Towards Distributed Local Search Through Neighborhood Combinators

Gustavo Ospina and Renaud De Landtsheer
CETIC Research Centre, Charleroi, Belgium

Keywords: Parallelization, Multi-core, Akka, Local Search, Combinatorial Optimization, OscaR.cbls.

Abstract: This paper presents an approach for making local search algorithms distributed, to get speed improvements thanks to the growth both in multi-core hardware and the massive availability of distributed computing power, notably in the cloud. Local search algorithms rely on the exploration of neighborhoods on a given solution space model. Our distribution approach relies on the exploration of multiple neighborhoods in parallel, performed by different workers located on different CPU cores (locally or distributed). This approach relies on neighborhood combinators, which are composite neighborhoods built out of basic neighborhoods. Combinators allows us to introduce metaheuristics (restart, tabu search, simulated annealing), neighborhood selection (hill-climbing, round-robin) and handle search strategies. We propose some parallel search combinators that can be instantiated to build search strategies encompassing parallel neighborhood exploration. An implementation is proposed in the OscaR.cbls framework, using the Actor model of computation.

1 INTRODUCTION

Nowadays, processing power available in a single CPU Core is somewhat reaching a plateau, while the number of available cores per CPU is regularly increasing. To be able to exploit such computing power, optimization algorithms should be redesigned to support multiple core computing.

There are a few challenges to solve in order to exploit distributed computation power and ensure that the resulting distributed algorithm is faster than the non-distributed one. These challenges include:

- keeping technical overhead to an acceptable level. This includes synchronization and message passing.
- finding a proper way to split up the algorithm, so that the different parts can be usefully executed in parallel.
- ensuring a fair load balancing among cores, so that there is as little idle time as possible. This is more complex when cores have different computing power.

This paper proposes a generic way to make use of distributed computing in local search engine by proposing a standard worker-supervisor approach, and a presentation of the latter in the form of neighborhood combinators, as part of a search procedure. Essentially, a local search algorithm is nothing else but a set of nested loops:

- higher-level loops compose the search procedure: the highest one is the global loop that repeatedly triggers solution exploration and moves.
- a series of intermediary loops are related to metaheuristics, such as restarts and search strategies.
- in lower-level loops, neighborhoods explore the different neighboring solutions for the current solution and evaluates the best solution.
- below the search procedure, there is another loop that updates the model in response to the changes in decision variables: the propagation process (Van Hentenryck and Michel, 2009).
- each constraint and invariant can also execute some loops during its propagation, although they are expected to have very good complexity. An $O(1)$ time complexity is rather common for constraints.

This paper focuses on making distributed search at the high level of loops, not distributed model evaluation at lower levels. Although promising, distributed model evaluation requires much more synchronization, and the overhead may be quite high.

Neighborhood combinators is an approach proposed in (De Landtsheer et al., 2016) to assemble a full-fledged local search procedure out of base neighborhoods, and of combinators that incorporate various
aspects such as metaheuristics, neighborhood selection, stop criteria, utility functions, among others.

We are currently developing this worker-supervisor approach into the OscaR.cbls engine using the Actor model implemented in the Akka framework (OscaR Team, 2012; Hewitt, 2017; Lightbend Inc., 2020). This position paper presents the first results of our work.

The paper is structured as follows: Section 2 recalls the concept of combinator and illustrates it on an example of simple warehouse location problem. Section 3 presents a worker-supervisor architecture to enable the distribution of neighborhood exploration. Section 4 presents the notion of distributed combinators and illustrates that concept on the same problem example. Section 5 shows the results of some benchmarks over the number of threads while solving several instances of the problem example. Section 6 concludes and introduces future work.

2 BACKGROUND

This section presents the notions of local search, the basics of neighborhood combinators and the existing approaches for parallelization of local search.

2.1 Constraint-based Local Search

Local search (Aarts and Lenstra, 1997; Van Hentenryck and Michel, 2009) is an approach for tackling large combinatorial optimization problems in a reasonable amount of time. Usually a local search algorithm is built on top of two main components: a model and a search procedure. The model is a representation of the optimization problem, composed of decision variables and constraints on these variables, including the objective function as a special constraint. A solution of the problem is a set of values for each variable that fulfills the constraints. The search procedure is an algorithm that aims at finding an optimal solution, minimizing the value of the objective function. The search procedure is basically a loop through the space of solutions, where the exploration is made within neighborhoods, representing sets of "close" solutions that can be reached from a given solution in one iteration (move), in order to find a better solution with respect to the objective function.

The main loop is enriched with several components. Besides neighborhoods, the search procedure may include strategies to escape from local minima, also called metaheuristics, as well as solution managers that handles the best solution found so far and restore it when needed, and stop criteria to be met when the current best solution is good enough to finish the search.

A good design of search procedures in local search is critical since it influences the efficiency of the algorithm and the quality of the solution. Most local search algorithms are built from scratch with problem-specific neighborhoods and procedural programming languages. One of the aims of OscaR.cbls is to facilitate the development of local search algorithms through standard bricks encapsulating the needed features for the model and the search procedure.

2.2 Neighborhood Combinators

In OscaR.cbls, a neighborhood is a data structure bound to a local search model, that manipulates the decision variables, and can be queried for a move, given a current solution, an acceptance criterion, and the objective function. The query triggers the actual neighborhood exploration. If an acceptable move is found, it returns a description of the move and the value of the objective function after the move if the move is committed. When the found move is committed, a propagation process is triggered to update all the variables and constraints according to the reached solution. Propagation is performed in a way that a variable is updated at most once and only when needed.

Oscar.cbls provides a library of standard domain-independent neighborhoods as well as specific neighborhoods for routing and scheduling problems. Neighborhoods can include features such as symmetry elimination, mechanisms to perform intensification or tabu search, move selection, and hot restarting, which allows the possibility of restart the neighborhood exploration from a last explored point of the previous query instead of the initial position at each query.

Neighborhood combinators were introduced in (De Landtsheer et al., 2016) as a declarative framework to elaborate richer search procedures with several neighborhoods, including operational aspects as metaheuristics, move selection, stop criteria, search restarting, and solution handling.

We illustrate the principles of neighborhood combinators with an example for solving the uncapacitated Warehouse Location Problem. The problem takes as input a set of warehouses $W$ and a set of delivery points $D$. Opening a warehouse has a fixed cost $f_w$ and the transportation cost from warehouse $w$ to a delivery point $s$ is $c_{ws}$. The solution is a subset of warehouses to open that minimizes the sum of fixed costs for open warehouses and transportation costs for
each delivery point to its nearest open warehouse.

Figure 1 presents a WLP solver in OscaR.cbls. The model is composed of an array of Boolean variables indicating which warehouses are open. The associated constraints are the open warehouses and the distances between points and their nearest open warehouse. The objective function is the total cost.

The search procedure is declared as follows: the base neighborhoods used are: assignNeighborhood, where the value of one warehouse is changed; swapsNeighborhood, where the values of two warehouses are swapped; and randomSwapNeighborhood, where the values of a random number of warehouses are swapped. In this problem, we use two neighborhood combinators: bestSlopeFirst evaluates a set of neighborhoods and select the move that decreases the most the objective function; onExhaustRestartAfter evaluates a neighborhood (here, the bestSlopeFirst) and select its moves until no more moves are found, then it performs a restart of the search using a second neighborhood to find a new starting point. The stop criteria is a given number of consecutive restarts without improving the objective function.

2.3 Parallelization of Local Search

Since the beginnings of Operational Research, the first algorithms and their improvements followed the sequential nature of the computers where those algorithms ran. With the arrival of parallel computing, the first approaches to parallelization were based on simple changes on the original sequential algorithm, for instance, replacing a loop with a parallel loop. This is not a trivial task, since some algorithms use sequential mechanisms that are lost when the algorithm is parallelized. An example of this loss is given in (Isoart and Régin, 2020) in a parallel constraint solver for the Travelling Salesman Problem. As a result, at some scale, parallel algorithms may be slower than an optimal sequential algorithm.

Since the first theoretical works about local search were developed (Aarts and Lenstra, 1997), several approaches were considered for parallelizing different aspects of local search algorithms. A first work is presented at (Verhoeven and Aarts, 1995), where a general approach independent of the problem is described. In that general approach we can distinguish between single-walk algorithms, where the solution space is explored only once, and multiple-walk algorithms, where several explorations are triggered concurrently and may or may not communicate with each other. In both kinds of algorithms, parallelism arises in other aspects like neighborhood exploration and move committing. The latest can be made in a single-step way, it means that only one move is committed at a time after a parallel exploration of neighborhoods, or in a multiple-step way, where several moves are committed in parallel. Most interesting applications use multi-walk based algorithms. For instance, in (Handa et al., 2004), a distributed algorithm with a worker-supervisor architecture is presented. The local search algorithm consists on splitting the solution space and trigger several workers that perform the search and specially the neighborhood exploration. Each worker can use a different neighborhood. The supervisor waits for the solutions found by each worker and performs the actual move committing. A recent work in (Codognet et al., 2018) proposes an extension of multiple-walk algorithms with a cooperation layer between the different explorers. The resulting framework is called Cooperative Parallel Local Search (Munera et al., 2014), and is implemented in the X10 parallel programming language.

After their design of Comet programming language, (Michel et al., 2009) propose parallel constructs to extend Comet. The proposed constructs are quite similar to the ones used in Java: monitors for synchronized blocks, threads, processes, and shared objects, as well as parallel loop statements. Those language constructors support the development of both single-walk and multi-walk algorithms.

The framework we propose in this paper is a multi-walk approach, based on the Actor model, where workers perform single neighborhood explorations of a part of the search space, as it is explained in next section.

3 A WORKER-SUPERVISOR ARCHITECTURE

Before this work, local search solvers in OscaR.cbls run as monolithic applications in a mono-thread environment. In this section, we present the architectural extensions which support the distribution of local search in a multi-threading environment.

The architecture shown in Figure 2 is based on the Akka actor model (Lightbend Inc., 2020). Akka makes easier the implementation of complex software communication protocols, and is also able to support network communication in a seamless way. Our architecture follows a Supervisor-Worker pattern, where a supervisor actor dispatches search requests to worker actors, who synchronize their search results to work giver actors. Work givers are associated to specific “remote” neighborhoods.

In the context of a multi-threaded local search
val W:Int = ...  //the number of warehouses
val D:Int = ...  //the number of delivery points
val defaultCostForNoOpenW = ... //default cost if no warehouse is open
val costForOpeningWarehouse = ...  //the costs for keeping open each warehouse
val distanceCost = ...  //the cost between a warehouse and a delivery point

//problem model
val m = Store()
val warehouseOpenArray = Array.tabulate(W)(w => CBLSIntVar(m, 0, 0 to 1, s"w_${w}"))
val openWarehouses = filter(warehouseOpenArray, _==1)
val distanceToClosestOpenWarehouse = Array.tabulate(D)(d =>
  min(distanceCost(d), openWarehouses, defaultCostForNoOpenW))
val obj = objective(sum(distanceToClosestOpenWarehouse) + sum(costForOpeningWarehouse, openWarehouses))

m.close()

//define the search procedure
val neighborhood = {
  bestSlopeFirst{
    assignNeighborhood(warehouseOpenArray, "SwitchWarehouse"),
    swapNeighborhood(warehouseOpenArray, "SwapWarehouses")
  } onExhaustRestartAfter{
    randomSwapNeighborhood(warehouseOpenArray, W/10),
    maxRestartWithoutImprovement = 2, obj)
}
//run the search
neighborhood.doAllMoves(obj)

Figure 1: A simple script solving the uncapacitated warehouse location problem.

Figure 2: Distribution of search in OscaR.cbls using actors.

with OscaR.cbls, the main thread executes the search procedure. When the search procedure executes a neighborhood combinator requiring some remote neighborhood exploration, appropriate requests are sent to the supervisor, which include the current values stored in the model and the set of neighborhoods to explore. The main thread can be stopped by synchronization in the combinator, on one or more results of the remote searches. Remote searches can also be cancelled by the combinator that requested these searches, notably when an acceptable move has been found by some worker.

The supervisor has an internal queue of searches waiting to start, and manages the set of available workers with their current status. Those status are either “idle” or “busy”. The supervisor assign searches to idle workers.

When a search request is processed by the supervisor, it creates a work giver actor and dispatches the search to an idle worker, with the reference of the work giver. Workers notify the search results to their work givers, who passes those results to the main thread, while workers notify the supervisor on their state change for eventually processing another search request.

The main thread and each worker have their own instances of the same search procedure and model, which includes variables, constraints, and the objective function. Each variable and base neighborhood in workers have a unique identifier, which is created in the same deterministic way for all workers. Duplicating the neighborhood data through workers is required since instantiating the model is time consuming, and we want to avoid creating and destroying workers too often, because those operations induces overhead in the solver.

Towards Distributed Local Search Through Neighborhood Combinators
4 DISTRIBUTING SEARCH WITH COMBINATORS

This section presents the extension of the neighborhood combinator framework for covering the distribution of search through several workers.

We defined three distributed combinators which take a set of base neighborhoods that will be explored remotely. Distributed combinators have a reference to the supervisor actor and sends messages representing search requests for each base neighborhood to that supervisor. The supervisor puts the requests in its search queue and creates the corresponding work givers. Requests in the queue will be eventually dispatched to workers, who perform the search for a move and send the results about the found move to the corresponding work givers.

The three distributed combinators deal with the results of parallel neighborhood explorations in a specific way:

The Remote combinator just takes a base neighborhood and performs its exploration remotely.

The DistributedFirst combinator dispatches all searches on base neighborhoods and selects the first move received as the next move. This implies to send cancel search messages to the other workers when the first move is found.

The DistributedBest combinator dispatches all searches on base neighborhoods and selects the move that best improves the objective function.

In Figure 3 is presented a solver of the uncapacitated warehouse location problem using OscaR.cbls with distributed search. The main difference with the sequential version is the configuration of the supervisor and workers. The Actor system is started by the main thread with the Supervisor actor and the main components of solver (model, neighborhoods, and objective function). Then, the local workers can be created with their own instances of both model and neighborhoods. We have also split the swapsNeighborhood into four parts with a module rule on their domain, so that they can be explored in parallel.

5 BENCHMARKING

In this section, we evaluate the efficiency of using distributed combinators through a set of benchmarks on the uncapacitated warehouse location problem. The benchmarks were performed in a laptop with Intel i7-7700HQ processor at 2.80 Ghz, with 4 cores and 8 logical processors, 16 Gb of RAM, and a SSD disk.

These benchmarks used the algorithm in Figure 3, which uses the DistributedFirst combinator, with two dimensional parameters: the problem size, expressed in the number of warehouses and delivery points, and the number of local search workers. Four different problem sizes were used, respecting a ratio 2:1 between warehouses and delivery points. The number of workers varies between 1 and 16. For each problem size, a random warehouse location problem was generated. The same problem is then solved by search procedures which are parameterized with the number of workers. Within a given number of workers, several iterations of the same search procedure are done, and their run times are averaged. Since there are non-determinism on workers, the objective value may be different on iterations of the same problem. The comparison between the different problem sizes are done with respect to the best (minimal) value found in all the iterations.

The results are presented in Figure 4. The X axis represents the number of workers, The Y axis is the average solving time in milliseconds. The best run time is shown in bold, whereas the green values represent the instances having the best value of the objective function.

For smaller problem sizes with short run times (W=1000, W=2000), there is no significant differences in the run times when the number of workers are between 3 and 12. In bigger problem sizes (W=3000, W=4000), the performance significantly decreases within 10 or more workers. This is probably due to the saturation of the CPU cores, CPU cache and the bus to the RAM, which is shared by all cores. In addition, since every worker has a copy of model variables and neighborhoods, RAM could also be saturated and computation relies on slower swapping memory.

These limitations might actually disappear by using cores from different CPUs, as they would have their own memory space, to the cost of creating higher communication overhead.

Considering that the supervisor and workers constitutes the principal threads in the solver, it is recommended to set the number of workers in a range between the number of processor cores and the number of logical processors.

6 CONCLUSION AND FUTURE WORK

We presented an extension of a local search framework to handle distributed computation in a multi-threading environment. Our current work covers the distribution of neighborhood exploration by extending the neighborhood combinators library with dis-
// loading instance data into constants (same as the non-parallelized case)...

def createSearchProcedure():(Store, Neighborhood, Objective) = {
  // instantiate model (same as the non-parallelized case)
  val m = Store()
  ...
  val obj = ...
  m.close()
  // instantiate search procedure
  val neighborhood =
    distributedFirst(
      assignNeighborhood(wOpen, "SwitchW"),
      swapsNeighborhood(wOpen, searchZone1=(0 until W/4).map(_*4 ), "SwapW0"),
      swapsNeighborhood(wOpen, searchZone1=(0 until W/4).map(_*4+1), "SwapW1"),
      swapsNeighborhood(wOpen, searchZone1=(0 until W/4).map(_*4+2), "SwapW2"),
      swapsNeighborhood(wOpen, searchZone1=(0 until W/4).map(_*4+3), "SwapW3"),
    onExhaustRestartAfter(randomSwapNeighborhood(wOpen, W/10), 2, obj)
  // result
  (m, neighborhood, obj)
}
// supervisor side
val (store, search, obj) = createSearchProcedure()
val supervisor = Supervisor.startSupervisorAndActorSystem(store, search)
// creating 5 workers in the same JVM as the supervisor
for(_ <- 1 to 5) {
  val (store2, search2, _) = createSearchProcedure()
  supervisor.createLocalWorker(store2, search2)
}
// run the search on the supervisor side, which delegates that to the workers
search.doAllMoves(obj)

Figure 3: A script solving the uncapacitated warehouse location problem with a distributed neighborhood.

Figure 4: Benchmarks for distributed solvers of warehouse location problems.

tributed combinators on an underlying supervisor-worker architecture implemented in the Akka Actor model.

The proposed extensions are functional and the first benchmarks show that a good efficiency of the solver is obtained with a limited number of worker actors running in separated threads. Besides, the integration with existing sequential neighborhoods is
However, the benchmarks also revealed some drawbacks. We could not see a direct relation between the solver speed and the number of CPU cores, event though it was evident that the efficiency decreases with a high number of workers. Another drawback is the need to make explicit the copy of the model and neighborhoods at the creation of the actor model, which implies an extra work to the developer.

Building a parallel version of an algorithm inherently hinders the use of some mechanisms that rely on sequential exploration. In the case of constraint-based local search solvers, we can find several mechanisms, implemented in OscaR.cbls. These will be carefully examined to check if they can cope with multi-core computation:

- some metaheuristics that select neighborhood or define a stop criterion rely on time measurement. These are affected because the main thread does not know when and where computation takes place anymore.
- some neighborhoods are stateful because state provides speed improvements. Our approach will instantiate neighborhoods on different machines, and their internal state is not shared, so these mechanisms cannot be enabled.
- constraints tend to work based on incremental model updates. So far, in our framework, when a remote neighborhood exploration is started, the start value of the model is loaded in a non-incremental way, thus disabling these mechanisms.

 These mechanisms must somehow be adapted to work within distributed search because their benefits generally surpass the ones achieved by the parallelization. Similar issues where encountered with distributed constraint programming, where a learning-based search heuristics is disabled because distribution forces a breadth-first search instead of sequential depth-first search (Isoart and Régis, 2020).

 Our library of distributed combinators can be extended to make existing neighborhood distributed as well, such as:

- restart metaheuristics, that could explore different restarts in a distributed way. Notice that this can be mimicked using the DistributedBest combinator.
- making an implementation of Very Large Scale Neighborhood that uses multi-core processing (Mouthuy et al., 2012).

 So far our local search framework is only working in a single machine with an unique thread. Akka actors make it reasonably easy to work in a distributed fashion, this was a rationale behind our choice of Akka to implement the distributed extensions. An alternative is the use of remote procedure calls mechanisms like Protocol Buffers (Google, 2020) for serializing data through remote workers, but the blocking nature of remote calls will not give a real speedup without using multi-threading.

 Further work will include reducing the technical overhead in the distribution layer, with the aim of improving the efficiency of the solvers as well as the expressiveness of the new programming idioms induced by the distribution of computation.

 Computational power available in multi-core or distributed systems might be exploited to speed up local search engines in other ways:

- the evaluation of the objective function can be performed in a parallel way. In some problems, this evaluation can be time consuming and it is worth to parallelize. To this end, the propagation algorithm that drives the whole CBLS engine could be made multi-core (Van Hentenryck and Michel, 2009).

- some constraints already available in our framework exhibit poor complexities and a multi-threaded version of these might be proposed.

ACKNOWLEDGEMENTS

This research was supported by the European project TrackOpt (grant number 753592).

REFERENCES


