

# Estimating Electric Vehicle Driving Range with Machine Learning

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**Abstract:** In the past years, we have witnessed an increase on the use of *electric vehicles* (EV), which are now widely accepted as reliable and eco-friendly means of transportation. When choosing an EV, usually one of the key parameters of choice for the consumer is its *driving range* (DR) capability. The DR depends on many factors that should be addressed when predicting its value. In some cases, the existing heuristic techniques for DR estimation provide values with large variation, which may cause driver anxiety. In this paper, we explore the use of *machine learning* (ML) techniques to estimate the DR. From publicly available data, we build a dataset with EV data suitable to estimate the DR. Then, we resort to regression techniques on models learned on the dataset, evaluated with standard metrics. The experimental results show that regression techniques perform adequate and smooth estimation of the DR value on both short and long trips, avoiding the need to use the previous heuristic techniques, thus minimizing the drivers anxiety and allowing better trip planning.

## 1 INTRODUCTION

In recent years, car manufacturers have moved to the manufacturing of *electric vehicles* (EVs), due to some factors, such as the concern on climate change, the dispositions of the Paris Agreement, and the need to be eco-friendly. EVs are accepted as a sustainable transport solution, which have grown in popularity. Vehicle manufacturers have increased the competitiveness on the vehicle's performance, namely the *driving range* (DR) capability, since it is a key factor for consumers (Egbue and Long, 2012).

The EV driving range at a given point in time of a trip, defined as the eRange, is an estimate of the remaining driving distance, expressed in kilometers. Its proper estimation eases the drivers anxiety on a trip to a charging station and allows the driver to do adequate trip planning (Smuts et al., 2017; Song and Hu, 2021). However, the accurate estimation of the eRange value is a challenging task, since it depends on many dynamic driving data parameters, such as: vehicle design; drivers behavior; weather conditions; road inclination; commute type - city driving or highway driving; battery *state-of-charge* (SoC).

Figure 1 depicts the eRange and SoC concepts (Coutinho, 2021b). Figure 2 shows the main

influencing forces on a vehicle that lead to the actual battery energy consumption. The accurate estimation of the eRange allows consumers to rely on its vehicle for longer travel time and efficient charging plans. The challenges and difficulties posed in the eRange estimation have lead to recent studies on this topic (De Cauwer et al., 2017; Varga et al., 2019). In the past years, *machine learning* (ML) techniques have shown their effectiveness in different fields. This is due to its nature of learning models from existing data to gradually achieve better results making it a widely recognized tool for many problems.

The existing eRange estimation techniques are based on some heuristics, such as the analysis of the average consumption of energy in the past minutes, on a trip. These simple estimations may not produce accurate results, since they account only for a small



Figure 1: An example of the EV eRange and state-of-charge concepts, along with other indicators (Coutinho, 2021b).

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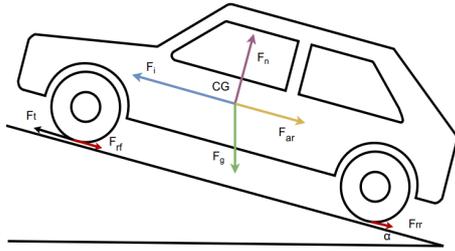


Figure 2: The key influencing forces on a moving vehicle. ( $F_i$ -inertial force;  $F_t$ -tractive force;  $F_g$ -gravitational force;  $F_{rr}$ -rear rolling resistance force;  $F_{fr}$ -front rolling resistance force;  $F_{ar}$ -aerodynamic (air) drag;  $F_n$ -normal force; CG-center of gravity;  $\alpha$ -the road slope ).

set of factors and DR estimation depends on different variables. It is expected that the use of ML methods and models will provide better estimates, by using datasets with more variables than the ones considered in heuristic methods. Although, the training of the models may take more time than the existing approaches, it is expected that their use will improve prediction accuracy. The challenge is to learn accurate models with adequate response time when placed on-board of the vehicles.

### 1.1 Our Proposal

In this paper, we address the eRange estimation problem with ML regression techniques, through a three phase approach: the dataset construction and pre-processing; learning ML models; evaluation of the learned ML models, with standard metrics.

The remainder of this paper is organized as follows. Section 2 refers to the state-of-the-art on existing eRange estimation solutions and their use with the available datasets. In Section 3, we present the approach and methodologies adopted in this work. The experimental evaluation and discussion are reported in Section 4. The paper ends in Section 5 with some concluding remarks and directions for future work.

## 2 STATE OF THE ART

In this section, we address the literature and resources for EV research, such as the eRange estimation problem, the availability of public datasets, and existing approaches without and with ML techniques.

### 2.1 Research on EV

The study of EV related topics, has been the focus of many works such as statistical measurement of charging (Brighente et al., 2021), eRange prediction (Varga

et al., 2019), charging topologies (Yilmaz and Krein, 2013), and regenerative braking (Yoong et al., 2010). The eRange prediction is an important EV feature to provide to consumers, as it reduces the driver's anxiety while driving and allows better trip planning. When devising a solution to the eRange estimation problem, real EV driving data in the form of a dataset is required to learn and evaluate the proposed models. It is also necessary to compare the learned models with the existing ones.

Vehicle manufacturers typically do not disclose vehicle driving data or prediction algorithms. As a good eRange prediction is a competitive factor among EV manufacturers, it is not disclosed to the public.

### 2.2 Public Domain EV Datasets

Some datasets regarding EV eRange estimation are publicly available, being composed by vehicle data and trip data, with mainly two types of features: *time-series features*, where the data points vary as a function of time; *trip-invariant features*, in which a given value is kept for the entire trip. Time-series features are usually the SoC, energy consumption, speed, acceleration, and elevation. The trip-invariant features refer to vehicle information such as battery capacity, *average energy consumption* (AEC), *full battery energy* (FBE), *full driving distance* (FDD) also known as *full battery distance* (FBD), vehicle weight, trip information such as commute type (city or highway), total energy consumption, and total distance. Table 1 summarizes the key publicly available EV datasets, namely: *Vehicle Energy Dataset* (VED) (Oh et al., 2019); *Emobpy* dataset (Gaete-Morales et al., 2021); *Classic EV X* project (Coutinho, 2021b) dataset; *Charge Car* project of the CREATE Lab at Carnegie Mellon University Robotics Institute, available at <https://www.chargecar.org>; the EV dataset of the *national big data alliance of new energy vehicles* (NDANEV), <http://www.ndanev.com>.

The VED dataset (Oh et al., 2019) provides 54 different EV driving trip data records for estimation, but lack trip and vehicle information as well as EV model variety. It contains data from three distinct EVs, all from the same model, the 2013 *Nissan Leaf*.

The *Emobpy* Python tool (Gaete-Morales et al., 2021) focuses on EV trip and charge data generation through empirical mobility statistics and customizable assumptions. This approach provides an infinite supply of EV trips as well as proper vehicle information. This dataset has some missing features such as speed, elevation, trip, and commute type.

The *Charge Car* project of the CREATE Lab at Carnegie Mellon University publicly supplies crowd-

Table 1: Public domain datasets with EV data and their key properties. N/A means that the data parameter is not available.

Ensures table is placed on correct location

	VED dataset	Emobpy	Classic EV X project	ChargeCar	NDANEV
<b>Trips</b>	507	Unlimited	3	373	2372
<b>EV Models</b>	1	102	1	N/A	1
<b>Number of EV</b>	3	N/A	1	N/A	5
<b>Features</b>	timestamp, speed, location, battery SoC, battery voltage, battery current, AC power, heater power, outside air temperature (OAT)	timestamp, distance, instant energy consumption (IEC), consumption, average power, state	timestamp, IEC, remain battery energy (RBE), speed	timestamp, elevation, planar distance, adjusted distance, speed, acceleration, model power, actual power*, current*, voltage*	timestamp, speed, total voltage, total current, battery SoC, temp. range, motor voltage, motor current, mileage

sourced data that has served previous eRange prediction models (Zheng et al., 2016). This dataset has a large vehicle diversity due to the open nature of the platform, allowing any user to upload combustion engine based vehicle information as well as the location data, speed, and weather, among other features.

A dataset collected through probe data from nearly 500 battery EVs by the *Japan automobile research institute* (JARI) from February 2011 to January 2013 has the following features: time, location, vehicle state (driving, normal charging, or fast charging), speed, air-conditioner, heater state, and SoC. Although useful and featured in some papers (Liu et al., 2017; Liu et al., 2018; Sun et al., 2015; Sun et al., 2016), for the research conducted in this paper, the authors were unable to access this dataset from <https://www.jari.or.jp/research-database>.

The cloud based EV dataset supplied by the NDANEV has been used in similar eRange prediction approaches (Zhao et al., 2020). This dataset includes battery cell temperature information, which measures the battery cell inconsistency.

As some datasets do not explicitly provide vehicle information, the EV-database website, <https://ev-database.org> offers a public database for existing EV, displaying AEC, DR, and usable battery energy. The availability of this data enables that datasets which lack this feature can be used in eRange prediction models.

### 2.3 EV Autonomy Estimation

The eRange estimation has been an interesting topic in research in recent years, in part due to the increase in EV usage, as they become more efficient. Its prediction difficulty is in part due to the fact that there are many factors to take into account when measuring it, such as battery and road information, previous vehicle trips, and vehicle weight. This has motivated researchers to find solutions for this problem, resort-

ing to ML techniques.

Related work has shown the use of eRange estimation on EV, stating the need for different types of accuracy on eRange estimation as a function of the SoC state. In (Zhang et al., 2012), the approach is to minimize the performance impact of minimum cost route searching from high accuracy eRange prediction.

The proposal in (Coutinho, 2021a) estimates the eRange through a *basic approach* (BA) algorithm, which uses manufacturers invariant vehicle information such as FBE and AEC, as well as the instant SoC value. In detail, the BA estimates eRange using:

- the maximum charge an electric vehicle battery can store, known as FBE;
- the *average energy consumption* (AEC) of the EV, which depends on the use of the *air-conditioner system* (AcS) and on the type of trip (highway or city driving).

It also requires the battery SoC value, at the time of the eRange estimation. Thus, the BA eRange estimation is given by

$$\text{eRange} = \frac{FBE}{AEC(AcS)} \times SoC \quad [\text{km}]. \quad (1)$$

The eRange estimation with an adaptive *history-based approach* (HBA), proposed by (Coutinho, 2021b), relies on the past 10 minutes AEC information gradually influenced by the vehicle instant consumption energy, as well as by the SoC. Once the first 10 minutes had passed, HBA applies a configured energy step to the previous prediction, depending on the computed AEC. This approach yields more optimistic eRange results, with slightly higher values than those of BA, thus easing consumer's anxiety when a higher energy consumption does not have a linear impact on the eRange. HBA relies on parameters such as the *full battery energy* (FBE), SoC, where an *instant energy consumption* (IEC) is used to calculate, at each minute, an *adaptive AEC* (AAEC). Thus, the eRange

estimation for the  $m$ -th minute is

$$\text{eRange}_m = \left\lfloor \frac{FBE}{AAEC_m} \times SoC_m \right\rfloor, \quad (2)$$

where  $\lfloor \cdot \rfloor$  is the floor operator. This algorithm requires three additional parameters: delta energy step,  $\Delta S$ , which is the amount of energy increment/decrement, at each minute  $m$ ; *constant AEC* (*CAEC*), as provided by the EV manufacturer; minimum instance energy.  $AAEC_m$  is updated by

$$AAEC_m = \begin{cases} CAEC, & m \leq N \\ AAEC_{m-1} - \Delta S, & MAAEC_m < AAEC_{m-1} \\ AAEC_{m-1} + \Delta S, & MAAEC_m \geq AAEC_{m-1}. \end{cases} \quad (3)$$

by adding or subtracting the pre-configured delta step,  $\Delta S$ , to the previous  $AAEC$  calculation of the previous  $m$  minutes. Initially,  $AAEC$  is equal to the pre-configured  $CAEC$ , until it is possible to calculate the moving average with minimum number of  $N$  samples. In Equation (3),  $MAAEC_m$  is the moving average of the current  $m$  minute IEC values, where every non-zero IEC value is averaged for its calculation by

$$MAAEC_m = \sum_{i=0}^{N-1} w_i \times AAEC_{m-i}, \quad (4)$$

where  $N$  is the number of past minutes of an observation moving window. The average weights are  $w_i = \frac{1}{2^{(i+1)}}$ , such that the most recent  $AAEC$  values have higher importance. The minimum instance energy's role is to prevent the algorithm from performing an eRange calculation when the average IEC values for the current  $m$  minute are less than a predefined threshold value. This is done so that in the event the vehicle consumes negligible power, it would not cause an  $\Delta S$  decrement or increment on the eRange estimation, thus preventing inaccurate eRange results.

## 2.4 The Use of Machine Learning

The use of ML for a multitude of cases (Amershi et al., 2019) in fields such as big data (Zhou et al., 2017) and data mining (Bose and Mahapatra, 2001) has proven its robustness on solving different problems. As a result, some approaches for the eRange estimation problem have resort to supervised learning techniques. The use of *decision trees* (DT) (Alpaydin, 2020), *random forest* (RF) (Breiman, 2001), and *K-nearest-neighbor* (KNN) (Alpaydin, 2020) in *ensemble stacked generalization* (ESG) approach (Ullah et al., 2021), through the *JARI* dataset (Ullah et al., 2021) shows better results than the use of its individual base models to predict the EV energy consumption. Recent models using *gradient boosted regression tree* (GBRT) have combined *extreme gradient*

*boosting* (XGBoost) and *light gradient boosted machine* (LightGBM) to provide better predictive performance from these ensemble methods (Zhao et al., 2020) with the NDANEV dataset. This approach classifies four driving patterns from three parameters (speed, motor current, and change rate of motor current), through K-means clustering algorithm and thus influencing the resulting eRange due to their different energy consumption rates.

The use of unsupervised clustering approaches by *self-organizing maps* (SOM) (Kohonen, 2001) have been addressed to cluster big data into driving patterns, prior to range estimation (Lee and Wu, 2015). The hybrid version of SOM with *regression tree* (RT) (Hastie et al., 2009) has taken advantage of SOM's neurons storage feature of nearing related neighbor information being kept closely together. Therefore, avoiding bushy trees and improving upon previous solutions by keeping meaningful knowledge extraction (Zheng et al., 2016) both approaches used different datasets from undisclosed monitored data sources.

Reinforcement learning has also been used for external energies disturbances on the speed profile of a driving profile so that it could then be combined with *multiple linear regression* (MLR) for the estimation (De Cauwer et al., 2017), using *EVteclab's* dataset. Although more complex than previous statistical-based approaches, the use of ML for eRange estimation reduces the error, and thus further justifying its use in this paper.

## 3 PROPOSED APPROACH

In this section, we detail the approach and the methodology that we have followed on this work. Figure 3 depicts the generic diagram of the approach in which we highlight that the ultimate goal is to provide the eRange estimation from the data in the input dataset, using ML techniques.

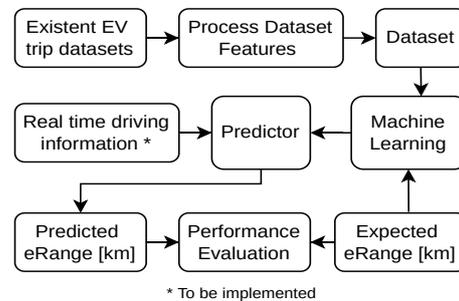


Figure 3: The detailed steps of the proposed approach with ML to estimate the eRange value, from a EV dataset.

### 3.1 Dataset Construction

As this work focuses on a relatively recent field of study, the dataset availability is both scarce and divergent, thus yielding the need to perform dataset construction and preprocessing phases. A dataset was created from historical traffic data with personally recorded vehicle trips, as well as external existing and publicly available datasets from both the *VED*, *Classic EV X* (Coutinho, 2021b) and *ChargeCar* datasets, integrated into our dataset. The resulting dataset contains multiple trips with their respective vehicle speed (in km/h), distance (in km) battery information such power consumption (in kW), current (in amps) and state of charge (in %) on a time series format.

The composed dataset is used to train the selected eRange prediction models on the learning phase through ML, allowing it to fit its eRange estimation for each trip on the dataset. Figure 4 shows the dataset construction phase.

The key reasons for building such a dataset are as follows. When training a ML model for regression problems, the accuracy of the results on test data will depend on the diversity of the data. To ensure model effectiveness on different vehicles and to avoid over-fitting, we opted for a diverse EV model dataset built from existing available datasets, mentioned in Table 1.

The algorithm integrates EV trip datasets for training, thus requiring EV trips time-series with the following features: SoC (in percentage), power consumption (in kWh), distance (in km) and speed (in km/h). We also have vehicle information: AEC (kWh), FBE (kWh), and FBD (km). For this reason, both *VED*, *Classic EV X* and *ChargeCar* datasets were selected.

The trip type and the minimum driving time are two variables found to influence ML methods performance. On the preprocessing phase, some features such as AEC, FBE, and FBD are sometimes missing on certain datasets. These features can be obtained from existing static EV information datasets such as <https://ev-database.org>. Other features such as acceleration and distance, are trip dependent being computed with mathematical formulas.

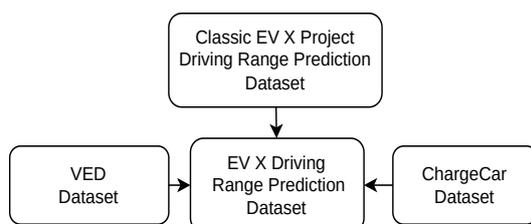


Figure 4: Dataset construction and preparation.

The constructed dataset is mainly composed by short vehicle trips with less than 20 minutes, with 457 out of 503 trips (90.9%) fitting in this category. The dataset is available at (Albuquerque, 2022).

This disparity in the training data could cause imprecise prediction on longer trips where different consumption profiles are observed, such as traveling on a highway. Another version of the dataset to be implemented in the future should contain longer EV trips, as well as the eMini project (Coutinho, 2021a) integration, for newer trip monitoring.

### 3.2 Learning the Models

The target (expected/baseline) eRange values are provided by an implementation of the HBA algorithm (Coutinho, 2021b), since it is not possible to obtain actual range values. Over the dataset, we apply this approach to compute the target eRange values  $y_i$ . This approach addresses real-time AEC values, that relies on the vehicle's past  $N = 10$  minute window of the trip's energy consumption history as well as the real-time SoC value. HBA was designed as a better alternative to BA, which was also included as a benchmark algorithm.

### 3.3 Regression Techniques

In this paper, we have considered the following regression techniques: *linear regression* (LR) (Hastie et al., 2009); *ensemble stacked generalization* (ESG) (Ullah et al., 2021).

LR is a well-known statistical technique (Hastie et al., 2009), such that it models the relationship between a scalar response and one or more independent variables. In this case, we have multiple linear regression, since we deal with several input variables and one output variable. The relationships between the input and output variables are modeled using linear predictor functions, whose unknown model parameters are estimated from the data.

The ESG algorithm follows the Wolpert stacking technique (Wolpert, 1992), combining two models. The first one, named as base-model (Level-0) encompasses DT, RF, and KNN classifiers. The second model (Level-1) is *adaptive boosting* (AdaBoost), combining base model predictions to provide a single output.

The ESG model follows the original (Ullah et al., 2021) implementation with some differences. The original application was the EV energy consumption prediction and not eRange. Moreover, the lack of availability of its *JARI* dataset could make this implementation's accuracy differ when training with

our dataset. An additional ESG implementation named *ESG\** was derived from the original ESG approach, changing some configurations to better fit the project’s constructed dataset. The maximum number of features configured for DT and RF algorithms are 9 and 7, respectively. As for the KNN, we set  $K = 7$  neighbors, the distance metric is *minkowski* with parameter  $p$  set to 1. Figure 5 depicts the ESG model.

After the training of these ML algorithms, they are used for the prediction of eRange. One of the predictors is then selected based on its performance with standard metrics. Then, it can be used for future execution on a real-time trip.

## 4 EXPERIMENTAL EVALUATION

In this section, we report on the experimental evaluation of our approach. First, we present the evaluation metrics considered in this work. Then, we report on experimental results on the built dataset.

### 4.1 Standard Evaluation Metrics

After training the ML algorithms with the dataset, we perform eRange estimation. The resulting prediction is then used for the computation of the evaluation metrics so that it can be compared with other algorithms.

As the estimation accuracy must be measured for each eRange estimation algorithm, five standard evaluation metrics were chosen for this task: *mean absolute error* (MAE), *mean squared error* (MSE), *mean absolute percentage error* (MAPE), *root mean squared error* (RMSE), and  $R^2$  metric, which is the coefficient of determination (Wright, 1921). These evaluation metrics are employed in the *k*-fold *cross validation* (CV) of the selected testing trip, minimizing the presence of bias.

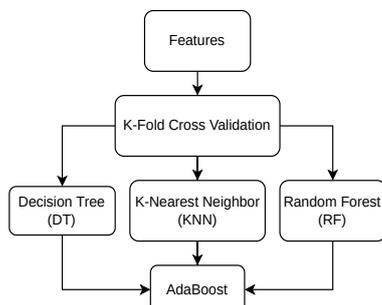


Figure 5: Ensemble Stacked Generalization (ESG) model (Ullah et al., 2021).

## 4.2 Experimental Results

The experiments were carried out on a computer with the Manjaro Linux operating system, 5.18.19-3-MANJARO kernel, AMD Ryzen 9 3900X (24) @3.800 GHz and 48 Gb of RAM. The Python runtime version is 3.9, using JetBrains’ Pycharm as the *integrated development environment* (IDE).

The constructed dataset holds multiple EV trips, most of them being short city commutes, which differ in consumption of traveling in highways on longer trips. This can cause training bias with worse predictions on longer trips due to the reduced samples in the training data. To study this effect, a longer 47 minutes Nissan Leaf 2013 model EV trip was chosen from the VED dataset (Oh et al., 2019) for testing, while the remaining trips were used for training, defining a *minimum trip time* (MTT) required for a trip to be included into the training set.

We have considered  $MTT \in \{0, 10, 20, 30, 40\}$ . The number of trips available for training decreases, as the MTT value increases. The eRange prediction will be calculated for the selected test trip. We report the time and evaluation metrics for the *k*-fold CV results, with  $k = 20$  folds.

We compute different eRange estimation results for the selected trip and estimation algorithms, providing an easy overview of the different dataset parameters, with multiple datasets.

Figures 6 and 7 present the eRange prediction from the BA, HBA (the ML baseline), LR, ESG and *ESG\** algorithms (in blue, red, purple, green, and light blue, respectively) for  $MTT = 0$ . The heuristic approaches provide similar estimates of the eRange values. On the 12 minutes to 20 minutes time window, HBA yields a stable estimation, with segments such that the minimum instance energy is not enough to trigger a recalculation for the eRange while the BA counterpart provides a continued decreasing estimate.

On ML approaches, LR provides a smoother prediction evolution, while the ESG method attains estimates with larger deviation and variance. This could be the result of DT having high sensitivity to the training data, as our dataset contains a larger number of smaller EV trips with different consumption profiles than of longer highway trips. The *ESG\** which re-

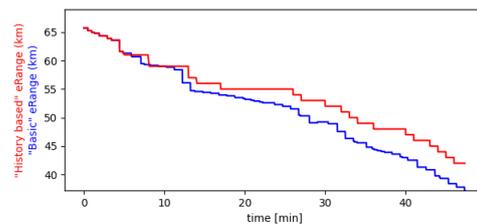


Figure 6: eRange estimation with BA and HBA algorithms.

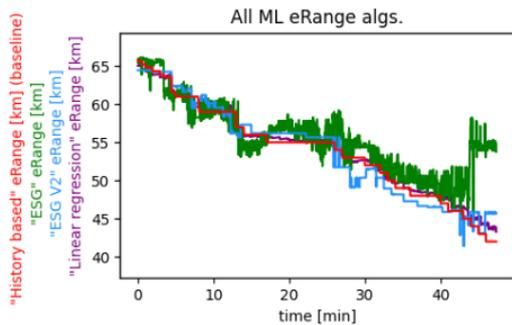


Figure 7: eRange estimation by the HBA (ML baseline), LR, ESG, and ESG\* algorithms.

sulted from a better configuration to our dataset has yielded a better predictive accuracy than the original model. These estimates can be smoothed with a moving-average filter applied to the sequence of ESG estimated values.

The test trip prediction metrics for the ML algorithms are reported on Table 2, and the CV metrics are presented on Table 3.

Table 2: LR and ESG metrics for all MTT. For each MTT value (in minutes), the best result is in bold face.

ML	MTT	MAE ↓	MSE ↓	MAPE ↓	RMSE ↓	R <sup>2</sup> ↑	Time (m,s,ms)
LR	0	<b>0.63</b>	<b>0.63</b>	<b>0.01</b>	<b>0.79</b>	<b>0.98</b>	<b>(0,0,138)</b>
ESG	0	2.61	17.17	0.05	4.14	0.56	(7,25,772)
ESG*	0	1.20	2.31	0.02	1.52	0.94	(14,10,940)
LR	10	<b>0.59</b>	<b>0.60</b>	<b>0.01</b>	<b>0.77</b>	<b>0.98</b>	<b>(0,0,72)</b>
ESG	10	2.31	12.13	0.04	3.48	0.68	(4,2,146)
ESG*	10	1.51	3.65	0.02	1.91	0.90	(7,37,998)
LR	20	<b>0.58</b>	<b>0.58</b>	<b>0.01</b>	<b>0.76</b>	<b>0.98</b>	<b>(0,0,29)</b>
ESG	20	3.88	30.72	0.07	5.54	0.21	(1,33,534)
ESG*	20	2.18	7.52	0.04	2.74	0.80	(2,52,129)
LR	30	<b>0.70</b>	<b>0.78</b>	<b>0.01</b>	<b>0.88</b>	<b>0.98</b>	<b>(0,0,14)</b>
ESG	30	9.28	142.91	0.17	11.95	-2.66	(0,41,343)
ESG*	30	4.66	37.70	0.08	6.14	0.03	(1,11,669)
LR	40	<b>0.90</b>	<b>1.47</b>	<b>0.01</b>	<b>1.21</b>	<b>0.96</b>	<b>(0,0,6)</b>
ESG	40	7.17	95.45	0.13	9.77	-1.44	(0,9,706)
ESG*	40	5.11	31.93	0.10	5.65	0.18	(0,15,505)

For both tables, as MTT values increase we observe a decrease on the training time. The LR algorithm training is always faster than ESG and ESG\* training. Moreover, LR achieves the best metric values.

Table 3: LR and ESG metrics for all MTT, with CV. For each MTT value (in minutes), the best result is in bold face.

ML	MTT	MAE ↓	MSE ↓	MAPE ↓	RMSE ↓	R <sup>2</sup> ↑	Time (h,m,s,ms)
LR	0	<b>0.53</b>	<b>0.72</b>	<b>0.34</b>	<b>0.80</b>	<b>0.99</b>	<b>(0,0,30,64)</b>
ESG	0	1.47	4.72	1.15	2.10	0.99	(4,3,54,919)
ESG*	0	1.27	2.99	1.10	1.67	0.99	(6,50,52,398)
LR	10	<b>0.69</b>	<b>1.07</b>	<b>0.48</b>	<b>0.98</b>	<b>0.99</b>	<b>(0,0,14,543)</b>
ESG	10	1.68	5.83	1.31	2.28	0.98	(1,57,29,701)
ESG*	10	1.33	3.34	1.05	1.77	0.99	(3,22,59,269)
LR	20	<b>0.94</b>	<b>1.80</b>	<b>0.67</b>	<b>1.26</b>	<b>0.98</b>	<b>(0,0,3,805)</b>
ESG	20	2.39	12.41	1.74	3.23	0.93	(0,41,38,272)
ESG*	20	1.71	5.42	1.36	2.21	0.96	(1,14,30,373)
LR	30	<b>1.16</b>	<b>2.80</b>	<b>1.04</b>	<b>1.46</b>	<b>0.93</b>	<b>(0,0,1,143)</b>
ESG	30	3.80	30.43	3.03	4.69	0.19	(0,18,14,883)
ESG*	30	2.83	14.02	2.47	3.39	0.51	(0,30,39,978)
LR	40	<b>1.55</b>	<b>5.15</b>	<b>1.48</b>	<b>1.91</b>	<b>-1.61</b>	<b>(0,0,0,230)</b>
ESG	40	3.26	25.78	2.91	4.17	-6.44	(0,5,26,732)
ESG*	40	2.87	14.41	3.01	3.43	-6.88	(0,8,40,895)

As the ML approaches were trained with HBA as the baseline eRange target, future integration with the eMini project would supply the algorithms with real eRange, improving their prediction accuracy over time.

## 5 CONCLUSIONS

The electric vehicle driving range estimation is a relevant problem, since this estimate relieves the driver anxiety on a trip and allows for a better trip planning. There are some useful heuristic approaches to perform this estimation. However, these techniques provide an estimate with some degree of error, which may alarm the driver. Machine learning techniques to provide this estimation have been proven adequate, despite being applied to a recent field of study. There are some public domain datasets with electric vehicle data, but their use is not straightforward, requiring a demanding construction and pre-processing stage for a reliable dataset with accurate and complete trip data.

In this paper, we have composed such a dataset in which we have assessed the use of regression techniques to estimate the driving range, based on different variables with vehicle data and trip data. The experimental results have shown the impact of different training configurations, on existing machine learning models. We have compared the prediction accuracy of these techniques with standard metrics and found that the linear regression technique shows promising prediction results as well as fast training. This model can be deployed on-board of a vehicle as it aims to be integrated with the eMini project (Coutinho, 2021a). The source code is available on the Github (Albuquerque, 2022), incentivising reproducibility on further studies.

### 5.1 Future Work

As future work, we plan to perform the integration of the developed application with the real-time data of the electric vehicle, continuously providing updated eRange estimations. The base model will be the one provided by the linear regression technique. We also plan to include more datasets and features, such as driving patterns and road elevation. The fine-tuning of the ESG\* parameters and results also deserves more attention. Moreover, additional machine learning techniques can be added to the established open source experimental setting.

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