Segmented ECG Bio Identification using Fréchet Mean Distance and Feature Matrices of Fiducial QRS Features

Abdullah Biran\textsuperscript{1} and Aleksandar Jeremic\textsuperscript{2}

\textsuperscript{1}Department of Biomedical Engineering, McMaster University, Hamilton, Canada
\textsuperscript{2}Department of Electrical Engineering, McMaster University, Hamilton, Canada

Keywords: Biomedical Signal Processing, Biometrics, Electrocardiogram, QRS Segmentation, Short Time Fourier Transform, Feature Lags.

Abstract: In this paper, we present a new segmented based method for human identification using Fréchet distances and the characteristics of the lag-feature matrices of six fiducial based QRS features. We examined the applicability of our methodology on 124 ECG records of 62 subjects from the publicly available ECG ID database. Our experiments show that the Fréchet distance can identify majority of the subjects (44 individuals) using the feature matrix of QRS segment lagged by one beat with an identification accuracy ranging from 80% to 100%. Our preliminary results indicate that identifying humans using segmented approaches can be potentially useful.

1 INTRODUCTION

One of the potential applications of wearable sensing devices is human identification using biometric signals. Historically, biometric has been using fingerprinting and more recently iris scans. In addition to identification accuracy issues some of the currently used techniques can be either spoofed and/or stolen. To this purpose, the identification using in vivo signals has gained considerable research interest in recent years. One of the most promising techniques is based on the electrocardiography (ECG) measurements. In addition to its in vivo characteristics, ECG has robust advantages including universality, hidden nature and simple acquisition (Joao, S. Cardoso, & Lourenco, 2018). Generally, ECG based human identification is done in two different ways: fiducial points based and non-fiducial feature based (Joao, S. Cardoso, & Lourenco, 2018). The fiducial techniques rely on locating heartbeat waveform points, onsets and offsets followed by extracting different temporal, morphological and amplitude features. The non-fiducial methods are based on extracting features without relying on segmentation algorithms such as using autocorrelation and wavelet coefficients algorithms (Chun Chi, Peng Tzu, & Pie Lun, 2019). Many methods have been applied for personal identification using ECG. Adrian et al. have proposed a method using wavelet-based distance measure for human identification (D.C. Chan, M. Handty, Badre, & Badee, 2008). Saiful et al. developed another method using the heartbeat morphology features (Islam, Alajlan, Bazi, & S. Hichri, 2012). Lin et al presented an algorithm by applying non-linear Lyapunov exponents, root mean square (RMS) and support vector machine (SVM) (Lin, Chen, Lin, Yang, & Chiang, 2014). Furthermore, Gutta and Cheng proposed discrete cosine transform (DCT) and autocorrelation techniques for extracting non-fiducial ECG features (Gutta & Cheng, 2016). In contrast, Arteaga-Falconi et al presented a numerical algorithm to extract fiducial based time and amplitude features (Arteaga-Falconi, Al Osman, & El Saddik, 2016). Moreover, Biran et al. have developed segmented and non-segmented techniques based on Short Time Fourier Transform (STFT), Euclidian distance and Fréchet distance to test the feasibility of using ECG as biometric modality (Biran & Jeremic, Non-Segmented ECG bio-Identification using Short Time Fourier Transform and Frecht Mean Distance, 2020). Liu et al. developed a multi scale autoregressive model method (MSARM) for personal identification using ECG (Liu, et al., 2018). Moreover, Sidek et al. investigated the feasibility of ECG signal as biometric
modality in abnormal cardiac conditions (Sidek, Khalil, & F. Jelinek, 2014). Furthermore, Odinaka et al. proposed a multibiometric identification system based on combining both the electrical originating signal, the ECG, and the laser Doppler vibrometry (LDV) (Odinaka, A. O’Sullivan, J. Sirevaag, & W. Rohrbaugh, 2015).

In this study, we present a fiducial based method using electrocardiogram (ECG) by creating four feature matrices of QRS segments. We segment the ECG signal using our results in (Biran & Jeremic, Automatic QRS Detection and Segmentation using Short Time Fourier Transform and Feature Fusion, 2020). We randomize the training/testing procedures and calculate feature matrices using four different lags. We identify the subjects using the Fréchet distance of feature matrices. In Figure 1 we illustrate the outline of the methodology.

2 PROPOSED METHODOLOGY

2.1 ECG Database

In this study, we use filtered ECGs of 62 subjects from the publicly available ECG ID database. The ECG signals were measured using single lead at 500 sampling frequency and for a duration of 20 seconds. The data record for each subject consists of two measurements obtained at different times/days. In the remainder of the paper, we use the normalized data as it is commonly used procedure in many of the machine learning based algorithms in order to account for possible variability in signal range. In this stage, we apply our previous work techniques on automatically segmenting QRS peaks using windowed STFT and QRS feature fusion. The previously proposed method correctly and accurately locates and segments the Q, R and S peaks. (Biran & Jeremic, Automatic QRS Detection and Segmentation using Short Time Fourier Transform and Feature Fusion, 2020).

Following majority of the methods that are used for individual identification, we create two sets of ECG data which are used for training/referencing and testing. To illustrate, we randomize the process of selecting the QRS peaks in order to evaluate the performance of the proposed algorithm. We arbitrarily set the number of selected beats for both test and reference ECG to 16. In Fig. 2 we show an example of the randomization in the training and test data selection.

Figure 2: An example of randomly selecting the training/referencing and testing QRS waves.

2.2 QRS Feature Extraction

Using the results from our previous work we extract the following features after aligning the corresponding QRS segments: R-Q peak interval \(P_1\), S-R peak interval \(P_2\), R-Q amplitude difference \(P_3\), R-S amplitude difference \(P_4\), QRS wave distances \(P_5\), and slope distances of the QRS wave \(P_6\). Note that since the last two features are calculated using the difference between the waves the number of the feature measurements will be smaller than the number of available heart beats.
In order to perform the identification task, we propose to calculate the feature matrices using the training set and then to identify unknown subject by calculating the distances between the testing data and training data and select a subject with the smallest distance.

Let \( F_g \in R^{1 \times f} \) and \( F_u \in R^{1 \times f} \) be the feature vectors for any two QRS waves, then we define the cross-feature (\( CF \)) matrix between any two QRS waves using equation (1).

\[
CF = F_g F_u^T
\]  
(1)

By utilizing equation (1), multiple cross-feature matrices can be calculated by applying particular lags between QRS waves. Accordingly, we apply equation (2) to calculate the QRS feature matrices from both the training and testing data sets.

\[
CF_L = \sum_{n=1-L}^{c-L} \frac{F_n F_n^T}{c-L-1}
\]  
(2)

Where \( L \) the lag coefficient, \( F \) is the QRS feature vector and \( n = 1 \) to \( c - L \) is the index of QRS wave where \( c \) is the number of segments.

Since we are using 4 different lags and we have two set of QRS data (training and testing), by applying equation (2), we define four training matrices and four examining matrices of QRS features for each subject.

### 2.3 Identification based on Fréchet Distance

In this study, we apply the findings of Joromi’s work; specifically, the Fréchet distance of covariance matrices using Riemannian distances (Jahromi, 2014). Technically, for any cross-feature matrix, we use equation (3) to define the feature matrix

\[
R = CF_L CF_L^T
\]  
(3)

Using equation (3) we first calculate the feature matrix using training set and label them \( E_{ij} \) where \( L \) is the lag coefficient and \( j = 1,2,...,N \) is the subject number. Similarly, \( T_k \) corresponds to lag 1 matrix calculated using the test data. Then, we use the following Fréchet distances between \( T_k \) and \( E_{ij} \)

\[
FMD1 = \sqrt{Tr(T_k) + Tr(E_{ij}) - 2Tr(T_k E_{ij}^T)}
\]  
(4)

\[
FMD2 = \sqrt{Tr(T_k) + Tr(E_{ij}) - 2Tr(T_k E_{ij}^T)}
\]  
(5)

where \( Tr \) is trace of the matrix.

### 3 RESULTS

We have applied our algorithm on 124 ECGs of 62 subjects from the ECG ID database. We test the performance of the proposed algorithm in terms of the average personal identification accuracy, which is computed using equation (6)

\[
A_{lj} = \frac{1}{K} \sum_{k=1}^{K} FMD_{Ljk} \times 100
\]  
(6)

where \( K \) is the total number of experiments.

Consequently, to obtain the average performance, we repeated the training and testing 10 times. Then we use equation (13) to find the average personal identification accuracy. As a result, Table 1 shows that majority of the subjects (44 from record 1 and 43 from record 2 using FMD2) are correctly identified with an average identification accuracy ranging from 80% to 100% at lag coefficient \( L = 1 \). In comparison, 40 subjects are correctly identified in the same accuracy range by using FMD1. This shows that FMD2 identifier has significantly better performance compared to FMD1 as seen in Table 1, Figure 3 and Figure 4. In addition, these findings indicate that personal QRS features for most subjects remain stable over one lag. However, for larger lag values, the identification accuracy is fluctuating and is highly dependent on the personal QRS properties. Figures 5 and 6 show examples of the fluctuating in the average personal identification accuracy over the remaining three lag coefficients.

### 4 CONCLUSIONS

In this paper, we proposed an automated fiducial algorithm based on Fréchet distance and features of QRS waves to identify subjects using their ECG. Our preliminary results indicate that by measuring the FMD2 distance between randomly created cross feature matrices calculated by one beat lag, majority of the individuals can be identified with high accuracy range. Furthermore, applying different lag coefficients can support the identification process when the personal QRS feature remain stable over time. Most importantly, our results indicate that the ECG based human identification using fiducial algorithms can achieve acceptable accuracy levels.
Figure 3: The average personal accuracy for all subject after 10 experiments using FMD2 and lag coefficient $L = 1$ of randomly selected QRS waves from record 1. We can see that majority of the subjects (44 subjects) have an identification accuracy ranging from (80 % to 100%).

Figure 4: The average personal accuracy for all subject after 10 experiments using FMD2 and Lag Coefficient $L = 1$ of Randomly Selected QRS Waves from Record 2. We see that majority of the subjects (43 subjects) have an identification accuracy ranging from (80 % to 100%).

Figure 5: The personal identification accuracy (Y-axis) of different subjects using FMD2 over 4 lag coefficients (X-axis) after 10 experiments. The top two are from record 1 and the bottom two are from record 2.

Figure 6: The personal identification accuracy (Y-axis) of different subjects using FMD1 over 4 lag coefficients (X-axis) after 10 experiments. The top two are from record 1 and the bottom two are from record 2.
Table 1: The total number of subjects identified per accuracy range over all the distance measurements and data records.

<table>
<thead>
<tr>
<th>Accuracy</th>
<th>50%</th>
<th>60%</th>
<th>70%</th>
<th>80%</th>
<th>90%</th>
<th>100%</th>
</tr>
</thead>
<tbody>
<tr>
<td>FMD2, record 1</td>
<td>2</td>
<td>8</td>
<td>8</td>
<td>15</td>
<td>15</td>
<td>14</td>
</tr>
<tr>
<td>FMD2, record 2</td>
<td>2</td>
<td>2</td>
<td>15</td>
<td>23</td>
<td>11</td>
<td>9</td>
</tr>
<tr>
<td>FMD1, record 1</td>
<td>2</td>
<td>6</td>
<td>14</td>
<td>20</td>
<td>8</td>
<td>12</td>
</tr>
<tr>
<td>FMD1, record 2</td>
<td>5</td>
<td>6</td>
<td>11</td>
<td>11</td>
<td>10</td>
<td>19</td>
</tr>
</tbody>
</table>

REFERENCES


