Visual Looming from Motion Field and Surface Normals

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Abstract: Looming, traditionally defined as the relative expansion of objects in the observer’s retina, is a fundamental visual cue for perception of threat and can be used to accomplish collision free navigation. In this paper we derive novel solutions for obtaining visual looming quantitatively from the 2D motion field resulting from a six-degree-of-freedom motion of an observer relative to a local surface in 3D. We also show the relationship between visual looming and surface normals. We present novel methods to estimate visual looming from spatial derivatives of optical flow without the need for knowing range. Simulation results show that estimations of looming are very close to ground truth looming under some assumptions of surface orientations. In addition, we present results of visual looming using real data from the KITTI dataset. Advantages and limitations of the methods are discussed as well.

1 INTRODUCTION

The visual looming cue, defined quantitatively by (Raviv, 1992) as the negative instantaneous change of range over the range, is related to the increase in size of an object projected on the observer’s retina. Visual looming can be used to define threat regions for obstacle avoidance without the need of range and image understanding. Visual looming is independent of camera rotation and can indicate threat of moving objects as well.

Studies in biology have shown strong evidence of neural circuits in the brains of creatures related to the identification of looming (Ache et al., 2019). Basically, creatures have instinctive escaping behaviors that tie perception directly to action. This way creatures can avoid impending threat from predators that project an expanding image on their visual systems (Evans et al., 2018)(Yilmaz and Meister, 2013). Also, there is evidence of looming being involved in specialized behaviors, for example controlling the action prior to an imminent collision with water surface as exhibited by plummeting gannets (Lee and Reddish, 1981) or acrobatic evasive maneuvers exhibited by flies (Fabian et al., 2022)(Muijres et al., 2014).

According to Gibson (Gibson, 2014), motion relative to a surface is one of the most fundamental visual perceptions. He argued that visual information is processed in a bottom up way, starting from simple to more complex processing. The perceived optical flow resulting from motion of the observer is sufficient to make sense of the environment where a direct connection from visual perception to action can be established. Optical flow analysis is a primitive, simple and robust method for various visual tasks such as distance estimation, image segmentation, surface orientation and object shape estimation (Albus and Hong, 1990)(Cipolla and Blake, 1992).

Optical flow is the estimation of the motion field, which is the 2D perspective projection of the true 3D velocity field as a consequence of the observer’s relative motion. Optical flow can be calculated using a number of algorithms that process variations of patterns on image brightness (Horn and Schunck, 1981)(Verri and Poggio, 1986)(Zhai et al., 2021).

Optical flow measurements, as the estimation of motion field, includes the necessary information about the relative rate of expansion of objects between two consecutive images from which the visual looming cue can be estimated (Raviv, 1992).

In this paper, we present two novel analytical closed form expressions for calculating looming for any six-degree-of-freedom motion, using spatial derivatives of the motion field. The approach can be applied to any relative motion of the camera and any
visual surface point. In addition, we show the theoretical relationship between the value of looming and surface orientation. In simulation results we show the effect of the surface normal to the accuracy of the estimated looming values. We demonstrate a new way to extract looming from optical flow using the RAFT model and derived relevant expressions. We show that egomotion is not required for estimating looming. In other words, knowledge of range to the point, as well as relative translation or rotation information are not required for computing looming and hence for autonomous navigation tasks.

2 RELATED WORK

2.1 Visual Looming

The visual looming cue is related to the relative change in size of an object projected on the observer’s retina as the range to the object increases (Figure 1.a). It is defined quantitatively as the negative value of the time derivative of the range between the observer and a point in 3D divided by the range (Raviv, 1992):

\[
L = \lim_{\Delta t \to 0} \frac{r_2 - r_1}{\Delta t} \frac{1}{r_1} \quad (1)
\]

\[
L = -\left( \frac{\dot{r}}{r} \right) \quad (2)
\]

where \( L \) denotes looming, \( t_1 \) represents time instance 1, \( t_2 \) represents time instance 2, \( \Delta t \) is \( t_2 - t_1 \), \( r_1 \) is the range to the point at time instance \( t_1 \), and \( r_2 \) is the range at time instance \( t_2 \). Dot denotes derivative with respect to time.

Please note that in this paper we use the terms camera, observer and vehicle interchangeably.

2.1.1 Looming Properties

Note that the result for \( L \) in equation (2) is a scalar value. \( L \) is dependent on the vehicle translation component but independent of the vehicle rotation. Also \( L \) is measured in \([time^{-1}]\) units.

It was shown that points in space that share the same looming values form equal looming spheres with centers that lie on the instantaneous translation vector \( \mathbf{t} \) and intersect with the vehicle origin. These looming spheres expand and contract depending on the magnitude of the translation vector (Raviv, 1992).

Since an equal looming sphere corresponds to a particular looming value, there are other spheres with varying values of looming with different radii. A smaller sphere signifies a higher value of looming as shown in Figure 1.b \((L_3 > L_2 > L_1)\).

Regions for obstacle avoidance and other behavior-related tasks can be defined using equal looming spheres. For example, a high danger zone for \( L > L_3 \), medium threat for \( L_3 > L > L_2 \) and low threat for \( L_2 > L > L_1 \).

2.1.2 Advantages of Looming

Looming provides time-based imminent threat to the observer caused by stationary environment or moving objects (Raviv, 1992). There is no need for scene understanding such as identifying cars, bikes or pedestrians. Threat regions can be obtained from looming values by assigning specific thresholds. Figure 2.a shows the looming sphere as a function of time for a given constant speed. For the same identical values of looming \( L_1, L_2 \) and \( L_3 \), Figure 2.b shows equal looming spheres using two (time based) threat zones. Figure 2.b1 shows looming spheres at low speed and Figure 2.b2 shows looming spheres at high speed. Note that the radii of the spheres are proportional to the speed of the vehicle.

Visual looming can provide indication of threat from moving objects as shown in Figure 3. Threats from approaching objects are visualized as bright red colors while receding objects appear in blue.

Figure 1: Visualizing looming cue: a) relative expansion of 3D object on spherical image, b) equal looming spheres as shown for a given translation \( \mathbf{t} \).

Figure 2: Looming spheres: a) Looming spheres superimposed on vehicle trajectory; b) for given identical looming values b1 shows the looming spheres for low speed and b2 shows the looming spheres for high speed.
2.1.3 Measuring Visual Looming

Several methods were shown to quantitatively extract the visual looming cue from a 2D image sequence by measuring attributes like area, brightness, texture density and image blur (Raviv and Joarder, 2000).

Similar to visual looming, the Visual Threat Cue (VTC) is a measurable time-based scalar value that provides some measure for a relative change in range between a 3D surface and a moving observer (Kundur and Raviv, 1999). Event-based cameras were shown to detect looming objects in real-time from optical flow (Ridwan, 2018).

2.2 Motion Field and Optical Flow

Motion field is the 2D projection of the true 3D velocity field onto the image surface while the optical flow is the local apparent motion of points in the image (Verri and Poggio, 1986). Basically, optical flow is an estimation of the motion field that can be recovered using a number of algorithms that exploit the spatial and temporal variations of patterns of image brightness (Horn and Schunck, 1981). From the computer vision perspective the question is how to obtain information about the camera motion and objects in the environment from estimations of the motion field (Aloimonos, 1992). Optical flow algorithms are divided into three categories: knowledge driven, data driven and hybrid. A comprehensive survey of optical flow and scene flow estimation algorithms were provided by (Zhai et al., 2021).

In this paper we make use of a state of the art approach to compute optical flow called RAFT (Recurrent all-pairs field transforms for optical flow) (Teed and Deng, 2020) which we use as a given input to our method to obtain estimations of visual looming.

2.3 Visual Looming from Simulation

Figure 3: Visual Looming from Simulation: left - a image sequence of the simulated scene. Note that the white and yellow cars are approaching the observer and the blue car is moving away from the observer; right - the corresponding looming values for the image sequence (the brighter the red the higher the threat; blue corresponds to negative looming).

3 METHOD

In this section we derive two different expressions for visual looming (L) for a general six-degrees-of-freedom motion. As mentioned earlier, the camera is attached to the vehicle and both share the same coordinate system.

3.1 Velocity and Motion Fields

Consider a vehicle motion in 3D space relative to an arbitrary stationary reference point \( \mathbf{F} \) (refer to Figure 4). At any given time, the vehicle velocity vector consists of a translation component \( \mathbf{t} \) and a rotation component \( \mathbf{\Omega} \) in world coordinates as shown in Figure 4.a. Also consider a local coordinate system centered at the camera which is fixed to the moving vehicle (Figure 4.b). We choose the z-axis to be aligned with the vertical orientation of the camera and the x-axis to be aligned with the optical axis of the camera. In this frame any stationary point in the 3D scene can be represented using spherical coordinates \((r, \theta, \phi)\) where \( r \) is the range to the point \( \mathbf{F} \), \( \theta \) is the azimuth angle measured from the x-axis and \( \phi \) is the elevation angle from the XY-plane.

In camera coordinates, a point \( \mathbf{F} \) has an associated relative velocity \( \mathbf{V} \) with a translation vector \(-\mathbf{t}\) and rotation vector \(-\mathbf{\Omega}\), given by (see (Meriam and Kraige, 2012)):

\[
\mathbf{V} = (-\mathbf{t}) + (-\mathbf{\Omega} \times \mathbf{r})
\]  (3)

Figure 4: General motion of a vehicle in 3D space. a) Vehicle trajectory in world coordinates with translation vector \( \mathbf{t} \) and rotation vector \( \mathbf{\Omega} \). b) Camera coordinate system.

Estimation of optical flow from a sequence of images is beyond the scope of this paper.

Note that \( \mathbf{r} \) in bold refers to the range vector and the scalar \( r \) refers to its magnitude, i.e., \( r = |\mathbf{r}| \). Notice also that for a given point \( \mathbf{F} \), the velocity vector \( \mathbf{V} \) is the velocity field in 3D due to egomotion of the camera.

By dividing equation (3) by the scalar \( r \) and expanding \( \mathbf{t} \) and \( \mathbf{\Omega} \) we get:
\[
\frac{V}{r} = \left(\frac{-t}{r}\right) + \left(\frac{-\Omega \times r}{r}\right)
\]
\[
= \frac{-(t \cdot e_r + t \theta e_\theta + t \phi e_\phi)}{r} - \frac{(\Omega \cdot e_r + \Omega \theta e_\theta + \Omega \phi e_\phi) \times e_r}{r}
\]
\[
= \frac{(-t_r e_r + (-t_\theta e_\theta + (-t_\phi e_\phi))}{r} + (-\Omega \theta e_\theta + \Omega \phi e_\phi)
\]

where:

\[
\begin{align*}
    t_r &= t \cdot e_r, \\
    t_\theta &= t \cdot e_\theta, \\
    t_\phi &= t \cdot e_\phi.
\end{align*}
\]

The velocity field \( V \) can also be expressed in spherical coordinates \((r, \theta, \phi)\) and directional unit vectors \((e_r, e_\theta, e_\phi)\) as shown in (Meriam and Kraige, 2012):

\[
V = \frac{dr}{dt} e_r + r \frac{dr}{d\theta} \cos(\phi) e_\theta + r \frac{d\phi}{dt} e_\phi
\]

By dividing equation (5) by \( r \) we obtain:

\[
\frac{V}{r} = \left(\frac{\dot{r}}{r}\right) e_r + \frac{\dot{\theta}}{r} e_\theta + \frac{\dot{\phi}}{r} e_\phi
\]

From (6) we can identify the 2D motion field \( f \) defined as:

\[
f = \frac{\dot{\theta}}{r} e_\theta + \frac{\dot{\phi}}{r} e_\phi
\]

Note that \( \frac{\dot{r}}{r} \) is not part of the motion field since it is along the range direction \( e_r \) from the camera to point \( F \). The motion field \( f \) in expression (7) is the projection of the velocity field \( V \) on the spherical image.

### 3.2 Looming from Spatial Partial Derivatives of the Velocity Field

The Looming value \( L \) is related to the relative expansion of objects projected on the image of the camera. This means that there is a direct relationship between the change in the motion field in the vicinity of a point and looming \( L \). In order to find this relationship we apply spatial partial derivatives with respect to \( \theta \) and \( \phi \) to the velocity field divided by \( r \) as described in equations (4) and (6) to get:

\[
\frac{\partial}{\partial \theta} \left(\frac{V}{r}\right) = \frac{\partial}{\partial \theta} \left[ \left(\frac{-t_r}{r}\right) e_r + \left(\frac{-t_\theta}{r}\right) e_\theta + \left(\frac{-t_\phi}{r}\right) e_\phi \right]
\]

\[
+ \frac{\partial}{\partial \phi} \left[ (-\Omega \theta) e_\theta + \Omega \phi e_\phi \right]
\]

\[
= \frac{\partial}{\partial \theta} \left[ \left(\frac{\dot{r}}{r}\right) e_r + \frac{\dot{\theta}}{r} e_\theta + \frac{\dot{\phi}}{r} e_\phi \right]
\]

\[
+ \frac{\partial}{\partial \phi} \left[ (-\Omega \theta) e_\theta + \Omega \phi e_\phi \right]
\]

By performing the corresponding derivations\(^1\) for equations (8) and (9), in addition to using equation (2) for \( L \), we obtain the following two independent expressions for looming \( L \):

\[
L = \frac{\partial \theta}{\partial \theta} - \frac{\dot{\theta}}{r} \tan(\theta) - \frac{t_\theta}{r} \left(\frac{1}{\cos(\phi)}\right) \left(\frac{1}{r} \frac{\partial r}{\partial \theta} \right)
\]

\[
L = \frac{\partial \phi}{\partial \phi} - \frac{\dot{\phi}}{r} \tan(\phi) - \frac{t_\phi}{r} \left(\frac{1}{r} \frac{\partial r}{\partial \phi} \right)
\]

In both expressions, \( L \) is a scalar value that can be computed from the spatial change in the motion field. Note that \( L \) is independent of the vehicle rotation \( \Omega \) and is dependent only on the translation components scaled by \( r, t_\theta/r \) and \( t_\phi/r \).

These expressions may also apply to any relative motion of a point in 3D for any six-degrees-of-freedom motion.

### 3.3 Estimation of Visual Looming

Expressions (10) and (11) contain \( r \), which is not measurable from the image. If we estimate looming by eliminating the components that contain \( r \) in (10) and (11) then estimates for \( L \) are obtained as:

\[
L_{est1} = \frac{\partial \theta}{\partial \theta} - \dot{\theta} \tan(\theta)
\]

\[
L_{est2} = \frac{\partial \phi}{\partial \phi}
\]

Later in the paper, we show the effect of eliminating the components in equations (12) and (13) that include \( r \) and its derivative on the error in calculating looming.

Notice that \( L_{est1} \) and \( L_{est2} \) can be obtained directly from measurements of the horizontal and vertical components of the motion field for a particular time instance, specifically, the changes of the values of the motion field in the spatial dimensions \( \theta \) and \( \phi \). This is the meaning of the spatial partial derivatives \( \frac{\partial \theta}{\partial \theta}, \frac{\partial \phi}{\partial \phi} \) in expressions (12) and (13).

\(^1\)Most of the detailed derivations were omitted from the paper due to page limit. The detailed derivations are available upon request.
3.4 Surface Normals

The point \( F \) lies on a infinitesimally small surface patch with normal vector \( n \). To find the relation between \( L \) and \( n \) we assume that the surface is planar in the vicinity of the point. This planar patch is represented by the triangle ABC and \( n \) is the normal at point \( F \) (see Figure 5.a).

We can identify two vectors, \( \frac{\partial \mathbf{r}}{\partial \theta} \) and \( \frac{\partial \mathbf{r}}{\partial \phi} \), located on the planar patch, that result from the displacement of \( r \) along the angles \( \theta \) and \( \phi \). Notice that these vectors are both perpendicular to the surface normal \( n \) and are located at the intersection of the planes \( ABC, e_\phi e_\theta \) and \( e_\theta e_\phi \). It can be shown that the following constraints hold for any infinitesimally small patch:

\[
\frac{\partial \mathbf{r}}{\partial \theta} \cdot n = 0 \tag{14}
\]

\[
\frac{\partial \mathbf{r}}{\partial \phi} \cdot n = 0 \tag{15}
\]

Using \( \mathbf{r} = r e_\theta \) and solving for \( \frac{\partial \mathbf{r}}{\partial \theta} \) and \( \frac{\partial \mathbf{r}}{\partial \phi} \) in (14) and (15) we obtain:

\[
1 \frac{\partial r}{r \partial \theta} = -\cos \phi \left( \frac{e_\theta \cdot n}{e_r \cdot n} \right) \tag{16}
\]

\[
1 \frac{\partial r}{r \partial \phi} = -\left( \frac{e_\phi \cdot n}{e_r \cdot n} \right) \tag{17}
\]

By defining the surface tilt angles as \( \gamma \) and \( \delta \) (see Figure 5.b) we obtain:

\[
\gamma = \tan^{-1} \left( \frac{e_\theta \cdot n}{e_r \cdot n} \right) \tag{18}
\]

\[
\delta = \tan^{-1} \left( \frac{e_\phi \cdot n}{e_r \cdot n} \right) \tag{19}
\]

We can rewrite equations (10), (11) using (16), (17), (18) and (19) as:

4 LOOMING RESULTS

We present two sets of quantitative results of the methods for estimation of looming using simulations and real data.

4.1 Looming from Simulation

We simulated a translating and rotating observer in 3D. Measurements were taken for a single stationary point on a tilted planar patch (see Figure 6.a).

The simulation duration was 23 seconds and samples were taken at 60 Hz (1380 samples in total). The vehicle starting position was \( P = [-75i + 75j + 44.3k] \) and the orientation was \([ forward, left, up ] = [-i, -j, k]. \) The planar patch was simulated by the following points: \( A = 80i - 40j + 35k, B = 80i - 80j + 35k, \) and \( C = 85i - 60j + 58k. \) All distances were in meters. The vehicle was moving at a speed of \( s = 11.11 \text{ m/s (or 40 km/h)} \) with translation and rotation vectors \( \mathbf{t} = s + 0.1 \cos(0.1t) \) and \( \mathbf{\Omega} = \cos(0.1t) - \cos(0.3t) + 8(\frac{m}{30}) \sin(0.3t) \).

Plots of the parameters \( t \) and \( \Omega \) over time are shown on Figure 6.b.

Ground truth looming \( L \) is computed from range and its time derivative using equation (1). In addition, two estimations of looming \( L_1 \) and \( L_2 \) are computed using equations (20) and (21) (see Figure 7). To compare \( L \) with each estimate of \( L_1 \) or \( L_2 \) we use the error percentage metric:

\[
\text{error}_i(\%) = \frac{L_i - L}{L} \times 100 \quad \text{for } i = 1, 2 \tag{22}
\]
4.2 Looming from Real Data

Visual looming estimates were obtained from optical flow (estimation of the motion field) from a sequence of images taken from a moving camera fixed on a vehicle. The block diagram in Figure 9 shows the process and the different components.

We processed real data using a particular city drive from the well-known KITTI dataset (Geiger et al., 2013). This dataset includes raw data from several sensors mounted on a vehicle. We used a video sequence from one of the color cameras (FL2-14S3C-C, 1.4 Megapixels, 1392x512 pixels). Then a pair of consecutive RGB images from this dataset were processed by a deep neural network called RAFT (Recurrent All-Pairs Field Transforms) (Teed and Deng, 2020). RAFT provides optical flow estimation as output, for each pixel in the image as a displacement pixel pair \((u, v)\).

We used the KITTI camera intrinsic parameters to transform from pixel image coordinates to spherical coordinates and obtained \((\theta, \phi, \dot{\theta}, \dot{\phi})\). Then the average of spatial derivatives from equations (12) and (13) were applied to estimate and visualize the looming values.

Looming estimation from frames 69 and 70 are shown in Figure 10.c. Positive values of looming are shown in red and negative values in blue. The brighter the red, the higher the looming threat.

Notice an edge effect around objects with high values of red and blue colors. This is due to occlusions that generate sudden changes in optical flow and cause distortion of looming, resulting in incorrect values. Those may be managed by discarding some blue regions using additional filtering.

Notice also some noise, shown as square artifacts, due the up-sampling interpolation stage of the RAFT...
algorithm (1:8 ratio). The noise is due to spatial partial derivatives that have a tendency to amplify minor differences of optical flow.

Moving objects, like the bike and the white car in the image sequence, are shown with darker red color (meaning less threat) due to small relative velocity with respect to the camera. This is an advantage of the approach where estimation of looming is able to catch the relevant threat of moving objects. This is clearly an advantage of looming over conventional perception of depth.

5 CONCLUSIONS

Visual looming has been shown to be an important cue for navigation and control tasks. This paper explores new ways for deriving and estimating visual looming for general six-degrees-of-freedom motion. The main contributions of the paper are:

1. We derived two novel analytical closed-form expressions for calculating looming for any six-degree-of-freedom motion. These expressions include spatial derivatives of the motion field. This approach can be applied to any relative motion between an observer and any visible point.

2. We showed the theoretical relationship of surface normal to the values of looming.

3. We presented simulation results of the effect of surface normals on values of calculated looming. Quantitative calculations showed the relationship between the angles of the surface normal relative to the angle of the range vector and the related effects on the accuracy of estimating looming values.

4. We demonstrated how to extract looming from optical flow. The output of the RAFT model was used to estimate looming values using expressions that were derived in the paper.

It should also be emphasized that knowledge of range to the 3D point, translation or rotation of the camera (egomotion) is not required for the estimation of looming and hence for autonomous navigation tasks.

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