A Very Large Scale Neighborhood Approach to Pickup and Delivery Problems with Time Windows

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Abstract: When solving optimisation problem in the presence of strong constraints, local search algorithms often fall into local minima. One approach that helps escaping local minima is using Very Large Scale Neighborhoods (VLSN). We applied VLSN to the pick-up and delivery problem with time windows (PDPTW). Unfortunately, VLSN can be rather slow: it requires to build a large graph of moves (the VLSN graph) and explore the graph to identify cycles in it. Most of the execution time is spent building the graph. Once a cycle is found, large parts of the graph are invalidated, hence the time spent building these portions of the graph is wasted. We introduce a generic speed improvement of the VLSN algorithm. The idea is to build the VLSN graph gradually and to perform the cycle search regularly throughout the construction of the graph, so that if the searched cycles are discovered, large portions of the graph under construction are not explored at all. Roughly speaking, on a specific standard PDPTW instance (LC1.2.1), only 43% of the graph needs to be built, and the sped up VLSN procedure only takes 53% of time taken by the original one.

1 INTRODUCTION

Pickup and delivery (Dumas et al., 1991) is a classical routing optimization problem where a set of deliverables (goods or people) must be transported from different origins to different destinations using one or several vehicles. The pick-up & delivery with time windows (PDPTW) is a variant where a time window is associated with each pick-up and delivery. We typically want to minimize the distance covered by the vehicles.

Local search is a combinatorial optimization technique that starts with a given solution, and repeatedly improves it by applying small changes to the current solution. These small changes are identified by exploring neighbourhoods, representing sets of standard modifications to be applied on the current solution, and selecting one that improves the quality of the current solution. The main drawback of local search is that it regularly ends up at solutions where no improvement can be found in the neighbourhoods, although there might be better solutions to the considered optimization problem. These sub-optimal solutions are called local minima. Local minima appear either because the objective function has an irregular profile, or because strong constraints prevent the local search from following the slope of the objective function towards the global optimum as it makes some solutions unacceptable.

Avoiding local minima, or at least trying to converge towards a high-quality one is one of the main issues to be solved when using local search. To this end, several approaches are usually deployed, including: (1) finding smart neighbourhoods that experience fewer local minima — for instance, in routing optimization, we can consider the 3-opt neighbourhood which experiences fewer local minima than the 1-opt neighbourhood; (2) using metaheuristics that perturb the monotonic descent such as restart, simulated annealing and tabu search (Glover and Kochenberger, 2003).

Very Large-Scale Neighbourhood (VLSN) is a generic technique that belongs to the first category. VLSN performs many small modifications in an atomic fashion, and efficiently searches for the proper combination of these small modifications that combines in a fruitful fashion, that is: they are together feasible and improve the objective function. These modifications are themselves the result of base neighbourhoods. VLSN is specifically trying to avoid local minima in problems structured into compartments, where items must be placed. Optionally, compartments might need to be optimized internally as well. VLSN requires that the global objective function is
the sum of the objective functions attached on each compartment; it supports strong constraints as long as the compartments do not interact with each other. The notions of compartments and items can be instantiated to problem-specific concepts.

This generally matches routing optimization problems, where compartments are vehicles, items are routing nodes, the objective function is generally the sum of a per-vehicle objective function and vehicles can be re-optimized independently of each other. We will therefore use the vocabulary from routing throughout the paper although VLSN can also be applied to problems with the same compartment structure, such as bin packing by instantiating compartments and items to bin and items.

VLSN has two major bottlenecks: (1) it is very complex to implement, even though some generic implementations are proposed, notably in (Mouthuy et al., 2011); (2) although it has the potential to deliver high quality solutions, it might be somewhat slow, up to the point that classical metaheuristics might sometimes be preferred to VLSN (Mladenovic et al., 2012).

This paper presents a generic domain-independent implementation of VLSN and apply it to PDPTW, we propose a generic speed improvement of VLSN, and present preliminary benchmarks of VLSN on standard PDPTW instances (Lim, 2008). The generic implementation of VLSN and PDPTW are available in the open source OscaR.cbls framework (OscaR Team, 2012).

This paper is structured as follows: Section 2 presents PDPTW and some basic neighbourhoods solving it, the problem of local minima induced by strong constraints, and VLSN as a way to tackle this problem; Section 3 presents how VLSN can be instantiated to solve PDPTW problems; Section 4 presents a generic speedup technique to make VLSN faster; Section 5 presents some benchmarks of our VLSN approaches on classical benchmark instances; Section 6 concludes.

2 BACKGROUND

This section introduces PDPTW, the problem of local minima and VLSN. For more information about VLSN, please refer for instance to (Mouthuy et al., 2011). The work is carried in the context of the OscaR.cbls optimization framework, so all code snippets follow the OscaR.cbls approach and are written in Scala (Scala, 2020).

2.1 PDPTW

Let us consider a pickup & delivery routing problem with time windows PDPTW: a fleet of \( v \) vehicles, each one starting from a different depot, has to transport a set of passengers. Each passenger must be loaded by any vehicle at some pick-up point and must be delivered at some delivery point \( d_p \). The total number of points is \( n \) and includes pick-up, delivery points and vehicle depots. Vehicles can carry at most \( c \) passengers at the same time, and there is some matrix containing the distance for any couple of points, including the vehicle depots, pick-up and delivery points. There is also a time window associated with each point: if the vehicle arrives to a point too early \( wrt \) the time window of the point, it must wait; if the vehicle arrives too late, the considered solution is infeasible. The decision variable is the route of each vehicle, and the objective functions include: the route length of each vehicle, and a global penalty for passengers that could not be transported.

In this paper, we do not consider how constraints and objective functions are evaluated, we exclusively focus on the search procedure. We therefore suppose that some computationally efficient model is available. It inputs the decision variables that are the routes of each vehicle. It outputs the route length per vehicle, the penalty for non-transported passengers and a boolean variable telling whether any route violates the strong constraints.

From an implementation perspective, a neighbourhood is a bunch of nested loops that iterate over the parameters of the move and try the move for all combination of parameters. For instance an \textit{insert point} neighbourhood tries to insert a point into the route of vehicles; it has two parameters, hence two nested loops: the inserted point, and the position where it is inserted.

A neighbourhood also inputs an objective function and an acceptance function and returns either that no move could be found or that a suitable move could be found; this also carries the resulting value for the given objective function and the move itself. Neighbourhoods restore the values of the decision variable to the value when the exploration started. The move must be \textit{committed} to take effect. When several possible moves are possible, the neighbourhood returns the one that decreases the most the objective function, among the acceptable moves.

We define some neighbourhoods for the PDPTW:

- \textit{routePD(pd,vehicle)}: insert the pick-up point \( p_{pd} \) and its related delivery points \( d_{pd} \) into the route of the vehicle, all positions are explored for \( p_{pd} \) and \( d_{pd} \) in this route as far as \( p_{pd} \) is before \( d_{pd} \).
• **movePD(pd, targetVehicle):** moves the pick-up point \( p_{pd} \) and its related delivery point \( d_{pd} \) from their current positions and vehicle to the route of the target vehicle, all positions are explored for \( p_{pd} \) and \( d_{pd} \) in this route as far as \( p_{pd} \) is before \( d_{pd} \).

• **removePD(pd):** removes the pick-up point \( p_{pd} \) and its related delivery points \( d_{pd} \) from their current position, making the pair unrouted;

• **optimizeVehicle(vehicle):** optimizes the route of the vehicle by performing some move within the vehicle itself.

### 2.2 Additional Local Minima Due to Strong Constraints

We can define a standard search procedure that repeatedly explores these neighbourhoods; however, it will encounter many local minima. Typically, it will attempt to insert points into the route of the available vehicles and move points within the routes. As the number of routed pick-up-delivery pairs grows, increasingly more moves are blocked by the strong constraints.

For instance, let be two vehicles, \( v_1 \) and \( v_2 \) and their respective routes, that include the pickup/delivery pairs \( pd_1 \) and \( pd_2 \), respectively. Let’s suppose that there is no solution to move \( pd_1 \) (resp. \( pd_2 \)) on vehicle \( v_2 \) (resp. on vehicle \( v_1 \)) because it will induce a time window violation, but there is a solution to move \( pd_1 \) on \( v_2 \) if \( pd_2 \) is moved on \( v_1 \). The strong constraint will forbid neighbourhoods \( movePD(pd_1, v_2) \) and \( movePD(pd_2, v_1) \) to find any acceptable move if the moves are performed independently, although these moves, once combined, are actually acceptable w.r.t. the strong constraints and improve the overall objective function.

### 2.3 Escaping from Local Minima via Composite Moves

We focus here on escaping from the local minima created by the strong constraints by performing composite moves. In the case of the PDPTW mentioned above, we can directly search for a chain of \( movePD \), possibly with a \( routePD \), and \( removePD \) at the extremities. These are two typical ways to search for such composite moves:

• in a depth first way, without any backtracking, leading to ejection chains (Pesch and Glover, 1997; Curtois et al., 2018): it basically moves a pick-up-delivery pair to another vehicle, at the cost of ejecting a pick-up-delivery pair of this vehicle, which in turn has to be moved to yet another one etc. until we can move the ejected pick-up-delivery pair on a vehicle without needing to eject any other \( pdp \) pair. Selecting the vehicle and/or the ejection chain can be based on some heuristics or random decisions. This approach is however incomplete; it might fail to identify a feasible and existing composite move.

• through a complete exploration of composite moves. This is naively achieved through a search approach with backtracking. This is inherently inefficient because we are facing a combinatorial explosion problem.

VLSN achieves the same results as depth-first search with backtracking, and avoids the combinatorial explosion.

### 2.4 Finding Composite Moves with the VLSN

The VLSN algorithm is illustrated in Figure 1. It repeatedly performs two main steps:

1. (1) Explore the base neighbourhoods, and build a directed graph called the \( VLSN \) graph, where nodes are nodes of the routing problem, and any directed edge from \( s \) to \( t \) has two attributes: a move, and a weight. The move is about moving the node \( s \) to the vehicle of node \( t \), under the assumption that node \( t \) has been moved elsewhere by performing a move associated by an edge leaving node \( t \). The weight is the delta that is achieved on the objective function by performing the move. Moves that would violate strong constraints are not allowed, so the related edge is not incorporated in the VLSN graph.

2. (2) Find cycles in this VLSN graph such that the sum of the weight encountered on this cycle is negative. Finding such cycle is a NP-complete problem, but efficient heuristics have been proposed, so that in practice the majority of the time is spent building the VLSN graph (Orlin et al., 1993).

After performing these two steps, an optional optimization is performed on vehicles that have been modified by the moves performed by the VLSN. We can use, for instance, a 2-opt neighbourhood here.

Figure 2 shows the procedure that explores moves with ejections. This is the most time-consuming part of the procedure and the one that justifies our contribution. It is a triple loop. The two outer loops iterate over all nodes and remove them from their vehicle. To do so, it has a remove operation that performs the remove and return a reinsert operation that will re-insert the removed node at its initial location. The inner iterates on all nodes from other vehicles and tries to move
while (true) {
    // Explore the base neighbourhoods
    // and build the VLSN graph
    val graph = buildVLSNGraph()
    // Find cycles in this VLSN graph
    val cycles = searchForCycles(graph)
    if (noCycleFound) return
    // perform the identified moves
    for (move <- cycles) move.commit()
    // optimize the vehicles
    // that have been modified
    for (vehicle <- impactedVehicles(cycles)) {
        optimizeVehicle(vehicle)
    }
}

Figure 1: generic VLSN algorithm.

these nodes to the first vehicle. To do so, it instantiates a basic neighbourhood and specifies the node to move and the targeted vehicle. If such move is possible, an edge is added to the VLSN graph. This edge starts at a VLSN node representing the moved node, ends at a VLSN node representing the removed node, and is decorated with the delta on the objective function of the target vehicle and the basic move found by the neighbourhood.

To build the graph faster, a cache can store edges of a VLSN graph from one iteration, so they can be reloaded into the VLSN graph of the next iteration without performing neighbourhood exploration for the cached edges. We do not present the details on this cache here for the sake of conciseness. Check (Mouthuy et al., 2011) for more details.

VLSN graphs are quite dense, with many edges wrt. the number of nodes. For instance, the LC1.2.4 instance discussed in Section 5 has around 150 nodes and, after a start-up phase, between 8,000 and 11,000 edges (check Figure 6). We can reasonably consider that there are $O(n)$ nodes and $O(n^2)$ edges in the VLSN graph.

3 INSTANTIATING VLSN TO PDPTW

Instantiating VLSN to PDPTW is about defining the basic neighbourhoods introduced in Section 2 and instantiating the VLSN algorithm with these neighbourhoods as parameters. This section presents how these basic neighbourhoods can be easily assembled as cross-product of standard routing neighbourhoods (De Landsheer et al., 2016) and how the VLSN algorithm is instantiated with them.

VLSN is instantiated by representing pick-up-delivery pairs by their pick-up points exclusively. The VLSN algorithm is only aware of these nodes, and all basic neighbourhoods must take this convention into account and move a pick-up-delivery pair when they are told to move the pick-up node. From that on, the basic neighbourhood defined in Section 2.1 can be used.

We explain in more detail how insertPDP is defined by means of combinators. The movePDP is like the insertPDP, and the removePDP is trivial.

The insertPDP procedure is shown in Figure 3. It creates a neighbourhood to insert a pick-up-delivery pair, among a set of non-routed ones, into the route of a specified vehicle. This neighbourhood construction is a cross-product of two InsertNodeVLSN neighbourhoods: one that inserts pick-ups, and one that inserts the related delivery. The cross-product is built using the dynAndThem neighborhood combinator supported...
by OscaR.cbls. The `dynAndThen` has two parameters: (1) a neighbourhood (here `InsertNodeVLSN`, instantiated to insert only pickup points), that is explored first, and (2) a function that given a move from the first neighbourhood, generates a second neighbourhood.

For each neighbour explored by the neighbourhood, the `dynAndThen` combinator calls the function with a description of the move currently explored by the first neighbourhood. This function generates a second neighbourhood, which is explored starting from the current neighbour of the first neighbourhood, creating a two-level search tree. The function generating the second neighbourhood is the proper place to implement pruning; here, it checks that time window constraints are still valid; if not, there is no need to try inserting the delivery point since time window constraints would be violated anyway after inserting the delivery point (Germeau et al., 2018).

The `insertPDPVLSN` neighbourhood can be quite time consuming to explore, since the neighbourhood can explore many positions both for the pick-up and the delivery point even with the presented pruning on time window constraints.

4 SPEEDING UP VLSN THROUGH GRADUAL GRAPH EXPLORATION

In this section, we present the incremental VLSN (iVLSN), a variant of the VLSN algorithm that builds the VLSN graph gradually and regularly perform the cycle search procedure.

The graph built by the VLSN algorithm is very large since the number of edges is $O(n^2)$. As explained in Section 1, VLSN requires that the global objective function is the sum of the objective functions of all the vehicles. One of the consequences is that each vehicle can be reached by at most one cycle when searching for cycles in the VLSN graph. This means that only a small part of the graph is useful (about $O(v)$ edges, $v$ being the number of vehicles). Furthermore, none of the edges related to a vehicle involved in that cycle can be stored in the cache and reused for the next iteration of the VLSN algorithm, because their impact on the target vehicle of the associated move must be re-evaluated, as the contents of the vehicle have changed. This makes VLSN graph construction a very time-consuming task and can causes the VLSN algorithm to be rather slow.

In the iVLSN algorithm, The VLSN graph being built is split into two parts: identification of potential edges, and exploration or filtering of the potential edges. The potential edges are identified once and for all, and the exploration is performed in fractions. Every time the exploration is called, it explores a fraction of the remaining potential edges. Exploring a potential edge means performing the associated neighborhood exploration to know if the associated move is feasible and compute the gain on the objective function. A cycle detection algorithm is executed between each exploration. Whenever the cycle detection finishes by detecting a cycle, all vehicles involved in the cycle are marked as "dirty", and all the nodes in these vehicles are marked as "dirty" as well. Potential edges reaching "dirty" nodes are not explored, which implies a potential gain in the speed of the iVLSN algorithm with respect to the standard VLSN.

```scala
def insertNodeVLSN(
    node: Int,
    predecessors: Iterable[Int]) =
  insertPoint{
    () => Some(node),
    () => _ => predecessors,
    selectInsertionPointBehavior = Best(),
    vrp=myVRP,
    positionIndependentMoves = true
  }

def insertPDPVLSN(vehicle: Int):
  Int => Neighborhood =
    val route = myVRP.getRouteOfVehicle(vehicle)
    pickup:Int => 
      val delivery = associatedDelivery(pickup)
      dynAndThen{
        insertNodeVLSN{
          pickUp,route},
          (insertMv: InsertPointMove) =>
            if (twConstraint.isViolated) {
              NoMoveNeighborhood
            } else {
              val p = insertMv.predecessor
              val nodesInRouteAfterPickup =
                pickUp:trimRoute(route,p)
              insertNodeVLSN{
                delivery,
                nodesInRouteAfterPickup
              }
            }
      }
}
```

Figure 3: A neighborhood that inserts PDP pairs into existing routes, built as a cross-product of two basic "insertPoint" neighbourhoods, with pruning.
5 BENCHMARKS

This section presents the benchmarks of our VLSN approach on standard PDP problems (Lim, 2008), with and without gradual enrichment, and compares them to the best known values. We selected a set of instances of various sizes. Each benchmark is run 13 times with the standard VLSN algorithm and 13 times with the iVLSN algorithm.

The official benchmarks are about: first, minimizing the number of vehicles, and second, minimizing the total distance. VLSN is not meant to minimize the number of vehicles, so this is not a relevant dimension. Yet, we report these numbers as well for the sake of completeness.

Figure 4 presents a comparison of the VLSN and iVLSN. As already mentioned, these approaches are not about minimizing \( v \), so the related columns are not relevant but mentioned for completeness. \( obj \) reports the median value for the objective function over the 13 runs with the ratio and \( run \ time \) reports the median run time for the algorithms, in seconds with the ratio. We observe two things: (1) the run time is improved by the incremental approach, as initially intended. However, the run time ratio does not seem to be strongly related to \( v \) or \( pdp \). iVLSN achieves a speedup factor of 3 in the best case. (2) there is a slight improvement in quality of the solution in iVLSN, which was not a primary goal of this algorithm. We conclude that iVLSN seems to be a relevant improvement over VLSN when applied on PDPTW problems.

The benchmarks have been run on a Dell laptop featuring Windows 10, an INTEL® core™ i7 with 4 physical cores (thus 8 logical cores) running at 2.2GHz and 16Gb of RAM. The benchmarks were performed in a single thread.

Figure 5 compares VLSN and iVLSN against the best values for the selected benchmarks, fetched from (Lim, 2008) in September 2020. We observe that VLSN and iVLSN do not reach the quality of the best-known solution.

We compare the inner behaviour of VLSN and iVLSN on a single run of the algorithms on the LC1_2_4 problem instance in Figure 6. At each iteration of the algorithm, it reports for both algorithms (1) the number of edges in the VLSN graph and (2) number of such edges that were fetched from the cache and (3) the number of edges that were explored. In this problem instance, VLSN and iVLSN took nearly the same number of iterations: 34 and 39, respectively.

At any time, iVLSN explores fewer edges than VLSN. In total, iVLSN explores 43% of the edges explored by VLSN. The total run time of iVLSN is 53% of the time taken by VLSN. The gain in time is not as high as the gain in number of edges because the iVLSN executes the cycle detection algorithm per iteration and performs a few more iterations in this case.

After a start-up phase, where the VLSN injects many pick-up-delivery pairs into the route, the total number of edges explored by the VLSN decreases throughout the search because the cache is more and more effective. The iVLSN has the opposite behaviour; it explores more and more edges throughout...
Figure 5: Comparing VLSN and iVLSN against the best known solutions.

The iVLSN algorithm generates a VLSN graph with fewer edges than the graph generated by the VLSN algorithm, except for the very last value of each algorithm, where these two numbers are equals because the iVLSN must build the full graph to check that no cycle exist in it.

Finally, more edges are fetched from the cache by VLSN than iVLSN, simply because iVLSN just does not populate the graph as much as VLSN, hence less edges can be stored in the cache.

More benchmarks must be performed to compare the iVLSN algorithm against the best results reported in (Li and Lim, 2001). So far, we hope that iVLSN can constitute a decent time/quality trade-off for small problem instances such as the LC1.X instances, considering that the best solutions for these instances are generally generated with a run time of 15 minutes (Curtois et al., 2018).

6 CONCLUSION

This paper presented a VLSN approach to the PDPTW problem. The approach could be applied easily using a generic VLSN algorithm, instantiated with PDP-specific neighbourhoods. The latter are built as cross-products of standard routing neighbour-

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Figure 6: Comparing internal metrics of VLSN and iVLSN on LC1_2.4.
hoods.

A generic approach is proposed to speed up the VLSN algorithm, based on incremental computation. It proceeds through a gradual enrichment of the VLSN graph instead of a full construction of the graph prior to cycle search. This provides a notable speed improvement on the PDPTW as illustrated through the benchmarks. A marginal quality improvement was also observed.

VLSN algorithms experience local minima, like any local search methods. On the considered benchmark instances, it could not reproduce the best known result for the standard PDPTW benchmarks (Lim, 2008). Yet for the small problem instance, it was not too far off the best known value, with a relatively small response time. More benchmarks must be performed to compare the VLSN approach against the best results reported in (Lim, 2008). So far, we hope that VLSN can constitute a decent time/quality trade-off at least for small problem instances.

To further improve the quality of the solutions, VLSN requires additional meta-heuristics. They can either be added around it, such as restarts, or added within it, for instance by accepting composite moves based on a simulated annealing acceptance criterion (Mouthuy et al., 2011).

To further speed up VLSN, several approaches might be considered, including:

- parallelizing the construction of the VLSN to exploit multiple hardware cores; the construction itself is easy to parallelize because each edge of the VLSN graph is evaluated independently to the others and requires some neighborhood exploration with a minimal amount of work, so this may compensate the overhead of parallelization.

- making the cycle detection algorithm incremental, so that it would only search for cycles involving at least one edge that was added since its previous execution.

- fine tune the number of edges that are explored between each run of the cycle detection algorithm. there is trade off to set as too many edges and lots of them are not useful, too few, and fewer cycles will be detected with an increased time overhead caused by the cycle detection algorithm.

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