Production Scheduling based on Deep Reinforcement Learning using Graph Convolutional Neural Network

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Abstract: While meeting frequently changing market needs, manufacturers are faced with the challenge of planning production schedules that achieve high overall performance of the factory and fulfill the high fill rate constraint on shop floors. Considerable skill is required to perform the onerous task of formulating a dispatching rule that achieves both goals simultaneously. To create a useful rule independent of human expertise, deep reinforcement learning based on deep neural networks (DNN) can be employed. However, conventional DNNs cannot learn the important features needed for meeting both requirements because they are unable to process qualitative information included in these schedules, such as the order of operations in each resource and correspondence between allocated operations and resources. In this paper, we propose a new DNN model that can extract features from both numeric and nonnumeric information using a graph convolutional neural network (GCNN). This is done by applying schedules as directed graphs, where numeric and nonnumeric information are represented as attributes of nodes and directed edges, respectively. The GCNN transforms both types of information into the feature values by transmitting and convoluting the attributes of each component on a directed graph. Our investigation shows that the proposed model outperforms the conventional one.

1 INTRODUCTION

In recent years, consumers’ needs have diversified, while the life cycles of products have shortened. Under these conditions, there are two issues in manufacturing industries for large-item small-volume production: First, the issues for managers to shorten the lead time (LT) from material input to product shipment and strengthen the ability to respond to short delivery time. Second, the issue for shop floors to perform efficiently subject to individual constraints for each product and production line. It is important for manufacturing industries to construct a production schedule that satisfies both managers and shop floors.

To make a production schedule, we use a general dispatching method (Pinedo, 2012), which makes schedules by successively allocating operations to resources based on dispatching rules. A dispatching rule is a criterion for selecting a remaining operation and a capable resource. Due to the simplicity of the existing rules, scheduling staff modify them so that a schedule satisfies both managers and shop floors, e.g., by combining multiple rules and/or adding individual constraints to the rules. However, to construct a good rule, we need trial and error based on experiences and expertise of scheduling staff. Therefore, this work can be a significant burden. Nowadays, due to labor shortage, especially in Japan, it is difficult to transfer the expertise to new staff. Thus, to reduce work load, we need a technology that automatically constructs a dispatching rule.

For the automatic construction of a dispatching rule, Riedmiller et al. (1999) applied deep reinforcement learning (DRL) to production scheduling. DRL is a machine learning method that learns a policy that selects an action for each state through trial and error. In the application of DRL to production scheduling, we make many schedules by using the learnt rule at that time and update the rule to select a good allocation.

In DRL, a dispatching rule is implemented as a DNN. The DNN receives a state of schedule-making and computes the probabilistic values for candidates of allocations. To construct a good schedule that satisfies both managers and shop floors, it is necessary for the DNN to extract two types of information: the factory’s overall performance and the fill rate constraint. However, the conventional DNN does not extract the latter, e.g., the resource
each operation is allocated to and the kind of operations allocated before or after. Therefore, a conventional DNN cannot be used to make a schedule that satisfies both managers and shop floors.

In this paper, we propose a new DNN model that can deal with both types of information. This model is based on the following two concepts: 1) a schedule can be represented as a graph structure and 2) a feature value of each node on the graph can be extracted by GCN.

The remainder of this paper is structured as follows. In section 2, we define the problem and production scheduling. In section 3, we explain the method of application of DRL to production scheduling and present the gaps in previous studies. In section 4, we propose a method to overcome the issue. In section 5 and 6, we present the experimental setup and the results. In section 7, we present the conclusion and future directions of research.

2 PRODUCTION SCHEDULING

In this paper, we deal with a job shop scheduling problem (JSP) (Pinedo, 2012) that models large-item small-volume production and add a practical extension to it. In a practical setting of the manufacturing industries, there are master data that define what can be produced and the orders are selected from the master data accordingly. To follow this setting, we define master data (mst for short) and artificially create a problem from it: transaction data (trn for short).

Master data is given as sets of \( n \) items \([\text{itm}_1, \ldots, \text{itm}_n]\) (itm for short) and \( m \) resources \([\text{rsc}_1, \ldots, \text{rsc}_m]\) (rsc for short). An item consists of \( m \) processes \([\text{prc}_1, \ldots, \text{prc}_m]\) (prc for short). A process requires processing time and one capable resource. Transaction data is given as a set of \( n \) jobs \([\text{job}_1, \ldots, \text{job}_n]\). A job is related to an item and should perform all processes of the item. We call these processes operations (opr for short). An operation should be allocated to a capable resource of a related process and follow a sequence of the process.

Algorithm 1: Deep Reinforcement Learning.

1. create \( N_{\text{train}} \) training problems
2. for \( t_{\text{train}} = 1, \ldots, T_{\text{train}} \):
   3. for each training problem:
   4. make \( N_{\text{EG}} \) schedules by EG with \( \epsilon \)
   5. select the best schedule
   6. update the DNN with selected schedules
7. \( \epsilon \leftarrow \epsilon - \Delta \epsilon \)

3 DEEP REINFORCEMENT LEARNING

3.1 Application to Scheduling

To generate a dispatching rule automatically, Riedmiller et al. (1999) proposed an approach using DRL. DRL applied to production scheduling generates a dispatching rule through trials and errors by repeatedly 1) making many schedules using the learnt rule at that time to obtain better supervised allocations and 2) updating the rules to select the supervised allocations.

In DRL, we make a schedule by successively allocating operations like in a dispatching method, but it differs from a dispatching method in that we use a DNN as a dispatching rule. A DNN receives a state of schedule-making and computes a policy, which is a set of probabilistic values for candidates of allocations. We select an allocation from the candidates that maximize the probabilistic value. A good schedule can be made by increasing the probabilistic value of a good allocation.

We show a general DRL algorithm in Algorithm 1. To construct a dispatching rule that makes a good schedule for several problems, we prepare \( N_{\text{train}} \) training problems from the master data. The algorithm consists of two phases and repeat it \( T_{\text{train}} \) times.

In the first phase, we make \( N_{\text{EG}} \) schedules for each training problem to obtain better supervised allocations by using an epsilon-greedy method (EG). For each scheduling step, we select an allocation by using the learned DNN or randomly with a probability \( 1 - \epsilon \) or \( \epsilon \). The search ratio \( \epsilon \) is initialized to \( \epsilon_0 \) and updated to \( \epsilon - \Delta \epsilon \) at the end of a training step.

In the second phase, we update the DNN so as to increase the probabilistic values of supervised allocations obtained in the previous phase. To reduce computational time and learn the best allocations, we select one schedule for each training problem that maximizes the value of a schedule. For each selected schedule and each scheduling step, we evaluate an error between an output of the DNN and a supervised allocation by a mean-squared error criterion (MSE) with one-hot representation and minimize them by Adam (Kingma et al., 2014) with default hyper parameters. (Although it is better to use a cross-entropy error criterion for the one-hot representation in general, we extracted better ability of the DNN in the MSE.)
3.2 Issues in Previous Studies

As mentioned in section 1, planning production schedules to satisfy the requirements of both factory management and operations is an urgent problem for manufacturers. When making schedules, manufacturers have to simultaneously consider the factory’s overall performance and the fill rate constraint on shop floors.

In the DRL framework, we construct a reward function based on the information to learn a better policy of allocating operations by repeatedly making trial production schedules and evaluating them. As such, it is necessary for a DNN to extract feature values that include both the information from the trial schedules satisfactorily. In general, it is easy to create a DNN model that deals with feature values of the factory’s overall performance as they are usually presented as numeric indices such as LT and availability. On the other hand, conventional DNN models, which are used in previous studies (Riedmiller et al., 1999; Zhang et al., 1995; Gabel et al., 2008), cannot extract feature values characterized by the satisfaction of the fill rate constraint. This is because such feature values are comprised of nonnumeric information about the schedules such as the resource each operation is allocated to and the kind of operations allocated before or after. It is difficult for a DNN model to accept the abovementioned nonnumeric information as input and transform them into feature values.

For example, Riedmiller et al. (1999) used only numeric information to extract feature values of schedules, e.g., tightness of a job with respect to its due date, an estimated tardiness, and an average slack. Thus, it is very hard to address the issues of production scheduling by employing the previous methods, which cannot deal with feature values of nonnumeric information in trial schedules. Therefore, we have to overcome this limitation of the conventional DNN model to learn a better policy of allocating operations for manufacturers so that production schedules contribute towards both satisfactory factory performance and higher fill rate constraint.

4 PROPOSED METHOD

To recognize both numeric and nonnumeric information by a DNN, we propose a new DNN model. Our approach is based on two concepts: 1) a schedule can be represented as a graph structure, 2) a feature value of each node on the graph can be extracted by GCN. In the graph structure of a schedule, we can represent numeric information as attribute values on nodes, and nonnumeric information as edges. In the GCNN, we can extract feature values on nodes from its adjacent relations defined by edges through graph convolutional operations. Therefore, we can extract feature values of nodes with respect to both numeric and nonnumeric information.

In section 4.1 and 4.2, we elaborate on the two basic concepts, respectively. In section 4.3, we add an enhancement that reduces the computational time of the proposed DNN. In section 4.4, we explain how to make a schedule by using the proposed DNN.

4.1 Schedule Graph

A graph structure is a data structure that consists of sets of nodes and edges. The relation of two nodes can be represented by an edge in a graph structure.

In a schedule graph, a node is used to represent a component of a schedule as shown in Table 1. A “block” column is used in section 4.3. We divide the node type of operation into “allocated operation” and “unallocated operation” so that a DNN can recognize the difference between the two.

Numeric information is represented as attribute values on nodes, e.g., an ability on rsc, processing time on prc, and working period on a/uopr. An ability attribute on the resource node is used to represent a difference among resources with the same function. For unallocated operations, we use the earliest start and end time that can be allocated because we cannot use a determined value.

Nonnumeric information is represented as directed edges, as shown in Table 2, e.g., process sequence (process) is from/to prc, capable resource of a process is an edge from prc to rsc, and allocated resource of an operation is an edge from aopr to rsc. There are redundant edges as well: process sequence edge (operation) and capable resource edge (operation). They are not necessary for defining the state of a schedule because using a process sequence edge (process) and a capable resource edge (process) is sufficient. As such, we use them to improve the efficiency of a GCN by connecting nodes that are not connected with a minimum element.

We show an example of a schedule graph in Figure 1. The graph on the right represents the state of a schedule, which is depicted on the left. Rsc (X, Y, and Z), prc (A ~ G), aopr (1, 2, 4, and 6), and uopr (3, 5 and 7) are defined as nodes. For simplicity, we do not show a capable resource edge (operation). For example, process sequence edge from prc A to prc B
Table 1: Node types of schedule graph.

<table>
<thead>
<tr>
<th>Name</th>
<th>Short</th>
<th>Block</th>
<th>Attributes</th>
</tr>
</thead>
<tbody>
<tr>
<td>Resource</td>
<td>rsc</td>
<td>mst</td>
<td>Ability</td>
</tr>
<tr>
<td>Process</td>
<td>prc</td>
<td>mst</td>
<td>Processing time</td>
</tr>
<tr>
<td>Unallocated</td>
<td>uopr</td>
<td>trn</td>
<td>Start date and time, End date and time, Working time</td>
</tr>
<tr>
<td>Allocated</td>
<td>aopr</td>
<td>sch</td>
<td>Start date and time, End date and time, Working time</td>
</tr>
</tbody>
</table>

Table 2: Directed edge types of schedule graph.

<table>
<thead>
<tr>
<th>Name</th>
<th>Block</th>
<th>From</th>
<th>To</th>
</tr>
</thead>
<tbody>
<tr>
<td>Process sequence (Process)</td>
<td>mst</td>
<td>prc</td>
<td>prc</td>
</tr>
<tr>
<td>Capable resource (Process)</td>
<td>mst</td>
<td>prc</td>
<td>rsc</td>
</tr>
<tr>
<td>Operation process</td>
<td>trn/sch</td>
<td>u/aopr</td>
<td>prc</td>
</tr>
<tr>
<td>Process sequence (Operation)</td>
<td>trn/sch</td>
<td>u/aopr</td>
<td>u/aopr</td>
</tr>
<tr>
<td>Capable resource (Operation)</td>
<td>trn/sch</td>
<td>u/aopr</td>
<td>rsc</td>
</tr>
<tr>
<td>Operation sequence</td>
<td>sch</td>
<td>aopr</td>
<td>aopr</td>
</tr>
<tr>
<td>Allocated resource</td>
<td>sch</td>
<td>aopr</td>
<td>rsc</td>
</tr>
</tbody>
</table>

Figure 1: Example of a schedule graph.

implies that prc A is a front process of prc B and prc B should be performed after prc A; allocated resource edge from aopr 1 to rsc X implies that aopr 1 is allocated to rsc X; and operation sequence edge from aopr 1 to aopr 6 implies that aopr 6 is to be processed after aopr 1 in the same resource.

This graph needs to be updated when a new operation is allocated. For example, we assume that uopr 3 is to be allocated to rsc Z after aopr 4. At first, node and edge types related to uopr 3 are changed from uopr to aopr. Next, the following edges are added to the graph: an operation sequence edge from aopr 4 to aopr 3 and an allocated resource edge from aopr 3 to rsc Z.

4.2 Graph Convolution

A GCNN is a form of DNN architecture that is developed to work on a graph structure (Gilmer et al., 2017). We define feature values on the nodes of a GCNN and update them by integrating them with their adjacent nodes. Through these processes, the feature values evolve into distinct values that contain information of their adjacent relations. We can obtain feature values of schedule components with both numeric and nonnumeric information and compute a policy with respect to them in a GCNN applied to a schedule graph.

Our GCNN consists of three layers: 1) an input layer, 2) a convolution layer, and 3) an output layer. All equations are shown from (1) ~ (10) below. \[ \] implies concatenation and \( \cdot \) implies inner product. \( \mathbf{h}_i \) implies a number of computations.

In input layer (1), we initialize a feature value \( h_i^0 \) of node i by an affine transformation from an attribute value \( \mathbf{x}_i \). Although the dimensions of the attribute values differ from each other, the dimensions of the feature values are unified to \( d \).

In a convolution layer, we integrate adjacent relations to a feature value. This layer consists of two functions: 2-1) a message function and 2-2) an update function. In a message function, for node i and its
adjacent node $j$ connected by edge type $e$, we compute a message $m_{ij}^e(e)$ from node $j$ to node $i$ through edge type $e$ in (2) and aggregate the messages that are categorized in the same edge type $e$ to one message $m_i^e(e)$ in (3). $\text{Adj}(i, e)$ denotes a set of adjacent nodes to node $i$ connected by edge type $e$. In update function (4), we reflect aggregated messages $m_i^e(e)$ on a feature value $h_i^e$ of node $i$ using a gated recurrent unit GRU$_i^e$ (Cho et al., 2014). #edge denotes the number of edge types that are connected to node $i$.

Nonnumeric information, represented as adjacent relations, is transformed to computations such that each node receives messages from its adjacent nodes only. Moreover, by repeating this layer $T_{conv}$ times, the entire information of the graph is reflected through feature values because feature values of indirectly connected nodes are propagated to each node.

We compute a policy in an output layer from feature values computed in a convolution layer. At first, we initialize $h_i$, and $a$ that are processed before/after uopr $i$.

Next, we compute a policy from a set of feature values of candidates by Set2Set architecture (Vinyals et al., 2015) in (6)-(10). Set2Set architecture is designed to work on a set of vectors and computes a feature value of the set itself. We compute a weight $p_k^{e, j}$ for each candidate $k$ of the set in (7) and (8) and summarize them in (9) as a feature value $r^s$ of the set. #cnd and Cnd denotes a number and a set of candidates, respectively. A feature value $r^s$ is used to update hidden values $q_{i,k}^s, c_{i,k}^s$ of candidate $k$ by a long short-term memory LSTM$_i^e, j$ (Hochreiter et al., 1997) in (10). By repeating (7)-(10) $T_{out}$ times, complete information of all candidates are reflected on feature value $r^s$ and weight $p^s$. In this paper, we use the weight $p^s$ as a policy.

As mentioned above, by using integrated feature values of both complete and detailed information, we can compute a policy with respect to the requirements of both managers and shop floors.

### 4.3 Speed-up of GCNN Computation

In the original concept of a GCNN in section 4.2, we re-make the feature values of all the nodes and convolute them using all the edges every time when selecting an allocation. However, there are minute changes between a schedule graph and its updated version, e.g., an operation sequence edge from aopr 4 to aopr 3 and an allocated resource edge from aopr 3 to rsc Z in the example in section 4.1. Assuming that there are few differences in the feature values of nodes with no change, almost all nodes have only a few differences in their feature values.

Therefore, to reduce computational time, we re-use feature values computed in previous scheduling steps and update them for nodes with changes only: dopr 2, 3, 4, prc C, and rsc Z in the example of section 4.1. We call this *partial convolution*. To construct a partial convolution, we reference a GCNN that can deal with a dynamic change in graph structure (Manessi et al., 2020; Ma et al., 2018).

An overview of a GCNN with partial convolution is shown in Figure 2. We prepare three blocks of GCNNs: 1) a master block, 2) a transaction block, and 3) a scheduling block, by combining layers of the original GCN. A scheduling block has a main function that updates feature values on nodes with changes only and is executed every time when selecting an allocation. We use the master and transaction blocks to extract feature values before we start scheduling.

![Figure 2: Overview of graph convolutional neural networks with partially convolutional.](image)

**Algorithm 2: Scheduling with partial convolution.**

1. execute master block
2. execute transaction block
3. initialize schedule
4. while schedule is not completed:
   5. compute a policy by output layer
   6. select an allocation by EG or top-k
   7. update the schedule
   8. execute scheduling block
9. return schedule

We show a procedure of scheduling with partial convolution in Algorithm 2. At first, we initialize feature values of nodes categorized to a master block by an input layer and convolute $N_{conv}^{master}$ times with nodes and edges categorized under a master block by a convolution layer. Then, we initialize feature values on nodes categorized under transaction block by an input layer and convolute $N_{conv}^{transaction}$ times with nodes and edges categorized under both master and transaction blocks. Thereafter, we can start scheduling. When we select an allocation, we compute a policy by an output layer with the feature values at that time. After an operation is
allocated, we update feature values of nodes with the changes by a scheduling block $N_{\text{env}}$ times.

### 4.4 How to Make a Schedule with DNN

Our DNN acquired a rich representation power and it can memorize a lot of supervised allocations. However, it is hard for the DNN to memorize all of them. There are always some mistakes in allocations in scheduling with a DNN.

Moreover, we make a schedule by successively selecting allocations and do not change a previously decided allocation. Therefore, there is some possibility that mistakes at the opening step of scheduling leads to the creation of a bad schedule.

To overcome these mistakes made by the DNN, we make $N_{\text{end}}$ schedules as candidates and select one that maximizes the value of a schedule. When we make candidates of schedules, we use candidates of allocations in only top-k of the probabilistic values and randomly select one from among them.

### 5 EXPERIMENT

We conduct an experiment to evaluate whether the value of a schedule made by the proposed method for problems not used in training gets better with the number of times of training.

We use a benchmark problem swv11 (50 items and 10 resources) in OR-Library (Beasley, 1990-2018). The abilities of resources are unified to 1.0. To create an artificial problem, we pick up 50 items randomly from the master data by allowing duplication. Therefore, each problem has 500 operations.

We evaluate a completed schedule by a makespan that is related to shortening LT from the perspective of managers and a degree of satisfaction of basic constraints of JSP from the perspective of shop floors. A makespan is a time span from start time to end time in which all operations are performed. In this paper, to simplify the problem, we assume that all candidates of allocations satisfy the basic constraints.

We compare the proposed method (conv.) with the one without convolution (no conv.). The comparison uses only numeric information (attribute values) and leaves out nonnumeric information (adjacent relations). This enables us to evaluate whether we need to use nonnumeric information to construct a good dispatching rule. Moreover, we use a dispatching method that is used for large-scale problems. A dispatching rule is the earliest start time rule as this rule makes the best schedule in a preliminary experiment.

#### Table 3: Setups of hyper parameters.

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>$N_{\text{test}}$</td>
<td>128</td>
</tr>
<tr>
<td>$T_{\text{train}}$</td>
<td>5</td>
</tr>
<tr>
<td>$N_{\text{train}}$</td>
<td>128</td>
</tr>
<tr>
<td>$T_{\text{env}}$</td>
<td>16 / 0</td>
</tr>
<tr>
<td>$N_{\text{BG}}$</td>
<td>128</td>
</tr>
<tr>
<td>$T_{\text{BG}}$</td>
<td>16 / 0</td>
</tr>
<tr>
<td>$N_{\text{end}}$</td>
<td>128</td>
</tr>
<tr>
<td>$T_{\text{env}}$</td>
<td>1 / 0</td>
</tr>
<tr>
<td>$\epsilon_0$</td>
<td>1.0</td>
</tr>
<tr>
<td>$T_{\text{out}}$</td>
<td>8</td>
</tr>
<tr>
<td>$\Delta$</td>
<td>0.1</td>
</tr>
<tr>
<td>$d$</td>
<td>8</td>
</tr>
<tr>
<td>top-k</td>
<td>2</td>
</tr>
<tr>
<td>Epoch</td>
<td>500</td>
</tr>
<tr>
<td>Mini-batch</td>
<td>4,000</td>
</tr>
</tbody>
</table>

#### Table 4: Experimental conditions.

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>OS</td>
<td>Windows 10 Pro</td>
</tr>
<tr>
<td>CPU</td>
<td>Intel Core i7-6700HQ, 2.60 GHz</td>
</tr>
<tr>
<td>Memory size</td>
<td>16.0 GB</td>
</tr>
<tr>
<td>Core number</td>
<td>8</td>
</tr>
<tr>
<td>DNN framework</td>
<td>PyTorch (1.0.1)</td>
</tr>
</tbody>
</table>

The procedure of the experiment is as follows. First, we prepare $N_{\text{test}}$ test problems. Next, we train a DNN with the algorithm 1 with the training problems. After step 6, we make a schedule for each test problem using the method in section 4.4 and evaluate their makespan. The setups of hyper parameters and experimental conditions are shown in Table 3 and Table 4, respectively.

### 6 RESULT

The results of the experiment are depicted in Figure 3. We use the ratio of makespan to dispatching method as
each problem has a different makespan. The mean values and standard deviations of $N_{\text{end}}$ schedules are presented in the figure 3. It takes about five weeks for complete training and about 100 seconds to make $N_{\text{end}}$ candidates of schedules.

The values derived by the proposed method with/without convolution are better than a dispatching method, even without training (number of times of training is 0). Thus, it is likely that they find a good schedule by making a lot of candidates, which is not an effect of convolutions.

A result worth noting is that a value given by the proposed method with convolutions improves with the number of times of training and outperforms the one without convolutions, which do not give the same results. With number of times of training at $T_{\text{train}}$, we achieve an 87%, 95%, or 97% reduction in makespan as compared to a dispatching method, where number of times of training is 0, and the proposed method without convolution. These differences are significant as per the t-test, which gives $\alpha = 0.05$. Therefore, we consider that the proposed method can select an appropriate allocation for each state of schedule-making because the DNN can recognize the state of making the schedule in detail as a result of convolutions.

7 CONCLUSION

We study the DRL method for learning dispatching rules automatically. Our contribution to the existing literature is a new DNN model that can recognize both numeric and nonnumeric information of schedule-making by applying graph structure of a schedule and a GCNN. Moreover, we reduce computational time of the GCNN by applying a partial convolution. After training a DNN using the DRL algorithm, we observed that the value of a schedule made by the proposed method for problems not used in training improves with the number of times of training. Therefore, we can automatically construct a good dispatching rule and expect to reduce the work load for scheduling staff.

However, this paper shows that the proposed method works on a restricted setting only. To use this method in a practical scenario, additional experiments and enhancements need to be conducted. First, the proposed method should work on problems with a scale of 1,000 operations. Second, the proposed method should make a schedule subject to individual constraints.

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REFERENCES


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