

DataFITR: An Open, Guided Input Modeling Tool for Creating Simulation-Based Digital Twins

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Keywords: Input Modeling, Simulation, Digital Twins, Open Source, Graphical User Interface.

Abstract: Input Modeling (IM) is a critical step in the process of building simulation-based digital twins. It involves selecting a family of distributions to model the observed data and finding the distribution parameter values that best fit the data. Subsequently, random variates adhering to the selected distribution can be generated to create a simulation-based digital twin of the system. For complex systems, IM can be a nuanced process involving a series of decisions that require visual feedback at each step. There is currently a dearth of open, GUI-based tools for aiding the non-expert user in the process of IM. This paper presents DataFITR, a GUI-based, open Input Modeling tool we have developed for guiding the non-expert user through the steps of input modeling and automating several intermediate tasks. DataFITR is cloud-hosted with a web-based user interface. The user can upload data as a file and the tool guides the user through the IM process by suggesting types and suitable distributions for each observed variable. It generates multiple goodness-of-fit measures for a large set of standard discrete and continuous distributions and can also support arbitrary (non-standard) distributions using a Kernel Density Estimation approach. DataFITR also assists in exploratory data analysis by providing various statistical properties of the observed data and in finding correlations between output measures. Once a matching distribution is found, the tool generates Python code for producing random variates from the matching distribution, which can be directly inserted into a simulation model. In this paper, we describe the DataFITR tool and its features, and compare it with existing open libraries and tools for assisting IM. We present a simulation case study of a bottling plant to demonstrate the utility of the DataFITR tool in building simulation-based digital twins.

1 INTRODUCTION

A **Digital Twin** refers to a virtual replica or model of a physical system whose state is kept in sync with the real system via a continuous stream of observations or data from the real system. A digital twin may also be used to control the real system via feedback paths. Figure 1 illustrates the main components (such as sensing and actuation, data aggregation, simulation and dashboarding) that make up a digital twin. The use of digital twins has the potential to revolutionize sectors such as manufacturing, healthcare, urban planning, and transportation by enabling real-time decision-making using Internet of Things (IoT) technology and real-time analytics (Kritzinger et al., 2018).

A digital twin can either be purely data-driven or

simulation-based. In a purely data-driven digital twin, the behavior of the system and future predictions are derived solely from data. In contrast, a simulation-based digital twin can be used when the modeler has prior knowledge or can make reasonable assumptions about the behavior of the system. The system behavior, structural components and/or state transitions in the system are described by the modeler to create a parameterized simulation model and the exact values of these parameters are derived from observed data. Depending on the type of real system under consideration, simulation models can either be deterministic or stochastic, and are typically implemented using either a discrete-event simulation approach or continuous simulation paradigms.

Input Modeling (IM) is a critical step in the creation of digital twins. When performed incorrectly or without due care, the resulting model is prone to suffer from the *Garbage-In-Garbage-Out* problem and may yield incorrect insights or predictions. For a dig-

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ital twin the process of IM needs to be automated as the model needs to remain continuously in sync with incoming data. Traditionally, IM involves deriving simulation parameters (which can either be constants or parameters of an appropriate probability distribution) from data corresponding to multiple measured entities. For example, in a manufacturing plant, one might have a continuous stream of data corresponding to attributes such as time taken by a machine to perform certain kinds of tasks, the periodically monitored levels of inventory or raw material, energy consumption of a machine per-task etc. If a quantity (such as the time taken per-task) is assumed to be random, it can be modeled by generating random variates inside a stochastic simulation model, where the parent distribution of this random variable can be obtained from observed data. IM refers to the systematic process of selecting the appropriate distributions for each physical quantity and fitting their parameters to best match the observed data. For time-independent data, this process involves selecting the right distribution and finding the maximum likelihood estimators for the distribution using data. Several *Goodness of fit* measures can be used to describe the extent of match between the selected distribution and the observed data. These steps need to be repeated until a reasonable fit is achieved. For time-dependent data, this involves selecting the appropriate models (stationary/non-stationary) and mimicking the time-dependence using mathematical models such as Markov Chains or Moving-Average (MA) models (Banks et al., 2010). In a real system, it is often the case that some of the measured quantities are correlated. For example, the energy consumption of a machine for performing a certain task and the time taken to perform that task may be positively correlated. This correlation needs to be identified right at the outset, and modeled using multivariate distributions for generating random variates in the simulation model.

Thus the task of IM is nuanced and may require time and effort. However, with increasing ubiquity of digital twins and their creation or use by non-expert users, it becomes necessary to have tools that assist and guide the user in IM or automate some aspects of this task. Recently, deep-learning based approaches such as generative neural architectures have been proposed to automate IM (Cen et al., 2020). Such methods may require a large amount of training data. For cases where a modeler has some prior knowledge about the system behavior, traditional approaches may be better suited and efficient as standard distributions often end up mimicking the observed data really well. While there exist commercial tools such as ExpertFit (Law, 2020) and Stat::Fit

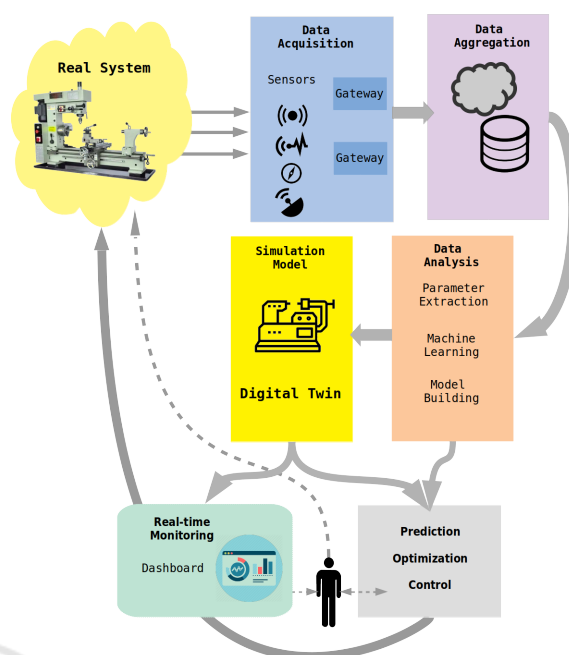


Figure 1: Components of a digital twin.

(Software, 2022) and libraries in programming languages (summarized in the next section) which can assist the user in IM by fitting distributions to data, there is currently a dearth of free/open IM tools targeted for the non-expert user. Desirable properties for an IM tool include a GUI interface, assistive features, support for a variety of goodness of fit tests, and the ability to fit correlated data and generate random variates. While some commercial tools provide some of these features, there is a lack of open/free tools for IM that offer a GUI-front-end and are targeted for the non-expert user.

This paper describes DataFITR - an open, GUI-based, cloud-hosted tool we have developed for assisting the non-expert user in input modeling. The tool is freely accessible via a browser at the URL: <https://datafitr.streamlit.app>. The user can upload their data as a csv (comma-separated-value) file. The tool then guides the user through the input modeling process in a step-wise manner while providing visual aids (such as data plots, histograms and color-coded correlation matrices) at each step. It automatically generates plots of the marginal distributions and a statistical summary of the data. The user can do exploratory data analysis of the columns in the data set and then proceed to find the distributions that best fit the data. The tool supports a large set of standard continuous and discrete distributions. It also implements and reports multiple goodness of fit measures such as Kolmogorov-Smirnov (KS) test metric, Chi-squared (χ^2) test measure, and Sum of Squares Error (SSE).

For data that does not match any standard distribution, the DataFITR tool can generate arbitrary uni-variate distributions to match the histogram using the Kernel Density Estimation (KDE) approach (Parzen, 1962). Most importantly, once a desired distribution is found, the tool automatically produces Python code for random variate generation corresponding to the selected distribution. This code can be directly copied into a stochastic simulation model to generate the random variates. DataFITR has been written in Python, and a GUI front-end is created using the Streamlit library (Streamlit, 2022). The tool is currently cloud-hosted on the Streamlit community cloud. DataFITR currently supports time-independent models (with a large set of standard distributions or arbitrary distribution), and for correlated data multi-variate Gaussian distributions are currently supported. We plan to add support for time-dependent models and arbitrary multi-variate distributions in future versions.

The rest of this paper is organised as follows: In Section 2 we provide a brief overview of open libraries and existing tools available for building digital twins with a focus on IM. In Section 3, we describe the features, usage flow and details of the DataFITR tool. In Section 4 we present a simulation case study of a bottling plant which serves to highlight the utility of the tool. In this case study, we generate data using a known reference model (a discrete-event simulation model) of a bottling plant, and use this data and some knowledge about the real system to create a matched model automatically using the DataFITR tool. We present results showing the extent of match between the original reference model and the matched model in terms of the system parameters and output/performance measures. Finally, we present conclusions and future plans in the last section.

2 RELATED WORK

A broad survey of tools and processes in creating digital twins is presented in (Fuller et al., 2020). Input Modeling (IM) is a critical step and historically IM techniques have focused on offline system models (Cheng, 2017). An overview of IM techniques for various problem domains is described in (Nelson and Yamnitsky, 1998). Commercial software tools such as *ExpertFit* (Law, 2020) and *Stat::Fit* (Software, 2022) support in IM by identifying probability distributions to fit observed data. These tools also assist the user in selecting a distribution when data is unavailable based on system knowledge, for aspects such as task times and equipment failures. *XL-STAT* (Lumivero, 2022) is a commercial Excel-based

tool that can be used for IM. Aside from commercial tools, a few libraries in popular programming languages such as Python and R exist for fitting probability distributions to data. *Distfit* (Taskesen, 2020) and *fitter* (Cokelaer, 2020) are two examples of open Python-based libraries. Both can be used to fit standard uni-variate distributions. *fitteR* (Boenn, 2022) is an R-based version for fitting distributions to empirical data. *Distribution fitter* (Distributionfitter, 2022) is a python based GUI application which is built using the *fitter* package. It can be used to fit univariate distributions. *Distribution Analyser* (DistributionAnalyser, 2022) is another Python-based application that helps users analyze univariate distributions. It also allows the users to fit the data into univariate distributions. While these are libraries that can be used via interface routines, the DataFITR tool described in this paper is a GUI-based tool that does not require any programming for its use. Table 1 summarizes the different features and scope of these libraries along with the DataFITR tool proposed in this paper.

3 DataFITR: FEATURES AND USAGE

DataFITR is open-source (released as a public repository on GitHub at (Lekshmi P, 2023)). It is currently hosted on Streamlit public cloud and freely accessible via a browser at <https://datafitr.streamlit.app>. The user can upload the data in a csv (comma separated value) format where each column corresponds to a single measured quantity and the first row is assumed to contain the names of each quantity. For categorical type of data, it is assumed that the data is integer-valued.

DataFITR currently supports modeling time-independent, *Independent and Identically Distributed (IID)* data where each measured quantity (column in the data file) is independent. It also supports modeling the case where some of the columns are correlated. For the multivariate case the tool currently supports only Gaussian distributions, and the ability to fit arbitrary multivariate distributions is planned to be implemented in future. The side panel in the tool can be used for selecting one of these cases for the IM flow. To fit time-independent IID data, user can upload the file on the on the page corresponding to the time-independent data. Once the user uploads a file, the tool automatically identifies the column headings and whether each column corresponds to real-valued (continuous) or integer-valued (categorical) data, creates histograms showing the marginal distributions of each columns. It also generates a statistical summary

Table 1: Comparison of tools and libraries for IM.

Features	Distfit	fitter	Distribution Analyser	Distribution fitter	DataFITR
GUI , Visualization	×	×	✓	✓	✓
Random Variable Gen	×	×	✓	×	✓
Arbitrary distributions	×	×	×	×	✓
Support for Multivariate Gaussian distribution	×	×	×	×	✓
Num Goodness of fit measures used	3	1	1	1	3
Std distributions	89	80	97	80	100
Dependencies	Scipy	Scipy	Scipy, Streamlit	Scipy, Streamlit	Scipy, Streamlit

of each column. The tool then produces a correlation matrix between every pair of columns and points out the columns with high correlation. This indicates to the user whether some quantities need to be modeled using the multivariate case. The user can then proceed with one column at a time to find the best-fitting distributions by confirming the details entered by the tool based on the data (as shown in Figure 2) and obtain Python code for generating random variates from that distribution. The user can also edit the options entered by the tool. The tool then generates histograms and plots for visualizing the extent of fit for a selected set of standard distributions (as shown in Figure 3) and also generates a distribution matching the histogram using the KDE approach for data that does not resemble any standard distribution.

DataFITR supports **97 standard continuous distributions** and **3 discrete distributions** (Poisson, Binomial and Geometric). For continuous distributions, users can either select the set of popular/common continuous distributions (such as Normal, Triangular, Uniform, Exponential, Lognormal, Weibull, and Gamma) or all of the 97 standard continuous distributions for performing a best fit with the data. For the selected set of standard distributions, the tool first finds the distribution parameters (maximum likelihood estimators) to best fit the data, and then for each distribution it reports three goodness of fit measures in a table. The Kolmogorov–Smirnov (KS) statistic quantifies the distance between the empirical distribution function of the sample and the cumulative distribution function of the reference distribution. The Chi-squared (χ^2) test measures the distance between the normalized data histogram and the probability density function of the reference distribution. The Sum of Squared Errors (SSE) metric is the sum of squares of the differences between the probability density function (pdf) of the reference distribution and the data histogram, with a specific bin size selected for the data. Once a matching distribution is found, the user can select the desired distribution and the tool generates Python code that can be directly copied to the simulation model as shown in Figure 4. Further, the

tool also has a feature for generating Python code for random variate generation for selected standard distributions. For this the user has to supply the distribution name and the parameters. Finally, the summary of the matched distributions can be seen by the user in the *View Output Summary* tab.

4 CASE STUDY

Table 2: Model parameters and their values used in the reference model and estimated values of the model parameters in the matched model.

Parameter (unit)	Reference model (distribution, parameter)	Matched model (distribution, parameter)
per job delay of cap unit (mins)	uniform a=1.25 b=2.00	uniform a=1.250 b=1.999
per job delay of bottle unit(mins)	exponential $\lambda=0.50$	exponential $\lambda=0.500$
per job delay of filling capping unit(mins)	normal $\mu=2.75$ $\sigma=0.05$	normal $\mu=2.7500$ $\sigma=0.0505$
interval of refill raw materials(mins)	uniform a=60 b=90	uniform a=60.52 b=88.99
amount of plastic for cap unit(numbers)	constant 1	constant 1
amount of plastic for bottle unit(numbers)	constant 3	constant 3
amount of drink for filling (millilitres)	constant 200	constant 200

We present a case study that illustrates the use of the DataFITR tool for creating simulation-based digital twins. In this case study we assume that the real system is represented by a *reference model* of a **bottling plant** containing various processes and components as illustrated in Figure 5. We have built a detailed Discrete-Event simulation model of this system using the SimPy library (Klaus G. Müller, 2020) in Python. Simulating this reference model generates data mimicking the data stream that would have been generated by a manufacturing IoT infrastructure in a real man-

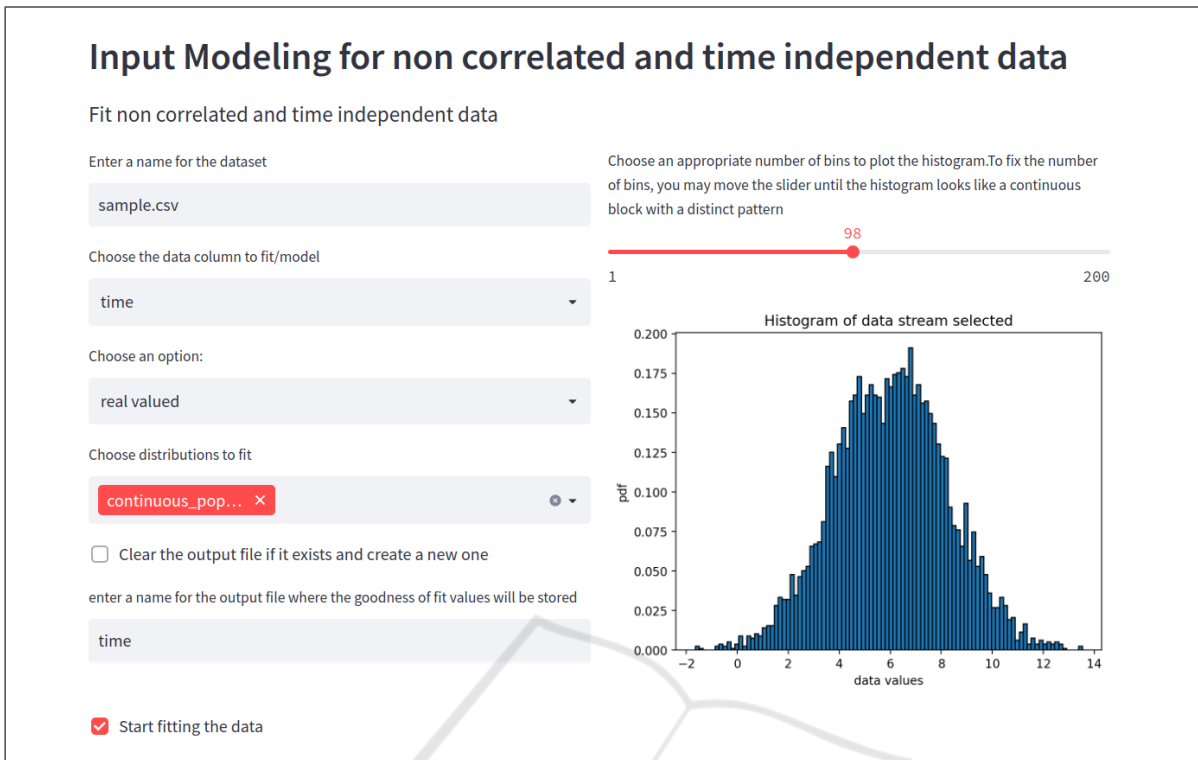


Figure 2: DataFITR: Choosing the datatype, the number of bins and the set of distributions to fit.

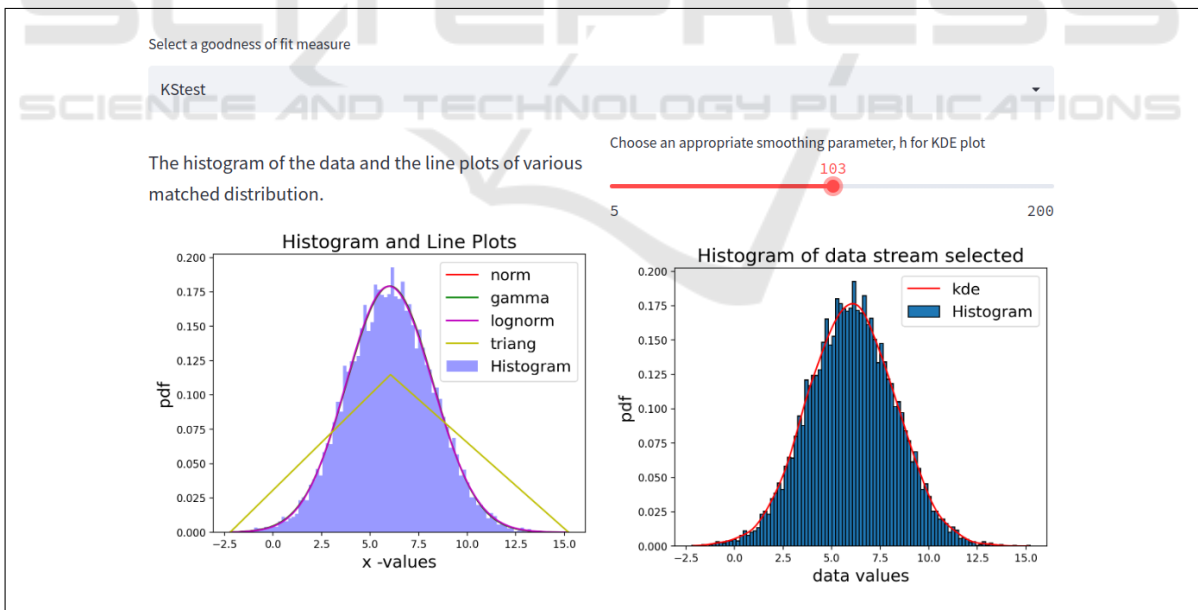


Figure 3: DataFITR: Results of IM for the selected column.

ufacturing system. This data is automatically saved into a csv file and serves as an input to the DataFITR tool. We then use the generated data along with the DataFITR tool to build another model (a *matched model*) of the system which would serve as the under-

lying model in a simulation-based digital twin. Because the reference model is known, we can then report the extent of match between the *reference model* and the *matched model*, serving as a validation exercise and an illustration of the utility for the DataFITR

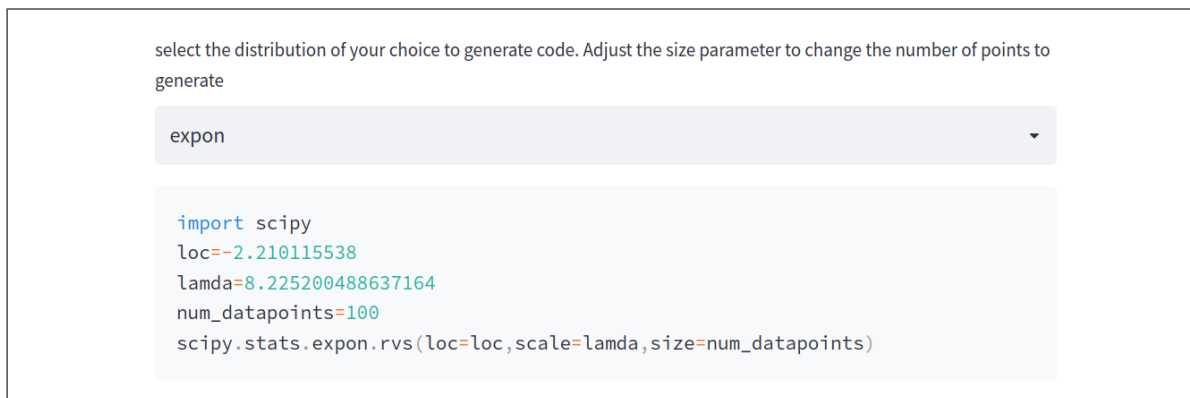


Figure 4: DataFITR: Random variate generation for the fit distribution.

Table 3: Comparison of output performance measures averaged across 750 simulation runs.

Parameter (unit)	Reference model	Matched model	Error in %
Throughput (Num products/hour)	18.92000	18.91000	0.035
Average cycletime (mins)	6.48700	6.48800	0.006
Resource utilisation of cap unit(%)	0.86970	0.86950	0.004
Resource utilisation of Bottle unit(%)	0.86863	0.86861	0.002
Resource utilisation of filling-capping unit (%)	0.86720	0.86710	0.005

tool.

Figure 5 shows a bottling plant with four stages connected in an assembly line fashion. The four stages are cap-making, bottle-making, bottle-filling, capping, and refilling. The green blocks supply the raw materials and are real-valued components and the red blocks are the integer-valued components. The yellow blocks are the machines where the active manufacturing process takes place. The model’s parameters are the per-job delays at each unit, the amount of plastic required to make a cap, a bottle and the amount of drink required to fill a bottle. These are shown in blue blocks. The raw materials are stored separately and their levels are monitored continuously. A refill process replenishes the raw materials periodically. There is downtime for all machines while the refilling process takes place. The caps and bottle bodies are manufactured and stored separately. The drink mix is filled into bottles and capped at the next stage. Finally, these bottles are moved to a store and can be supplied to various distribution units.

The process delays are modeled as random variables with parameters summarized in Table 2. The *reference model* generates timestamped data which is similar to what an IoT framework in a manufacturing

unit would have generated. This data becomes the input to the DataFITR and the generated code from the DataFITR is used for generating random variables in the *matched model*. After this, both the simulation models are run and a comparison of the output performances is presented to evaluate the extent of the match of both models.

4.1 Model Parameters and Implementation

The simulation model parameters identified from the *reference model* are listed in Table 2. The first four parameters are variable and the remaining three are constant. This *reference model* is implemented in a python package called SimPy. It is a framework for developing Discrete Event Simulation. It is based on processes which are simple python generator functions. In the *reference model*, separate processes are developed to simulate a cap-making unit, a bottle-making unit, a filling and capping unit, and a refilling unit. Units that are used to store the raw materials are modeled as containers which is a shared resource. In the *reference model*, plastic and drink mix are stored in a shared resource called a container with a capacity of 1000 no.s and 25 L, respectively. The manufactured caps, bottle bodies, and the filled and capped bottles are stored in another type of resource called a Store. In one simulation, the plant is run for 1000 hours. 750 such simulations are run, and the parameters listed in Table 3 are estimated from the simulation runs.

4.2 Performance Estimation and Results

The output performance measures (such as system throughput, average cycle time and resource utiliza-

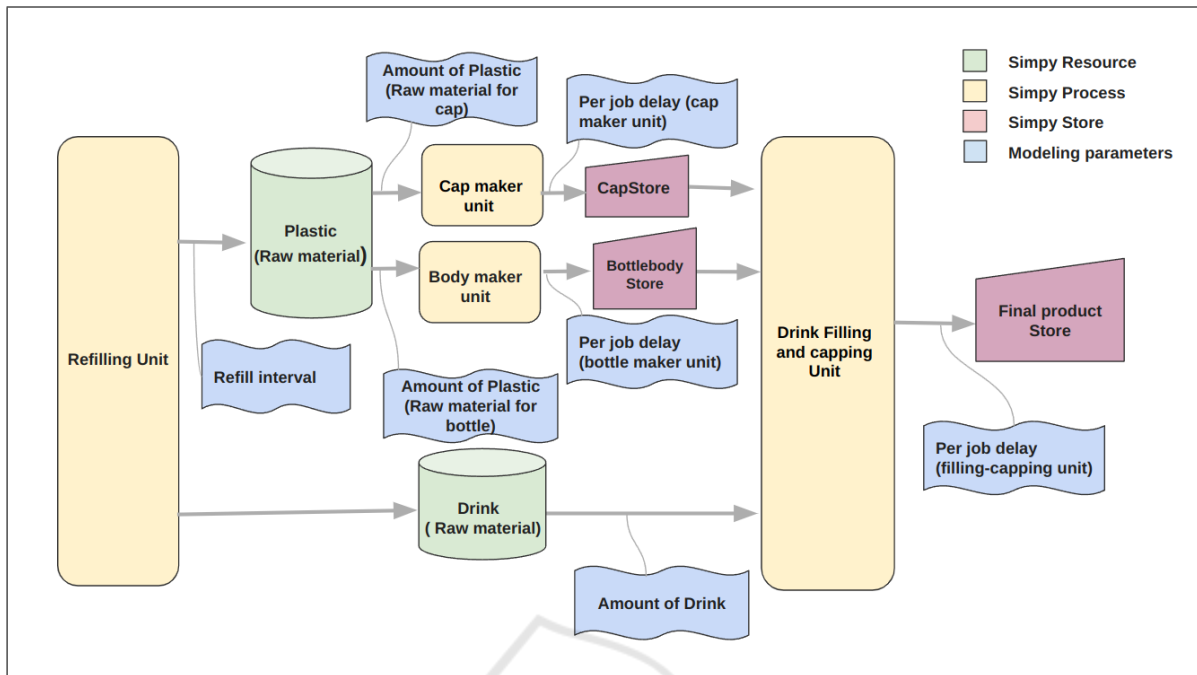


Figure 5: Schematic of a bottling plant.

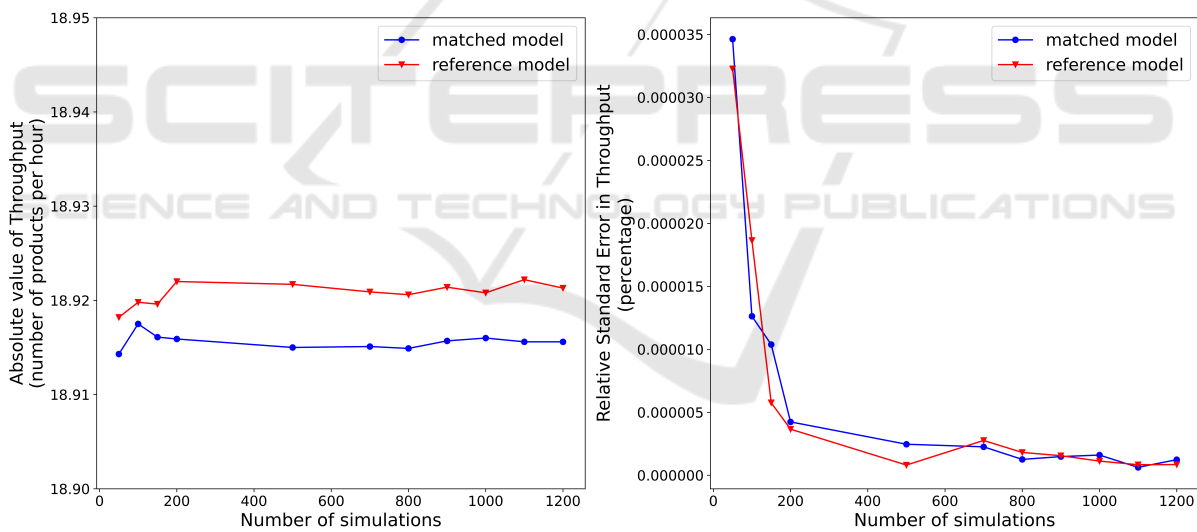


Figure 6: Plot showing the extent of match between the *reference model* and *matched model*. Plot on the left shows the variation of absolute value of throughput with respect to the number of simulation runs and the plot on the right shows the variation of the relative standard error in throughput with respect to the number of simulation runs.

tion of each of the processing machines) are estimated after averaging the results from multiple stochastic simulation runs. The number of simulation runs required to get an estimate with reasonable accuracy is determined after calculating the relative standard error. Figure 6 shows the extent of match between the *reference model* and *matched model*. The x-axis is the number of simulation runs, and y-axis are absolute value of throughput and relative standard error in

throughput. The result from the *reference model* are compared with the results from the *matched model* and summarized in tables 2 and 3. We observe that the percentage error between the two models is small. In this exercise, we assumed that a modeler has prior knowledge about the structure and components in the model and the DataFITR tool was simply used to match the parameter values of one model to another. Inferring the model structure/behavior itself from data

is an interesting problem relevant to rapid deployment of digital twins. The case study highlights the ease of use of the DataFITR tool.

5 CONCLUSIONS

This paper presented DataFITR, an open, cloud-based tool for assisted input modeling. The tool has features to perform automatic exploratory data analysis, find correlations between measured quantities, and identify distributions and their parameters to best match the observed data using multiple goodness of fit measures. At each step the tool generates visual aids (such as histograms and plots) to help the user select an appropriate model and the tool also takes input from the user such as prior knowledge about the possible set of distributions likely to mimic observed data. For data that cannot be modeled using standard distributions, the tool supports generating arbitrary density functions using the KDE approach. Most importantly, DataFITR automatically generates Python code for producing random variates of the matching distribution which the user may directly copy into a simulation model of the system. We have also presented a comparison of our tool with other open-source packages. A case study of a bottling plant was presented to illustrate the utility of the tool. Currently, the tool implements models for iid data. Fitting arbitrary multi-variate distributions and modeling time-dependent data are features planned to be implemented in future versions.

REFERENCES

- Banks, J., II, J. S. C., Nelson, B. L., and Nicol, D. M. (2010). *Discrete-Event System Simulation, 5th New International Edition*. Pearson Education.
- Boenn, M. (2022). fitteR: Systematic fit of hundreds of theoretical univariate distributions to empirical data. <https://cran.r-project.org/web/packages/fitteR/index.html>.
- Cen, W., Herbert, E. A., and Haas, P. J. (2020). Nim: Modeling and generation of simulation inputs via generative neural networks. In *2020 Winter Simulation Conference (WSC)*, pages 584–595.
- Cheng, R. (2017). History of input modeling. In *2017 Winter Simulation Conference (WSC)*, pages 181–201.
- Cokelaer, T. (2020). fitter: A Python library for fitting probability distributions to data. <https://fitter.readthedocs.io/en/latest/index.html>.
- DistributionAnalyser (2022). Distribution Analyser: An app to interactively explore and fit continuous distribution functions. <https://rdzudar-distributionanalyser-main-45cc69.streamlit.app/>.
- Distributionfitter (2022). Distribution fitter: An app to compare multiple distributions and find the best one that fits your data. https://github.com/rahul-raoniar/distribution_fitter_streamlit_app.
- Fuller, A., Fan, Z., Day, C., and Barlow, C. (2020). Digital twin: Enabling technologies, challenges and open research. *IEEE Access*, 8:108952–108971.
- Klaus G. Müller, T. V. (2020). SimPy: Discrete-event simulation framework for Python. <https://simpy.readthedocs.io/en/latest/>.
- Kritzinger, W., Karner, M., Traar, G., Henjes, J., and Sihm, W. (2018). Digital twin in manufacturing: A categorical literature review and classification. *IFAC-PapersOnLine*, 51(11):1016–1022. 16th IFAC Symposium on Information Control Problems in Manufacturing INCOM 2018.
- Law, A. M. (2020). ExpertFIT. <http://www.averill-law.com/distribution-fitting/>.
- Lekshmi P, Neha Karanjkar, T. L. (2023). DataFITR: public repository. <https://github.com/NehaKaranjkar/DataFITR>.
- Lumivero (2022). XLSTAT: DISTRIBUTION FITTING. <https://www.xlstat.com/en/>.
- Nelson, B. and Yamnitsky, M. (1998). Input modeling tools for complex problems. In *1998 Winter Simulation Conference. Proceedings (Cat. No.98CH36274)*, volume 1, pages 105–112 vol.1.
- Parzen, E. (1962). On estimation of a probability density function and mode. *The Annals of Mathematical Statistics*, 33(3):1065–1076.
- Software, G. M. (2022). Stat::Fit Distribution Fitting Software. <https://www.geerms.com>.
- Streamlit (2022). Streamlit: A open-source app framework for Machine Learning and Data Science. <https://docs.streamlit.io/>.
- Taskesen, E. (2020). Distfit: A python package for probability density fitting of univariate distributions. <https://erdogant.github.io/distfit/pages/html/index.html>.