

A Control Engineering Framework for Quadrotors: An Application for the Crazyflie 2.X

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Keywords: Non-linear Systems, Autonomous Robots, Control Laboratories, Crazyflie 2.X, Control Education.

Abstract: In this work, a new framework to develop and investigate new control algorithms in quadrotors is presented. The proposed system includes two main elements: 1) a simulation laboratory and 2) a real environment based on the Crazyflie 2.X quadcopter. Both elements offer all the necessary tools to design and implement a wide variety of controllers in the real system. The phases to carry out the controller's designs and how to apply them to the real quadrotor are explained in detail. A practical application to check the proposed framework and some additional experiments have been investigated in depth. The simulation and experimental results corroborate the validity of the proposed framework.

1 INTRODUCTION

In recent years, the industry and the scientific community are showing a growing interest in robotics. Robots are becoming more and more prevalent in industries such as manufacturing, medical, space, automotive, etc. They have a crucial role in dangerous, routine or high accuracy tasks. The use of aerial robots is increasing rapidly in both scientific and commercial fields. In fact, it has been one of the areas where the researchers have focused their efforts. The quadrotor architecture has been chosen in many research groups for its low dimension, simple mechanisms and good manoeuvrability. However, controlling a quadrotor is not easy because of the coupled dynamics and its commonly under-actuated design configuration (Mahony et al., 2012). In addition, the quadrotor presents a highly non-linear dynamics and several uncertainties during its missions (Lee et al., 2013). These facts make flight control an interesting research area.

A large number of techniques are proposed in the literature: one of the most used techniques is the PID control strategy. This control method has a good performance in this kind of problems and the control laws can be implemented in a simple way (Zhou

et al., 2017). The Linear Quadratic Regulator (LQR) provides optimal feedback gains to enable the stability and the high performance of the closed-loop system (Zhang et al., 2016). The Lyapunov techniques guarantee, under certain conditions, the asymptotical stability of the quadrotor (Safaei and Mahyuddin, 2016). When there are parametric uncertainties or it is difficult to model the dynamic of the system, the adaptive control methods provide a good performance (Andrievsky et al., 2005). Backstepping control techniques guarantee the stability of the quadrotor, but a lot of computation is required (Fan et al., 2017). If the dynamic feedback control is used, it allows to transform the dynamic of the quadrotor into a linear system and the fly movements can be decoupled (Taniguchi et al., 2014). In environments where GPS (Global Positioning Systems) signal is not available, the visual feedback control techniques are the most popular solutions (Shirai et al., 2017). Other techniques such as fuzzy logic (Wahyunggoro et al., 2016) or neural networks (Emran and Najjaran, 2017) are being lately used to solve these control problems.

From the research and control point of view today many researchers focus on designing new control strategies that use quadrotors platforms. Whatever control technique is used, its validation is usually performed through simulations, since performing experiments over real platform requires much effort. Moreover, most of the developed platforms may be difficult to replicate and not be directly available

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to other research groups. Recently, a nano quadrotor low-cost platform has been developed (Giernacki et al., 2017). Crazyflie is an open-source and open-hardware project which is supported by a very active community where the software and the projects are accessible and many applications for developing are available.

In this paper, a new framework that provides great flexibility for investigating and developing new control techniques for quadrotors, and more specifically for Crazyflie 2.X, is presented. Our proposal includes methodologies and tools to validate the control tasks, in such a way that the presentation of real results will be an enhancement to the theoretical contributions. Using the framework all the stages of development, from the design of the controllers to the final adjustment in a real environment can be carried out. In contrast to other works such as (Giernacki et al., 2017), the aim of this paper is to provide a step by step guide to have the platform ready so that researchers, engineers and students can easily develop and test new control algorithms for Crazyflie 2.X and, if desired, add new layers on the top of the developed tools easily.

The paper is organized as follows. Section 2 includes an overview of the Crazyflie 2.X platform (Giernacki et al., 2017). In section 3, the control scheme of the system is shown. The new control engineering framework is described in section 4. In section 5, a practical application is investigated including simulation and experimental results. Finally, the conclusions and future work are discussed.

2 OVERVIEW OF THE DYNAMIC MODEL OF THE QUADROTOR

To define the dynamic model of the Crazyflie 2.X, some hypothesis have been taken into account: the aircraft is a rigid body with a constant mass and the geometry and the propulsion are symmetrical. This vehicle has six degree of freedom: the position of the CG (Center of Gravity) of the aircraft with respect to the inertial frame ($\mathbf{P}_{CG} = \{x, y, z\}$) and the orientation of the quadrotor which is described by the Euler angles ($\Phi = \{\phi, \theta, \psi\}$). These angles, the roll ϕ , the pitch θ and the yaw ψ represent the rotation of the body frame with respect to the inertial frame. The position and the orientation of the drone are depicted in Figure 1.

The state of the system can be obtained taking into account the mechanical classical laws of motion. The angular speeds of the body frame (p, q, r) are described by (1)-(3),

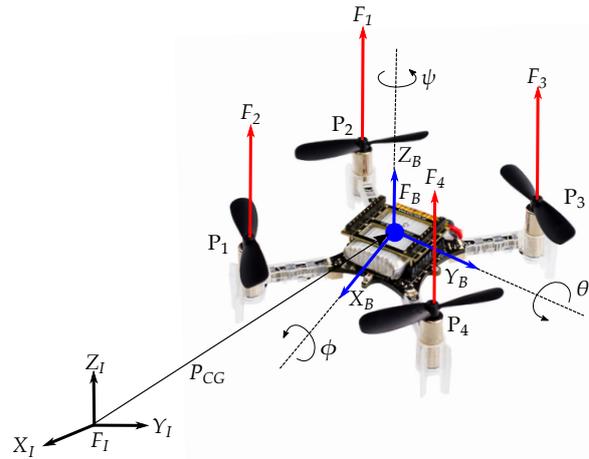


Figure 1: Position $\mathbf{P}_{CG} = \{x, y, z\}$ and orientation $\Phi = \{\phi, \theta, \psi\}$ of the quadrotor.

$$\dot{p} = \frac{1}{I_{xx}} (qr(I_{yy} - I_{zz}) + M_x) \quad (1)$$

$$\dot{q} = \frac{1}{I_{yy}} (rp(I_{zz} - I_{xx}) + M_y) \quad (2)$$

$$\dot{r} = \frac{1}{I_{zz}} (pq(I_{yy} - I_{xx}) + M_z) \quad (3)$$

where M_x , M_y , and M_z are the momentums defined by (4)-(6)

$$M_x = \frac{dC_T}{\sqrt{2}} (-\Omega_1^2 - \Omega_2^2 + \Omega_3^2 + \Omega_4^2) \quad (4)$$

$$M_y = \frac{dC_T}{\sqrt{2}} (-\Omega_1^2 + \Omega_2^2 + \Omega_3^2 - \Omega_4^2) \quad (5)$$

$$M_z = C_D (-\Omega_1^2 + \Omega_2^2 + \Omega_3^2 - \Omega_4^2) \quad (6)$$

where d denotes the distance from the CG to the center of each motor, C_T is the thrust coefficient that represents the upward force generated by each propeller where $F_i = C_T \Omega_i^2$ (Ω_i is the angular speed of each propeller) and C_D the aerodynamic drag coefficient, see Figure 1. In these equations the angular accelerations have been neglected because they tend to be small compared to the other terms. On the other hand, the gyroscopic moments have also been neglected due to the inertia moments of the motors tends to be small (Sabatino, 2015). The terms I_{xx} , I_{yy} and I_{zz} denote the inertia moments about its three axes. Based on the hypothesis that the body of the quadcopter is symmetrical around all its axes, all crossed terms (I_{xy} , I_{yz} , etc.) can be considered equal to zero. Then, the Euler angles can be obtained by the integration of the equation (7)

$$\begin{pmatrix} \dot{\phi} \\ \dot{\theta} \\ \dot{\psi} \end{pmatrix} = \begin{pmatrix} 1 & S_\phi T_\theta & C_\phi T_\theta \\ 0 & C_\phi & -S_\phi \\ 0 & \frac{S_\phi}{C_\theta} & \frac{C_\phi}{C_\theta} \end{pmatrix} \begin{pmatrix} p \\ q \\ r \end{pmatrix} \quad (7)$$

where S_i denotes $\sin(i)$, C_i represents $\cos(i)$ and T_i means $\tan(i)$ with $i = \{\phi, \theta, \psi\}$. And, the position of the CG of the quadrotor with respect the inertial frame is obtained by the integration of (8)-(10)

$$\ddot{x} = \frac{F_z}{m} (C_\psi S_\theta C_\phi + S_\psi S_\phi) \quad (8)$$

$$\ddot{y} = \frac{F_z}{m} (S_\psi S_\theta S_\phi - C_\psi S_\phi) \quad (9)$$

$$\ddot{z} = \frac{F_z}{m} (C_\theta C_\phi) - g \quad (10)$$

where $F_z = \sum F_i$, m is the total mass of the aircraft and g the acceleration of gravity (9.81 m/s^2). In (Luis and Ny, 2016) more details of the dynamic model of the Crazyflie 2.X are presented. Finally, in (Förster, 2015) an exhaustive work has been done to identify the main parameters of Crazyflie 2.X.

On the other hand, linearisation is useful to design a control system using linear classical design techniques. It also allows to analyse the system characteristics such as system stability, disturbance rejection, and reference tracking. Considering the Crazyflie 2.X as it was analysed in (Luis and Ny, 2016), the trim point is $F_z = mg = 4C_T \Omega_e^2$, it means that the drone is hovering at constant altitude. Taking into account this assumption, the equilibrium propeller speed is

$$\Omega_e = \sqrt{\frac{mg}{4C_T}} \quad (11)$$

Once the linear model is obtained the flight modes can be decoupled. In this case, four models can be obtained: vertical, directional, lateral and longitudinal.

3 QUADROTOR'S CONTROL SCHEME

The control architecture for the Crazyflie 2.X or for similar quadrotors is depicted in Figure 2 (Landry et al., 2015). It is divided in two groups: the on-board controllers inside the drone and the off-board controllers that are implemented in external systems such as a PC. The communication between these two groups, the on-board and the off-board controllers, is made by a radio interface of 2.4 GHz. There is a modem in the drone side and the crazyradio PA in the PC side. Over this radio link, the Sensor Information $\mathbf{SI} = (z, \phi, \theta, \psi, p, q, r)$ and the Control Commands $\mathbf{CC} = (\Omega, \phi_r, \theta_r, r_r)$ are interchanged. In this architecture, the input Ω in the control mixer denotes the thrust. This kind of robots needs high frequency control to get a stable flight. For this reason, the on-board controllers are required. In this architecture, the rate

controller works with 500 Hz and the attitude controller with 250 Hz. The set of on-board controllers is composed by the control mixer, the rate controller and the attitude controller, these controllers are implemented in the firmware of the drone Crazyflie 2.X.

The rate controller and the attitude controller are implemented by discrete-time PID controller (12)

$$u_k = K_p e_k + K_i \sum_{n=1}^k e_n + K_d [e_k - e_{k-1}] \quad (12)$$

where u_k is the control signal, e_k the error signal and K_p , K_i and K_d are the controller's gains. In the firmware of the Crazyflie 2.X the gains for the rate and for the attitude controllers are defined.

The Control Commands \mathbf{CC} are used to set the references for the on-board controllers. On the other hand, the Sensor Information \mathbf{SI} can be obtained with a maximum frequency of 100 Hz. This is the main reason why the rate and the attitude controllers cannot be implemented outside the drone. Finally, in the off-board controllers, the altitude, x-y position (if additional sensors are included to get the x and y coordinates) and yaw position controllers can be implemented using the \mathbf{SI} and the \mathbf{CC} .

4 THE NEW CONTROL ENGINEERING FRAMEWORK

The framework proposed in this work is based on the control architecture of the Crazyflie 2.X. This framework will help to develop quadrotor control techniques (see Figure 3). With methodologies and tools included in it, the researchers and students will be able to investigate and develop new control techniques applied to these types of aircrafts. This new framework offers the necessary tools to undertake all the stages of development, from the design of the controllers to the final adjustment in the real environment. The proposed framework is composed of two main elements: 1) a simulation laboratory based on Matlab/Simulink tools and 2) The instructions to setup a real-world environment testing area based on the drone Crazyflie 2.X with its hardware and software components.

4.1 Simulation Laboratory

In the simulation laboratory (Figure 3a)) two models of the Crazyflie 2.X are available: the linear and the non-linear model, both elements have been implemented as Simulink blocks. The output is the Sensor Information $\mathbf{SI} = (z, \phi, \theta, \psi, p, q, r)$. The input of the

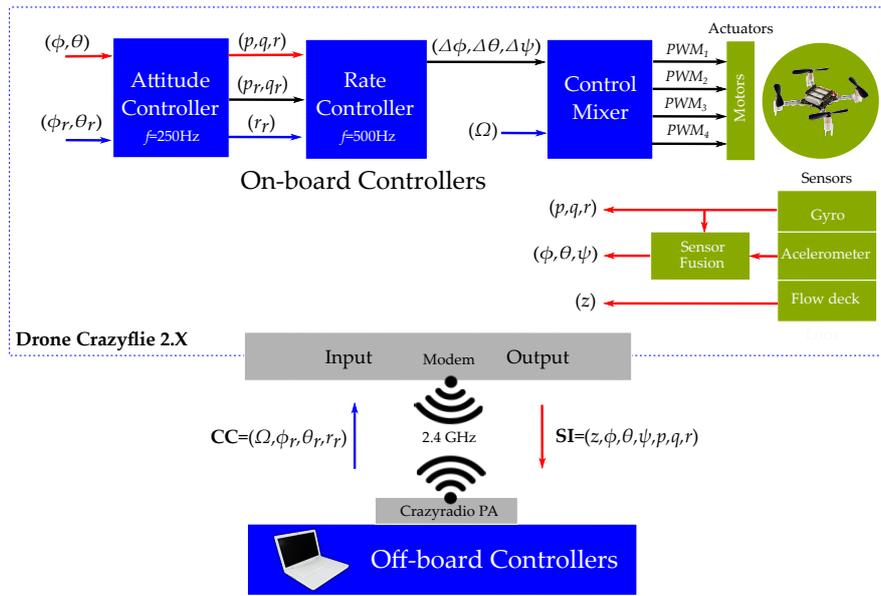


Figure 2: Control architecture of the Crazyflie 2.X.

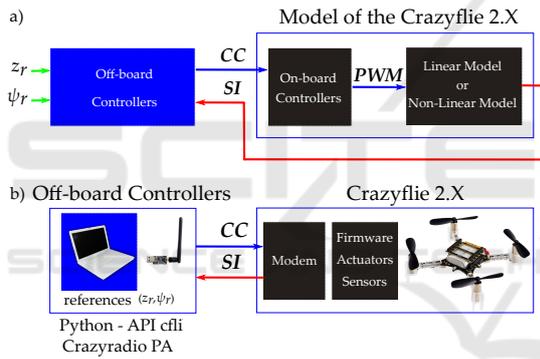


Figure 3: Control engineering framework. a) Simulation laboratory in MatlabTM/SimulinkTM, b) real environment based on the Crazyflie 2.X.

model should be the moments M_x , M_y , M_z and the force F_z , but for practical reasons, it is better to use the motor signals PWM_i . To use these inputs in the models, the following relationship between the variables PWM_i and Ω_i is used (Luis and Ny, 2016):

$$\Omega_i = 0.2685PWM_i + 4070.3 \quad (13)$$

The input of the on-board controllers is the Control Commands $\mathbf{CC} = (\Omega, \phi_r, \theta_r, r_r)$. Finally, some off-board controllers have been defined in the system, these controllers will be described later in the practical application.

4.2 Real Environment

The real environment is composed by a PC with the Crazyradio PA and the drone Crazyflie 2.X including

the hardware flow deck (Figure 3b). The Crazyradio PA is connected to the PC and it allows the radio interface to communicate the PC with the drone. In the PC the off-board controllers are implemented in python scripts based on the API cflib. Using this API a set of commands are available to interact with the drone, some of them for getting the sensor information (logging functionality) and others for sending control commands to the drone. Although python is an interpreted language, the real-time is guaranteed because the sample rate in the radio interface is relatively low.

To get the sensor information \mathbf{SI} the logging functionality of the Crazyflie 2.0 has been used. This feature allows to read the sensor information with maximum frequency of 100 Hz ($sampling_time=0.01s$). Using the API cflib, this task can be implemented in a simple way. Using this methodology to read the sensor information, the noise in these devices can be easily estimated. After calibrating the sensors, the noise in the sensors can be modelled by a normal distribution $N(\mu, \sigma)$, where μ is the mean and σ the standard deviation. In this system $\mu \approx 0$ and σ is presented in Table 1. In order to get more realistic results in the simulation laboratory, these models of the noise will be included in the experiments. To send a control command \mathbf{CC} to the drone the API cflib provides the command `cf.commander.send_setpoint(roll, pitch, yawrate, thrust)` where $roll=\phi_r$ and $pitch=\theta_r$ in degrees, $yawrate=r_r$ in degrees/s and $thrust=\Omega$ a value between 0 and 65,535. With this command is very easy to build many control schemes. For example,

Table 1: Standard deviations (σ) for the noise model of the sensors.

Model variable	σ
z	0.00132 m
ϕ	0.119 $^\circ$
θ	0.180 $^\circ$
ψ	0.149 $^\circ$
p	0.795 $^\circ/s$
q	0.752 $^\circ/s$
r	0.695 $^\circ/s$

to define a PID controller, the algorithm presented in Figure 4 can be used. On the other hand, if an event-based PID controller (Årzen, 1999) is needed the structure in Figure 5 can be implemented. There

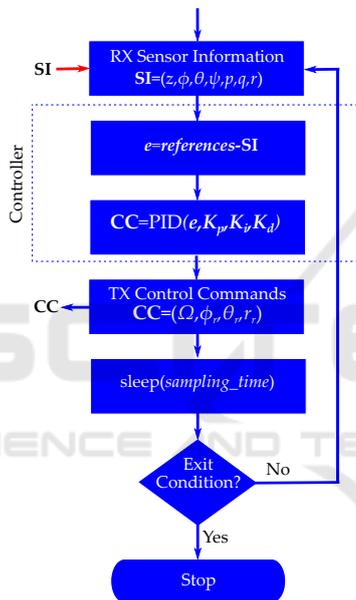


Figure 4: Algorithm for the periodic PID. The error signal e is obtained from the desired setpoint signals $references$ and the SI . In this scheme, $PID()$ denotes a PID controller whose parameters are the error signal e and K_p , K_d , K_i which mean the proportional, integral and derivative terms.

is a wide variety of control techniques that can be used and investigated in depth both in the simulation environment and in the real system.

5 PRACTICAL APPLICATIONS AND EXPERIMENTAL RESULTS

To check the functionality and the uses cases of the presented framework some experiments have been proposed. To investigate the control design capabil-

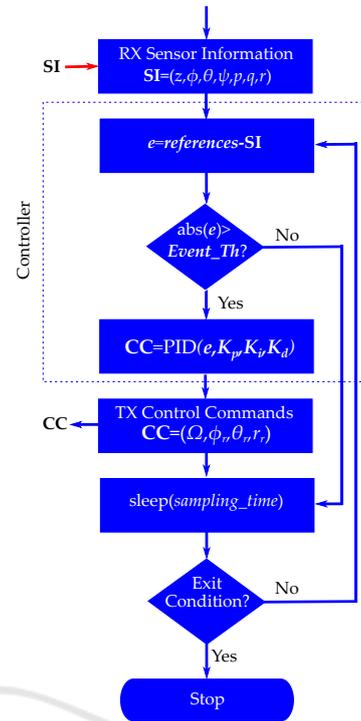


Figure 5: Algorithm for the event-based PID. This structure has similar blocks that the PID controller but includes an addition element called event detector (ED). The ED checks if the error signal e crosses the event threshold $Event_Th$.

ities of the framework, in this experiment, two autopilots have been developed in the off-board controllers. The first autopilot AP1 is an altitude (z) controller and the second one AP2 is a directional (ψ) controller (see Figure 6). These autopilots have been

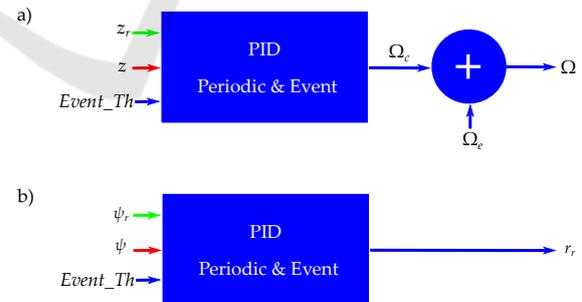


Figure 6: The proposed autopilots. a) AP1: altitude controller, b) AP2: directional controller.

developed by classical periodic PID controllers and by event-based PID controllers. In this way, these two control schemes can be compared. These controllers can work in both modes: periodic PID or event-based PID. On the one hand, when the parameter $Event_Th=0$, the system works in a periodic mode. On the other hand, when this parameter is higher than zero it works as an event-based controller. The ob-

jective of the altitude controller (Figure 6 a)) is the tracking of the reference signal z_r . The output Ω that is set to the on-board controller, it is composed of the output of the PID, Ω_c , and the equilibrium signal Ω_e . The directional controller (Figure 6 b)) uses the reference signal ψ_r and the sensor information ψ to calculate the reference signal r_r for the on-board controller. In this application, the reference signals ϕ_r and θ_r are set to zero because these autopilots allow the hovering of the drone.

To design these controllers, the Matlab Control System Toolbox has been used. With these tools, the controller's gains have been obtained, at the same time, to check the event-based implementation the thresholds *Event_Th* has been set. In (Socas et al., 2015) some methodologies to set event-based controllers have been presented, using these methods the event-based controller can be set in a simple way. In Table 2 the parameters of the designed off-board controllers are shown.

Table 2: Parameters of the off-board controllers.

Parameter	Altitude	Directional
K_p	9,500	40
K_i	0	10
K_d	45,000	25
<i>Event_Th</i>	0.008 m	5°

In the simulation laboratory the linear and the non-linear model of the Crazyflie 2.X have been analysed considering the previous controllers. Once it has been checked that the results of both models are similar, only the non-linear model of the drone has been considered in this work because it is the most realistic one. The experiments last 15s and the two reference signals have been modified. The altitude reference z_r is set to 0.4 m at $t = 0s$ and at $t = 5s$ the yaw reference ψ_r has a slope of 15°/s until it reaches 90° at $t = 11s$. In these experiments, the models of noise presented in Table 1 are also included. The simulation results are depicted in Figure 7. In these figures the results for the periodic controller and for the event-based controller are presented. The designed controllers have similar behaviour and present a good tracking of the reference signals, according to Figure 7 a) and b). The main difference between the periodic and the event-based schemes is the activity of the controllers. In these experiments, the periodic controllers take around 3,000 control actions but the event-based implementation only needs 67% of the control actions than the periodic system (see Figure 7 d)).

In view of these simulation results, the Crazyflie 2.X can be operated safely in the real environment. Once satisfactory results have been achieved in the

simulation setup, the next step is to check the behaviour of these controllers in the real environment. The results obtained in these experiments are shown in the Figure 8. In this case, both controllers have a stable response and present a good tracking of the reference signals (see Figure 8 a) and b)). In the real environment the controllers have to compensate the disturbances that occur during takeoff, the turbulence produced by the drone in the air and the noise in the sensors. These effects are clearly observed in the variable r in Figure 8 c), and also to a lesser extent in the variables z and ψ (see Figure 8). In the simulation models, only the noise of the sensors has been considered. This is a good approach because the real event-based solution and the simulation model generate the same number of events (see Figure 7 d) and Figure 8 d)).

To evaluate the performance of these controllers and also to compare the event-based controllers with respect to periodic classical approaches, the performances indexes introduced in (Sánchez et al., 2009) can be used. In this work, the *IAE* Integral Absolute Error and the N_N ratio of events have been considered. Taking into account the results of the experiments, the performance indexes for these controllers are presented in Table 3.

Table 3: Performance indexes for the altitude and directional controllers.

Altitude Controller	<i>IAE</i> (m)	N_N (%)
Periodic PID	38.34	100
Event PID	39.52	73
Directional Controller	<i>IAE</i> (°/100)	N_N (%)
Periodic PID	28.44	100
Event PID	36.80	59

In these experiments, if the periodic PID controller is considered as the reference, the event-based altitude controller presents better results than the event-based directional controller. In this case, the *IAE* is 39.52 vs. 38.34 for the altitude (3% higher) and 36.80 vs. 28.44 (29% higher). Moreover, regarding the ratio of events N_N the altitude controller reaches a value of 73% while the directional controller obtains 59%. Thus the directional controller shows better results than the altitude controller. The results illustrate that the accuracy of the altitude controller is better than the directional controller. However if the activity is taken into account, the directional controller has a better behaviour than the altitude controller (59% vs. 73% respectively).

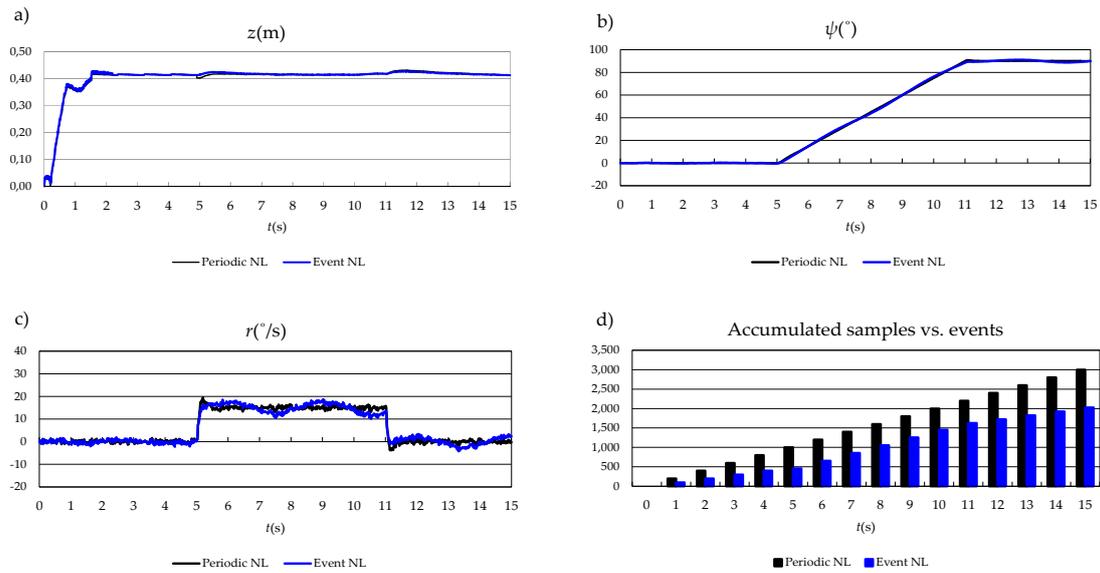


Figure 7: Simulation results for the non-linear model. Black line represents the response for the periodic controller and blue line for the event-based implementation. a) Altitude z , b) yaw ψ , c) yaw rate r and d) accumulated samples vs. accumulated events.

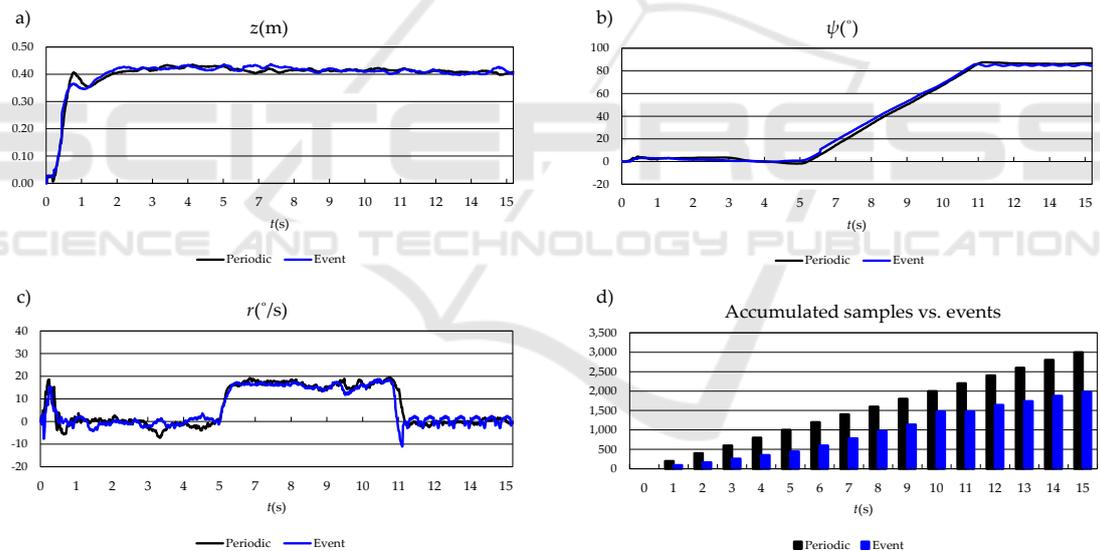


Figure 8: Experimental results. a) Altitude z , b) yaw ψ , c) yaw rate r and d) accumulated samples vs. accumulated events. Black line represents the response for the periodic controller and blue line for the event-based implementation.

6 CONCLUSIONS

A new framework for quadrotor control engineering has been proposed. The two main elements, the simulation laboratory and the real environment offer to engineers and researchers all the tools needed to develop control applications on drone platforms. In this work, the solution has been particularized for the Crazyflie 2.X, but it can be applied to other quadrotors in a sim-

ple way. All elements in the framework have been described in detail and the guidelines to develop control applications for the Crazyflie 2.X have been explained in depth. A practical application to test this new proposal has been investigated. In this case, two autopilots have been designed and analysed in this framework using periodic PID and event-based PID. The simulation and experimental results show that it is very simple to design these controllers using this

approach. Finally, some performance indexes have been introduced to validate the response of the designed controllers.

ACKNOWLEDGEMENTS

This work was supported in part by the Spanish Ministry of Economy and Competitiveness under the Project CICYT RTI2018-094665-B-I00 and the Project CICYT DPI2017-84259-C2-2-R. Also, the Project GID2016-6 supported by UNED.

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