Detection, Tracking, and Speed Estimation of Vehicles: A Homography-based Approach

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Abstract: In this research we present a parsimonious yet effective method to detect, track, and estimate the speed of multiple vehicles using a single camera. This research aims to determine the efficacy of homography-based speed estimations derived from details extracted from objects of interest. At first, a neural network trained to detect vehicles outputs bounding boxes. The output of the neural network serves as an input to a multi-object tracking algorithm which tracks the detected vehicles while, at the same time, their speed is estimated through a homography-based approach. This algorithm makes no assumptions about the camera, the distance to the objects, or the direction of motion of vehicles with respect to the camera. This method proves to be accurate and efficient with minimal assumptions. In particular, only the mean dimensions of a passenger vehicle are assumed to be known and, using the homography matrix derived from the corners of a vehicle, the speed of any vehicle in the frame irrespective of its motion direction and regardless of its size is able to be estimated. In addition, only a single point from each tracked vehicle is needed to infer its speed, avoiding repeatedly computing the homography matrix for each and every vehicle, thus reducing the time and computational complexity of the algorithm. We have tested our algorithm on a series of known datasets, the results from which validate the approach.

1 INTRODUCTION

In this research we demonstrate our findings from detecting, tracking, and estimating the speed of multiple vehicles using only a single camera. Estimating the speed of vehicles, especially on highways, has been an important topic of research for several decades. In the last few years, however, there has been a resurgence of interest in this field due to the imminent advent of autonomous vehicles. Most of the research in this field relies on Time-of-Flight (ToF) sensors where a transceiver emits a signal measuring the time it takes to hit a target vehicle and return to the receiver (Sarbolandi et al., 2018), (Li et al., 2013). This method has been proven accurate, however, there are several drawbacks. One drawback in particular being that only one vehicles' speed can be estimated at a time.

On a highway, there are many vehicles passing at any moment, and more than one of them may need attention. Having only one vehicle targeted by a measuring device is not enough as there may be several vehicles whose speed may need to be estimated. In addition, the handling of the device needs to be precise enough to target a vehicle adequately to have an estimate of its speed as the signal emitted needs to reach the right vehicle. Line of sight is also another drawback. More specifically, targeting one vehicle with a ToF device may be occluded or obstructed by another passing vehicle thus giving erroneous estimated of a vehicles' speed. Finally, ToF sensors estimate the speed of a vehicle at a given point in time. A vehicle's speed throughout a period of time cannot be determined.

Other popular methods for estimating vehicles' speed include piezoelectric sensors embedded into the ground in two different parts of a road with a known distance between them, thus the time taken for a vehicle to move from one piezoelectric sensor to the other is recorded and the speed is, therefore, inferred (Rajab et al., 2014), (Markevicius et al., 2020). Other similar approaches for estimating a vehicle's speed are based on the use of magneto-resistive sensors (Markevicius et al., 2017). This method, in spite of its accuracy, suffers also from some major drawbacks. More specifically, if several vehicles cross either the first or the second piezoelectric sensor at the same time, it may

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be difficult to know which estimated speed belongs to which vehicle. This is the reason this method is more frequently used in country side roads and less, if at all, on busy highways. In addition, this method requires installation of equipment on the ground. Finally, this method, suffers, too, from calculating a vehicles' speed at a given point in time, therefore, making it impossible to track the speed of a vehicle continuously in time. A work by (Dailey et al., 2000) uses assumptions drawn from distributions about the mean height, width, and length of vehicles.

Computer vision has played an important role in estimating the speed of vehicles (Hassaballah and Hosny, 2019). Several methods make use of computer vision sensors only. In several of these approaches, assumptions about the environment or the camera need to be made. For example, in many works, the computer vision system has to be at a known distance from the vehicles. This is, in particular, the case where a camera is placed atop a bridge with a known height from the ground. Other methods rely on known marks on the ground or in the image plane. Furthermore, in some instances, the direction of motion plays an important role in the estimation process. In a work by (Diamantas and Dasgupta, 2014) the direction of motion of the vehicle needs to be perpendicular to the optical axis of the camera.

In this research, our algorithm addresses all of the above shortcomings yet still provides accurate and continuous estimates of multiple vehicles using only a single, non-invasive sensor, that is, a camera. In particular, our algorithm does not require the installation of any specialized equipment on the road nor does it make any assumptions about any known distances to the target vehicle or the camera. Moreover, it does not compute the instantaneous speed of a vehicle but rather it computes and records the speed of a vehicle throughout the whole duration of the video, thus, providing concrete evidence of a vehicles' speed and acceleration which might otherwise be spurious if an instant estimate is drawn.

Furthermore, the direction of motion of a vehicle does not affect the speed estimates. Our algorithm provides precise estimates irrespective of the motion and direction of the vehicle with respect to the camera. Finally, homography matrix estimation is carried out once during the initialization process of our algorithm in any one given vehicle, thus, significantly minimizing the computational complexity for continuously computing the homography matrix in every frame and for every vehicle. Our algorithm has been tested on several datasets with multiple cars on busy highways. Additionally, we have also carried out experiments with a known vehicle speed serving as the ground truth with the view to infer the error in our approach.

This paper consists of five sections. In the next section, background and related works in the fields of detection, tracking, and speed estimation are presented. In Section 3, we present and describe our methodology as well as the different algorithms encompassing our approach for detection, tracking, and speed estimation. Section 4, presents the results of our proposed algorithm. Qualitative, as well as quantitative results, are provided and compared with the ground truth. Finally, Section 5 epitomizes our paper with a discussion on the conclusions drawn from this research as well as the current work that is taking place and the plans for future work.

2 RELATED WORKS

Tracking many objects simultaneously, especially in busy difficult environments, and extracting information such as height and speed from them over a period is, in fact, a multitude of different challenges wrapped into one. The task of tracking objects alone requires identifying the object, recognizing the movement and updated locations of objects, and concluding which object is which at any given point. Individual aspects of object tracking have seen significant research, especially in recent years with research being spurred by autonomous vehicles. Because so many challenges construct one singular goal, there can be a large amount of benefit to the overlap in tying together multiple systems that solve individual problems.

2.1 Object Detection

You Only Look Once (YOLO) is a darknet-based object detector that takes a unique approach to object detection. Darknet-53 (Redmon, 2021) is the specific convolutional neural network used as the backbone for YOLO v3 and YOLOv4 (Redmon and Farhadi, 2018). Compared to prior object detectors which use classifiers and localizers applied to multiple locations and at different scales to the image, YOLO applies a single neural network to the entire image. The image is subdivided into regions or blobs which are analyzed and are given bounding boxes and probabilities for different object classes. This approach allows predictions to be informed by global context because the neural network is applied to the entire image at once. This approach is also many times faster than classifier-based detectors, allowing for real-time object detection.

Because object detectors are typically neural net-

work models, they need to be trained on a dataset. Microsoft's Common Objects in Context (COCO) is one of the leading object recognition datasets. COCO contains images with complex scenes which have objects in a natural context (Lin et al., 2015). 91 object types are defined in the dataset.

2.2 Feature Detection and Tracking

Kanade-Lucas-Tomasi (KLT) point trackers find the best fit linear translation between images by using spatial intensity information to make the process of finding the regression less computationally costly (Lucas and Kanade, 1981). Minimum eigenvalue feature detection finds where large gradient changes in the image intersect. Corner points become features to track when the minimum of both computed eigenvalues of the gradient is above a set threshold. These corner points can then be found repeatedly and tracked from frame to frame. In addition to detection and tracking, an affine transformation is found between nonconsecutive frames to identify and potentially reject tracked points that are too dissimilar (Shi and Tomasi, 1994). KLT point trackers are used broadly in the field of computer vision for camera motion estimation, video stabilization, and object tracking. When applying KLT point tracking, points can be lost because of occlusion, lack of contrast, etc. Because of this, many tracked features end up short-lived, and therefore, an additional tracking framework can often be needed to redetect points of interest.

2.3 Multiple Target Tracking

The uniqueness of different objects of interest is an important condition to maintain in many tracking scenarios. Knowing which object is which can be imperative in many instances and applications. Data association techniques such as global nearest neighbor (GNN) (Konstantinova et al., 2003) and multiple hypothesis trackers (MHT) aim to solve the issue of uniqueness in cluttered environments. Algorithms like these usually employ gating techniques along with filtering such as Kalman filtering to make broad decisions before making finer deductions. Various algorithms are then used to update the identifications of the tracks (Bardas et al., 2017).

3 METHODOLOGY

This section provides the process and workflow behind estimating speed. Speed and depth estimation are at the summit of a long multifaceted path consisting of finding objects to track, tracking the objects which are found, solving for uniqueness, image manipulation, and every hurdle and complication in-between. Methods that rely on depth appear in (Diamantas et al., 2010), (Diamantas, 2010). Because tracking objects and estimating depth is such a complex challenge, we decided to split it into smaller more manageable problems, with each step providing new challenges to solve, not only in it of itself, but also in order to work with each step of the rest of the process.

In order to find an object's speed, first, where the object is must be known. For this, object detection is needed. With current object detection algorithms arises another challenge, computational power. Object detection requires a large amount of computing resources. If we want to find, for example, vehicle speeds in real-time using easily accessible computing power, object detection for every new input (frame) isn't feasible. It is also quite a waste of resources when there are much less demanding ways to track object positions frame-to-frame, such as point tracking. An object detector still needs to be run periodically to detect new objects and regather points on already tracked objects, but point tracking or other tracking algorithms are the frame-to-frame solutions for tracking changes in object position.

In order to track object speed, first, detection of the object is done, then tracking of changes in object position. The next issue arises when we consider tracking multiple objects. In the case of speed estimation, we must know which object is which. If a car is being tracked, and a new car appears nearby, there needs to be a protocol in place to decide which object is which from frame to frame and with each new round of detection. This is another challenge faced on the way to speed estimation.

3.1 Detection Phase

The first step for any tracking or collection of data of objects of interest is to detect those objects. Object detection is a rapidly advancing field in computer science, and there are many different detectors out there. One thing most modern detectors have in common is that they are neural network models, but beyond that, the structure, design, and techniques used can vary greatly.

For this project, we decided to implement YOLOv4 in this detection algorithm. YOLO was the detector of choice because of its balance of detection accuracy and detection speed. One of the primary goals in speed estimation is for it to be real-time. YOLOv4 achieves 43.5% AP (65.7% AP50) on the MS COCO dataset with a speed of roughly 65 frames per second using a Tesla V100 graphics card. Compared to EfficientDet, another state-of-the-art detector, YOLO boasts twice the detection speed at comparable accuracy (Bochkovskiy et al., 2020).

Using code to import the YOLO models to MAT-LAB (YOLOv4, 2021), YOLOv4 is periodically run to detect new objects and recollect features on already tracked objects. In much of our testing, 500 millisecond intervals proved to be an appropriate interval rate for real-time operation, quick detection of newly presented objects, and consistent point recollection. YOLO produces axis-aligned bounding boxes for all detected objects as well as categories and confidence values for each detection. Objects with a confidence value over a certain threshold are kept. Nonmaximum suppression (NMS) keeps objects from being double-counted.

3.2 Tracking and Data Collection Phase

In order to progress from object detection to object tracking, a few issues need to be addressed. Firstly, in multi-object tracking, the uniqueness of each object needs to be maintained. In other words, when tracking multiple objects, knowing which object is which is important. Second, in-between detections being run, the movement of objects needs to be tracked and their bound boxes adjusted accordingly. Lastly, because the view of objects can in many cases be temporarily obstructed and because some objects may be difficult to detect, predicting the future position of tracks can be utilized to produce more consistent tracking and allows the tracking to be more robust in many more challenging situations.

There are a number of approaches for deducing which object is which. We chose a ranked assignment method (Murty, 1968) which uses a cost matrix to determine assignments with the least cost. The optimized ranked assignment method we implemented greatly optimizes the method by partitioning in an optimized order, inheriting partial solutions, and sorting sub-problems (Miller et al., 1997).

Utilizing a KLT algorithm (Tomasi and Kanade, 1991) with the bounding boxes provided by object detection as the region of interest, we were able to get consistent feature extraction and tracking (Shi and Tomasi, 1994). Since the objects of interest were often moving objects, we used bidirectional error alongside point tracking to determine and eliminate points detached from the objects being tracked (Kalal et al., 2010). With these measures in place, points that proved to be quality points on the object to track were then used to interpolate the object's change in position from frame to frame. The interpolation arises from the geometric transform estimation derived from the points' change in position between frames (Torr and Zisserman, 2000).

For predictions and data collection, a Kalman filter for each bounding box continually updates with the current position of the midpoint of the bottom edge of each bounding box. With the path of this point being fed to the Kalman filter, the Kalman filter can then predict, in a linear fashion, the future positions of this point (Welch and Bishop, 2006). This point serves two purposes. Its first purpose is as a reference from which the bounding box can be reconstructed when the object is lost. If an object is a particularly difficult detection or if an object is temporarily occluded, all tracked points can be lost. In a short time, if a new detection is found which matches the predicted position of a lost track, we can say with some confidence this is the same object. The Kalman filtered point's second purpose will be discussed in the next subsection. Variations of an extended Kalman filter could be implemented for more advanced predictions (Simon, 2006), but because the confidence of an object reappearing drastically reduces quickly in most scenarios we presented, the computationally light basic Kalman filter was used.

3.3 Homography-based Speed Estimation

Speed estimation lies at the summit of this algorithm. Although the large push for autonomous vehicles has caused greatly accelerated advancements in computer vision, speed estimation and 3D scene recreation have continued to be very challenging topics. More and more complex techniques for data collection such as lidar and multi-camera systems have come to the forefront of depth perception research, but many of these techniques are expensive, inaccessible, or too invasive a solution in certain environments with certain constraints. There is a need to create a robust speed estimation algorithm that needs very minimal information to work reliably.

The biggest hurdle in speed estimation with a single camera is projecting a 3D scene from a 2D representation, i.e. an image, in a meaningful way to then gather speed. Many ways of doing this have the basic requirement of knowing the camera's extrinsic parameters such as pose and height. In many scenarios, extrinsics like this are unknown and difficult to find. Making the simple assumptions that 1) the ground in the scene is flat and 2) the objects you are tracking are moving along the ground, planar homography can be used to shift the perspective of the image in a way which speed can then be extracted. Homography is a bijective isomorphism of a projective space. Homography is traditionally used for image rectification and computation of camera motion between images.

The question then arises, how do we find the homography transform of an image in order to find the speed of vehicles and the like? First, a set of points parallel to the ground plane is needed with known mappings to real-world distances. Keeping in mind the primary goal in this paper is to monitor vehicle speed, points from passing vehicles can be collected and used as the foundation for a homography matrix derivation. In this work, four corners of a passing vehicle, where the headlights and tail lights are located, were manually picked during the initialization of the algorithm. Lastly, using these points along with the average dimensions of a vehicle, we were able to consistently produce an image transformation productive for speed estimation utilizing planar homography in MATLAB (Corke, 2017). Assuming the ground is relatively flat, the transformed image acts essentially as a Bird's Eye View where pixel-wise distances on the same plane as the ground are known. For each object, the midpoint of the bottom bounding box edge, where the vehicle meets the ground plane, discussed in section 3.2 can be processed though the homography transformation matrix. The changes in the position of the now transformed midpoints can then be mapped to real world distances. The homography matrix H transforms the set of points (x_1, y_1) to set of points (x_2, y_2) .

$$H = \begin{bmatrix} h_{11} & h_{12} & h_{13} \\ h_{21} & h_{22} & h_{23} \\ h_{31} & h_{32} & h_{33} \end{bmatrix}$$
(1)

$$\begin{bmatrix} x_1 \\ y_1 \\ 1 \end{bmatrix} = H \begin{bmatrix} x_2 \\ y_2 \\ 1 \end{bmatrix} = \begin{bmatrix} h_{11} & h_{12} & h_{13} \\ h_{21} & h_{22} & h_{23} \\ h_{31} & h_{32} & h_{33} \end{bmatrix} \begin{bmatrix} x_2 \\ y_2 \\ 1 \end{bmatrix}$$
(2)

$$x'_{2}(h_{31}x_{1} + h_{32}y_{1} + h_{33}) = h_{11}x_{1} + h_{12}y_{1} + h_{13} \quad (3)$$

$$y_2'(h_{31}x_1 + h_{32}y_1 + h_{33}) = h_{21}x_1 + h_{22}y_1 + h_{23} \quad (4)$$

8 degrees of freedom can safely be enforced by setting h_{33} to 1:

$$x_2' = \frac{h_{11}x_1 + h_{12}y_1 + h_{13}}{h_{31}x_1 + h_{32}y_1 + 1}$$
(5)

$$y_2' = \frac{h_{21}x_1 + h_{22}y_1 + h_{23}}{h_{31}x_1 + h_{32}y_1 + 1}$$
(6)

From this derivation, further corresponding sets of points can be included to fit a homography matrix to all points. The corners of a reference vehicle and the



Figure 1: A sample image from a dataset showing detected, tracked, and speed estimates of various vehicles' sizes. In the lower right corner, two of the camera sensors used in experiments with self-owned vehicle are shown.

average dimensions of a vehicle where used to compute the transformation matrix of the image. Thus, having computed the homography matrix, the following equation (7) is used to estimate the speed between consecutive frames:

$$v(t) = \frac{\Delta s}{\Delta t} = \frac{ds}{dt} \tag{7}$$

where Δt is given by the extracted frame rate of the camera. With an appropriate camera angle paired with YOLO's ability to distinguish between cars, trucks, and buses, semantic segmentation (Jégou et al., 2017) and optical flow techniques could be used to automate point acquisition during the initialization process, and, further, repeatedly find transformations from passing vehicles, allowing for a further rectified transformation matrix over time, or even allow for a moving camera (Diamantas and Alexis, 2020), (Diamantas and Alexis, 2017).

In Fig. 1 various detected and tracked vehicles (passenger cars, trucks, large trucks) along with their estimated speed is shown. In the lower right corner the sensors (FLIR *Blackfly* and Intel *Realsense* D455) used for the experiments are also depicted.

4 EXPERIMENTS AND RESULTS

The following figures present experimental work with videos taken from datasets as well as videos created with a self-owned vehicle that served as a ground truth to compute the error in estimated speeds. Figure 2 shows the output of the algorithm using datasets with different videos. Each column contains vehicles going in different directions. This algorithm is robust to scale as well as to motion direction of vehicles. Figure 3 shows images with a self-owned vehicle and a known speed. The error has been estimated to be as low as 0.3 km/h and as high as 7.5 km/h in some few



Figure 2: Output of proposed algorithm. Speed estimations of a number of vehicles with various sizes moving into different directions validate the effectiveness of our proposed algorithm. Videos from different data sets have been used in this set of experiments.

instances. In most experiments the error is between 3-5 km/h. Figure 4 images have been taken using a smartphone camera. In this experiment, the error lies within the afore-mentioned range. The resolution of frames varies with most videos having a resolution of 1920 × 1080 and in one case, a resolution of 2560×1920 (Fig. 2, last row). The frame rate varies between 10 fps and 50 fps. In all different settings our algorithm performed remarkably well. The source code of our approach is available at *Github*¹. Several videos with the output of our algorithm can be found on our *YouTube* channel².

5 CONCLUSIONS AND FUTURE WORK

In this research, we have presented an algorithm for detecting, tracking, and estimating the speeds of multiple vehicles. In particular, this method comprises of several sub-algorithms, at first a neural network algorithm, based on YOLOv4, detects multiple vehicles on the highway which in turn serves as input to a multiple-object tracker based on the KLT algorithm. Using the homography matrix, which is computed only once based on the mean dimensions of passenger vehicles and the four corners of any passenger vehicle at the beginning of our video, we are able to estimate and track the speed of all vehicles for the entire duration of the video. This algorithm requires only a single feature from any vehicle to be tracked in order to infer its speed. The algorithm is, thus, computationally cheap yet it provides accurate estimates of vehicles' speeds irrespective of the direction of motion of vehicles or their size. The results validate our algorithm which is tested on a series of known datasets as well as compared with ground truth data.

The vehicle corner-based homography derivation could be expanded in a number of ways. One significant development would be automating the corner collection and repeatedly applying it. This would eliminate any initialization procedure, and allow for a homography derivation which improves with time. With some modulation, the methods of this work could be expanded and applied along with automated corner collection of vehicles to not only provide much more accurate speed estimation, but also allow for speed estimation from a moving camera with very minimal assumptions.

Currently, we are developing methods to detect vehicles using semantic segmentation which will provide an even more accurate estimate of the homography matrix. As a future work, we plan on testing future iterations of this algorithm on a moving vehicle with the aim to estimate the time to collision as well as to run our algorithm on a parallel processor

¹https://github.com/TSUrobotics/SpeedEstimation

²https://www.youtube.com/channel/ UCeyQfeblSg2eyX2gGSUpIOw



Figure 3: Output of proposed algorithm. In these set of images controlled experiments have been carried out with a self-owned vehicle with the view to estimate the error.



Figure 4: Output of proposed algorithm. Images are taken by a smartphone camera and a self-owned vehicle is driven with the view to estimate the error.

platform. Moreover, we plan on combining the current approach with optical flow techniques with the view to provide more robust results especially in scenarios where a vehicle is stopped and a small amount of speed is estimated with the proposed algorithm. Finally, we plan on implementing this approach on an Unmanned Aerial Vehicle (UAV) and use thermal camera imaging to infer speeds at night.

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