A Sequential Heuristic for the Efficient Management of a Work Center’s Stocking Area

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Abstract: In our partnership with a leading company specializing in automatic cutting machines for reinforcement processes, we address the management of a work center whose optimization calls for the solution of four distinct subproblems. Focusing on the third one, the subproblem asks for the effective packing of items on the identical buffers of a stocking area. The items arrive divided into subgroups (i.e., patterns), are associated with orders, and have time windows. We devise an SVC heuristic that efficiently determines feasible packing solutions while simultaneously minimizing the number of used buffers, lowering operations and fragmented orders. The SVC incorporates the idea of reachable points to restrict the location sets on the buffers. The experimental campaign highlights the SVC’s effectiveness in achieving optimality for small realistic instances, with a specific emphasis on reducing fragmented orders. Additionally, the approach showcased its ability to explore the multi-objective space and demonstrated scalability in solving practical instances.

1 INTRODUCTION

In today’s rapidly evolving manufacturing landscape, efficiency, precision, and flexibility are paramount for companies striving to remain competitive. Cutting processes are employed by a large variety of companies to realize products and semi-finished products, distinguishing the treated materials and shapes and depending on the subsequent destinations and uses. The assortment of raw materials, the variety of the parts to cut and their distribution of demands typically affect the practical difficulty of identifying effective patterns with small fractions of waste (Wässcher et al., 2007). The uses of parts cut, such as further manufacturing, assembly, or handling operations, call for a wider perspective in which cutting processes are tightly interlaced with the whole firm environment, and their effective management must go beyond the simplistic material saving. Aspects that cannot be neglected are, for instance, the number of setups (i.e., changes among cutting patterns) (Umetani et al., 2003), the schedule of the operations (Arbib and Marinelli, 2014) and the collection of parts into temporary stacks (Below and Scheithauer, 2007).

One significant development in this pursuit of operational excellence is the utilization of work centers designed for cutting material and seamlessly handling it through integrated stock areas. These advanced work centers represent a convergence of cutting-edge technologies, automation, and intelligent logistics management. They have modified traditional manufacturing paradigms by offering a holistic solution that addresses the challenges of material processing.

Based on the model of a prominent partner company (see the diagram in Figure 1), known for its leadership in designing and assembling automatic manufacturing machines, we illustrate the characteristics and the operations of a sophisticated work center employed for both cutting and handling iron bars in the reinforcement processes.

Figure 1: Block diagram of the manufacturing work center. Arrows represent tracks for material handling.
The work center includes a material loading machine for bar provision, capable of storing up to three assortments of materials. Each material has its specific length and diameter and includes a certain quantity of bars. Operators also can manually introduce additional materials into the loading machine.

A conveyor belt serves as the conduit for transferring batches of uniform iron bars to an automatic hydraulic cutter. This cutting system carries out sequential cuts according to cutting stock solutions pre-calculated by the company’s optimizing software.

Following each cutting operation, the resulting parts are released onto a transfer track. These are subsequently moved to specific coordinates, a process facilitated by mechanical dividers.

The transfer track is positioned between two symmetrical and identical unloading stations. Here, the parts are overturned among the stations and grouped into homogeneous lots; i.e., lots that share the same order code and have identical geometric attributes. Two portals equipped with grippers are stationed at the unloading stations. A portal empties its related station by collecting all the available lots and allocating the lots through lowering operations in a dedicated stocking area. This area hosts identical parallel buffers designed for lot collection. Importantly, homogeneous lots may be efficiently stacked together.

The portals offer flexibility by translating over the stocking areas, while lots are transferred exclusively lengthwise without altering their horizontal coordinates. Furthermore, the grippers on each portal operate independently, allowing for the separate allocation or retrieval of individual lots.

Once an order is consolidated, requests may arrive from downstream departments. The portals are then tasked with transporting the consolidated orders to releasing depots, positioned on both sides of the system. From these depots, the finalized orders leave the work center for further processing or distribution.

In the work center, the automatic cutter plays a critical role and acts as a bottleneck. It must halt its operation if the produced parts cannot find an allocation on the unloading stations, resulting in machine idle time. To maximize system efficiency, it is needed to effectively utilize the unloading stations, the buffers in stocking areas, and the portals. Given the challenging nature of the problem at hand, we divide the process into four distinct subproblems:

i) **Pattern Sequencing Optimization**: This entails determining the optimal sequence of patterns to minimize the spread of orders.

ii) **Part Partitioning on the Unloading Stations**: Subsets of parts are allocated between the two unloading stations to compose homogeneous lots, limiting the number of offloading operations.

iii) **Optimal Management of the Stocking Area**: The lots on an unloading station are transferred through a portal on the buffers of the stocking area, optimizing the occupied space and the stacking of lots.

iv) **Schedule of the Releases of Consolidated Orders**: The timing and scheduling of consolidated orders’ release are decided to minimize the portal’s busy time.

Because of the limited space, in this paper we focus on addressing subproblem iii). We introduce a sequential value correction heuristic (SVC) designed to optimize the packing of lots onto parallel buffers within a stocking area in a multi-objective fashion, generating a pool of non-dominated solutions. Optimization criteria are the minimization of the occupied space, the reduction of portal lowering operations, and the mitigation of order fragmentation. The SVC embeds the concept of reachable points to effectively describe the set of feasible destinations for lots on the buffers.

## 2 PROBLEM DEFINITION

In this section, we formalize the problem by describing the problem features and details while introducing some convenient notation.

The stocking area is modeled as a discretized grid of locations \((b,s) \in B \times S\), where the \(m\) buffers in \(B\) correspond to rows and slots in \(S\) are the columns. Each row has a width \(W\) given by the total width of the \(|S|\) identical slots of size \(w\).

We indicate with \(L\) the bill of orders and with \(I\) the set of items (lots) to allocate, such that \(|I| = n\). Each order \(i\) is a subset of homogeneous items with the same width \(w_i = w\) (assumed as multiple of \(w\)), a release date \(r_i\), and a due date \(d_i\). A subset of items \(S_i \subset S\) can be trivially identified for each item \(i\), limited to eligible items \(s \in S\) such that \(s \leq W - w + 1\). An order is considered fragmented if at least two items \(i, j \in I\) are packed in different locations. We use \(I_i^j\) to refer to the order comprising item \(i\).

Items arrive partitioned into unloading groups (patterns) according to an ordered list \(P = < p_1, \ldots, p_\Phi >\). Each pattern is a subset of items fitting within the capacity of the station \(W\). Items must be packed without overlapping on the buffer slots and a safety slack (i.e., a minimum number of empty slots between any two items) can be requested for application extent. The only exception holds for items shar-
ing an order, which can be stacked on the same buffer locations.

Each item in a pattern requires the selection of an absolute position \( s \) (i.e., left-side slot coordinate) to be occupied both on the station, before being packed, and on the destination buffer \( b \), after the lengthwise transport and the portal lowering. Note that, due to the independent grippers of the portal, two items in a pattern can be packed on different buffers using two distinct lowering operations (see Figure 2).

![Figure 2: A pattern made by three items 5, 3 and 2 on the unloading station (light grey area). Item 3 is stacked on the homogeneous item (bolded), the shaded area is the overlap- ping area. Dashed bars indicate the selected locations of 2 and 5. (a) is a feasible selection of locations, (b) is unfeasible due to the overlap on the unloading station.](image)

We express for brevity with \( i \in p \) if item \( i \) belongs to the pattern \( p \), with \( p' \in P \) the pattern containing \( i \).

Concerning the item dates, \( r' \) and \( d' \) are set as multiples of the unloading cycle (i.e., input patterns); e.g., \( r' = 2 \) and \( d' = 7 \) indicate respectively \( p' = p_2 \) and \( p' \) as the instant for the release of \( l' \). In our setting, \( d_l \) coincides with the last pattern containing an item in order \( l \). Thus, an item \( i \in l \) persists in the stocking area within the time window \([r_i, d_l] \). At time \( d_l \), all the items in \( l \) are collected and moved toward downstream departments through the release depot. Hence, two items \( i \) and \( h \) such that \( l' \neq l'' \) cannot share buffer locations only if their time windows overlap; that is, \([r_i, d_i] \cap [r_h, d_h] \neq \emptyset \).

As evaluation criteria for the problem, three measures are optimized in a multi-objective framework: the number of buffers employed during the whole packing procedure \( D \), the total number of lowering operations performed by the portal \( L \), and the number of fragmented orders \( F \). While \( D \) is an estimation of the required stocking area’s size \( m \), \( L \) evaluates the portal workload and \( F \) gives a measure of the potential saving in terms of space (and time, if looking at the finalized order release) that one may reach by relying on the stacking. To avoid trivial fragmentation, we assume that in any pattern \( p \) each item \( i \in p \) belongs to a distinct order \( l \).

### 2.1 Related Problems

The problem at hand is an extended one-dimensional bin packing problem (BPP) (Martello and Toth, 1990) that incorporates four additional peculiarities: the input consists of item groups (patterns), packing is done through lengthwise movements, items can be opportunely stacked and have time windows. To the best of our knowledge, no literature has addressed all these aspects simultaneously.

Regarding the input, the concept can be related to the bin packing with fragmentation problem (Casazza and Ceselli, 2016). In this problem, objects (our patterns) can be fragmented into multiple parts, and the goal is to minimize the number of bins used while limiting fragmentation or vice versa. However, in our scenario, fragments are restricted to the items within a pattern. Additionally, it can be easily seen that the cost associated with the item fragmentation does not directly correspond to the number of required lowering operations.

The constraint imposed by portal lengthwise movements must be considered alongside the first aspect; otherwise, singleton patterns (single items) wouldn’t be affected. The use of portals suggests a connection with storage yard operations in container terminals (Carlo et al., 2014) where rail-mounted gantry cranes are employed for container storage/retrieval and are limited by rails. In container yard operations, containers arrive separately by trucks, and the options for concurrent storage operations depend on the yard layout and crane type, but these operations follow different allocation rules from our packing problem.

The opportunity to stack homogeneous items has also been explored in virtual machine packing or pagination problems (Grange et al., 2018). Virtual machine packing involves allocating virtual machines (tiles) to a minimum number of servers (pages) to save resources between VMs sharing memory pages (symbols). In our context, virtual machines can be seen as patterns, servers as buffers, and symbols as items. However, there are differences: item sizes are not unitary as the symbols, and items within the same pattern may be placed in different locations.

This last point mismatches the assumptions set in the hypergraph partitioning problem (Catalyurek et al., 2023). In this problem, hypergraph vertices represent our patterns, hyperedges represent orders.
shared by connected vertices, and hyperedge weights are order widths. Hypergraph partitioning typically asks a fixed number of partitions (used buffers) and focuses on balancing the partition sizes, in place of observing a capacity constraint.

Lastly, time windows recall the recent temporal bin packing problem (Dell’Amico et al., 2020). Release and due dates are associated with items and the number of used bins must be reduced while considering the renewable resources. Although relatively new, several contributions have already been made to this problem; for a detailed literature review, refer to (Martinovic et al., 2023).

In conclusion, the SVC heuristic warrants some attention. Instead of opting for a rigorous yet time-consuming approach involving exact dual prices for pricing problems, algorithms of this kind use pseudoprices to gradually construct individual patterns. This approach has proven to efficiently compute good primal bounds in various packing scenarios, including the classical BPP (Cui et al., 2015) and CSP (Belov and Scheithauer, 2007), as well as their extended (Arbib et al., 2021) and enriched (Arbib et al., 2018) versions.

### 2.2 Reachable Points

Any solution to the problem provides a packing of items on the buffer locations. The set of slots amenable for placing the left side of item \( i \) are the ones that geometrically allow to respect buffer boundaries, and the ones that, once selected, admit a feasible position of the other items in \( p' \) at the unloading station. While the former was naturally embedded in the definition of each \( S'_i \), the latter can be exploited to reduce the set of feasible locations.

We call reachable points, namely \( r \)-points, the set \( R'_i \) of the slots in which the left-side of item \( i \) can be located and there still exists a way to pack each \( h \in p' \setminus \{i\} \). Clearly, \( R'_i \subseteq S'_i \) holds. Similarly to the procedure described in (Arbib et al., 2023), for all \( i \in p \) the sets \( R'_i \) can be computed through dynamic programming for the enumeration of the items left-side coordinates where \( p \) gives rise to a normal pattern (Christofides and Whitlock, 1977). A standard dynamic programming algorithm requires \( O(|p|^2W) \) operations per pattern.

An additional step can be further implemented to reduce the number of potential locations in each \( R'_i \). Given an order \( l \), each \( i \in l \) has a restricted \( R'_i \) given only by the \( r \)-points common to all items in \( l \). Formally, we are imposing:

\[
R'_i = \cap_{k \in P} R'_k,
\]

for each item \( i \in I \). Experiments on small instances showed that such construction can reduce the total number of \( r \)-points up to 27.0% compared to the \( r \)-points counted in \( \sum_{i \in l} |R'_i| \). The major drawback lies in pruning some of the solutions with fragmented orders, which can end up with an unfeasible instance if any \( R'_i = \emptyset \) holds.

### 3 A SEQUENTIAL VALUE CORRECTION HEURISTIC

Preliminary experiments carried out on real-world instances by using the mixed integer linear program \( M \) presented in (Pizzuti et al., 2022), showed the non-viability of the formulation. More in general, the company’s requirements demand a sufficiently efficient (and effective) solution method able to quickly identify packing strategies from scratch, and possibly re-optimizing for replying to the modifications of operations planning and work center status. For these reasons, we designed an SVC heuristic.

Given an ordered list \( P \) of unloading patterns, the SVC is used to build a tentative packing of items on the buffers of the stocking area. The algorithm initializes a pseudo-price \( \lambda_l \) to each order \( l \in L \) according to formula

\[
\lambda_l = \frac{w_l}{n} + \frac{d_l - \min_{r' \in R'_l} \{r\}}{|P|},
\]

The initialization promotes orders (items) with higher widths and longer time windows, which are critical to finding initial feasible (and possibly good) solutions. The SVC runs by packing orders’ items following non-increasing values of \( \lambda_l \) and the sequence of the patterns in \( P \); i.e., given \( i, h \in l, i \) is packed before \( h \) if \( i \in p_k, h \in p_j \) and \( k < j \). A packing decision must select a location \((b, s)\) for the left side of the item \( i \). Only its \( r \)-points, \( R'_i \) or \( R^i \) depending on the searching strategy, are considered feasible slots. Thus, each couple \((b, s)\) is tested and a location can be chosen if all \((b, s), \ldots,(b, s+w_i-1)\) are available within \([r', d_l]\), or are occupied by \( h \in l' \).

The best location \((b, s)\) is selected according to hierarchically ordered local criteria:

1. the smallest number of \( r \)-points forbidden to the remaining items of \( p' \) after packing \( l \);
2. the smallest number of locations used by items \( i \in l \);
3. the largest number of simultaneous packing on buffer \( b \);
4. the largest number of simultaneous collections from buffers;
5. the smallest number of available slots to the right of \(\tilde{s}\) in \(\tilde{b}\), divided by the length of \([r', d']\).
6. the largest number of unused periods (i.e., patterns) of the selected location.

Whenever an item is packed, locations \((\tilde{b}, \tilde{s}), \ldots, (\tilde{b}, \tilde{s} + w_i - 1)\) are flagged as occupied for each time step \([r', d']\). The \(r\)-points of each \(h \in p'\) are coherently updated to prevent overlapping.

Once all orders’ items are processed, a new feasible solution is stored in the pool if non-dominated with respect to \(D, L\), and \(F\) criteria.

The pseudo-prices are then conveniently enlarged by accounting for two terms: firstly, the ratio between the number of the used different locations by items \(i \in I\) and the number of patterns including any such \(i\); secondly, only for the orders with an item packed in the \(D\)-th buffer, the ratio between the current \(D\) and \(m\). While the former contributes to prioritizing currently fragmented orders, the latter advantages the orders packed after long persisting ones.

The SVC heuristic is repeated up to \(N_{SVC}\) times and the pool of non-dominated solutions is finally returned.

Using the sets \(R_i\) as \(r\)-points may lead to unfeasible partial solutions due to the over-reduction induced by the intersection step. To avoid this, in our implementation the algorithm firstly tries the packing with \(R_i\), then looks for alternative feasible locations in \(R_i\) once an unfeasibility occurs. Only if this second attempt fails, the current iteration is interrupted without a valid solution.

By using this scheme, in our experiments the SVC was able to converge to high-quality packing, in particular with low values of \(F\) and \(D\), while avoiding unfeasible states.

To provide a concise overview of the SVC heuristic, its pseudocode is provided in Algorithm 1. The initialization steps are performed by using dynamic programming (Line 1, see Section 2.2) and in linear time (Line 2), respectively. Sorting is done in \(O(|L| \cdot \log |L|)\) (Line 3) and \(r\)-points matrices are refreshed in \(O(|I| \cdot W)\) (Line 4). Finding the best locations (Lines 9 and 11) demands testing at most \(O(m \cdot |S|)\) positions, packing item \(i\) (Line 16) requires \(O(|P| \cdot W)\) locations modifications, and updating the \(r\)-points matrices (Line 17) is done in \(O(|L| \cdot W)\) as \(|p| \leq |L|\) for any \(p \in P\). These three steps are performed for each item \(i \in I\), thus asking \(O(|I| \cdot m \cdot |S| + |P| \cdot W + |L| \cdot W)\). To compute the objective criteria (Line 20), one needs to find the largest employed buffer \(b\) in the process lasting \(|P|\) time frames, and to count the number of lowering operations and fragmented orders; i.e., \(O(\sum_{p \in P} |p|^2)\) and \(O(\sum_{l \in L} |l|^2)\), respectively. Updating the pseudo-prices is done in linear time. Finally, the core (Lines 4-24) is repeated \(N_{SVC}\) times.

Algorithm 1: SVC heuristic.

Data: Sets \(L, I\) and \(P\), parameters \(B\) and \(S\)
Result: Pool \(Sol\) of non-dominated solutions.
Initialize \(R_i\) for each \(i \in I\);
Initialize \(\lambda_i\) for each \(l \in L\);
for \(N_{SVC}\) times do
    Sort orders by non-increasing \(\lambda_i\);
    Reset \(R_i\) for each \(i \in I\);
    \(sol = \emptyset\);
    \((\tilde{b}, \tilde{s}) = \emptyset\);
    for \(l \in L, i \in l\) do
        Find best location \((\tilde{b}, \tilde{s}) \in B \times R_i\);
        if \((\tilde{b}, \tilde{s})\) then
            Find best location \((\tilde{b}, \tilde{s}) \in B \times R_i\);
            if \((\tilde{b}, \tilde{s})\) then
                \(\text{go to 21}\);
        end
    end
    Pack \(i\) to \((\tilde{b}, \tilde{s})\) within \([r', d']\);
    Update \(R_i\) and \(R_i\) for each \(h \in p'\);
end
Update \(sol\);
Compute criteria values \(D, L\) and \(F\);
if \(\text{not dominated(sol)}\) then
    Add \(sol\) to pool \(Sol\);
end
Update \(\lambda_i\) for each \(l \in L\);
return \(Sol\);

4 COMPUTATIONAL RESULTS

Computational experiments were carried out on an Intel® Core(TM) i7-7500U 2.70 GHz with 16Gb RAM. The SVC algorithm was coded in C++ and runs with \(N_{SVC} = 1000\). For the sake of comparison on small cases, the mixed integer linear program \(M\) presented in (Pizzuti et al., 2022) was employed by using IBM® CPLEX® 12.8.0.0 with a time limit of 3600 seconds.

The experimental campaign counted two test beds: ten small realistic instances \(S = \{I_1, \ldots, I_{10}\}\) with 15 orders, whose features were generated similarly to the real ones; five real-world instances \(R = \{J_1, \ldots, J_5\}\) provided by the industrial partner with up to 105 orders. The grid sizes were set to \(|S| = 33\) and \(m = 12\), although the model \(M\) employed only 5 buffers. This allowed to optimally solve some of
the instances in $S$ by using $M$ within the time limit, whereas on $R$, this never occurred. Given the poor performance of $M$ on the second test bed, we do not explicitly report the results.

In the first set of experiments, the objective function was assumed to be $D + L + |J| \cdot F$ compliantly with the hypothesis set in $M$. Furthermore, the model made use of the tighter sets of r-points $R$. Starting from the left, Table 1 reports the details of the instances in $S$ within the first three columns. Then, statistics are given about the employed r-points: $R$ ($\bar{R}$) counts the total number of r-points in the sets $R_i$ ($\bar{R}_i$), whereas $R_{eg}$ ($R_{eg}$) gives the percentage used points with respect to the initial $\sum_{i \in S}$. Columns 8 and 9 provide the CPU times of the MILP, where $T$ generally indicates the time required to compute the best primal solution and $T_{tot}$ refers to the total approach running time. For $M$, when $T_{tot} = 3600$ means that the time limit was reached without proving the solution optimality. Finally, the remaining six columns show, the objective function components of the minimum cost solutions, the CPU times, and the number of non-dominated solutions $|Sol|$ found by the SVC for the multi-objective problem.

By using the sets $R_i$, the r-points diminished on the mean by 26.3%, lasting 512.6 per instance on the average. The further intersection step cut an additional 18.1% of the remaining r-points, leaving on the mean 419.9 per instance (the 60.3% of the original ones).

Moving to the SVC performance, the algorithm was always able to find the best primal solution computed by $M$. The objective function prioritized the reduction of the fragmented orders, which were 0.9 on the mean. Expect for $I_3$ and $I_7$, the CPU time demanded by the SVC was always smaller at least by one order of magnitude. Looking at $T_{tot}$, the SVC always terminated in 1.3 seconds and took 11.2 seconds in total to run on the whole test bed. To certify the optimality on closed instances (6 out of 10) $M$ needed 870.6 seconds in total.

Finally, the SVC identified 2.5 solutions on the mean per instance, only in 20% of the cases with $B > 5$ (in instances $I_2$ and $I_3$).

For the group $R$, Table 2 reports the instance features and the analysis of the r-points. Without recurring to the intersect step, the r-points in $R$ are 89.0% on the average of the initial points, which is significantly more than the 73.3% achieved in $S$. On the other hand, the intersection cut widely more points on this set, up to 75.1% in $I_1$ and 48.8% on the mean. Overall, the 53.3% of the original points were pruned by the procedure.

### Table 2: Basic features of instances $R$ and analysis on the r-points.

| $R$ | $|L|$ | $|P|$ | $n$ | r-points | $R$ | $R_{eg}$ | $R_i$ | $R_{eg}$ |
|-----|-----|-----|-----|---------|-----|-----|-----|-----|
| $J_1$ | 24  | 25  | 89  | 1724  | 72.3 | 430 | 18.0 |
| $J_2$ | 25  | 26  | 30  | 580  | 98.8 | 447 | 76.1 |
| $J_3$ | 80  | 60  | 156 | 3723 | 93.3 | 1723 | 43.2 |
| $J_4$ | 84  | 90  | 118 | 3219 | 91.6 | 1841 | 52.4 |
| $J_5$ | 105 | 74  | 186 | 4072 | 89.0 | 2063 | 45.1 |
| avg. | 63.6| 55.0| 119.8| 2663.6| 89.0| 1300.8| 47.0|

Table 3 shows the full pool of non-dominated solutions per instance, ordered by the required running time $T$. The SVC identified 5.8 solutions on the mean per instance, demonstrating its capability of diversifying the search. The values of $L$ and $F$ showed a more pronounced variability (with standard deviations up to 4.5 and 3.9 in $J_1$) than $D$ (at most 1.2 of standard deviation in $J_3$). This is understandable since an excessive increment in the number of the employed buffers typically compromises the performance on $L$ and $F$, both asking for compact packing (the former among a pattern’s items, the latter among order’s items).

The algorithm required 13.7 seconds on average
Table 3: Results obtained by SVC on instances $\mathcal{R}$.

<table>
<thead>
<tr>
<th>$\mathcal{R}$</th>
<th>Sol</th>
<th>$T_{tot}$</th>
<th>D</th>
<th>L</th>
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<th>T</th>
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<td>avg.</td>
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to terminate and at most 19.2 seconds for the largest instance with 105 orders. The computational burden scaled reasonably along with the input size.

Overall, the solutions provided by the SVC fulfilled the prescribed requirements and the algorithm is currently exploited in the partner company’s system.

5 CONCLUSIONS AND PERSPECTIVES

In the context of a partnership with a leading company in the design and assembly of automatic cutting machines for the reinforcement processes, we described the process performed by a work center model whose efficient management asks for the challenging solution of four distinct subproblems.

We focused on a peculiar packing subproblem for the optimal management of the identical buffers in the stocking area. In our problem items belong to orders, can be stacked in the same location if homogeneous and each has a relevant time window. Moreover, items arrive according to a prescribed list of patterns and, for each pattern, the items included cannot occupy coordinates that overlap even on different buffers.

We implemented an SVC heuristic to efficiently compute feasible packing minimizing the number of employed buffers, the total number of lowering operations, and the number of fragmented orders in a multi-objective fashion. The performance of the procedure was enhanced by embedding the concept of $r$-points as restricted sets of feasible destinations.

The experimental campaign highlighted the efficacy and efficiency of the SVC in optimally solving small realistic instances while prioritizing the reduction of fragmented orders. Moreover, on real-world instances results assessed the capability of exploring the multi-objective space by diversifying the search, and the scalability of the approach.

As future work we aim at handling subproblem iv), concerning the schedule of finalized orders’ release with arbitrary due dates, in the solution algorithm to reduce the portal workload for the evacuations of the buffers. Furthermore, the design of an algorithmic scheme that embeds the SVC and can efficiently solve the work center management problem as a whole is currently under investigation.

REFERENCES


Casazza, M. and Ceselli, A. (2016). Exactly solving pack...