GPTree: Generator of Phylogenetic Trees with Overlapping and Biological Events for Supertree Inference

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- Abstract: Summary: More and more evolutionary and molecular biologists are interested in building alternative supertrees. Often, developing new approaches or testing new metrics requires relevant datasets that are not always easy to obtain. In order to solve this problem of lack of data, we propose a new approach and developed a program in Python to generate overlapping phylogenetic trees with biological events to simplify the process of obtaining this type of data. The new tool takes the number of phylogenetic trees the user wants to generate, the maximum number of leaves per tree to generate, and the average level of leaf overlap between phylogenetic trees as input parameters. The program returns to the user a set of phylogenetic trees in Newick format, respecting the parameters given as input, in order to use them to infer a supertree (or supertrees). This data can be an important resource for research; the user can download the generated data and use it later in their relevant application tasks.
 - Availability and implementation: The generator is freely and publicly available to the entire scientific community on the GitHub platform, without any registration, https://github.com/tahiri-lab/gptree under the MIT licence. The pipeline is written in Python 3.7.

1 INTRODUCTION

More and more phylogenetic researchers are dealing with phylogenetic supertrees in order to improve our understanding of species evolution. A supertree is assembled from individual gene trees, but these trees can be defined in different, but mutually overlapping, sets of taxa. Studies on supertrees are essential to reconstructing the phylogenetic trees of all living species (i.e., the OpenTree Online project (Hinchliff *et al.*, 2015)). Among the unsolved problems, classification problems play an important role and have several practical applications, i.e., the creation of the tree of life in order to know and understand the biodiversity of species.

The reliability of species phylogeny can be validated through the merging of related gene trees, considering the present topological conflicts (Maddison *et al.*, 2007). As part of this aspect, it is possible to examine the consensus tree issue, where trees for merging are constructed for the same set of taxa, or the supertree issue, where trees for merging are constructed for different but overlapping sets of taxa. There are a number of methods for inferring a consensus tree, examples of which are the majority-rule consensus trees, the extended majority-rule consensus tree, and the strict consensus tree (Bryant, 2003). It is worth noting that, in practice, researchers do not often work with phylogenies on the same set of taxa, and, therefore, the issue of inferring a supertree becomes important (Bininda-Emonds, 2004). One approach is to combine a collection of small phylogenetic trees with a partial level of overlap between them into complex supertrees (Wilkinson *et al.*, 2007).

We should also highlight the aspects of tree clustering in situations, where combining the overlapping trees into a supertree can be performed for the identified clusters. There are a number of approaches to tree clustering that include k-means (Stockham *et al.*, 2002), *k*-medoids (Tahiri *et al.*, 2018), MultiPolar Consensus (MPC) method (Bonnard *et al.*, 2006), and Multiple Consensus Trees (MCT) method (Guénoche, 2013). Recently, (Tahiri *et al.*, 2022a) have introduced a method for building alternative consensus trees and supertrees using *k*-means and the Robinson and Foulds (RF) distance alongside with adaptation of

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several popular cluster validity indices.

Researchers who work with phylogenetic trees and supertrees may experience a lack of availability of datasets that they can use to test their solutions, for example, classification, clustering, and testing new metrics for comparing trees ((Swenson *et al.*, 2010); (Tahiri *et al.*, 2022b)). In this context, the creation of software for generating overlapping phylogenetic trees to infer supertrees that can be used later by scientists, i.e., in biology, medicine, ecology, bioinformatics, may become a relevant tool for phylogenetic studies.

Generation of a supertree through its inference from a set of trees as the core of the solution should have the functionality to generate phylogenetic trees with a certain set of features, including the different number of leaves in trees, the presence of overlapping between trees, and the incorporation of biological events, which provide the generated set with the property of approximation to the processes of evolution rather than randomness.

2 RELATED WORK

There are various software solutions for the generation of individual phylogenetic trees based on different approaches and with additional features incorporated. An overview of some of these implementations is shown in Table 1.

We analyzed and tested these generators and evaluated the possibility of using them for the specified task. Some applications are aimed at random tree generation, and such solutions are usually part of a larger software product with broader functionality (e.g., a web service (T-Rex) or a library for working with phylogenetic trees in Python (ete3)). Most of these simulators are capable of introducing additional features into the generated trees, which include birth and death events (e.g., based on the Gillespie algorithm (Gillespie, 1977)) and horizontal gene transfer (HGT). The most popular languages for the generators considered are Python, Java, and C.

None of the existing tree simulators provides the functionality to generate phylogenetic tree sets with partially overlapping sets of taxa, so there is a need to propose an approach to get this kind of data (with the possibility to use the existing simulator as a base generator). We chose the AsymmeTree library (Schaller *et al.*, 2022) version 2.2 as the basic simulator for generating a single tree (or a pair of species trees and gene trees), since it is the closest option according to the requirements we set for the tree: the availability of evolutionary scenarios (duplication, loss, and

horizontal gene transfer events), the possibility of setting additional parameters (such as loss, duplication, and HGT rates), and the Python programming language (this is the programming language that commonly used to prototype solutions using a wide range of data and algorithm libraries for bioinformatics and machine learning). We use ete3 library as an additional tool for working with generated trees (using the features available in Python). It provides a possibility to visualize the data, calculate comparison parameters of two trees (including RF distances), and save the generated trees in Newick format. More information about this is in the following sections.

Special attention should be given to horizontal gene transfer, which plays an essential role in evolution ((Davín *et al.*, 2018); (Wolfe and Fournier, 2018); (Bapteste *et al.*, 2004)) and its incorporation into the dataset makes the data closer to realistic. Since each gene has its own evolutionary history, which can be represented by its own phylogenetic tree, it (the gene) can demonstrate evolutionary patterns based, in particular, on horizontal gene transfer events (Tahiri *et al.*, 2022a). HGT in AsymmeTree is implemented as follows (Schaller *et al.*, 2022):

- 1. A species tree is generated.
- 2. A copy of a gene present at time t in any branch of the species tree is moved to another branch of the species tree. This branch, where the copy of the gene is placed, is chosen uniformly among the branches available at time t, but without considering the branch with the parent gene.

Visualization of the presence of HGT in the generated dataset will be shown in the Results and Discussion section. The selected generator of a single phylogenetic tree with the presence of duplication, loss, and horizontal gene transfer events was used as the basis for the pipeline, which is described in the next section.

3 METHODS

Several basic conditions have to be fulfilled to generate a phylogenetic tree dataset in order to obtain a phylogenetic supertree:

- 1. Generation of trees with different numbers of leaves in each tree;
- 2. Presence of simulated biological events in trees (in particular, horizontal gene transfer);
- 3. Presence of overlaps between trees.

The level of overlap of the two trees we determine

| Package name | Incorporation of additional features | Programming | Reference |
|--------------------------------------------|------------------------------------------------------------------------------------------------|---------------------|----------------------------------------|
| | (in simulators) | Language | |
| AsymmeTree | Speciation, duplication, loss, gene conversion, and horizontal gene transfer events | Python | (Schaller <i>et al.</i> , 2022) |
| Castor | Horizontal gana transform gana | D | (Louise and Deshali 2018) |
| Castor | duplication, and gene loss events | ĸ | (Louca and Doeben, 2018) |
| ete3 (populate() function) | Random generation | Python | (Huerta-Cepas et al., 2016) |
| GenPhyloData | Gene duplication, gene loss, lateral gene transfer, clock models, and sequence evolution | Java | (Sjöstrand et al., 2013) |
| HGT-gen | Horizontal gene transfer | Perl | (Horiike et al., 2011) |
| HybridSim | Divergence speciation, hybrid speciation, and introgression | Java | (Woodhams et al., 2016) |
| Ngesh | Birth and death models, mutation, and horizontal gene transfer | Python | (Tresoldi, 2021) |
| SaGePhy | Gene birth, speciation, gene duplications, horizontal gene transfers, and gene losses | Java | (Kundu and Bansal, 2019) |
| SimPhy | Lineage sorting, gene duplication and loss, and horizontal gene transfer | C | (Mallo <i>et al.</i> , 2016) |
| TreeSim | Speciation and extinction | R | (Stadler, 2011) |
| TreeSim GM | Bellman–Harris models with lineage-specific shifts of speciation and extinction | R | (Hagen and Stadler, 2018) |
| T-Rex (Random tree generator module) | Random generation | C++, web service | (Makarenkov, 2001); (Boc et al., 2012) |
| Zombi | Birth-death model | Python | (Davín <i>et al.</i> , 2020) |

Table 1: Overview of phylogenetic tree simulators. Several solutions for generating species and gene trees with the inclusion of additional features (such as horizontal gene transfer) are presented in the table in alphabetical order (by package name).

by the following formula 1:

$$OL(T_1, T_2) = \frac{n(T_1, T_2)}{n(T_1) + n(T_2) - n(T_1, T_2)},$$
 (1)

where, $OL(T_1, T_2)$ is the overlap level between tree 1 (denoted T_1) and tree 2 (denoted T_2), $n(T_1, T_2)$ is the number of common leaves between T_1 and T_2 , $n(T_1)$ is the number of leaves in T_1 , $n(T_2)$ is the number of leaves in T_2 .

As mentioned above, an analysis of current solutions in phylogeny and bioinformatics did not detect the availability of dataset "generators" with the above conditions. In this work, we propose a dataset generation pipeline of phylogenetic trees for use in generating supertrees. A scheme of the pipeline is shown in Figure 1.

The main steps in the proposed workflow are as follows:

1. Input step. The user enters the initial values:

- *L_{min}* is the minimum possible number of leaves for each tree;
- *L_{max}* is the maximum possible number of leaves for each tree;
- N_{gen} is the number of trees to be generated;
- *p*_{*level*} is the average level of overlap (common leaves) between the trees in the set.
- 2. Validation step. The input values should satisfy the following constraints: L_{min} is an integer and $5 \le L_{min} < 500$; L_{max} is an integer and $L_{min} < L_{max} \le 500$; N_{gen} is an integer and $N_{gen} \le 500$; p_{level} is a floating-point number in the range from 0.2 to 0.7 in increments of 0.05 (which corresponds to the range from 20% to 70%).
- 3. Original tree step. Generate the first tree with L_{max} leaves. Each tree is generated in 2 steps: first, a species tree is generated, and then a gene tree (with HGT) is generated on its basis. We distinguish separately the generation of the first tree as



Figure 1: The scheme of data generation. The following values are used in this workflow: Lmin is the minimum possible number of leaves for each tree; L_{max} is the maximum possible number of leaves for each tree; N is the current number of generated trees; Ngen is the number of trees to be generated; p_{level} is the average level of overlap (common leaves) between the trees in the set; n_l is the number of leaves. The workflow uses HGT rate = 0.2 by default (this value is within the range estimated in (Koonin et al., 2001) based on biological data), but the user can change this parameter depending on their experience and objectives. The principle of HGT implementation is described in the "Related work" section. As a result, the user will get a dataset of N_{gen} gene trees, each with a number of leaves from the range (L_{min}, L_{max}) with HGT incorporated. The user can save both sets of species trees and gene trees in Newick format as text files and download them for their own purposes.

the base tree, which is used to calculate the level of overlap with the subsequent tree. The L_{max} value is used to provide a large spread in the comparison of leaves in trees during calculations.

- 4. Pairwise tree step. Generate the next tree with a random number of leaves from the range (L_{min}, L_{max}) .
- 5. Overlap level evaluation step. Calculate the average pairwise (without repetitions) level of overlap between trees and check how the new tree affects the average level of overlap. If they overlap in the specified range ($p_{level} 0.01$; $p_{level} + 0.01$), this new tree is saved to the dataset (the user can adjust the size of this range). If not, return to step 4.
- 6. Repeat steps 4 and 5 until the dataset includes the required number of trees (N_{gen}) .
- 7. Output step. Save the generated data (trees in Newick format) to a text file.

The user can save two datasets as a result of this workflow: the first dataset (main dataset) is a set of gene trees, the second dataset is a set of species trees (for individual purposes). In both datasets, the tree positions in the files correspond to each other. We will use individual pairs of trees to analyze the presence of horizontal gene transfer events.

This workflow can be extended for the case of inferring a single or multiple supertrees based on the generated data using additional packages. One of the most popular solutions for supertree inference is the CLANN tool (Creevey and McInerney, 2005), which is freely available on GitHub and widely used by a large number of researchers. In order to perform it, the user needs to follow several steps:

- 1. Dataset preparation (input): Generating phylogenetic trees defined on different, but partially overlapping sets of species, based on *GPTree*.
- 2. Prepare the input data: it can be data generated from the GPTree generator of phylogenetic trees with a different number of overlapping leaves.
- Prepare a text file with commands: basic recommendations are provided in the tool documentation.
- 4. Run CLANN.
- 5. Save the output data.

A sample command file with recommended parameters is available on the project's GitHub repository.



Figure 2: Visualization of 6 trees from the generated dataset with the following parameters: $L_{min}=7$, $L_{max}=12$, $p_{level}=0.5$. Basic visual analysis shows that these trees have different numbers of leaves (one tree has 8 leaves, three trees have 9 leaves, one tree has 10 leaves, and one tree has 12 leaves), and they are within the given parameters. In addition, these trees have a certain proportion of common leaves, and, in fact, the average level of overlap is 0.5 with a small margin of error.

4 RESULTS AND DISCUSSION

This solution is implemented in Python and structured as an interactive Jupiter Notebook (in .ipynb format). The generator was tested in Google Colaboratory (Google Colab with a basic free version).

First, we generated and visualized a small number of trees in order to show their structure (Figure 2). The resulting image reflects the basic parameters set by the user.

Second, we tested the functionality of the phylogenetic tree dataset generator with relation to three basic parameters: the number of generated trees with different set of leaves from the defined range, evaluation of the level of overlap between trees, and analysis of the presence of HGTs. The identified parameters and the basic results are shown in Table 2.

Figure 3 shows a visualization of the results by the level of overlap between trees. It should be noted that the distribution resembles a normal distribution. The bell-shaped curve can show us the degree of diversity in the number of common leaves belonging to pairs of trees. In parts (a) and (b), we may see a small number of rare values (left and right), which actually are outliers. Part (b) may also help to evaluate the standard deviation, which can be relatively large for a flat bell-shaped distribution. The boundaries in the left and right tails region are also estimable using formula 1 (for the cases of L_{min} and L_{max} number of leaves) and considering the initial parameters set by the user.

We analyzed for the presence of horizontal gene transfer in the generated dataset. For this purpose, we used a random pair of species and gene trees Table 2: Dataset generation parameters and basic results.

| Actions | Values |
|--------------------------------------------------------------------------|-------------------------------------------------------------------------------------------------------------------------------------------|
| Setting parameters | • $L_{min} = 15;$ • $L_{max} = 25;$ • $N_{gen} = 50;$ • $plevel = 0.5$ |
| Checking the final number of trees in the generated dataset | Desired number of trees = 50; Real number of trees = 50; Number of unique trees in the dataset = 50 |
| Calculation of the ac- tual average level of overlap between trees | Desired level of overlap = 0.5; Average level of overlap between each pair of trees = 0.5 |

and checked for the presence of HGT using the T-Rex web service (Boc *et al.*, 2012). The results are shown in Figure 4. This service utilizes a polynomial-time algorithm with the possibility to choose between several optimization criteria (in particular, bipartition dissimilarity, Robinson and Foulds distance, and least-squares) and a bootstrap HGT detection (Boc *et al.*, 2010). To infer a horizontal gene transfer scenario, the user needs to provide a pair of species and gene trees.

We observe that the generated dataset corresponds to our criteria. It should be noted that the generator works slower for overlap levels less than 0.2 and greater than 0.7, and therefore in the current version of the generator the recommended value of the overlap level is in the range (0.2, 0.7). In future releases of this generator, we plan to expand this range.

A version of Jupiter Notebook with code to analyze the generated dataset and examples can be found in the project repository on GitHub (https://github.com/tahiri-lab/GPTree).

The inference of supertrees based on the generated dataset is also an important subject. Depending on the objectives of the study, we can refer to the clustering approach, when the supertree inference is performed on the basis of a cluster of trees. The first option is to



Figure 3: Visual analysis of the level of overlap in the dataset. Part (a) shows the level of overlap relative to the number of pairs of trees. It may be observed that most of it is around 0.5 (as set by the user as initial parameters) with a slight deviation left and right. Part (b) shows the distribution according to the number of common leaves in possible pairs of trees (without overlaps). It can be seen that this visualization is bell-shaped with peaks in the center of the indicated range.



Figure 4: Analysis of the presence of HGT. The results of the analysis are as follows: HGT 1: from subtree (46, 47) to subtree (41); HGT 2: from subtree (37) to subtree (27); HGT 3: from subtree (29) to subtree (39); HGT 4: from subtree (42, 43) to subtree (41, 46, 47); HGT 5: from subtree (32, 33) to subtree (27, 37); HGT 6: from subtree (41, 42, 43, 46, 47) to subtree (27, 32, 33, 37); HGT 7: from subtree (27, 32, 33, 37, 41, 42, 43, 46, 47) to subtree (45). Total number of HGTs = 7. The analysis was performed using T-Rex web service (Boc *et al.*, 2012).

generate a large dataset, then cluster this dataset using existing algorithms (e.g., k-means or k-medoids, see (Tahiri *et al.*, 2022a)) to build a supertree for each cluster that is found. The second option is to use the generator in a loop and generate several datasets of clusters for each set of parameters to infer a supertree.

One of the use cases of the developed tool is the generation of data to test new distance measures between phylogenetic trees defined on different, but mutually overlapping, sets of taxa, or supertrees. Although metrics between trees have been studied for more than 40 years, the story is different for supertrees since most distances were introduced in the last decade or so. The Robinson and Foulds distance is the most popular phylogenetic tree distance, but no such standard is known for supertrees. On the one side, it is possible to adapt existing metrics to compare phylogenetic trees (with overlapping leaves) in the context of clustering. This can help to effectively use phylogenetic tree clusters to infer supertrees. On the other side, this foundation can help to evaluate, adapt and improve metrics for comparing phylogenetic supertrees relying on distance properties. Researchers can use simulated data with incorporated biological events in such tasks.

5 CONCLUSION

The analysis and comparison of several phylogenetic tree simulators did not reveal phylogenetic tree generators with partially overlapping taxon sets, which can be used in problems using phylogenetic supertrees. This paper proposes a new approach for generating a dataset of phylogenetic trees for further use in the building of phylogenetic supertrees. The generator takes the minimum possible number of leaves for each tree, the maximum possible number of leaves for each tree, the number of trees to be generated, and the average level of overlap (common leaves) between the trees in the set as input parameters. The output is a dataset consisting of gene trees with incorporated biological events, including duplication, loss, and horizontal gene transfer events. The trees in the generated dataset are in Newick format.

The generator presented in this paper can be useful for biologists, bioinformaticians, ecologists, and computer scientists to conduct experiments with phylogenetic trees and supertrees, for example, in the problems of developing new metrics of distance between supertrees, clustering, and classification problems. This solution is freely available in the repository on GitHub, where there are also additional scripts for testing the generated dataset with detailed comments, and sample datasets. The possibility to run the generator in Google Colaboratory makes it easier and more accessible for the scientific community.

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