Classification Scheme for the Concrete Syntax of Graph-like Modeling Languages for Layout Algorithm Reuse

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Abstract: Graph-like modeling languages (GLML) are deployed in various domains. In model-based software engineering they are used directly or indirectly for the development of software. In different engineering systems, graph-like models are artifacts (circuit diagrams, energy flow diagrams) of the respective domain, which serve as input for downstream specialized applications (simulators, optimizers). When developing modeling tools, the concrete syntax of a language for creating, editing, and understanding models is immensely important. In order to develop tools with good usability, layout algorithms for the used languages have to be integrated. The development of these layout algorithms is particularly complex. With graph drawing there is a specialized field that deals with the development of layout algorithms for graphs. Some of these algorithms can be used for the layout of GLML or be adapted for GLML. In order to allow the reuse of layout algorithms and their assignment to a certain class of GLML, a classification scheme for the concrete syntax for GLML is presented in this paper.

1 INTRODUCTION

Abstract models and modeling languages are used in software engineering and classical engineering sciences to describe systems. Graph-like languages were introduced as suitable modeling tools as early as the turn of the 20\textsuperscript{th} century. Many inventions in the field of electricity were published in patent specifications using graph-like visualizations e.g., (Tesla, 1901). The prevalence of computer technology and especially the propagation of model-based design (MBD) have increasingly led to the rise of GLML in the sciences.

The concrete syntax of a language is of utmost importance for the understanding of the language (Karsai et al., 2009). In this context, the comprehensibility of modeling languages strongly depends on the modeling skills of the users. The users deploying model based software development (MBSD) are typically software engineers with experience in abstract languages (e.g., programming languages) and general purpose modeling languages (GPML) like UML. In model based engineering (MBE) the users are often classical engineers with little modeling experience. They are supported by domain-specific languages (DSL).

Another important aspect is the usage of the created models. Applications that only need a single model to be generated do not have high demands on the usability of the modeling process. But when models are created and edited frequently, the modeling itself becomes an important part of the user’s work. This is then linked to high demands regarding usability, comparable to the demands of UI/UX design.

To meet these requirements, modeling tools have to offer algorithms both for drawing of and interacting with the GLML.

The layout of GLML is complex compared to the concrete syntax of textual languages. Although graph drawing is the specialized field that is concerned with the visualization of graphs, it has not systematically been applied in MBD yet (Binucci et al., 2019). There are two reasons for this. On the one hand, the
automatic drawing of graphs is less important than the implementation of layout algorithms and interaction methods that support the creating and editing of models. Here aspects such as dynamic graph drawing and layout stability are more important than static graph drawing. On the other hand, graphical models within the scope of MBD are structurally very varied. They differ from the classic, simple graph model consisting of vertices and edges. Graph models in MBD can be port graphs, hyper graphs, nested graphs, and labeled graphs. In this paper, these models are encapsulated in the term graph-like.

The multitude of different graph models, which are often defined in the concrete syntax of the metamodels for GLML, and the different use cases for layout procedures complicate their reuse and adaptation considerably. Reuse and compatibility (of languages) are two of the TOP 10 challenges faced in MDE artifact sharing (Damasceno and Strüber, 2021). Typical artifacts in MDE include models, metamodels, model transformations, and modeling tools. In addition, for widely used languages, especially GPML, the concrete syntax is defined only very superficially, even though it should be an important part of the language. For UML 2.5.1, the specification takes up just 20 of 754 pages of documentation (OMG UML 2.5.1). A major shortcoming is that for many languages there is de-facto no sufficient definition of the concrete syntax to provide state-of-the-art layout algorithms.

This paper presents a classification scheme for the concrete syntax of GLML. This provides the possibility to assign layout algorithms not to a specific language or tool, but to a class of modeling languages according to the classification scheme. A classifier provides developers with the ability to more effectively use existing layout procedures, which may be grouped in libraries (e.g. the Eclipse Layout Kernel (Eclipse Foundation, 2021)), for the layouting of GLML. In particular, if layout procedures can be used via parameters for the layout of different concrete syntaxes, classifiers enable the mapping between GLML and layout procedures. This facilitates the reuse and adaptation of layout algorithms and greatly simplifies tool development.

The proposed classification scheme does not claim to be exhaustive. It will be continuously extended in further work.

Chapter 2 of the paper presents a metamodel for GLML. The metamodel describes the essential model elements, for which features are listed in the classification scheme. In chapter 3, the classification scheme is detailed. Using the examples of the classical graph model, a GPML, and a DSL, Chapter 4 applies the classification scheme and assigns corresponding layout algorithms. Chapter 5 describes the state of the art and Chapter 6 gives a short outlook on further work.

2 FEATURES AND METAMODEL OF GLML

Figure 1 shows a possible metamodel for GLML. The essential model elements are nodes, ports, edges, labels, and symbols. Nodes, ports and edges have a graphical expression (symbol) and thus reflect domain-specific semantics. This makes the model elements distinguishable and recognizable. The symbols are irrelevant for layout procedures and are not part of the classification scheme.

![Figure 1: A metamodel for GLML.](image)

Compared to the "classical" graph model, GLML differ in particular in that the edges do not directly connect the nodes and the connection is made via ports that are located on the nodes. Ports for connecting nodes are used in many graphical languages. On the one hand, ports can be specified explicitly, and they can have a graphical or textual form, for example with fixed ports in ladder diagrams and function block diagrams in IEC 61131-3. On the other hand, ports can also be used to specify connection positions of edges to nodes. These ports can have no expression and would then not be recognized as such in the graphical representation.

Nodes are nested in some graphical modeling languages. They in turn contain nodes and edges and can also be connected to them via edges (e.g., UML activity diagrams).

The main classification features for edges are the number of possible edge connections, specifications

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1 In the metamodel in Figure 1, edges must always be connected to ports. To use this metamodel to represent a graph model without ports, each node is assigned exactly one port that has no symbol and is located in the center of the node.
for routing of the edges (straight or orthogonal), and the distinction between directed and undirected edges. On the one hand, hyperedges can be used to visualize the real properties of technical networks, e.g., power grids, and thus to better understand them (Wrobel et al., 2021). On the other hand, hyperedges increase the clarity of, e.g., UML diagrams (Purchase et al., 2001). A language where edges can only be associated with one port is, e.g., IDEF (Menzel and Mayer, 2006; IDEF, 2021).2

Labels describe the other elements in more detail and make them distinguishable and recognizable. Ports must be distinguished from each other, e.g., to ensure that they are connected to valid edges (e.g., in circuit diagrams according to EN 60617-2).

3  CLASSIFICATION SCHEME

Chapter 3 provides a classification scheme for GLML. The first subchapter introduces the notation of the scheme and the following subchapters describe the classifiers for nodes, ports and edges of GLML.

3.1 Notation

The notation of the classification scheme is based on a classification for assembly line balancing problems (Boysen et al., 2007). The concrete syntax of a GLML is described by a 3-tuple \( (\alpha, \beta, \gamma) \), where \( \alpha, \beta, \) and \( \gamma \) are vectors. The vectors

\[
\alpha = \begin{pmatrix}
\alpha_1 \\
\vdots \\
\alpha_i \\
\vdots \\
\alpha_j \\
\end{pmatrix}, \quad \beta = \begin{pmatrix}
\beta_1 \\
\vdots \\
\beta_i \\
\vdots \\
\beta_j \\
\end{pmatrix}, \quad \gamma = \begin{pmatrix}
\gamma_1 \\
\vdots \\
\gamma_i \\
\vdots \\
\gamma_j \\
\end{pmatrix}
\]

describe the classifiers for vertices (\( \alpha \)), ports (\( \beta \)), and edges (\( \gamma \)). The description of the classifiers is in terms of vectors, because GLML can have different vertex types (\( \alpha_i \)), port types (\( \beta_i \)), and edge types (\( \gamma_i \)).

Each type is described by a set of classifiers, so that:

\[
\alpha_i = \{\alpha^1_i, \alpha^2_i, \alpha^3_i, \alpha^4_i\} \quad \text{for each vertex type,}
\]

\[
\beta_i = \{\beta^1_i, \beta^2_i, \beta^3_i, \beta^4_i\} \quad \text{for each port type, and}
\]

\[
\gamma_i = \{\gamma^1_i, \gamma^2_i, \gamma^3_i, \gamma^4_i\} \quad \text{for each edge type.}
\]

To keep the classifiers as short as possible, default classifiers are marked with the symbol \( o \) in the classification scheme, as in (Boysen et al., 2007). These can be omitted when using the classifiers.

An asterisk (\( * \)) after a classifier means that a subset (without \( o \)) of the specified classifiers is used for classification; without the \( * \), exactly one classifier applies.

All classifiers are unique so that their feature assignment can be omitted.

3.2 Vertex Classification

Nesting Restriction \( \alpha^1_i \in \{o, nested\} \)

\[
\alpha^1_i = o \quad \text{Non-nested vertices.}
\]

\[
\alpha^1_i = nested \quad \text{Nested vertices.}
\]

Orientation Restriction \( \alpha^2_i \in \{o, rot^\phi, ref^a\} \quad * \)

\[
\alpha^2_i = o \quad \text{No rotation or mirroring allowed.}
\]

\[
\alpha^2_i = rot^\phi \quad \text{Rotation of the vertex by degree } \phi \quad * \]

\[
\phi = a; \text{ no rotation } (\phi = 0^\circ),
\]

\[
\phi; \text{ rotation to the horizontal.}
\]

\[
\alpha^2_i = ref^a \quad \text{Mirroring of the vertex allowed:}
\]

\[
a = h; \text{ horizontal mirroring allowed},
\]

\[
a = v; \text{ vertical mirroring allowed,}
\]

\[
a = hv; \text{ horizontal and vertical mirroring allowed.}
\]

Label Position \( \alpha^3_i \in \{o, l_free, l_ref\} \)

\[
\alpha^3_i = o \quad \text{No vertex label.}
\]

\[
\alpha^3_i = l_free \quad \text{Arbitrary placement of labels.}
\]

\[
\alpha^3_i = l_ref \quad \text{Placement of labels is fixed.}
\]

Label Orientation \( \alpha^4_i \in \{o, l_rot, l_ref\} \quad * \)

\[
\alpha^4_i = o \quad \text{No rotation or mirroring allowed.}
\]

\[
\alpha^4_i = l_rot \quad \text{Rotation of the label by degree } \phi \quad * \]

\[
\phi = a; \text{ no rotation } (\phi = 0^\circ),
\]

\[
\phi; \text{ rotation to the horizontal.}
\]

\[
\alpha^4_i = l_ref \quad \text{Mirroring of the label allowed.}
\]

As a result, many algorithms exist and it is difficult for developers to assign existing procedures to a concrete task (reuse).

2 Angles are always assumed to be positive clockwise.

3 This does not mean mirrored writing, but rather “readable from below/top”.

4 Using the metamodel from Figure 1 to visually represent edges connected only by a port, a symbolless pseudo node with a symbolless port must be created.

5 A communality between assembly line balancing problems and the layouting of GLML is that although there is a family of related tasks, the concrete use cases of these tasks differ concerning parameters and constraints.
3.3 Port Classification

**Position Classification** $\beta^j_i \in \{o, f, s, d, f_j, s_j, d_j \}$

- $\beta^j_i = o$ No ports. As in the classical graph model, nodes are directly connected via edges.
- $\beta^j_i = f$ Ports can be arbitrarily placed on the shape of a vertex.
- $\beta^j_i = s$ Ports can be assigned to specific sides of the vertex shape. Ports can then be freely placed on their assigned side. The sides are defined by the directions $d \in \{north, south, east, west\} \ast$, $d = north$; top side, $d = south$; bottom side, $d = east$; right side, $d = west$; left side.
- $\beta^j_i = d$ Ports can be assigned to multiple allowed sides by enumerating the directions (comma separated).
- $\beta^j_i = fixed_j$ Ports have a fixed position on the vertex shape.

**Connection Number** $\beta^j_i \in \{o, n^j_i\}$

- $\beta^j_i = o$ Exactly one edge allowed.
- $\beta^j_i = n^j_i$ Ports can connect to $n$ edges. The qualifier $q$ specifies:
  - $m = o$; exact number,
  - $m = max$; maximum number,
  - $m = min$; minimum number.

**Port Direction** $\beta^j_i \in \{o, in, out\}$

- $\beta^j_i = o$ No port direction.
- $\beta^j_i = in_j$ Input port.
- $\beta^j_i = out_j$ Output port.
- $\beta^j_i = con_j^j$ Connection port on nested vertices.

The direction of the edges connected on this port is classified by:
- $d = o$; No port direction.
- $d = in-out$; Input port from outside and output port from inside.

**Label Position** $\beta^j_i \in \{o, l_free, l_{ref}\}$

- $\beta^j_i = o$ No port label.
- $\beta^j_i = l_{free}$ Arbitrary placement of labels.
- $\beta^j_i = l_{ref}$ Placement of labels is fixed.

**Label Orientation** $\beta^j_i \in \{o, l_{rot}^\phi, l_{ref}\}$

- $\beta^j_i = o$ No rotation or mirroring allowed.
- $\beta^j_i = l_{rot}^\phi$ Rotation of the label by degree $\phi$: $\phi = o$; no rotation ($\phi = 0^\circ$).
- $\beta^j_i = l_{ref}$ Label can be mirrored.

3.4 Edge Classification

**Structure** $\gamma^j_i \in \{o, hyper^n, one\} \ast$

- $\gamma^j_i = o$ Port to port connection. An edge is connected to exactly two ports.
- $\gamma^j_i = hyper^n$ An edge can connect to multiple ports. The multiplicity of ports is specified as $m$ with $m \in \{o, ItoN\} \ast$.
  - $m = o$; $m$ to $n$ relation.
  - $m = ItoN$; $l$ to $n$ relation.
  - A 1 to $n$ relation implies, that the edge is directed ($\gamma^j_i = dir^l$) and either source or sink are connected to a single port.
- $\gamma^j_i = one$ Edge is connected to exactly one port.

**Routing** $\gamma^j_i \in \{o, ort, k-lin^{\phi^6}, polys\}$

- $\gamma^j_i = o$ Straight routing without bends.
- $\gamma^j_i = ort$ Orthogonal routing, only horizontal or vertical line segments.
- $\gamma^j_i = k-lin^{\phi^6}$ Routing of line segments whose angles to each other have an integer multiple of $360^\circ/2k$, for example:
  - $f = 2$; orthogonal,
  - $f = 3$; hexagonal,
  - $f = 4$; octolinear.

The rotation angle of the routing relative to the horizontal is $\phi$.

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6 An extension of the classifier so that a fixed, maximum or minimum number of edge connections is specified is conceivable. However, the authors do not know of any graphical language that meets these criteria at this time.

7 So-called $k$-linear maps (cf. Nickel and Nöllenburg (2019)) occur mainly in transportation maps, and the octolinear routing ($\gamma^j_i = k-lin^{\phi^6}$) is the de-facto standard for such diagrams (cf. Wu et al. (2020)).
4 EXAMPLES

In this section, the classification scheme presented for the concrete syntax is applied to three examples, a simple graph model, the UML diagram from Figure 1, and a DSL. For the second example, the description of the classification is more detailed.

4.1 Simple Graph Model

For the simple graph model consisting of nodes, (undirected) edges, and no labels, the classification tuple is $(o,o,o)$ or $(||)$ for short.

Figure 2 shows the famous Königsberg bridge problem (Euler, 1735): The vertices A, B, C, and D represent the districts and the edges represent the seven bridges of Königsberg, drawn as a graph according to the classification $(||)$.

![Figure 2: Graph model of the Königsberg bridge problem.](image)

4.2 UML Class Diagram

The UML is very vague in defining the concrete syntax for diagrams. Tool developers are tasked with defining a concrete syntax for diagrams and implementing it in software tools via layout algorithms. The UML class diagram in Figure 1 will be used as an example with the following concrete syntax:

1. Classes should be arranged in such a way that the inheritance hierarchy is taken into account.
2. Hyperedges are to be used for the inheritance relationships.
3. All edges must be routed orthogonally.
4. The ports for the inheritance relationship must be arranged in such a way that the ports on the base classes are placed on the lower outer border and the ports for the derived classes are placed on the upper outer border of vertices.
5. All other ports can be placed freely.
6. Ports of aggregation and association relations have labels (describing the multiplicities).
7. All ports are supposed to be evenly distributed on the outer contour of a node.

This results in the following classifier of vertices, ports and edges for the UML diagram in Figure 1:

**Vertices:** Because the example UML class diagram has only one type of vertex (class), the default features apply, so that $\alpha = o$.

**Ports** can be separated into 5 types:

1. Ports of the base classes to which the edges for the inheritance relation are connected have the following classifier: $\beta_1 = \{side^{out};in\}$.
2. Ports of the derived classes to which the edges for the inheritance relation are connected have the following classifier: $\beta_2 = \{side^{out};out\}$.
3. Ports of the owning classes to which edges for the aggregation relation are connected have the classifier: $\beta_3 = \{free;in;\_\_free\}$.
4. Ports of the not owning classes to which edges for the aggregation relation are connected have the classifier: $\beta_4 = \{free;out;\_\_free\}$.
5. Ports for association relations are classified with $\beta_5 = \{free;\_\_free\}$.

**Edges** can be separated into 3 types:

1. Edges for inheritance relations are orthogonal hyperedges. Their classifier is $\gamma_1 = \{hyper^{out};ort\}$.
2. Edges for aggregation relations are port-to-port connections to be routed orthogonally. Their classifier is $\gamma_2 = \{ort\}$. 

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3. Edges for association relations have the same classifier as aggregation relations:
\[ \gamma_3 = \{\text{ort}_1\} \].

This results in the following classification of the concrete syntax for the UML diagram in Figure 1:
\[
\begin{array}{c}
\text{side}^\text{math} \cap \text{in}_i \\
\text{side}^\text{work} \cap \text{out}_i \\
\text{free} \cap \text{in}_i \cap \text{free}_i \\
\text{free} \cap \text{out}_i \cap \text{free}_i
\end{array}
\begin{array}{c}
\text{hyper}^\text{in}_{i} \cap \text{ort}_i \\
\text{hyper}^\text{out}_{i} \cap \text{ort}_i \\
\text{ort}_2 \\
\text{ort}_3
\end{array}
\]

This classification for a concrete syntax for UML class diagrams can be used to develop suitable layout algorithms or to reuse or adapt existing algorithms. For example, a static automatic layout for this graphical language is provided in (Eiglsperger, 2003), whereas (Helme et al., 2021) provide dynamic layout support for orthogonally routed hyperedges \( \{ \text{hyper}^\text{in}_{i} \cap \text{ort}_i \} \) with topological stability.

4.3 Parameter Map of CAD-Model

The third example is the concrete syntax of a DSL. The model in Figure 3 represents the parametric relationships of a 3D-CAD model of a deep drawing tool. The vertices represent the elements of the CAD model and their hierarchical structure. Identical model components are represented by a thick connection (e.g., the green connection between the occurrences of “punch assembly” in Figure 3). The central vertex of the parameter map represents a specific parametric relationship (here a formula) between input variables (top) and output variables (bottom) (Scheffler et al., 2016).

![Parameter map of a parametric 3D-CAD model for deep drawing tools (Scheffler et al., 2016).](image)

The concrete syntax of the DSL can be described by the following classifier:

All vertices have the default properties of the classifier.

5 RELATED WORK

The concrete syntax of a modeling language is the interface to the modeler. It is thus important for the usability of the language (Karsai et al., 2009), and building editors is a particular challenge for developers (Völter et al., 2013). Their proximity to graphs and the requirements to develop layout algorithms for languages suggest a consideration of graph-drawing.

Graph-drawing methods exist for different classes of graphs. In (Di Battista et al., 1999) a general framework for graph drawing is presented, which contains parts of the features of the presented classification scheme (e.g., port/edge direction \( \beta^3 \) and routing classification \( \gamma^3 \) ). However, the framework is strongly focused on concrete layout aspects (planarity) and properties of graphs (connectivity). Ports, nested graphs, hypergraphs, and labeling are not included in this framework.

For port graphs, an important feature, the port position \( \beta^2 \), is classified as part of the development of layout methods (Schulze et al., 2014).

Problems of labeling were researched intensively in the environment of geographic maps. In (Poon et al., 2004) a model with 9 different possibilities for the placement of axis-parallel enveloping label rectangles is presented. An overview of publications on map labeling is provided by (Wolff, 2009).

Label orientation is also a relevant and widely researched topic in traffic maps. An overview of existing work is provided by (Wu et al., 2020).
Graph drawing represents only one side of the related work: the possible layout procedures for graphical languages to be used in graphical editors. Originating from model driven development (MDD), so-called language workbenches are also to be considered. In language workbenches, the abstract and the concrete syntax as well as the mapping between them is defined as a metamodel (MetaEdit+, 2021; Microsoft DSL, 2021, 2021; OBEOK, 2021; Sirius, 2021; GMF, 2021) and graphical editors for DSLs are generated from it. This is where the challenges arise regarding the development of suitable layout algorithms, which are currently not always well solved for practical applications (Cooper et al., 2021).

Furthermore, there are some languages, especially technical languages, for which the concrete syntax is very precisely defined. These are mainly established modeling languages from engineering science. Their concrete syntax is more precisely specified, e.g., in the form of a standard (USAS Y14.15-1966; IDEF, 2021).

The presented classification scheme distinguishes nodes, ports, edges, labels, and symbols as the most important model elements. These model elements are explicitly included in several metamodels (Pellow and Simeonov, 1989; Wrobel et al., 2007; Barzdins and Kalnins, 2016; Eclipse Foundation, 2021), but the authors are not aware of any classification scheme for the concrete syntax of GLML.

6 CONCLUSION AND FURTHER WORK

Layout is an important component of the usability of a GLML. Good layout algorithms enable even users with limited modeling experience to build, modify, and understand complex models. GLML appear in the form of both GPML and DSL. They are important artifacts in MBD tools and technical engineering tools. For graphs, there are very many layout methods that have been adapted for GLML, especially for static drawings. The large variety of structurally different GLML makes the development, reuse, and adaptation of graph drawing algorithms very costly for tool developers. In modeling tools, dynamic layout algorithms are of greater importance compared to static layout algorithms, although their development is underrepresented in graph drawing.

With the developed approach for the classification of concrete syntax, the presented classification scheme offers the possibility to better relate GLML and layout methods. This facilitates tool development for MDD. It is an important contribution to the reuse of layout algorithms and intra-language compatibility of GLML, one of the current challenges in MDE.

The presented classification will be continuously extended in further work. Aspects of automatic node placement, for which there are a number of classical static graph drawing methods and adaptations for GLML, are currently not present in the classifier. In particular, for GLML where model visualization rather than model building is the focus of a tool, the inclusion of placement can be valuable.

Furthermore, model-to-model transformations between GLML with distinct classifiers are to be investigated. With the help of these model-to-model transformations, layout methods of another class can be reused for a GLML. Further possible next steps would be to classify existing languages (e.g., GPML) and layout methods according to the presented features in order to facilitate mutual mapping.

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9 The DSL in the example of chapter 4.3 is a GLML that is automatically generated to show relations inside a 3D-CAD model.
Classification Scheme for the Concrete Syntax of Graph-like Modeling Languages for Layout Algorithm Reuse


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