Explainable Outlier Detection Using Feature Ranking for k-Nearest Neighbors, Gaussian Mixture Model and Autoencoders

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Abstract: Outlier detection is the process of detecting individual data points that deviate markedly from the majority of the data. Typical applications include intrusion detection and fraud detection. In comparison to the well-known classification tasks in machine learning, commonly unsupervised learning techniques with unlabeled data are used in outlier detection. Recent algorithms mainly focus on detecting the outliers, but do not provide any insights what caused the outlierness. Therefore, this paper presents two model-dependent approaches to provide explainability in multivariate outlier detection using feature ranking. The approaches are based on the k-nearest neighbors and Gaussian Mixture Model algorithm. In addition, these approaches are compared to an existing method based on an autoencoder neural network. For a qualitative evaluation and to illustrate the strengths and weaknesses of each method, they are applied to one synthetically generated and two real-world data sets. The results show that all methods can identify the most relevant features in synthetic and real-world data. It is also found that the explainability depends on the model being used: The Gaussian Mixture Model shows its strength in explaining outliers caused by not following feature correlations. The k-nearest neighbors and autoencoder approaches are more general and suitable for data that does not follow a Gaussian distribution.

1 INTRODUCTION

Outlier detection was first introduced in the late 60s in order to detect and often remove possible incorrect instances from a data set. Grubbs (1969) was the first to introduce the term outlier and he also defined it as an outlying observation that appears to deviate markedly from other members of the sample in which it occurs.

Today, the reason for performing outlier detection is very different: The goal is mainly to identify the outliers or anomalies in the data, since they can be of great interest in various application scenarios. For example, in intrusion detection, attackers or compromised machines in computer networks can be found. When applied on financial or transaction data, fraudulent records such as credit card fraud can be identified. Sometimes, outlier detection is also called anomaly detection, novelty detection, or has a specific name based on the application scenario (fraud detection, intrusion detection).

Furthermore, outlier detection can be performed in a supervised, a semi-supervised or an unsupervised setting. The latter is by far the most relevant scenario since outliers are often not available for training in ad-

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Other approaches are based on probabilities and assume that normal data can be represented as a stochastic model. The underlying principle of these statistical-based outlier detection techniques is that an outlier is an observation that is suspected of being partially or totally incorrect because it is not generated by the stochastic model assumed (Anscombe, 1960; Chandola et al., 2009). Statistical-based algorithms fit a model using the given data first and then apply a statistical inference test to determine whether or not an instance belongs to that model. Instances that have a low probability of being generated by the learned model are considered as outliers. A prominent approach here is the Gaussian Mixture Model (GMM), which represents the underlying data distribution with a fixed number of Gaussian distributions (called components).

Besides the two groups, Chandola et al. (2009) further categorizes outlier detection algorithms into clustering-based and classification-based. The latter category also contains autoencoder neural networks, which will be used in this work as a third algorithm. All of the categories have today in common that state-of-the-art algorithms focus on detecting the outliers and do not provide insights about what led to the outlier decision. These insights often have to be determined by experts manually by analyzing the outliers in order to determine their root cause. In practice, this is often a challenging task since the causes of outliers are complex and even often hidden in multiple dimensions. Furthermore, detailed domain knowledge is often required by the experts. Therefore, this paper proposes a method for providing explainability of the k-NN and GMM algorithms for outlier detection. The basic idea is to rank each individual dimension depending on its influence on the detected outliers by analyzing the distances per dimension based on the learned model. The goal is to support the experts while analyzing the outliers by presenting the dimensions that need to be examined more closely in order to identify the cause or causes of the outlier.

2 RELATED WORK

2.1 k-Nearest Neighbors Outlier Detection Algorithm

The global k-NN approach, often simply referred to as k-NN, is a distance-based outlier detection approach that uses the assumption that outliers occur far away from their closest neighbors in comparison to normal instances. As described by Goldstein and Uchida (2016), this approach detects outliers by first calculating the k nearest neighbors for every data point in the data set. Afterwards, the outlier score is computed by either using the distance to the kth nearest neighbor (a single one) (Ramaswamy et al., 2000) or the average distance to all k nearest neighbors (Angiulli and Pizzuti, 2002). The second approach is used in the following. Here, the average Euclidean distance for a given point \( q \) to the k-nearest neighbors set \( N = \{ n^1, n^2, \ldots, n^k \} \) is calculated in the \( d \)-dimensional space:

\[
\text{dist}(q, N) = \frac{1}{k} \sum_{j=1}^{k} \sqrt{\sum_{i=1}^{d} (q_i - n_{ij})^2}
\]

The choice of the parameter \( k \) is crucial for the results. If it is too small, the local density estimate might not be reliable. On the other hand, the density estimate may be too coarse and thus outliers not found if it is selected too large.

Several publications exist, in which this approach is used for outlier detection. Amer and Goldstein (2012) evaluated different distance-based outlier detection approaches including k-NN for anomaly detection on three different data sets. The authors found that this approach performs especially well in detecting global outliers.

2.2 Using a Gaussian Mixture Model for Outlier Detection

A mixture model is a collection of probability distributions or densities \( C_1, \ldots, C_k \) and mixing weights or proportions \( w_1, \ldots, w_k \), where \( k \) is the number of component distributions (Lindsay, 1995; McLachlan and Peel, 2000).

Therefore, the mixture model \( P \) is a probability distribution of the data based on a mixture of multiple component distributions and their corresponding mixing weights and is given as (Baxter, 2017):

\[
P(x|C_1, \ldots, C_k, w_1, \ldots, w_k) = \sum_{j=1}^{k} w_j P(x|C_j)
\]

For the GMM, the probability distribution \( C \) is given by the Gaussian distribution \( C = \mathcal{N}(\mu, \sigma^2) \) in the one-dimensional case with a mean of \( \mu \) and variance of \( \sigma^2 \). In the multidimensional case, \( C \) is given by the multivariate Gaussian distribution \( C = \mathcal{N}(\mu, \Sigma) \) with a mean vector of \( \mu \) and the covariance matrix of \( \Sigma \).

\[
P(x|\theta) = \sum_{j=1}^{k} w_j P(x|\mathcal{N}(\mu, \Sigma))
\]

To estimate the parameters \( \theta = (w, \mu, \Sigma) \) of the components, the expectation maximization (EM) algorithm
introduced by Dempster et al. (1977) is applied. This algorithm aims to estimate the parameters \( \theta \) in such a way that they maximize the joint probability of the data set by solving the following optimization problem:

\[
\arg\max_\theta P(X|\theta) = \arg\max_\theta \prod_i P(x_i|\theta)
\]

\[
= \arg\max_\theta \prod_i \left( \sum_{j=1}^k w_j P(x_i|\mathcal{N}(\mu_j, \Sigma_j)) \right)
\]

In practice, GMMs are used in several unsupervised learning setups, e.g., density estimation, model-based clustering and outlier detection. In the latter, the estimated likelihood or, due to computational reasons, the log-likelihood per data point is then used as an outlier score.

### 2.3 Autoencoder for Outlier Detection

An autoencoder (AE) is a neural network trained in a specific way in order to learn reconstructions that approximate the original input (Goodfellow et al., 2016, p.499). An AE consists of two parts, an encoder and a decoder part. An AE with a single hidden layer could be represented by the following equations, where \( w, \hat{w}, h, \hat{h}, b, \hat{b} \) are the weights and biases of the encoder and decoder and \( \sigma, \tilde{\sigma} \) are the activation functions (An and Cho, 2015):

\[
h = \sigma(wx + b)
\]

\[
\hat{x} = \tilde{\sigma}(\hat{w}h + \hat{b})
\]

Equation 5 describes the encoder step, mapping an input vector \( x \) to a hidden representation \( h \) by an affine mapping following an activation function. Equation 6 shows the decoder step, reconstructing the hidden representation \( h \) back to the original input space by the same transformation as the encoder. The difference between the input vector \( x \) and the reconstructed output \( \hat{x} \) in the \( d \) dimensional space, described in Equation 7, is called the reconstruction error. As a metric, the mean absolute error (MAE) or the mean squared error (MSE) is often used to calculate the reconstruction error. During the training, the AE learns to minimize the reconstruction error by using backpropagation and stochastic gradient descent.

Due to the usage of a non-linear activation function, the AE is capable of learning non-linear relationships. Using the hidden representation of an AE as an input to another one makes it possible to stack AEs, also known as deep autoencoder. To force a compressed representation in the hidden layers, the number of units in the hidden layers is subsequently reduced. This introduces a bottleneck that forces the AE to learn the most relevant features and relationships of the data. Hawkins et al. (2002) first used this concept for the task of outlier detection. The key idea is that during training, the weights of the AE are adjusted to minimize the reconstruction error for all training patterns. As a result, frequent patterns are more likely to be well reproduced by the trained AE, so the patterns that represent outliers are less well reproduced and have a higher reconstruction error. The reconstruction error is then used as the outlier score.

### 2.4 Explainability in Outlier Detection

To understand explainability within the context of outlier detection, first a definition in the wider area of artificial intelligence (AI) is reviewed. Explainability in AI (XAI) refers to the concept of being able to understand the machine learning model. This is often crucial since the underlying machine learning algorithms construct complex models which are often opaque to humans (Burkart and Huber, 2020) and appear as black box models. It is important to stress that it aims to explain causal effects in the model and not casual effects in the domain (Herskind Sejr et al., 2021). The focus towards XAI is currently in the context of supervised learning. However, also in the field of unsupervised learning, the principles of XAI are applicable. We believe that the widespread application of unsupervised outlier detection in practice is still behind due to missing confidence and trust. In particular, the algorithms lack of association between detected outliers and their root causes. This is especially relevant for multivariate outlier detection: Here, outliers are often complex situations, where causes are hidden in multiple dimensions. It is difficult to identify them without additional insights.

Explainability in outlier detection has just recently gained importance. In comparison to other sub-areas of AI, only limited work on this topic is available. However, a summary of the current state of this topic is provided by Panjei et al. (2022) and Sejr and Schneider-Kamp, who refer to the topic of explainable outlier detection with the term XOD.

In this work, we present two approaches that provide a weight vector as output, which can be interpreted as feature ranking and is intended to provide an explanation of which features are most important according to the used outlier detection algorithm.
3 EXPLAINABLE OUTLIER DETECTION

3.1 Explainable k-Nearest Neighbors Outlier Detection

For the k-NN approach, we propose an outlier explanation by ranking individual dimensions accordingly to how strongly they contribute to the detected outlier. This is achieved by computing the average Euclidean distance per dimension $d$ for an outlier point $q$ to the $k$-nearest neighbors set $N$ as described in Equation 8:

$$\text{dist}_d(q, N) = \frac{1}{k} \sum_{j=1}^{k} |q_d - n^j_d| \forall d$$

As it is well-known for $k$-NN outlier detection, the results of the described dimensional ranking are strongly dependent on the parameter $k$.

Figure 1 shows the outcome for different values of $k$ in a two-dimensional space. Here, the solid green and dashed black lines visualize the mean distance of the $X$ and $Y$ dimension of two selected outliers $q_1$ and $q_2$. On the left-hand side, it can be seen how this approach behaves for small values of $k$. Dimensions that have large deviations to the nearest, more dense area result in a larger distance. This indicates which dimension would have to be shifted to get to a more dense area (e.g. causing the outlier). However, on the right-hand side, it can be seen that the average distance per dimension approaches the global average indicated by the red dot for large values of $k$.

This approach is later used to assess the influence per dimension on the outlier and therefore to provide an explanation of why a particular instance was detected as an outlier.

An example of how this feature ranking behaves on a data set generated from two Gaussian distributions is visualized in Figure 2. On the left, the Mahalanobis distance per dimension of the outliers $q_1$ to the best fitting component $C_1$, and $q_2$ to the component $C_2$ is presented for the $X$ and $Y$ dimension. A GMM with $k=2$ is fitted to the data. Both outliers show a larger Mahalanobis distance on the $Y$ dimension than on the $X$ dimension. This is because they are both close to the mean of their best-fitting component on the $X$ dimension. However, on the $Y$ dimension, they are both off. Therefore, this is used as an indication that the $Y$ dimension is mainly causing the outlier. Also, the outlier $q_2$ shows a larger Mahalanobis distance on the $Y$ dimension than $q_1$, even though the difference on this dimension to the mean of the best-fitting component is larger for $q_1$. This presents the difference of the Mahalanobis distance in comparison to the Euclidean distance. It also considers the variance per dimension and thus results in a larger distance of $q_2$ to $C_2$ on dimension $Y$ in comparison to $q_1$ to $C_1$.

3.2 Explainable Gaussian Mixture Model Outlier Detection

To enable explanations for the GMM model, also a ranking of individual dimensions accordingly to how strongly they contribute to the outlier is proposed. Since the data is described by a finite set of Gaussian components, the Mahalanobis distance is used. Therefore, for an outlier $q$, the vector $\vec{m}$ is calculated, representing the Mahalanobis distances for each dimension to the best fitting component $C$ (cf. Equation 9). This is obtained by replacing the dot product of the Mahalanobis distances equation with the element-wise product. From the resulting vector, the element-wise absolute values are taken to eliminate negative values. $C$ is chosen based on which component maximizes the log-likelihood for the data point $q$.

$$\vec{m} = \sqrt{\left((q - \mu_C)\Sigma^{-1} \circ (q - \mu_C)\right)}$$

An example of how this feature ranking behaves on a data set generated from two Gaussian distributions is visualized in Figure 2. On the left, the Mahalanobis distance per dimension of the outliers $q_1$ to the best fitting component $C_1$, and $q_2$ to the component $C_2$ is presented for the $X$ and $Y$ dimension. A GMM with $k=2$ is fitted to the data. Both outliers show a larger Mahalanobis distance on the $Y$ dimension than on the $X$ dimension. This is because they are both close to the mean of their best-fitting component on the $X$ dimension. However, on the $Y$ dimension, they are both off. Therefore, this is used as an indication that the $Y$ dimension is mainly causing the outlier. Also, the outlier $q_2$ shows a larger Mahalanobis distance on the $Y$ dimension than $q_1$, even though the difference on this dimension to the mean of the best-fitting component is larger for $q_1$. This presents the difference of the Mahalanobis distance in comparison to the Euclidean distance. It also considers the variance per dimension and thus results in a larger distance of $q_2$ to $C_2$ on dimension $Y$ in comparison to $q_1$ to $C_1$.
This approach is again highly dependent on the parameter \( k \) of the GMM. When choosing \( k \) to large, the GMM tends to learn low-weighted components which describe the outliers. This is contrary to the idea of using the best-fitting components, since here the best-fitting component is distorted by the outlier. The right plot visualizes this behavior where a GMM with \( k = 3 \) is fitted on the data, whereas the low-weighted component \( C_3 \) with a weight factor of \( w = 0.03 \) is distorted due to the outlier \( q_2 \). To avoid such a situation, the parameter \( k \) should be chosen large enough to sufficiently describe the normal data but low enough to prevent overfitting on the outliers. Another solution could also be to ignore low-weighted components.

### 3.3 Explainable Outlier Detection for Autoencoders

To explain how much each dimension contributed to the detected outlier using an AE, the reconstruction error per dimension between the input vector \( \hat{x} \) and the reconstructed output \( \hat{\hat{x}} \) is used. The assumption is, that in case certain dimensions show a higher reconstruction error than other dimensions, they are more likely to deviate from their usual distribution. This idea was introduced by Antwarg et al. (2019) using a similar approach for explaining the outcome of an AE for anomaly detection.

### 4 EVALUATING EXPLAINABLE OUTLIER DETECTION ALGORITHMS

To assess the effectiveness and compare the outcomes of the presented approaches, an evaluation using a synthetically generated data set and two real-world data sets Wine Quality and KDD-HTTP-Cup are used. The source code for this evaluation is publicly available on GitHub\(^1\). Although outlier detection is done in practice using unsupervised learning, the hyperparameters per data set are listed in Table 1 and were selected by hyperparameter tuning based on the maximization of the AUC of the ROC curve. This was done to ensure that the selected methods are suitable for outlier detection on the used datasets in the first place. Since the focus of this work is on how these approaches are explaining outliers, it requires that outliers are detected reliably. Furthermore, only true positive detected outliers were used for further analysis.

#### Table 1: Hyperparameters for the approaches applied on the synthetic, wine quality and KDD-Cup99 data set.

<table>
<thead>
<tr>
<th>Approach</th>
<th>Hyperparameter</th>
<th>Values (Synthetic)</th>
<th>Values (Wine quality)</th>
<th>Values (KDD-Cup99)</th>
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<td>20-22-22-20</td>
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<tr>
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<td>Batch Size</td>
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</table>

#### Figure 3: ROC-AUC of the different methods on the wine quality data set (left) and the KDD-Cup99 data set (right).

### 4.1 Synthetic Data Set

The synthetic data set consists of 2,000 6-dimensional data points sampled from two Gaussian distributions \( \mathcal{N}(\mu_1, \Sigma_1) \) and \( \mathcal{N}(\mu_2, \Sigma_2) \) where the elements of the vector \( \mu_1 \) are all set to 0 and for the covariance matrix \( \Sigma_1 \) the diagonal is set to 1 and all other elements are set to 0.9. The elements of the vector \( \mu_2 \) are all set to 12 and for the covariance matrix \( \Sigma_2 \) the diagonal is set to 1 and all other elements are set to 0.3. Then, the four outliers \( q_1 \ldots q_4 \) were introduced by shifting the point in the first two dimensions while keeping the last four dimensions. The resulting data set is visualized in Figure 4. Here it can clearly be seen that the data set consists of two clusters and the four outliers are only observable in the projection of the first two dimensions.

The methods presented are applied to the synthetic data set. Afterwards, the feature ranking of the outliers are calculated. For a better comparison, the results are scaled into a common interval of [0, 1]. The feature rankings are visualized in Figure 5. It can be seen that all three approaches identified either the first dimension (D1), the second dimension (D2) or both as important for detecting the outlier.

In addition to identify the important features, the feature ranking can also be interpreted as a distance per dimension. This provides information about the direction in which the point would have to be moved to reduce the outlier score. For example, in Figure 6 the outlier \( q_3 \) including the feature ranking given by the different approaches is visualized in the dimensions D1 and D2. On the left, the distance to the \( k \)
features are the root causes and should be most important for identifying the outliers (red wine) within the data set was collected for classification or regression. As a first real-world data set, a modified version of the SYN10 is applied on this data set. All three approaches achieved an AUC-ROC of over 96% as visualized in Figure 3 (left). This means, overall the approaches are suitable to detect the outliers. Therefore, the presented explainability approaches are applied to explain the outliers using feature ranking. For every approach, first the relevant features of the data set causing outliers are identified. For this purpose, the feature ranking for all three approaches across all outliers are summed up, and scaled into a common range of [0, 1]. The results are visualized in Figure 7. As can be observed all three approaches detect the feature total sulfur dioxide as the most relevant followed by the features fixed acidity, volatile acidity and sulphates.

Figure 4: Synthetic data set consisting of 2,000 6-dimensional data points sampled from two Gaussian distributions including four outliers in the first two dimensions.

Figure 5: Feature ranking for the introduced outliers over all 6-dimensions for the three approaches scaled into the common range of [0, 1].

Figure 6: Feature Ranking for the dimensions D1 and D2 for the outlier q1. The outlier is mainly caused by D1.

4.2 Wine Quality Data Set

As a first real-world data set, a modified version of the wine quality UCI data set (Cortez et al., 2009) is used. The data set describes the physicochemical properties of the red and white variants of the Portuguese "Vinho Verde" wine by 11 continuous features. Initially, the data set was collected for classification or regression tasks. For the task of outlier detection, the data set was modified: The class white wine is used as the normal class. The class red wine is down-sampled to 50 instances representing the outliers. This results in a data set containing 4821 normal instances and 50 outliers with an outlier rate of approx. 1.03%.

The presented algorithms are also applied on this data set. All three approaches achieved an AUC-ROC of over 96% as visualized in Figure 3 (left). This means, overall the approaches are suitable to detect the outliers. Therefore, the presented explainability approaches are applied to explain the outliers using feature ranking. For every approach, first the relevant features of the data set causing outliers are identified. For this purpose, the feature ranking for all three approaches across all outliers are summed up, and scaled into a common range of [0, 1]. The results are visualized in Figure 7. As can be observed all three approaches detect the feature total sulfur dioxide as the most relevant followed by the features fixed acidity, volatile acidity and sulphates.

Figure 7: Wine Quality data set: Summed-up feature ranking of the outliers (red wine) over all 6-dimensions for the three approaches scaled into the common range of [0, 1].

Recalling the insights from the experiment, these features are the root causes and should be most important for identifying the outliers (red wine) within the
normal instances. Therefore, we try to verify the results by additionally using the class labels of the data set in a plot. Figure 8 visualizes the density estimation of the outlier (red wine) and regular (white wine) for the top four features. It can be seen that especially the feature total sulfur dioxide clearly separates the outlier and normal instances. The other three features also show large areas of non-overlap in the density estimation, but there is also a certain overlap where these features are not sufficient to distinguish between outliers and normal instances.

Figure 8: Density estimation for the top 4 features for the outliers (red wine) and normal instances (white wine).

Additionally, the feature ranking is also suitable for analyzing and explaining single outliers. As shown in Figure 7, the feature total sulfur dioxide is the most dominant feature overall. However, when analyzing individual outliers, it can be seen that in a few cases there are differences in what the second most important features is, depending on the approach chosen. In concrete terms, this behavior can be observed for outliers, such as the one shown in Figure 9. Here, the feature ranking is visualized for a single outlier. It can be seen that the k-NN approach considers the feature volatile acidity and the AE the feature citric acid as the second most important feature (cause). The GMM approach even ranks the feature alcohol above the feature total sulfur dioxide.

Figure 9: Wine Quality data set: Feature ranking for a single outlier over all 6-dimensions for the three approaches scaled into the common range of [0, 1].

This shows that the feature ranking is model dependent and therefore does not provide a general explanation. An example of this is visualized in Figure 10. Here we can see that both, the AE and k-NN approaches, rank the features with the largest Euclidean distance the highest. The correlation between certain features does not seem to have any effect in this situation. The GMM approach, however, learns a component that represents the negative correlation between the feature total sulfur dioxide and the feature alcohol. The outlier under consideration deviates from this correlation, which results in a larger Mahalanobis distance. In summary, the presented approaches are suitable to identify the most relevant features to distinguish outliers and normal instances. Furthermore, it is possible to explain a single outlier in terms of which features are decisive for the model to identify it as an outlier. Using the wine quality data set, these approaches show which features are most important in distinguishing white wine from the few outlier instances representing red wine. It also explains why certain instances are recognized as outliers by pointing out the features that deviate from the usual white wine features. Concerning the outliers, the feature ranking does not explain the domain, but rather provides a model dependent explanation.

4.3 KDD-Cup99 HTTP Data Set

As a second real-world data set, a modified version of the KDD-Cup99 HTTP data set (Tavallaee et al., 2009) is used. Originally, this data set is used for benchmarking intrusion detection classification systems. It contains simulated normal and attack traffic on an IP level in a computer network environment in order to test intrusion detection systems. The dataset has been modified to serve as an outlier detection benchmark as well as described by Goldstein (2015). To serve for the purpose of outlier detec-
tion this data set uses HTTP traffic only and limits the outlier class to DoS attacks. Furthermore, the features protocol and port were removed since only HTTP traffic was used. Additionally, all categorical non-binary features were removed. This results in a larger data set containing 620,098 normal records and 1,052 outliers with an outlier rate of approx. 0.17%.

Similar to the previous data set, all outlier detection approaches achieved an AUC-ROC of over 98%, as visualized in Figure 3 (right), meaning the approaches are suitable for detecting the outliers. Again, it was analyzed which features are the most relevant root causes per approach for detecting the outliers. Figure 11 presents the summed-up and scaled feature ranking for all outliers contained in the data set. Interestingly, the summed up feature ranking is not as consistent between the different approaches as in the previous data sets. Overall, the feature same_srv_rate shows a high relevance by all three approaches. For the other features, there is no clear consensus on their importance. When analyzing the density estimation of the top features, presented in Figure 12, the feature same_srv_rate shows that for the regular class it is centered in a dense area whereas for the outlier class it shows a high variance. Therefore, data instances outside of this dense area are detected as outliers. The same can be observed for the feature src_bytes. Both features are considered most important by the GMM. However, as the second most important feature the k-NN identifies dst_host.count and the AE same_srv.diff_host_rate. The density estimation of these features shows, there is only a marginal difference and no clear separation between outliers and normal instances. It can be assumed that these features in relationship with the feature same_srv_rate are decisive for the identification of the outliers. This example shows again the basic premise of the approach: The feature ranking is algorithm dependent and different approaches achieve a different feature ranking.

The GMM models the data by a fixed number of multidimensional Gaussian distributions. Inspecting this data set carefully, it can be derived that it is difficult to be model by a GMM due to the nature of the underlying distributions. Therefore, this approach learns components with a high variance and a covariance that approaches 0. In terms of feature ranking, this means that the GMM particularly indicates features that deviate strongly from the global norm and are crucial for detecting global outliers. In this case the features src_byte and same_srv_rate. However, in comparison to that, the AE can also model non-linear relationships and is not bound to a Gaussian distribution of the data. Therefore it achieves a different feature ranking and ranks the feature srv_diff_host_rate as the second most important feature. Likewise, the k-NN is not bound to a specific distribution of the data due to its non-parametric functionality and ranks the feature dst_host.count as the second most important feature. In these cases, both approaches are also able to explain outliers which are not only identified by deviating from an underlying Gaussian distribution. In terms of feature ranking, this means that features are selected, which in combination uniquely explain the outliers. Therefore, the features srv_diff_host_rate and dst_host_count do not independently explain the outliers, but potentially in combination with other features e.g. same_srv_rate.

5 CONCLUSION AND OUTLOOK

This paper proposes two approaches enabling explainability for outlier detection based on feature ranking and thus support the root cause analysis of outliers. First, the Euclidean distance per dimension to the k-nearest neighbors for the k-NN algorithm and the Mahalanobis distance to the best fitting component estimated by the GMM was introduced to identify dimensions causing outliers. A third, already previously published algorithm, utilizes the reconstruction error of an autoencoder neural network to identify the features causing outliers was included for comparison as well.
To assess the effectiveness of these approaches, they were qualitatively evaluated in experiments on a synthetic data set and two real-world data sets, namely wine quality and KDD-Cup99 HTTP. The experiments showed that all three approaches are suitable for increasing the explainability of the outlier detection results by identifying the features which are most relevant for the algorithm to detect the outliers. Furthermore, it was found that the feature ranking results depend on the algorithm used. The GMM focuses strongly on linear relationships between the features and is particularly suitable when the data can be modeled by a fixed number of Gaussian components. If this is not the case (e.g. the underlying distribution is not a Gaussian distribution), the GMM neglects the relationship of different features to each other and tends to explain global outliers only. This leads to a feature ranking assuming independent features, which is often not the case. The AE approach can model by its non-linearity also various feature relationships. Likewise, the k-NN approach is not bound to linear relationships as well. This leads to a different feature ranking that is more helpful in general, especially if the underlying distribution is unknown.

Overall, all three approaches support the task of outlier analysis to better understand the results of the algorithms and explain the outliers. Since many other commonly used outlier detection algorithms are also distance- or probability-based, this work can serve as a basis for investigating further into the topic of explainable outlier detection using feature ranking.

REFERENCES


