

Patient Similarity Networks Integration for Partial Multimodal Datasets

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Abstract: Integration of partial samples in Patients Similarity Networks, i.e. the combination of multiple data sources when some of them are completely missing in some samples, is a largely overlooked problem in the multi-omics data integration literature for Precision Medicine. Nevertheless in clinical practice it is quite usual that one or more types of data are missing for a subset of patients. We present an algorithm able to combine multiple sources of data in Patients Similarity Networks when data of one or more sources are completely missing for a subset of patients. The proposed approach relies on a message-passing learning strategy to recover and combine completely missing data leveraging the Similarity Network Fusion algorithm. Preliminary results on TCGA breast cancer data show the effectiveness of the proposed approach.

1 INTRODUCTION

In the last decade, Patient Similarity Networks (PSN) emerged as a convenient model to integrate multiple data views and perform clustering/classification tasks to support Precision Medicine (PM) (Pai and Bader, 2018; Gliozzo et al., 2022). The aim of PM is to tailor the diagnosis, prognosis and treatment of each patient making decisions based on her/his genomic, environmental and lifestyle data. This approach represents a paradigm shift from the use of broad disease categories typical of a “one size fits all” method (Akhoon, 2021). PM requires by definition the use of big heterogeneous data acquired from each patient at different levels (e.g. clinical, omics, images, etc), which is currently possible thanks to the advent of high-throughput technologies (Lightbody et al., 2019).

PSN are a simple yet powerful way to exploit such diverse array of data sources. A PSN is a graph where nodes are patients and edges represent the pairwise

similarity between individuals computed using their clinical and/or biomolecular profiles. The underlying assumption is that patients described by similar profiles should show a similar clinical outcome (Gliozzo et al., 2022). PSN are suitable for heterogeneous data since they can be computed from every data type (Pai and Bader, 2018) providing an overview of the relationships among patients across the different data views.

The integration of the computed PSN is not trivial and many methods were proposed in literature to tackle this issue, which are collectively classified as “PSN-fusion methods” (Gliozzo et al., 2022). Surprisingly, the vast majority of methods require “complete datasets” having all data sources for every considered sample. However, it is quite common to have completely missing data sources in multi-omics datasets (Rappoport and Shamir, 2019; Xu et al., 2021) due to the limited availability of samples, cost of the assays and experimental design (Conesa and Beck, 2019). A naive strategy to integrate multimodal data having partial samples, i.e. samples with one or more data sources not available, is to remove them from the dataset. While this approach is simple, it can significantly reduce the amount of samples available for the integration and for further

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analysis. More sophisticated approaches attempt to impute missing data exploiting information coming from other data sources (e.g. KNN imputation on the concatenated data matrices (Rappoport and Shamir, 2019)). Unfortunately state-of-the-art approaches to recover missing data usually work when only some parts of the data are missing (e.g. when only a relatively small subset of the gene expression data for a given patient are missing), but are not able to recover a completely missed source of information for a given patient (Xu et al., 2021).

Another related open problem regards the development of methods to integrate “partial datasets”, i.e. datasets having individuals with completely missing data sources. Hence performing a good quality imputation and partial samples data integration in PSNs represents an open problem, largely overlooked in literature (Rappoport and Shamir, 2019; Xu et al., 2021).

In this work, we propose miss-SNF: a novel algorithm that can integrate partial datasets through the cross-diffusion of information among PSN computed from different data sources. Differently from other proposed approaches able to handle partial datasets, miss-SNF can partially reconstruct missing data by using information from different sources during the cross-diffusion process.

2 METHODS

Miss-SNF is a novel PSN-fusion method able to combine multiple biological data sources having partial samples. In particular, miss-SNF leverages the Similarity Network Fusion (SNF) algorithm (Wang et al., 2014) to integrate two or more data sources and manages partial samples using a message-passing learning strategy to recover and combine completely missed data.

2.1 SNF

SNF is a method that exploits a cross-diffusion process to pass information among PSN built from different data sources, until convergence to an integrated network. The first step of SNF is the computation of a PSN W , expressing the pairwise similarity between the biomolecular profiles of individuals x_i and x_j , from each data modality. A scaled exponential similarity kernel is exploited to compute similarity for continuous data:

$$W(i, j) = \exp\left(-\frac{\rho(x_i, x_j)^2}{\mu \epsilon_{ij}}\right) \quad (1)$$

where $\rho(x_i, x_j)$ is the Euclidean distance between patients, μ is a hyperparameter related to the variance of the local model and $\epsilon_{i,j}$ is a scaling factor taking into account the neighbourhoods N_i and N_j of the considered patients:

$$\epsilon_{i,j} = \frac{\text{mean}(\rho(x_i, N_i)) + \text{mean}(\rho(x_j, N_j)) + \rho(x_i, x_j)}{3} \quad (2)$$

From the initial PSN $W(i, j)$, other two matrices P and S are computed for each data modality. The “global” similarity matrix P , which is essential to capture the overall relationships between patients and it is computed through the following normalization:

$$P(i, j) = \begin{cases} \frac{W(i, j)}{2 \sum_{k \neq i} W(i, k)} & , \text{ if } j \neq i \\ 1/2 & , \text{ if } j = i \end{cases} \quad (3)$$

where for equation 3 the property $\sum_j P(i, j) = 1$ holds. Then a “local” similarity matrix is obtained as follows:

$$S(i, j) = \begin{cases} \frac{W(i, j)}{\sum_{k \in N_i} W(i, k)} & , \text{ if } j \in N_i \\ 0 & , \text{ otherwise} \end{cases} \quad (4)$$

where $N_i = \{x_k | x_k \in kNN(x_i) \cup \{x_i\}\}$. S is able to capture the local structure of the network because considers only local similarities in the neighbourhood of each individual, setting to zero all the others.

Given m data modalities, m different W , S and P matrices are constructed and an iterative process is applied where similarities are diffused through the P s until convergence, that is, until all the matrices P become similar. In the simplest case, when $m = 2$, we have $P_t^{(v)}$ that refers to P matrices for data $v \in \{1, 2\}$ at time t . In this case, the following recursive updating formulas describes the diffusion process:

$$\begin{aligned} P_{t+1}^{(1)} &= S^{(1)} \times P_t^{(2)} \times S^{(1)T} \\ P_{t+1}^{(2)} &= S^{(2)} \times P_t^{(1)} \times S^{(2)T} \end{aligned} \quad (5)$$

In other words $P^{(1)}$ is updated by using $S^{(1)}$ from the same data source but $P^{(2)}$ from a different view and vice-versa.

SNF can be easily extended to $m > 2$ data sources:

$$P^{(s)} = S^{(s)} \frac{\sum_{k \neq s} P^{(k)}}{m-1} (S^{(s)T}) \quad (6)$$

and the final “consensus” matrix $P^{(c)}$ is:

$$P^{(c)} = \frac{1}{m} \sum_{k=1}^m P^{(k)} \quad (7)$$

2.2 Miss-SNF

As above-mentioned, a common issue in biological multi-modal datasets regards the presence of partial samples, i.e. samples that present one or more completely missing data sources. The original SNF algorithm (described in the previous section 2.1) requires the presence of all data modalities for each sample to perform integration. A naive solution to this problem cannot consist in setting the feature vector of the missing data source to $\vec{0}$ (vector of zeros). Indeed it is easy to see that if we use any similarity measure to compute the weights we obtain a value different from zero.

To tackle this problem, we propose two different extensions of SNF:

1. Reconstruction of missing data by propagation of the information from other available sources. This approach is able to partially reconstruct missing data by using information from different sources during the cross-diffusion process performed by SNF. This can be accomplished by appropriately setting the initial values for $W^{(s)}$, $P^{(s)}$ and $S^{(s)}$ matrices for the patients having no data for the source s and then by run the SNF algorithm.
2. Managing missing data by ignoring them. This second solution simply ignores the missing data by setting to zero all the entries of the patient x_i in the matrices $W^{(s)}$, $P^{(s)}$ and $S^{(s)}$ and then by running the vanilla SNF.

2.2.1 Miss-SNF with Partial Reconstruction of Missing Data (miss-SNF ONE)

The first solution, that handles missing data by partially reconstructing them during the diffusion process of SNF, is performed by changing the similarity matrices W , P and S . If for a patient x_i we have a completely missing source s , the similarity matrices are modified as follows:

- set $W^{(s)}(i, j) = 0 \forall j \neq i$ and $W^{(s)}(i, i) = 1$
- set $P^{(s)}(i, j) = 0 \forall j \neq i$ and $P^{(s)}(i, i) = 1$
- set $S^{(s)}(i, j) = 0 \forall j \neq i$ and $S^{(s)}(i, i) = 1$

Having a second data source $s' \neq s$, this implies that the update equation for node x_i will be:

1. when $k \neq i$

$$P_{t+1}^{(s)}(i, j) = \sum_{k \in N_i} \sum_{l \in N_j} S^{(s)}(i, k) S^{(s)}(j, l) P_t^{(s' \neq s)}(k, l) = 0$$
2. when $k = i$

$$P_{t+1}^{(s)}(i, j) =$$

$$\sum_{l \in N_j} S^{(s)}(i, i) S^{(s)}(j, l) P_t^{(s' \neq s)}(i, l) > 0,$$

if $\exists l$ s.t. $S^{(s)}(j, l) > 0$ and $P_t^{(s' \neq s)}(i, l) > 0$

The result of the second equation can be different from 0 when there is a common neighbour x_l between x_i and x_j such that $S^{(s)}(j, l) > 0$ and $P_t^{(s' \neq s)}(i, l) > 0$. In other words, we have a contribution to the missing $P_{t+1}^{(s)}(i, j)$ when does exist a common neighbour between i and j in respectively the “global” network P for a different source $s' \neq s$ and in the “local” network S for the missed source s .

This implies that we can populate $P^{(s)}(i, j)$ also when data are missed for source s .

This procedure can be easily extended to manage missing data having m different sources. Indeed, the update equation can be written as:

$$P_{t+1}^{(s)}(i, j) = \sum_{k \in N_i} \sum_{l \in N_j} S^{(s)}(i, k) \left(\frac{\sum_{v \neq s} P_t^{(v)}(k, l)}{m-1} \right) S^{(s)}(j, l)$$

Referring to $\frac{\sum_{v \neq s} P_t^{(v)}(k, l)}{m-1}$ as $\mathbf{P}_t^{v \neq s}(k, l)$, and having set $S^{(s)}(i, k) = 0 \forall k \neq i$ and $P^{(s)}(i, i) = 1$, then:

$$\begin{aligned} P_{t+1}^{(s)}(i, j) &= \sum_{k \in N_i} \sum_{l \in N_j} S^{(s)}(i, k) \mathbf{P}_t^{v \neq s}(k, l) \\ &= \sum_{l \in N_j} S^{(s)}(i, i) \mathbf{P}_t^{v \neq s}(i, l) S^{(s)}(j, l) = \\ &= \sum_{l \in N_j} \mathbf{P}_t^{v \neq s}(i, l) S^{(s)}(j, l) \end{aligned}$$

According to the above equations, if x_j is not missing, then $P_{t+1}^{(s)}(i, j)$ is “imputed” if x_i and x_j share common neighbours respectively in the “global” network $\mathbf{P}^{v \neq s}$ and in the “local” network $S^{(s)}$.

2.2.2 Miss-SNF Ignoring Partial Samples (Miss-SNF ZERO)

The second solution, which handles missing data by ignoring partial samples in the diffusion process, is again performed by changing the similarity matrices W , P and S . If for a patient x_i we have no data for source s , the similarity matrices are modified as follows:

- set $W^{(s)}(i, j) = 0 \forall j$
- set $P^{(s)}(i, j) = 0 \forall j$
- set $S^{(s)}(i, j) = 0 \forall j$

In this way, the following update rule is obtained:

$$\begin{aligned} \forall j : P_{t+1}^{(s)}(i, j) &= \sum_{k \in N_i} \sum_{l \in N_j} S^{(s)}(i, k) S^{(s)}(j, l) P_t^{(s' \neq s)}(k, l) \\ &= 0 \end{aligned}$$

Hence, there will be no contribution to $P_t^{(s)}(i, j)$ because it will remain $P_t^{(s)}(i, j) = 0$ for every value of t .

The final integrated ‘‘consensus’’ $P^{(c)}$ is computed as:

$$P^{(c)} = \left(\sum_{k=1}^m P^{(k)} \right) \odot M.$$

where \odot is a pointwise multiplication, and M is a matrix of the same dimension of P where $M(i, j)$ is the reciprocal of the sources s available for the edge (i, j) . In other words $M(i, j)$ counts how many sources are available for the edge (i, j) . Note that $M = M^T$.

In this way, we obtain a ‘‘consensus’’ $P^{(c)}$ that averages edge weights with respect to the actually available data source for each patient.

3 RESULTS

We present some preliminary results to show the effectiveness of the proposed approach. By using multi-omics data from The Cancer Genome Atlas (TCGA) (Hutter and Zenklusen, 2018), we compared SNF using the complete data sets with miss-SNF when amputated data are used instead. We both compared predictions on early/late stage cancer patients and the resulting integrated adjacency matrices to estimate the recovery capabilities of miss-SNF when partial samples are present in the available data.

3.1 Dataset

To evaluate the performance of miss-SNF, a breast cancer multi-omics dataset from TCGA (Tomczak et al., 2015) was downloaded through the R package ‘‘curatedTCGAData’’ (Ramos et al., 2020). Only primary solid tumors are considered and technical replicates were not present in each data view. The following data sources are considered:

- miRNA gene-level expression values (log2 RPM) from RNA-sequencing
- mRNA gene expression values (TPM) from RNA-sequencing
- normalized protein expression values from Reverse Phase Protein Array

Moreover, cancer stages were downloaded and the samples dichotomized into early-stage cancer (stage I and stage II) and late-stage cancer (stage III and stage IV) (Dianatinasab et al., 2018). We considered a common set of 628 patients across data sources and removed features having missing values in protein data. In this way, a complete multi-omic dataset is obtained, where each data view has the same set of samples. The dataset was further filtered to retain only the most interesting features for each data source. A feature is removed if it has zero variance or if it has very few unique values with respect to samples cardinality and the ratio of the frequency of the most common value to the frequency of the second most common value is large (Kuhn, 2021). After min-max normalization, features were again filtered based on Pearson correlation. In particular, features with an absolute correlation higher than 0.75 are selected and the one with the largest mean absolute correlation with respect to the other features is removed (Kuhn, 2021). At the end of this filtering stage, we have 494 miRNA, 13220 mRNA and 202 proteins. Moreover, the complete dataset is randomly amputated removing 10%, 20% and 30% of the features from each data source. The only constraint is avoiding to remove the same patient in the third data source if it was already removed in the other two views. In this way we avoid to have no data across sources for a specific sample. At the end, we obtained four different datasets:

1. Complete dataset: no partial samples are present
2. Amputated 10%: each view has 10% of samples completely missing
3. Amputated 20%: each view has 20% of samples completely missing
4. Amputated 30%: each view has 30% of samples completely missing

3.2 Experimental Setup

We aim at comparing the performance of SNF (Wang et al., 2014) with respect to our proposed approach miss-SNF. Since SNF can integrate only data sources without partial samples, we used SNF to integrate the breast cancer complete dataset and we used miss-SNF to integrate the amputated datasets. In particular, we run both the algorithms setting 20 iterations for the diffusion process and $k = 20$ for the k-Nearest Neighbours used to build the ‘‘local’’ similarity matrix S (see equation 4), as suggested by SNF’s authors (Wang et al., 2021). In both cases, scaled exponential euclidean distance is used to compute the unimodal similarity matrices ($k = 20, \mu = 0.5$). The integrated matrices obtained with SNF and miss-SNF are used to

perform the prediction of late vs early-stage samples using a 10 multiple hold-out procedure.

The label propagation algorithm (Zhu et al., 2003) is exploited to perform a ranking of the predicted late vs early stage breast cancer patients. A threshold of 0.5 was used to dichotomize the computed normalized scores (scores are normalized between 0 and 1 by min-max normalization) and the following metrics are computed to evaluate the generalization performance on the test set: precision, recall, specificity, F-measure, accuracy, AUC, AUPRC. Moreover, the RMSE (Root Mean Squared Error) between the integrated matrix obtained by SNF ($P_{comp}^{(c)}$) and the integrated matrices obtained by miss-SNF on the amputed datasets ($P_{amp}^{(c)}$) is computed, in order to evaluate whether the proposed algorithm is able to recover the integrated data set when partial samples are present:

$$RMSE = \sqrt{\sum_{i=1}^n \frac{(P_{comp}^{(c)} - P_{amp}^{(c)})^2}{n}}$$

3.3 Experimental Results

Figure 1 shows the performance of SNF and miss-SNF ONE on the different amputed datasets, while Figure 2 shows the performance of miss-SNF ZERO. In Figure 1, we can see that miss-SNF ONE has competitive results with respect to SNF in terms of precision, AUC and AUPRC for all the percentages of dataset amputation, while it is even able to surprisingly improve recall and F-measure. On the other hand, we can spot a drop in specificity and accuracy for 10% and 20% of amputation, while the results seems comparable with miss-SNF when the dataset has a 30% of missing samples. A similar behaviour is shown by miss-SNF ZERO even if performance are generally slightly worse (except for recall and F-measure) with respect to miss-SNF ONE, probably due to the missing data reconstruction performed by the latter. Indeed, Table 1 shows a slightly lower RMSE for miss-SNF ONE with respect to miss-SNF ZERO and the difference increases when the percentage of missing data is higher, showing that, as expected, miss-SNF ONE is able to partially recover the missing samples.

4 DISCUSSION AND CONCLUSIONS

In this work we presented miss-SNF, a novel algorithm able to integrate PSN built from different bio-

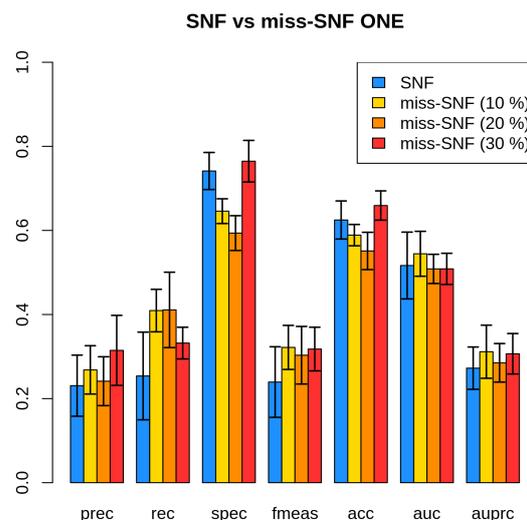


Figure 1: Performance of SNF and miss-SNF ONE on the different amputed datasets (10%, 20%, 30%). Results are averaged across multiple holdouts and error bars show standard error. “Prec” is precision, “Rec” is recall, “Spec” is specificity, “fmeas” is F-measure, “acc” is accuracy, “auc” is the Area under the ROC Curve and “auprc” is the Area under the Precision-Recall Curve.

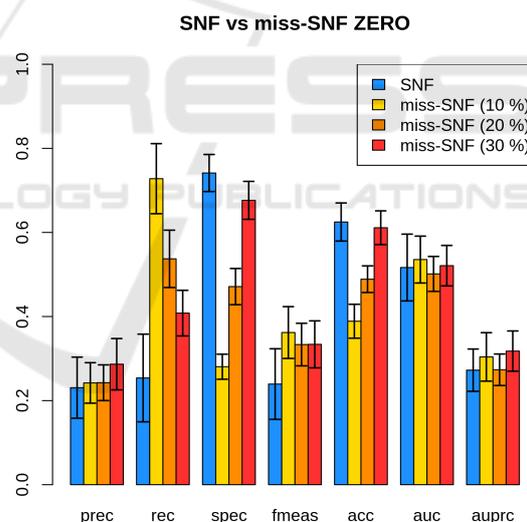


Figure 2: Performance of SNF and miss-SNF ZERO on the different amputed datasets (10%, 20%, 30%). Results are averaged across multiple holdouts and error bars show standard error. “Prec” is precision, “Rec” is recall, “Spec” is specificity, “fmeas” is F-measure, “acc” is accuracy, “auc” is the Area under the ROC Curve and “auprc” is the Area under the Precision-Recall Curve.

logical data sources having partial samples. The proposed method leverages the non-linear integration approach based on message-passing theory presented in SNF (Wang et al., 2014) to fuse multi-modal data and to partially reconstruct missing data coming from the presence of partial samples, i.e. samples having one

Table 1: RMSE of miss-SNF ONE and ZERO for the different amputated (Amp.) datasets with respect to SNF applied on the complete dataset.

	Amp. 10%	Amp. 20%	Amp. 30%
miss-SNF ONE	0.0020	0.0021	0.0022
miss-SNF ZERO	0.0022	0.0025	0.0028

or more completely missing data sources. Many approaches able to integrate PSN computed from different sources stem from the algorithm SNF (see (Ma and Zhang, 2017; Liu and Shang, 2018; Jiang et al., 2019; Ruan et al., 2019; Rappoport and Shamir, 2019; Liu et al., 2021; Li et al., 2022; Wu et al., 2021)), but only NEMO (Rappoport and Shamir, 2019) modified the original method to take into account the presence of partial samples, which is a largely overlooked problem in literature. Of note, NEMO requires that each pair of patients should have at least one common data source to be integrated. This assumption is absent in miss-SNF. To the best of our knowledge, miss-SNF is the first “SNF-based approach” (Gliozzo et al., 2022) able to handle partial samples without such constraint. We showed on a breast cancer multi-omic dataset that miss-SNF can achieve comparable or even better performance with respect to SNF considering different percentages of partial samples present in the dataset. Moreover, we showed that SNF is able to reconstruct missing data. In future works, we plan to extensively test miss-SNF on other multi-omics cancer datasets of different sample size and on non-cancer datasets. Moreover, we will compare miss-SNF with state-of-the-art methods able to integrate multiple data sources and handle the presence of completely missing samples in the dataset (Rappoport and Shamir, 2019; Xu et al., 2021).

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