the context of the SAT Competition and the MaxSAT Evaluation. Moreover, different formats and tools have been developed to represent the problems to solve, such as DIMACS (DIMACS, 1993) for SAT, OPB for PB problems and OPL (van Hentenryck, 1999), MiniZinc (Nethercote et al., 2007) (Stuckey et al., 2010), Essence (Frisch et al., 2007) and PyCSP³ (Lecoutre and Szczepanski, 2020) (which can be used to generate XCSP³ instances (Boussemart et al., 2020)) for CP instances. Not all solvers support all these representation languages, preventing the interoperability of these tools.

To ease the development and deployment of CP solutions, this paper presents a suite of synergistic tools that facilitate the integration of constraint programming solutions across diverse software applications. The core component of our toolset is a solver interface called Universe, which provides a unified API for interacting with different constraint solvers directly from the code. By offering a consistent and intuitive interface, it is possible to seamlessly switch between various solvers without the need for extensive modifications, enabling greater flexibility and the exploration of different solver capabilities, without relying on a particular modelization format. This is a very different philosophy compared to that of MiniZinc or PyCSP³, for instance, which require to encode the problem in their own formats before asking a solver to read this modelization and solve it. Universe is defined in two different popular programming languages, namely C++ and Java, enabling the use of solvers almost independently of the language in which they have been implemented, which is not the case of tools like, for instance, CP0py (Guns, 2019).

The second component is a graphical remote control system inspired by (Le Berre and Roussel, 2014) that allows one to finely configure a chosen solver before...
running it on a particular instance, and even to change its configuration on the fly for solvers that support such updates. During the solver’s execution, the behavior of the solver may be observed live, by showing statistics about the decision it makes and the conflicts it encounters. Additionally, the search tree can also be displayed as the solver explores it.

The rest of this paper is organized as follows. In Section 2, we give some preliminaries regarding constraint programming and solving. In Section 3, we present the Universe solver interface. In Section 4, we give examples of the capabilities offered by our remote control application, and in Section 5, we conclude and give some perspectives for future works.

2 PRELIMINARIES

In this section, we briefly describe how the different solvers implementing the different considered paradigms (SAT, PB, and CP) work.

2.1 SAT Solving

A Boolean variable \( x \) is a variable that can either take the value 0 (false) or 1 (true). We call a literal \( \ell \) a Boolean variable \( x \) or its negation \( \bar{x} \). A literal \( \ell \) is satisfied when \( \ell \) is assigned to 1, and falsified otherwise. A clause is a disjunction of literals, requiring at least one of its literals to be satisfied. A problem is in Conjunctive Normal Form (CNF) when it is a conjunction of clauses. The SATisfiability problem (SAT) is to determine whether such a conjunction is consistent. It is the first problem that has been proven to be NP-complete (Cook, 1971).

2.2 Pseudo-Boolean (PB) Constraints

A pseudo-Boolean (PB) constraint is a constraint of the form \( \sum_{i=1}^{n} \alpha_i \ell_i \delta \), where \( n \) is a positive integer, the weights (or coefficients) \( \alpha_i \), and the degree \( \delta \) are integers, \( \ell_i \) are literals and \( \delta \in \{<,\leq,=,\geq,>\} \). A PB constraint is said to be normalized when all the coefficients and the degree of this constraint are positive, and \( \delta \) is \( \geq \). Any PB constraint may be rewritten as a conjunction of normalized PB constraints. A PB cardinality constraint is a normalized PB constraint in which all the coefficients are equal to 1, and a clause is a PB cardinality constraint with its degree equal to 1. This definition is equivalent to the definition of clauses as disjunctions of literals, and shows that PB solvers generalize SAT solvers.

2.3 Constraint Programming

A constraint network (CN) is composed of a set of discrete variables and a set of constraints. Each variable \( X \) takes its value in a finite set called domain of \( X \), denoted \( \text{dom}(X) \). Each constraint defines a relation on a set of variables. A solution of a CN is an assignment of values to all its variables such that all the constraints of the CN are satisfied. A CN is said to be consistent if it has at least one solution, and the corresponding decision problem, called Constraint Satisfaction Problem (CSP), is to determine whether a CN is consistent.

2.4 Solving Techniques

Let us now give a brief overview of how the solvers of these different paradigms work. Most of them follow a similar approach, which interleaves variable assignments (or refutations), and a constraint propagation mechanism to filter the search space. Typically, a search tree ‘\( T \)’ is built: at each internal node of ‘\( T \)’, (i) a pair \( (x, v) \) is selected where \( x \) is an unfixed variable and \( v \) is a value in \( \text{dom}(x) \), and (ii) several cases (branches) are considered, corresponding to either an assignment \( x = v \) or a refutation \( x \neq v \). The solver chooses the variable to assign by using a variable selection heuristic (e.g., VSIDS (Moskewicz et al., 2001), its PB variants (Le Berre and Wallon, 2021) or \( \text{dom/wdeg} \) (Boussemart et al., 2004) for CP solvers).

A value selection heuristic then decides the order in which the values are chosen when assigning variables (this heuristic is often called phase selection in SAT or PB solvers). After each assignment, constraint propagation is applied to filter out values from the domain of the variables, such as unit propagation (Zhang and Stickel, 1996) for SAT solvers, its extension to PB constraints (Dixon and Ginsberg, 2002) or MAC (Sabin and Freuder, 1994) for maintaining arc consistency in CP solvers. Each time the solver encounters a conflict, it can learn a new constraint, called a nogood. This is particularly true for SAT solvers implementing the CDCL architecture (Silva and Sakallah, 1996) (Eén and Sörensson, 2004). When a conflict is detected, it is analyzed by repeatedly applying the resolution proof system to infer a new clause explaining the reason of the conflict. PB solvers also implement a similar conflict analysis (Dixon, 2004), based on the cutting-planes proof system (Gomory, 1958). CP solvers also learn nogoods, but to a lesser extent than SAT and PB solvers (Lecoutre et al., 2007). Because there may be a huge amount of recorded nogoods, solvers may delete them regularly, both to preserve memory space and to avoid slowing down constraint
propagation. To this end, the solver applies a so-called learned constraint deletion strategy to decide which constraints to remove and when. Restart policies finally play an essential role in modern constraint solvers, as they permit addressing the heavy-tailed runtime distributions of SAT, PB and CSP instances (Gomes et al., 2000). In essence, a restart policy corresponds to a function \( \text{restart} : \mathbb{N}^+ \rightarrow \mathbb{N}^+ \), that indicates the maximum number of steps allowed for the search algorithm per attempt, called run. It means that a backtrack search piloted by a restart policy builds a sequence of binary search trees \( \langle T_1, T_2, \ldots \rangle \), where \( T_j \) is the search tree explored at run \( j \). Note that the cut-off, which is the maximum number of allowed steps during a run, may correspond to the number of backtracks, the number of wrong decisions (Bessiere et al., 2004), or any other relevant measure.

3  UNIVERSER: A UNIVERSAL SOLVER INTERFACE

There exists a large number of solvers implementing the different paradigms presented in the previous section. These solvers are often very efficient in practice, but they are also somehow complementary. Indeed, some solvers may have very good performance on some kinds of problems, while they may be very slow on some other problems. For instance, SAT solvers are able to solve very efficiently a wide variety of instances, but it is well-known that they perform poorly on instances requiring the ability to “count”. This is illustrated by the pigeonhole principle problem, which states that it is not possible to put \( n \) pigeons in \( n-1 \) holes. Proving the unsatisfiability of such problems requires an exponential number of resolution steps for SAT solvers (Haken, 1985). However, PB solvers based on the cutting-planes proof system (Gomory, 1958) can prove it with a linear number of derivation steps (Hooker, 1988). Such a complementarity can also be observed between solvers implementing the same paradigm while using different strategies, see, e.g., (Le Berre et al., 2020). Identifying the best solver for a particular problem may be critical in some applications, such as those involving human interactions: end-users may find it unacceptable to wait for a long time for the solution to their problem. In order to select the best solver, one may want to try different ones, and thus to be able to plug any solver in one’s application, and evaluate its performance. However, changing the solver integrated in an application often requires a lot of effort, as solvers most of the time define their own interface (when they provide one). Choosing another solver thus implies rewriting the part of the application invoking the functions of the solver’s API. In this section, we present the C++ Universe interface, which provides a common interface for the solvers of the different paradigms, allowing one to seamlessly switch between different solvers. This interface may either be natively implemented by existing solvers, or be used in solver adapters that forward method invocations to the adapted solver’s API. We already provide adapters for the solvers Sat4j (Le Berre and Parrain, 2010) and ACE (Lecoutre, 2023), and other ones will be available in the near future.

3.1 An Overview of Universe

Figure 1 gives an overview of the interfaces defined in Universe. In the following, we give a detailed description of the features they provide.

The main interface of Universe is IUniverseSolver. It allows any solver to be invoked to check whether a problem is consistent, and to get a solution when it is. This interface does not depend on the paradigm implemented by the underlying solver: the solver is expected to read the problem itself from the file given to loadInstance() when this method is invoked. This interface is extended by the IUniverseSatSolver interface to allow one to programmatically add clauses to the solver, which is extended by IUniversePseudoBooleanSolver for adding PB constraints, which is itself extended by IUniverseCspSolver for adding general CP constraints (e.g., sum, count, etc.). These methods allow one to dynamically build the problem to solve, and to incrementally solve it. Note that the interface hierarchy we described follows an is-a principle: for instance, a CSP solver is-a SAT solver in the sense that it is able to solve a SAT problem, while a SAT solver is-not-a CP solver, as it does not natively recognize CP constraints (it can only deal with clauses). Universe also defines the abstract factory IUniverseSolverFactory, which provides methods to create SAT, PB, and CP solvers. This factory allows implementing solvers to be easily instantiated, and also to provide various default configurations that can be used as-is in user applications.

3.2 Configuring a Solver

Optionally, the IUniverseConfigurableSolver interface may be implemented by solvers to allow the users to finely configure the solver according to their needs. In particular, users can choose the variable and value selection heuristics, the restart policy and the learned constraint deletion strategies the
solver will apply during its execution. To be as generic as possible, these strategies are identified by their names, and not by their types. Solvers implementing the IUniverseConfigurableSolver are expected to provide the list of the names of the strategies they support, and to switch to the desired strategy when asked to. Optional parameters may be specified to configure the strategies (for instance, the number of conflicts before performing the first restart).

The IUniverseConfigurableSolver also provides method for manually performing a restart or deleting learned constraints.

### 3.3 Listening to Search Events

Solvers implementing Universe may notify instances of IUniverseSearchListener during the search, for instance when a decision is made, a conflict is en-
countered, a constraint is learned, a restart is performed, constraints are deleted or a solution is found. Listeners may be very useful to allow one to trace the solver execution, as well as monitor it. This interface is for instance the basis of the remote control application we present in Section 4.

3.4 JUniverse: Universe in Java

All the interfaces defined in Universe are also defined in JUniverse, the Java equivalent to the Universe library. The signatures of the methods they define are similar: they have the same name, and similar parameters (common classes from the Java standard library replace those of C++, such as List which is used instead of std::vector). Thanks to an integration with Java Native Interface (JNI) in Universe, any Java solver implementing an interface from JUniverse can be used as a Universe solver. Said differently, developers of Java solvers do not need to provide a C++ port to their solvers: they only need to implement JUniverse in Java, and Universe does the rest.

4 A REMOTE CONTROL FOR SOLVERS

SAT, PB, or CP solvers may be considered as black-boxes for laypeople. They often provide many parameters, and understanding the impact of changing one of them is not straightforward. On the contrary, solver developers often know well how to interpret the behaviour of their solver, and how to tune it to get the best performance on a hard instance. In both cases, monitoring the behaviour of the solver is crucial. The most common approach is to regularly output the solvers statistics in the console in which the solver is run. Another approach is that implemented in Sat4j (Le Berre and Roussel, 2014), which pro-
vides a remote control to modify its configuration and to graphically visualize the statistics of the search. Based on the Universe interface, we present a universal remote control inspired by that of Sat4j, that can be used to control and monitor any solver implementing the Universe interface. This tool may be useful for both solver developers and end-users, as it can be used either for debugging purposes and for finding the most appropriate configuration for solving a particular problem. This tool is publicly available on GitHub. In the following, we describe the different features it provides.

4.1 Solver Configuration

The remote control provides a graphical interface for configuring the solver by exploiting the methods provided by the IUniverseConfigurableSolver. The user interface is dynamically built based on the strategies that are recognized by the solver for variable and value selection heuristics, restart policies and learned constraint deletions (a different tab is provided for each of these features, see Figure 2). Users can choose the strategy they want to apply by selecting it in a combobox, and they can then set the (optional) parameters of the selected strategy to finely configure it. The critical feature of the remote control is that this configuration can be applied before running the solvers, but also while it is running (of course, if the underlying solver supports such an update). This allows one to immediately see the impact of a strategy compared to another, and thus to guide users towards finding the most appropriate one to solve their problem. In the same spirit, the remote control allows one to manually trigger a restart or a learned constraint deletion. For solvers that do not implement IUniverseConfigurableSolver, the remote control can still be used, but the configuration tabs are disabled. Only the solver execution and its monitoring are available for such solvers.

4.2 Live Statistics

As for the remote control provided by Sat4j, the solver’s statistics are displayed live during its execution. In addition to the solver’s logs that are redirected to the remote control window, six plots are updated at each conflict encountered by the solver, as shown in Figure 4:

- the size of the constraint learned by the solver after this conflict,
- the quality of the learned constraints,
- the number of negative (resp. positive) decisions made before the conflict,
- the decision level at which the conflict occurred, and
- the total number of assigned variables when the conflict occurred.

Together, these plots provide a representation of the solver behaviour that is more visual and interpretable than their textual counterpart printed in the logs.

4.3 Live Search Tree

The remote control also offers to display the search tree while it is being explored by the solver. Each time a new decision is made by the solver, a node is added to the tree, with a label displaying the corresponding decision. Conflicts and solutions are the leaves of the tree, and are displayed in red and green, respectively. An example of such a tree is given on Figure 3. This feature should however be used with caution, and on rather small inputs. Indeed, the search tree that is built by the solver may be very large, and displaying it may not be possible in the window of the remote control. Additionally, showing the search tree live may have an impact on the solver performance, which may become very slow.
5 CONCLUSION

In this paper, we introduced the Universe interface, which provides a universal interface for SAT, PB and CP solvers. Universe allows one to configure a solver, fill it with constraints, solve the associated problem and follow its trace while it is being executed, making it possible to seamlessly integrate various solvers in different applications. Based on this interface, this paper also introduced a universal remote control for solvers, providing a graphical user interface for performing the operations described above while the solver is running. As perspective for future works, we plan to develop more adapters for other popular solvers developed by the community. We also would like to complete the Universe ecosystem by designing new tools, such as, e.g., a modeling system that can be integrated into any application.

ACKNOWLEDGEMENTS

The authors would like to thank Michaël Valet, who did a significant contribution to the remote control presented in this paper during its internship at CRIL.

REFERENCES


