Study of Uncertainty Quantification Using Multi-Label ECG in Deep Learning Models

Raquel Simão¹,²,∗, Marília Barandas¹,², David Belo², and Hugo Gamboa¹,²

¹LIBPhys (Laboratory for Instrumentation, Biomedical Engineering and Radiation Physics), NOVA School of Science and Technology, Campus da Caparica, 2829-516, Portugal
²Associação Fraunhofer Portugal Research, Rua Alfredo Allen 455/461, 4200-135 Porto, Portugal

Keywords: Uncertainty Quantification, Monte Carlo Dropout, Deep Ensemble, Dataset Shift, Active Learning.

Abstract: Machine Learning (ML) models can predict diseases with noteworthy results. However, when implemented, their generalization are compromised, resulting in lower performances and render healthcare professionals more susceptible into delivering erroneous diagnostics. This study focuses on the use of uncertainty measures to abstain from classifying samples and use the rejected samples as a selection criterion for active learning. For the multi-label classification of cardiac arrhythmias different methods for uncertainty quantification were compared using three Deep Learning (DL) models: a single model and two pseudoensemble models using Monte-Carlo (MC) Dropout and Deep Ensemble (DE) techniques. When tested with an external dataset, the models’ performances dropped from a F1-Score of 96% to 70%, indicating the possibility of dataset shift. The uncertainty measures for classification with rejection resulted in an increase of the rejection rate from 10% in the training set to a range between 30% to 50% on the external dataset. For the active learning approach, 10% of the highest uncertainty samples were used to retrain the models and their performance increased by almost 5%. Although there are still challenges to the implementation of ML models, the results show that uncertainty quantification is a valuable method to employ in safety mechanisms under dataset shift conditions.

1 INTRODUCTION

Over the years, medical technology has been developed and improved in order to ensure the most effective healthcare to the general public. Artificial Intelligence (AI) is quickly evolving due to its potential to assist evidence-based clinical decision-making and achieve value-based care (Chen and Decary, 2020). As a result, there has been a growing amount of scientific research regarding the use of ML algorithms in the medical domain. ML models have progressed to the point that they can predict a variety of diseases, with performances that can be superior to those achieved by healthcare professionals. This is achievable because ML models are trained with patient data in order to identify patterns that would otherwise be undetected and, thereby, produce an estimate of a patient’s current or future clinical state.

However, while showing promising results, these models still have some limitations for their deployment on clinical settings since their generalization capabilities are often compromised, resulting in lower performances and rendering healthcare professionals more susceptible into delivering erroneous diagnostics. This occurs since conditions in which we use the medical systems diverge from the conditions in which these systems were created, leading to mismatches between the training data and the data intended to be classified. This problem is called dataset shift and, in general, the greater the degree of shift, the poorer is the model’s performance (Malinin et al., 2021). This is one of many problems that contribute to the limited number of models implemented in real life setting, with only 64 AI/ML medical systems approved by the FDA up until 2020 (Benjamens et al., 2020). As a result, it is critical that ML models include safety mechanisms to mitigate the dataset shift problem and improve the trustworthiness of these models. If AI/ML models fail to possess these mechanisms, they will be unable to be effectively implemented with FDA approval, leading AI/ML models to oblivion as decision support models.

Quantifying the uncertainty of models’ predictions is a key method to assess the model’s confidence in their decisions. Although uncertainty quan-
tification has already demonstrated promising results in different fields, the literature on ECG classification is scarce. The works of (Vranken et al., 2021) and (Aseeri, 2021) are relevant works under this topic; however a single-label classification is applied, even though multi-label datasets are used.

In this paper, we develop a classification approach with rejection option based on uncertainty measures and evaluate the uncertainty as a selection method for active learning. Although the main purpose is to develop an agnostic framework for the classification of cardiac arrhythmias, this work will concentrate on establishing the practical value of the uncertainty quantification applied in three types of DL models in different medical datasets and their role in the referred methods. This research aims at providing a better understanding of the capacity of the model’s generalization through uncertainty estimation as well as demonstrate that uncertainty aware models are capable of containing safety mechanisms and, therefore, be considered trustworthy systems to be implemented in clinical settings.

2 RELATED WORK

2.1 Uncertainty Estimation Measures

In the general literature (Shaker and Hüllemeier, 2020; Barandas et al., 2022), a distinction between two intrinsically different sources of uncertainty is done: aleatoric and epistemic. Aleatoric Uncertainty (AU) is associated with the variability in the outcome of an experiment which is due to intrinsic randomness of the data generating process that cannot be explained away given more observations or data samples (Shaker and Hüllemeier, 2020). Epistemic Uncertainty (EU) refers to the lack of knowledge of the model and usually is caused by incomplete domain coverage since unknown regions of the data space will always be presented. The presence of new classes that were not contemplated in the training of the model, are an example of high EU. This uncertainty can be reduced by increasing the training data, better modeling or better data analysis (Barandas et al., 2022).

In traditional probabilistic modeling and Bayesian inference, the uncertainty of a prediction is given by the posterior distribution. Considering a finite dataset \( D \) composed of instances \( x \) ans labels \( y \), where \( y_k \in \{y_1, ..., y_K\} \) is a set of \( K \) class labels, an hypothesis \( h \) maps the instances \( x \) to the outcomes \( y \). The posterior \( P(h|D) \) can be obtained via the Bayes rule:

\[
P(h|D) = \frac{P(D|h)P(h)}{P(D)} \tag{1}
\]

where \( P(D|h) \) is the probability of data given \( h \) and \( P(h) \) is a prior distribution. For a single probability distribution, an uncertainty measure that combines both aleatoric and epistemic uncertainty can be calculated through the probability of the predicted class, given by:

\[
p(y|x) = \max_k p(y_k|x, D) \tag{2}
\]

The entropy of the predictive posterior modeled by Shannon’s entropy is also an uncertainty measure for single probability distribution defined by:

\[
H[p(y|x)] = -\sum_{k=1}^{K} p(y_k|x) \log_2 p(y_k|x) \tag{3}
\]

In DL the randomness induced during training and inference can be used to obtain an uncertainty estimation (Mi et al., 2019). DE and MC Dropout are techniques commonly used for this quantification. DE consists of training repeatedly the same neural network with different parameters due to the randomness in the initialization and training process (Stähl et al., 2020). Each model makes its own prediction and the final prediction is derived from the composition of all models in the ensemble. MC Dropout is a method that omits a certain percentage of neurons at each layer of a neural network during training and testing, with the missed neurons randomly selected for each iteration and each test time (Gal et al., 2016). The final prediction is obtained from the composition of all the predictions with distinct dropouts.

For these methods, the approximation proposed by Depeweg et al (Depeweg et al., 2018) can be used to obtain a measure of total, aleatoric and epistemic uncertainty:

\[
-u_{total}(x) := H\left[\frac{1}{M} \sum_{i=1}^{M} p(y|x, h_i)\right] \tag{4}
\]

\[
u_{aleat}(x) := \frac{1}{M} \sum_{i=1}^{M} H[p(y|x, h_i)] \tag{5}
\]

\[
u_{epis}(x) := u_{total}(x) - u_{aleat}(x) \tag{6}
\]

2.2 Classification with Rejection Option

When a classifier is not sufficiently confident in the prediction, the model can abstain from producing an answer or discard a prediction if the uncertainty is sufficiently high. Therefore, a classifier with rejection can cope with unknown information, reducing the threat caused by the existence of unknown samples or mislabeled training samples that can compromise the performance of the model. The standard
approach for classification with rejection option, also known as Chow’s theory (Chow, 1970), is the calculation of a rejection threshold that minimises the classification risk. One approach to achieve this is through the uncertainty associated with every prediction. The empirical evaluation of methods for quantifying uncertainty is a non-trivial problem, due to the lack of ground truth uncertainty information. A common approach for indirectly evaluating the predicted uncertainty measures is using Accuracy-Rejection Curve (ARC). The ARC represents the accuracy of a classifier against its rejection rate, varying from 0 to 1 (Nadeem et al., 2009).

2.3 Active Learning

ML models, particularly DL models, demand a vast labelled dataset to learn properly. The number of labelled data required grows with the complexity of the problem or the complexity of the input data. This issue is particularly dominant in the medical field. In order to automate the analysis of a given medical exam, it would be necessary an expert to annotate a large number of exams, labelling them to indicate if the patient has certain condition or not. However, obtaining the amount of the needed labelled data is time-consuming and expensive. One possible solution to this problem is active learning. In this approach, the model chooses what unlabelled data is appropriate for training, and request an external “oracle”, for example a medical work, for the label of the selected data (Settles, 2009). The choice of the data to be labelled is selected by an acquisition function, which ranks points based on their potential informativeness (Gal et al., 2016). There are a variety of acquisition functions and many of them rely on model uncertainty to evaluate the potential informativeness of the unlabelled data points. The more informative is the selected data, the fewer labelled training examples are necessary to achieve a greater classifier accuracy. Therefore, the quantification of uncertainty plays a central role in active learning and can be valuable to improve the model’s performance when implemented in clinical settings.

3 METHODOLOGIES

3.1 Databases

Four public multi-label cardiac arrythmia datasets from various countries were employed, having been provided by the PhysioNet/Computing in Cardiology Challenge 2020, as proposed by Perez Alday et al. (Alday et al., 2020). A subset of five classes were selected for classification: Atrial fibrillation (AF), First-degree atrioventricular block (IAVB), Left bundle branch block (LBBB), Right bundle branch block (RBBB) and Sinus rhythm (NSR). These classes were chosen since almost all of them are presented in each dataset and are the most frequent classes overall. The training database is composed of the CPSC2018 and PTB-XL dataset. The PTB and G12EC databases are used as external data in this research.

3.2 Data Preparation

To reduce the computational costs, only the ECG aVR lead was used since this lead produced the best results in the work of Chen et al. (Chen et al., 2020). The data was downsampled to 125 Hz and a 10 seconds window size was used. Data with length below that value were excluded and data above 10 seconds were truncated, so that all the samples have 1250 sample data points. The ECG signals were filtered using a 2nd order band-pass Butterworth filter between 1 and 40 Hz and it was also employed a smooth function using a window of 10 samples. Lastly, the data was normalised through a z-normalisation.

3.3 Proposed Algorithm

The model developed is a one-dimensional CNN. The architecture consists of three convolutional blocks, each with a convolutional layer followed by a batch normalization layer, a PRelu activation function with an initializer of 0.25, a max pooling layer and a dropout layer with rate of 0.25. Each convolutional layer has the same kernel size (31x31) but different number of filters (the first has 512 filters, the second has 256 and the last one has 128 filters). After the convolutional blocks, a flatten layer was applied, resulting in a Latent Vector. Three fully connected layers are added and the last one has a sigmoid activation function with the same number of neurons as classes. The flowchart of the proposed algorithm is shown in Figure 1.

The model was trained in 30 epochs with a batch size of 64. The loss function employed was the binary cross-entropy and an Adam optimizer with a learning rate of 0.1. Since the model is trained with imbalanced datasets, it was added the class weight parameter that defines the weighting to adopt for each class when fitting the model.
3.4 Training and Testing

The data from CPSC2018 and PTB-XL database was split into 60% training, 20% validation and 20% testing. The test set from this database was used as an in-distribution set and will be referred as test-in from now on. The test set composed from all the samples in the PTB and G12EC datasets is named test-out. Two approaches were employed: the MC dropout and the DE. Both approaches were applied 30 times to both test sets, resulting in 30 models for each. To obtain the final prediction with both MC Dropout and DE approach, it was applied the majority vote for each class.

3.5 Uncertainty Approaches

For the single CNN, the predicted posterior probability, also known as maximum probability, and the Shannon entropy of the predicted probabilities were used as uncertainty measures. In the case of MC Dropout and DE, the total uncertainty, EU and AU measures were estimated. Since a prediction in a multi-label classification can return more than one class, the network sigmoid values do not sum 1. For this reason, in this multi-label scenario, each class was assumed as an independent binary case and the uncertainty calculated by each class. Besides the uncertainty by class, an aggregation mechanism based on the sum of all class uncertainties was employed as the final prediction uncertainty.

Regarding the uncertainty evaluation, a common approach for evaluating the predicted uncertainty is by using ARC. However, due to the imbalance data, instead of using accuracy as a performance measure, the F1-score was used and the F1-Rejection curve was computed to evaluate the behaviour of the developed models. These curves were performed for the uncertainty measures mentioned previously with the rejection occurring from the sample with the highest uncertainty in its classification to the sample with the lowest uncertainty. This evaluation was performed considering the overall performance. Since the data is multi-label, the uncertainty of an ECG sample is the sum of each class uncertainty and, therefore, each sample uncertainty is represented by a value between 0 and 5.

3.6 Active Learning

Uncertainty estimation can be used to select the samples with higher uncertainty, taking advantage of the separation between epistemic and aleatoric uncertainty, where the former is more relevant as a selection criterion (Hüllermeier and Waegeman, 2021). Following this idea, the retraining process was performed for the single model and the DE model, where a new set was added to the previous training set for the retraining process. Each model was retrained for four more epochs using the newly dataset and the same parameters previously used to train the initial models.

To validate if samples with high epistemic uncertainty are more informative to the DE model, three different sets composed by 10% of the test-out were defined to the retraining process, namely: 1) random samples; 2) samples with the highest epistemic uncertainty; 3) samples with the highest total uncertainty. For the single model, the retraining was done with...
samples with the highest Shannon Entropy and for random samples as well.

4 RESULTS

In order to access the models’ generalization capacities, it was compared the performance of the single, MC Dropout and DE models tested with test-in and tested with test-out.

As it can be seen in Figure 2, the three models, when tested with the test-in set, have similar performances, with micro average F1-score around 96%-97%, being comparable to the state of the art results. However, when the models are tested with the test-out set, their performances decrease significantly in all three models, having a micro-average F1-Score of approximately 70%. The DE model obtained the highest F1-score in both test sets with a maximum difference of 3% from the other models.

Regarding the classification with rejection option, even though this method does not solve the problem of model’s generalization that leads to poor performance results under data shift, it can be a viable approach to abstain to predict a class under high uncertainty conditions. For each model, the uncertainties measures presented in Section 2.1 were calculated for the test-in and test-out sets and the results can be seen in Figures 3 and 4. For the single model, the behaviour of both uncertainties measures in test-in and test-out are similar. However, both uncertainty measures obtain higher uncertainty in the test-out set.

As for the results in Figure 4, for the test-in set, the MC Dropout and DE models estimate similar values of uncertainty, presenting the same median and the same range of total uncertainty. The MC Dropout presents a higher range of AU while the DE detects higher EU. As for the test-out set, both models capture higher uncertainty than for the test-in set in all the three types of uncertainty measures.

To investigate the role of uncertainty in rejection, the F1-rejection curve was produced for the three models, rejecting the samples according to the highest calculated uncertainties. To validate the rejection rate in both sets, a 10% rejection in the training set was ap-
plied and the uncertainty thresholds obtained. Using the same thresholds on test-in and test-out, the rejection rates increased to approximately 12% and 40%, respectively, using the single model for both maximum probability and entropy measures. For the MC Dropout the rejection in test-in was 9% and vary between 31% and 34% for test-out depending on the uncertainty measure used. The DE model vary the rejections rates between the intervals 13%-16% and 45%-51% for test-in and test-out, respectively. Furthermore, as it can be deducted for the micro average F1-Scores presented in the Table 1, for all the three models and for all uncertainty measures, the more samples rejected, the better is the models’ performance. Even though the curves based on the different uncertainty methods are quite similar, throughout the rejection, the DE model presents better micro average F1-Score results for the same rejection rate.

Apart from employing the rejection option, a possible method to deal with dataset shift is by retraining the model with samples that have crucial information to help improve its performance. A potential solution is the active learning approach, in which the samples used to retrain the model contain the highest uncertainty associated with their classifications. To evaluate the three uncertainties in this approach, the retrained models were tested with the test-out set without the 10% samples to fairly compare the increase between the retrained model and the baseline model. Thus, the following nomenclature was used: 1) Previous trained model using the complete test-out set (Baseline - test-out-100); 2) Previous trained model tested only on 90% of test-out, i.e 10% of test-out was used to retrain the model (Baseline - test-out-90); 3) Retrained model using the selected 10% data and tested on the remaining 90% (Retrain - test-out-90). Furthermore, to serve as control, this process was performed for 10% of random samples in order to observe the role of uncertainty in this approach. This procedure was conducted 10 times and the mean and standard deviation of the results are represented in Figure 5.

As it can be observed in Figure 5, when the samples with the highest uncertainty are removed from the test-out, the model performance increases slightly, from 2%-4%. After retraining the two models with these samples and evaluating it without them, a maximum increase of almost 5% is observed when compared to the baseline models that are tested with all the samples of test-out. These conclusions are supported through the results served as a control, where the samples selected are random and the trained models have similar performance as the original models.

5 DISCUSSION

To make the decision support systems as trustworthy as possible, it is critical to access the confidence that ML models have in their classifications. This work studied these concepts using four large public ECG databases for the classification of cardiac arrhythmias. As multiple cardiac arrhythmias can be presented within the same recording, a multi-label classification setting was adopted for the development of DL models.

The performance of the three models developed were assessed for two test sets, where the test-in has data from the same database as the training and the test-out presents data from a different database. Although these models produced similar performance results for the same test set, the DE and MC Dropout outperform the single model, as expected since these models assist in reducing models’ high confidence in incorrect classifications. The DE model revealed has the better performance in both test sets, which it is consistent with the literature. When tested with the test-out set, the performance of all the three models drops significantly, confirmed by the decrease of F1-Score from around 96% to 70%. These results indicate the possible presence of dataset shift since the data from test-out has different characteristics and distributions than the data used for training.
Table 1: Rejection rate results and the respective F1-Score values for each uncertainty.

<table>
<thead>
<tr>
<th>Model</th>
<th>Uncertainty</th>
<th>Test-in</th>
<th>Test-out</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>Rejection</td>
<td>F1-Score</td>
<td>Rejection</td>
</tr>
<tr>
<td>Single CNN</td>
<td>Maximum Probability</td>
<td>12.24%</td>
<td>98.54%</td>
</tr>
<tr>
<td></td>
<td>Shannon Entropy</td>
<td>12.16%</td>
<td>98.38%</td>
</tr>
<tr>
<td>MC Dropout</td>
<td>Aleatoric</td>
<td>9.51%</td>
<td>98.46%</td>
</tr>
<tr>
<td></td>
<td>Epistemic</td>
<td>9.35%</td>
<td>98.29%</td>
</tr>
<tr>
<td></td>
<td>Total</td>
<td>9.41%</td>
<td>98.47%</td>
</tr>
<tr>
<td>DE</td>
<td>Aleatoric</td>
<td>16.21%</td>
<td>99.34%</td>
</tr>
<tr>
<td></td>
<td>Epistemic</td>
<td>13.46%</td>
<td>99.10%</td>
</tr>
<tr>
<td></td>
<td>Total</td>
<td>15.75%</td>
<td>99.41%</td>
</tr>
</tbody>
</table>

Regarding the uncertainty estimations, the Shannon entropy and maximum probability were estimated for the single model and the aleatoric, epistemic, and total uncertainty for the MC Dropout and DE models. For the single model, both maximum probability and entropy obtained similar results, while for the MC Dropout and DE the total uncertainty presented slightly better result. This suggests the benefit of estimating uncertainty using the combination of epistemic and aleatoric uncertainty. Additionally, all uncertainties computed for the test-out were significantly higher than for the test-in set. This shows that the model is less confident on the classification of cardiac arrhythmias and as result there is higher probability of misclassified samples. This is an indication of dataset shift and the main reason of models’ performance drop in test-out set. Furthermore, it is important to mention that it was expected that the EU would be higher than the AU in test-out since the data comes from a different source and might be a different distribution. This reveals that there are still challenges in capturing these two uncertainties correctly.

In order to improve the trustworthiness of the models, the classification with rejection option was applied. For both test sets, the models performance increased with rejection, revealing that the higher the uncertainty in a given classification, the higher is the probability of the models to misclassify the samples. Additionally, the uncertainty threshold, selected from the training data, increased from 10% to a range between 30% to 50% depending on the model or uncertainty measure employed. The increase in rejection rate confirms that high uncertainty is presented in the classifications and the uncertainty is higher in the test-out set. This is another evidence of the dataset shift effect and that the models are not as prepared to classify data with different distributions.

Another alternative to improve the models’ performance and reliability is through the retraining of models with unseen data. In this manner, it was employed an active learning approach, using 10% of the samples with the highest uncertainty in the test-out set. The results showed that the models improved their performance by a maximum of almost 5% when using uncertainty versus 2% when using a random selection. These results demonstrate that data with high uncertainty has information that the model has not yet learned and hence the models benefit from the retraining with this selection method. Moreover, when removing the 10% of the samples with the highest uncertainty and test 90% of the test-out in the baseline models, the performance improved, showing that the samples with highest uncertainty are misclassified. This underlines the importance of the uncertainty quantification in detecting incorrect classifications.

6 CONCLUSIONS

The evaluation and comparison of uncertainty measures has proven to be essential in an in-depth analysis of ML models, allowing us to understand their limitations. Furthermore, the preliminary results reveal that the quantification of uncertainty should be considered a key feature of any ML model as a safety mechanism. Although there are still no ground truth for the estimation of uncertainty, all the metrics used were capable to detect uncertainty in multi-label data. Nevertheless, there are still challenges in capturing the uncertainty through the employed measures, specially in
the separation of epistemic and aleatoric uncertainty. It is also possible to infer the role of uncertainty as a valuable method under dataset shift conditions and in strategies such classification with rejection option and active learning approaches.

Thus, the development of uncertainty aware models will provide healthcare professionals with access to the model’s confidence in its predictions but also refrain the model from delivering classifications with high uncertainty. Furthermore, samples that have different characteristics and distributions than the ones learned by the models have higher uncertainty associated with their classifications and, therefore, can be used to retrain the ML models and improve its generalization and robustness. The active learning approach is a reliable method for this purpose, demonstrating that it is a technique capable to self-regulate the learning of the models in a real life setting, with a reduction in computational cost as well as in the cost of labelling the data usually required. Despite the encouraging results, much more research is needed in the area of clinical data uncertainty, particularly in multi-label data.

To conclude, data with different characteristics and distributions from those learnt by the ML models will always exist, so it is imperative that AI systems possess uncertainty associated methods as safety mechanisms to produce reliable models to implement as a decision support system in clinical settings.

REFERENCES


