Mechanism of Overfitting Avoidance Techniques for Training Deep Neural Networks

Bihi Sabiri¹¹^a, Bouchra El Asri¹^b and Maryem Rhanoui²^c

¹IMS Team, ADMIR Laboratory, Rabat IT Center, ENSIAS, Mohammed V University in Rabat, Morocco ²Meridian Team, LYRICA Laboratory, School of Information Sciences, Rabat, Morocco

- Keywords: Data Overfitting, Machine Learning, Dropout, Deep Learning, Convolutional Neural Network, Max Pooling, Early Stopping.
- Abstract: The objective of a deep learning neural network is to have a final model that performs well both on the data used to train it and the new data on which the model will be used to make predictions. Overfitting refers to the fact that the predictive model produced by the machine learning algorithm adapts well to the training set. In this case, the predictive model will capture the generalizable correlations and the noise produced by the data and will be able to give very good predictions on the data of the training set, but it will predict badly on the data that it has not yet seen during his learning phase. This paper proposes two techniques among many others to reduce or prevent overfitting. Furthermore, by analyzing dynamics during training, we propose a consensus classification algorithm that avoids overfitting, we investigate the performance of these two types of techniques in convolutional neural network. Early stopping allowing to save the hyper-parameters of a model at the right time. And the dropout making the learning of the model harder allowing to gain up to more than 50% by decreasing the loss rate of the model.

1 INTRODUCTION

Overfitting is a concept in data science and a serious problem in Deep neural networks with a large number of parameters that are very powerful machine learning systems (Hinton et al., 2012).

Deep neural networks contain multiple non-linear hidden layers and this makes them very expressive models that can learn very complicated relationships between their inputs and outputs. With limited training data, however, many of these complicated relationships will be the result of sampling noise, so they will exist in the training set but not in real test data even if it is drawn from the same distribution. This leads to overfitting and many methods have been developed for reducing it (Wu et al., 2022).

Early stopping is a method that seeks to pause training before the model starts to overfit or before learning the noise within the model(Yingbin et al., 2021). This approach risks halting the training process too soon, leading to the opposite problem of underfitting. Finding the "sweet spot" between underfitting and overfitting is the ultimate goal.

Dropout is another technique for addressing this overfitting problem (Senen-Cerda and Sanders, 2020). Dropout is a powerful and widely used technique to regularize the training of deep neural networks (Xiaobo et al., 2021). The key idea is to randomly drop units (along with their connections) from the neural network during training. This prevents units from co-adapting too much. During training, dropout samples from an exponential number of different thinned networks. At test time, it is easy to approximate the effect of averaging the predictions of all these thinned networks by simply using a single unthinned network that has smaller weights. This significantly reduces overfitting and gives major improvements over other regularization methods.

But how is it possible to add malfunctions in the learning of our machines to allow them to be more efficient ?

In general, making errors in a program prevents the program from functioning well but strangely if we program a neural network then it is indeed desirable to artificially create random bugs including the functioning of the neurons of the network.

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^a https://orcid.org/0000-0003-4317-568X

^b https://orcid.org/0000-0001-8502-4623

^c https://orcid.org/0000-0002-0147-8466

Well, to combat overfitting, we could simply seek to have more training data, but suppose that we only have access to the data that has been collected for us and there, instead of seeking to collect more data, we could try to create data from those that we typically have if we want to learn to recognize cats from a car image we can slightly rotate the zoom out of the zoom small changes in the white balance or make a mirror image of the photo in order to obtain new data which we can still reasonably think of as images of cars, we then speak of an increase in data or data augmentation.

In this article, we will take a closer look at two techniques for addressing the overfitting problem ealy-stopping and dropout. The rest of this paper is organized as follows. In Section 2 we briefly compare and position our solution with other proposals find in the literature. Section 3 describes the problem handled. In Section 4, we describe our proposed method that can be potentially applied to convolutional neural network. Section 5 describes the Dropout Neural Network Model. Finally, we carry out extensive experiments with standard datasets and different network architectures to validate the effectiveness

2 STATE-OF-THE-ART

Without any attempt at being exhaustive, here we point out a few connections between dropout and previous literature (Shaeke and Xiuwen, 2019) (Senen-Cerda and Sanders, 2020) :

Sochastic Gradient Descent Method: The first description of a dropout algorithm was in (Hinton et al., 2012) as an effective heuristic for algorithmic regularization. The authors used the standard stochastic gradi- ent descent procedure to train neuronal stall networks on mini-batches of training cases, but they modified the penalty term which was normally used to keep weights from getting too big. At the time of the test, they used the "average network" which contains all units hidden but with their the outgoing weights have been halved to compensate for the fact that twice as many of them are active. In practice, this gives very similar performance to the average over a large number of dropout networks.

Regularized Dropout for Neural Networks: R-drop is a simple yet very effective regularization method built upon dropout, by minimizing the bidirectional KL-divergence of the output distributions of any pair of sub models sampled from dropout in model training (Liang et al., 2021). Concretely, in each minibatch training, each data sample goes through the forward pass twice, and each pass is processed by a different sub model by randomly dropping out some hidden units. R-Drop forces the two distributions for the same data sample outputted by the two sub models to be consistent with each other, through minimizing the bidirectional Kullback-Leibler (KL) divergence between the two distributions (Liang et al., 2021).

Implicit and Explicit Regularization. In a recent work, (Wei et al., 2020) disentangle the explicit and implicit regularization effects of dropout; i.e. the regularization due to the expected bias that is induced by dropout, versus the regularization induced by the noise due to the randomness in dropout. They propose an approximation of the explicit regularizer for deep neural networks and show it to be effective in practice. Their generalization bounds, however, are limited to linear models and require weights to be norm bounded (Arora et al., 2020).

3 PROBLEM DESCRIPTION

Overfitting is a concept in data science, which occurs when a statistical model fits exactly against its training data, but badly in the test set. When this happens, the algorithm unfortunately cannot perform accurately against unseen data, defeating its purpose (IBM_Cloud_Education, 2021). When machine learning algorithms are con-structed, they leverage a sample dataset to train the model. However, when the model trains for too long on sample data or when the model is too complex, it can start to learn the "noise," or irrelevant informa- tion, within the dataset. When the model memorizes the noise and fits too closely to the training set, the model becomes "overfitted," and it is unable to gen- eralize well to new data. If a model cannot generalize well to new data, then it will not be able to perform the classification or prediction tasks that it was intended for. Low error rates and a high variance are good in- dicators of overfitting. In order to prevent this type of behavior, part of the training dataset is typically set aside as the "test set" to check for overfitting. If the training data has a low error rate and the test data has a high error rate, it signals overfitting. There are too many feature dimensions, model assumptions, and parameters, too much noise, but very few training data. As a result, the fitting function perfectly predicts the training set, while the prediction result of the test set of new data is poor.

4 HOW TO AVOID OVERFITTING

Much has been written about overfitting and the bias/variance tradeoff in neural nets and other ma-

chine learning models (Brownlee, 2018).

4.1 Early Stopping

Early termination is the default option for overfitting prevention in ML programs. When premature termination is enabled, the loss of excluded data is monitored during training, and it is terminated when the loss improvement in the last iteration falls below a given threshold. Since the excluded data is not used during training, it represents a good estimate of model loss on the new data. The behavior of the early stopping is controled by the activation of early_stop option (Maren et al., 2017).

There are three elements to using early stopping, they are :

4.2 Training Model over a Predefined Number of Epochs

This method is a simple method but risks stopping the training early before reaching a satisfactory training point. With a higher learning rate, the model could eventually converge with fewer epochs, but this method requires a lot of trial and error. Due to advances in machine learning, this method is quite obsolete.

4.3 Stop When the Loss Function Update Becomes Small

This approach is more sophisticated than the first because it relies on the fact that the gradient descent weight updates become significantly smaller as the model gets closer to the minima. Usually, the drive is stopped when the update becomes as small as 0.001, because stopping at this point minimizes loss and saves computing power by preventing unnecessary epochs. However, overfitting can still occur.

4.4 Overall Validation Strategy

This smart technique is the most popular early stopping approach (see Figure 2) (Caruana et al., 2001). To understand how this works, it is important to look at how the training and validation errors change with the number of epochs (as in Figure 2). The learning error decreases exponentially until the increasing epochs no longer have such a large effect on the error. The validation error, however, initially decreases with increasing epochs, but after a certain point it begins to increase. This is the point where a model should be stopped early because beyond that the model will start to overfit.

While the validation set strategy is the best in terms of preventing overfitting, it usually takes a large number of epochs before a model starts to overfit, which can cost a lot of computing power. A smart way to get the best of both worlds is to design a hybrid approach between the commit set strategy and then stop when the loss function update gets small. For example, training may stop when either is achieved.

4.5 Dropout

Dropout is a regularization technique for neural networks that drops a unit (along with connections) at training time with a specified probability. Dropout changed the concept of learning all the weights together to learning a fraction of the weights in the network in each training iteration (Moolayil, 2019). It significantly improve the performance of deep neural networks on various tasks (Hinton et al., 2012), including vision problems (Krizhevsky et al., 2017) and randomly sets hidden Unit activities to zero with a probability of 0.5 during training. In Figure 1: Left(a):All neurons are used during training of a model. Right(b) : Dropout a simple way to prevent neural networks from overfitting, When p = 0.5, each neuron has a 50 in 100 chances of being turned off in training.



This issue resolved the overfitting issue in large networks. And suddenly bigger and more accurate Deep Learning architectures became possible (LeCun et al., 2015).

Before Dropout, a major research area was regularization. Introduction of regularization methods in neural networks, such as L1 and L2 weight penalties, started from the early 2000s (Bengio et al., 2007). However, these regularizations did not completely solve the overfitting issue. The reason was Co-adaptation.

4.6 Co-adaptation in Neural Network

One major issue causing overfitting in learning large networks is co-adaptation. So, in neural network, coadaptation means that some neurons are highly dependent on others. If those independent neurons receive "bad" inputs, then the dependent neurons can be affected as well, and ultimately it can significantly alter the model performance, which is what might happen with overfitting. In such a network, if all the weights are learned together it is common that some of the connections will have more predictive capability than the others. In such a scenario, as the network is trained iteratively these powerful connections are learned more while the weaker ones are ignored. Over many iterations, only a fraction of the node connections is trained. And the rest stop participating.



Figure 2: Co-adaptation of node connections.

In figure 2, the red circles are neurons that are independent on others, the green one are the neurons that are highly dependant on others. This phenomenon is called co-adaptation. This could not be prevented with the traditional regularization, like the L1 and L2 (Ng, 2004). The reason is they also regularize based on the predictive capability of the connections. Due to this, they become close to deterministic in choosing and rejecting weights. And, thus again, the strong gets stronger and the weak gets weaker. A major fallout of this was: expanding the neural network size would not help. Consequently, neural networks' size and, thus, accuracy became limited. Then came Dropout. A new regularization approach. It resolved the co-adaptation. Now, we could build deeper and wider networks. And use the prediction power of all of it. With this background, let's dive into the Mathematics of Dropout.

Model combination always improves the performance of machine learning methods. With large neural networks, however, the obvious idea of averaging the outputs of many separately trained nets is prohibitively expensive. Combining several models is most helpful when the individual models are different from each other and in order to make neural net models different, they should either have different architectures or be trained on different data. Training many different architectures is hard because finding optimal hyperparameters for each architecture is a daunting task and training each large network requires a lot of computation. Moreover, large networks normally require large amounts of training data and there may not be enough data available to train different networks on different subsets of the data. Even if one was able to train many different large networks, using them all at test time is infeasible in applications where it is important to respond quickly.

Dropout is a technique that addresses both these issues. It prevents overfitting and provides a way of approximately combining exponentially many different neural network architectures efficiently. The term "dropout" refers to dropping out units (hidden and visible) in a neural network. By dropping a unit out, we mean temporarily removing it from the network, along with all its incoming and outgoing connections, as shown in Figure 1. The choice of which units to drop is random.

In the simplest case, each unit is retained with a fixed probability p independent of other units, where p can be chosen using a validation set or can simply be set at 0:5, which seems to be close to optimal for a wide range of networks and tasks. For the input units, however, the optimal probability of retention is usually closer to 1 than to 0:5. (The mathematical aspect of the choice of these values will be treated below in section 5)



Figure 3: Partial learning with random choice of inactive neurons : color red are the neurons that are not used during training.

This very simple technique which is dropout which consists quite simply in programming the temporary vulnerability of artificial neurons is in fact a formidably effective technique to fight against overinterpretation. Since it makes it possible both to fight against the lack of learning data against errors in learning data and against learning a single model rather than learning a whole forest in short, neural balls are in fact very intelligent errors.

The Initialization Process, through the idea of multi start, amounts to starting with several initial neural networks whose initialization is random and we can keep the best of our neural networks during learning or perhaps even better.

5 DROPOUT NEURAL NETWORK MODEL

This section describes the dropweak neural network model (Srivastava N et al., 2014). Consider a neural network with L hidden layers.

Let
$$l \in \{1, 2, ..., L\}$$

indexes the hidden layers of the network (Srivastava N et al., 2014). Let z^l denote the vector of inputs into layer l, y^l denote the vector of outputs from layer l (y^0 is the input vector of the neural network). W^l and b^l are the weights and biases at layer l. The feed-forward operation of a standard neural network (Figure 4a) can be described as

$$(for \quad l \in \{0, 1, 2, \dots, L-1\}$$

and any hidden unit i)

The training phase of the standard network without dropout can be represented mathematically as:

$$Z_{i+1}^{l+1} = W_{i+1}^{l+1} * Y^{l+1} + b_{i}^{l+1}$$

 $y_i^{l+1} = f(z_i^{l+1})$ where f is any activation function, for example sigmoid function, $f(x) = \frac{1}{1+e^{-x}}$

The dot product of the weights w_i^{l+1} and the input(y^l) are added to a bias term(b^{l+1}) and passed through an activation function(f), to introduce non-linearity to give the output y^{l+1} , which is the prediction, meaning all the neurons are involved in the making of a decision.

During dropout, the training is updated to become: (Figure 4b)

$$\begin{aligned} r_i^l &= Bernoulli(p) \\ \hat{y}^l &= r^l \times y^l \\ z_i^{l+1} &= w_i^{l+1}haty^l + b_i^{l+1} \\ y_i^{l+1} &= f(z_i^{l+1}) \end{aligned}$$

The training is very similar to the standard network, but a new term r which is a new neuron, is introduced, which keeps the neuron active or turns it off, by assigning a 1 (neuron participates in the training) or 0 (neuron does not participate or is turned off), then the training process continues. This way, overfitting



Figure 4: Comparison of the basic operations of a standard and dropout network.

is reduced and our model can now make excellent and accurate predictions on real-world data (data not seen by the model). At test time, the weights are scaled as W(l)test = pW(l). The resulting neural network is used without dropout.

6 EXPERIMENTAL SETUP AND RESULTS

In this section, first, we confirm empirically that hyper-parameters provide characterizations after a certain number of iterations. In early stopping regularization, we stop training the model when the performance of the model on the validation set starts to deteriorate, which decreases accuracy or increases loss.

6.1 Experimental Results with Stop-early

By plotting the error on the training dataset and the validation dataset together, the errors decrease with a number of iterations until the point where the model begins to overfit. After this point, the validation error increases, but the training error still decreases. So even though training continues after this point, stopping early essentially returns the set of parameters that have been used at this point and is therefore equivalent to stopping training at this point. Thus, the final parameters returned will allow the model to have better generalization and low variance.

The model at the time when the training is stopped will have a better generalization performance than the model with the least training error. Early cessation can be considered implicit regularization, unlike regularization through weight loss. This method is also efficient because it requires less training data, which is not always available. Because of this, early quitting requires less training time compared to other regularization methods. Repeating the early stopping process multiple times can lead to overfitting of the model to the validation dataset, just as overfitting occurs in the case of training data. The number of iterations taken to train the model can be thought of as a hyperparameter. Then the model must find an optimal value for this hyperparameter for the best performance of the training model.

Early stopping is a regularization technique for deep neural networks that stops training when parameter updates bring no improvement over a validation set. Therefore, we store and update the current best parameters during training, and when parameter updates no longer produce improvement (after a set number of iterations), we stop training and use the latest best settings. It works as a regularizer by limiting the optimization procedure to a smaller volume of parameter space.

From the plot bellow (Figure 5) we can see that without Early Stopping (Caruana et al., 2001) the model continues to diverge after the optimal point where the two errors are equal and if the process does not stop the performance of the model will be further degraded



Figure 5: Loss & Early Stopping checkpoint.

At this point the performance of the model is optimal. EarlyStopping needs the validation loss to check if it has decreased, and in this case it will make a checkpoint of the current model

6.2 Experimental Results with Dropout

Experiments are conducted on three datasets : MNIST (Etzold, 2022), SONAR (Brownlee et al., 2017) and Diabetes (Larxel, 2021).

In order to test the robustness of dropout, classification experiments were done with networks of many different architectures keeping all hyperparameters, including p fixed. Figure 9a and 9b shows the test error rates obtained for these different architectures as training progresses. The same architectures trained with and without dropout have drastically different test errors as seen as by the two separate clusters of trajectories.

Dropout gives a huge improvement across all architectures, without using hyperparameters that were tuned specifically for each architecture. The algorithm tested with some classification datasets gives the results as indicated in Figure 6a and 9b : It illustrates accuracy and loss without Dropout on the left and with Dropout on the right): The model is formed of is formed of 7 hidden layers alternated by 6 dropout layers with a percentage of 50%, i.e. p = 0.5, each neuron has a chance in 2 to be deactivated. At each epoch, this random deactivation is applied. That is, with each pass (forward propagation) the model will learn with a configuration of different neurons, the neurons activating and deactivating randomly. This procedure effectively generates slightly different patterns with different neural configurations at each iteration. The idea is to disrupt the characteristics learned by the model.

Usually, model learning is based on the synchronicity of neurons... with dropout, the model must exploit each neuron individually, its neighbors can be randomly disabled at any time. The Dropout is active only during model training. In tests, each neuron remains active and its weight is multiplied by probability p. With Keras & Tensorflow it is enough to add a dropout layer is to indicate the desired probability of deactivation.

It is true that dropout hinders performance, in some way, since it suppresses neuron activations during training. However, dropout is highly useful as a regularization technique - since any one neuron has a decent change of being ignored during one forward pass, the neural network cannot rely strongly on any one neuron. This has the effect of preventing overfitting and helping the neural network generalize to examples it has never seen before, since it becomes harder to simply memorize training data with this added suppression. This means that performance is improved during inference/validation even if performance during training is reduced. After training is completed, however, dropout is generally removed when the neural net is used for prediction.

According to the curve of the accuracy and that of the loss of the Figure 6a, we can see that the predictive model produced by the automatic learning algorithm adapts well to the Training Set in the event of non-use of dropout, which justifies an overfitting, because the training data has a low error rate and a high accuracy. while this adaptation is less remarkable when using



Figure 6: Dropout slows down everfitting.

dropout.

Another example with different dataset (diabetes.csv, 2021) gives the results bellow [Figure 7a and b]:



Figure 7: By using dropout layer test accuracy increased from 0.75 to 0.81 while loss decreased from 81% to 45%.

In this example, unlike the previous case, we represent the evolution of the precision for the test sample with or without dropout and we see that if the dropout is not used, the loss of test dataset increases constantly (81% at iteration 100) whereas with dropout it stabilizes around 45% at the same iteration. As for the accuracy of the test sample, it is 75% without dropout and 81% with dropout

In this third example, experiments are conducted on MNIST which consists of 28x28pixel images with 1 channel. We use rectified linear function (Cerisara et al., 2021) for dense layer and Maxpooling for convolutional and fully-connected layers, and softmax activation function for the output layer.

The CNN (Iraji et al., 2021) architecture for MNIST is 1x28x28, which represents a CNN with 1 input image of size 28x28, a convolutional layer with

6 feature maps and 5x5 filters, a pooling layer with pooling region 2x2, a convolutional layer with 16 feature maps and 5x5 filters, a pooling layer with pooling region 2x2, a fully-connected layer with 1000 hidden units, and an output layer with 10 units (one per class).

We represent the evolution of the precision and the loss for the training and test sample with or without dropout and we note that in the case where the dropout is not used the accuracies of the dataset of training and test diverge (Figure8), the same is true for the losses of the 2 datasets which shows an overfitting, while with dropout the accuracies and the losses converge after ten iterations.

In this example, each hidden unit is randomly omitted from the network with a probability of $p \in [0.2, 0.5]$, so a hidden unit cannot rely on other hidden units being present.

In the other example, the dropout technique consists of to zero the output of each hidden neuron with probabilities 0.25 on the first two layers, 0.5 on the third and 0.25 on the last. The neurons that are "dropped" in this way does not contribute to forward passage and does not participate in backpropagation. This way, each time an input is presented, the neural network samples a different architecture. Because a neuron cannot count on the presence of other specific neurons. It is therefore forced to learn more robust features that are useful in conjunction with many different random subsets of other neurons, which reduces co-adaptations of neurons. During the test, we use all the neurons by multiplying their outputs by the coefficients indicated above which is a reasonable approximation for taking the geometric mean of the predictive distributions produced by the many dropout networks.

From the figure 8 above (upper part), we can see that the accuracy of the validation has almost become stagnant after a few epochs. The accuracy grows linearly at the beginning and stagnates rapidly thereafter.

As for the loss of validation, the figure 8 (lower part) shows that it decreases linearly at the beginning to increase after a few epochs, which shows that it is a sign of overfitting.

In this case, it is advisable to introduce some dropout in our model and see if that helps reduce overfitting.

Using the dropout, we can see that validation loss and validation accuracy are both synchronized with training loss and training accuracy, see Figure9. The gap between the training and the validation accuracy is very small, even if the validation loss and the accuracy line are not linear, it shows that the model is not overfitting and the validation loss decreases when the



Figure 8: Full Network: Accuracy & Loss.



Figure 9: Dropout Network : Accuracy & Loss.

activation of the dropout.

As a result, we can conclude that the model's generalization capability became much better since the loss on the validation set was only slightly higher compared to the training loss.

Another example for classification based on of dataset (Dogs vs. Cats) (M.Sarvazyan, 2022), we will investigate the performance of Full network on simulated data, and compare it to standard dropout.



The gap between training accuracy and validation accuracy is very high showing that the model is overfitting (see figure 10). Training accuracy approaches 1 and training loss approaches 0. Thus, the model perfectly fits the training set, which is a sign of overfitting.

Using the dropout technique (figure 11), although the model is not totally stable, we can see that the the gap between training accuracy and validation converge slowly and the gap between training and validation loss is smaller. Actually, the difference between these two curves is small enough to consider that the model is not overfitting anymore. Training and validation loss confirm that the model doesn't overfit. Both loss values are similar.

Also, the model does not predict the training set perfectly anymore.

This is also a sign that the model is not overfitting and it generalizes better.

These tables show the variation of the accuracy [Table 1] and loss [Table 2] of validation dataset with and without Dropout. We observe a pretty good performance, this further reinforces the motivation about the potential of Dropout methods for improving the predictive performance (Belciug, 2020).



7 CONCLUSION

This paper mainly addresses the problem of understanding and using Early stopping as well as Dropout on the entry into the maximum pooling layers of convolutional neural networks. Early stopping is a method to stop the training of a neural network when the validation loss stops improving.

Dropout is a technique for improving neural networks by reducing overfitting. It forces a neural network to learn more robust features that are useful

by deactivating certain units (neurons) in a layer with a certain probability p. We presents precise iteration complexity results for dropout training in twolayer ReLU networks using the logistic loss.

In the future, we would like to explore applications of deep network compression (Li et al., 2020) and investigate the sparsity property of learned retention rates to encourage a sparse representation of the data and the neural network structure (Wang et al., 2019). Another line of research is to dynamically adjust the architecture of deep neural networks and therefore reduce the complexity of the model using dropout rates.

REFERENCES

- Arora, R., Bartlett, P., Mianjy, P., and Srebro, N. (2020). Dropout: Explicit Forms and Capacity Control. OCLC: 1228394951.
- Belciug, S. (2020). Artificial intelligence in cancer: diagnostic to tailored treatment. OCLC: 1145585080.
- Bengio, Y., Lamblin, P., Popovici, D., and Larochelle, H. (2007). Greedy Layer-Wise Training of Deep Networks. Advances in neural information processing systems., (19):153–160. Place: San Mateo, CA Publisher: Morgan Kaufmann Publishers OCLC: 181070563.
- Brownlee, J. (2018). How to Avoid Overfitting in Deep Learning Neural Networks.
- Brownlee, J., Machine Learning, and Mastery (2017). develop deep learning models on Theano and Tensor-Flow using Keras, volume 1. Machine Learning Mastery, Melbourne, Australia.
- Caruana, R., Lawrence, S., Giles, L., and 14th Annual Neural Information Processing Systems Conference, N. . (2001). Overfitting in neural nets:. Adv. neural inf. proces. syst. Advances in Neural Information Processing Systems. OCLC: 5574566588.
- Cerisara, C., Caillon, P., and Le Berre, G. (2021). Unsupervised post-tuning of deep neural networks. In *IJCNN*, Proceedings of the 2021 International Joint Conference on Neural Networks (IJCNN), Virtual Event, United States.
- diabetes.csv.en. URL: https://kaggle.com/saurabh00007/di abetescsv (visited on 12/29/2021)
- Etzold, D. (2022). MNIST Dataset of Handwritten Digits.
- Hinton, G. E., Srivastava, N., Krizhevsky, A., Sutskever, I., and Salakhutdinov, R. R. (2012). *Improving neural* networks by preventing co-adaptation of feature detectors, volume 1.
- IBM_Cloud_Education (2021). What is Overfitting?

- Iraji, M. S., Feizi-Derakhshi, M.-R., and Tanha, J. (2021). COVID-19 Detection Using Deep Convolutional Neural Networks. *Complexity*, 2021:1–10.
- Krizhevsky, A., Hinton, G. E., and Sutskever, I. (2017). ImageNet classification with deep convolutional neural networks. *Commun ACM Communications of the ACM*, 60(6):84–90.
- Larxel (2021). Early Diabetes Classification.
- LeCun, Y., Hinton, G., and Bengio, Y. (2015). Deep learning. *Nature*, 521(7553):436–44. OCLC: 5831400088.
- Li, C., Mao, Y., Zhang, R., Huai, J., and SpringerLink (Online service) (2020). A revisit to MacKay algorithm and its application to deep network compression. OCLC: 1196515065.
- Liang, X., Wu, L., Li, J., Wang, Y., and Meng, Q. (2021). *R-Drop: Regularized Dropout for Neural Networks*. OCLC: 1269560920.
- Maren, M., Lukas, B., Christoph, L., and Philipp, H. (2017). *Early Stopping without a Validation Set.* OCLC: 1106261430.
- Moolayil, J. (2019). Learn Keras for deep neural networks: a fast-track approach to modern deep learning with Python. OCLC: 1079007529.
- M.Sarvazyan, A. (2022). Kaggle: Your Home for Data Science.
- Ng, A. Y. (2004). Feature selection, L1 vs. L2 regularization, and rotational invariance. OCLC: 8876667046.
- Senen-Cerda, A. and Sanders, J. (2020). Almost sure convergence of dropout algorithms for neural networks. OCLC: 1144830913.
- Shaeke, S. and Xiuwen, L. (2019). Overfitting Mechanism and Avoidance in Deep Neural Networks. OCLC: 1106327112.
- Srivastava N, Hinton G, Krizhevsky A, Sutskever I, and Salakhutdinov R (2014). Dropout: A simple way to prevent neural networks from overfitting. J. Mach. Learn. Res. Journal of Machine Learning Research, 15:1929–1958. OCLC: 5606582392.
- Wang, Z., Fu, Y., and Huang, T. S. (2019). Deep learning through sparse and low-rank modeling. OCLC: 1097183504.
- Wei, C., Kakade, S., and Ma, T. (2020). The Implicit and Explicit Regularization Effects of Dropout. OCLC: 1228392785.
- Wu, J.-W., Chang, K.-Y., and Fu, L.-C. (2022). Adaptive Under-Sampling Deep Neural Network for Rapid and Reliable Image Recovery in Confocal Laser Scanning Microscope Measurements. *IEEE Trans. In*strum. Meas. *IEEE Transactions on Instrumentation* and Measurement, 71:1–9. OCLC: 9359636331.
- Xiaobo, L., Lijun, W., and Juntao, L. (2021). *R-Drop: Regularized Dropout for Neural Networks*. OCLC: 1269560920.
- Yingbin, B., Erkun, Y., and Bo, H. (2021). Understanding and Improving Early Stopping for Learning with Noisy Labels. OCLC: 1269561528.