Nash Equilibria in Multi-Agent Swarms

Carsten Hahn, Thomy Phan, Sebastian Feld, Christoph Roch, Fabian Ritz, Andreas Sedlmeier, Thomas Gabor and Claudia Linnhoff-Popien

Mobile and Distributed Systems Group, LMU Munich, Munich, Germany
{carsten.hahn, thomy.phan, sebastian.feld, christoph.roch, fabian.ritz, andreas.sedlmeier, thomas.gabor, linnhoff}@if.i.lmu.de

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Abstract: In various settings in nature or robotics, swarms offer various benefits as a structure that can be joined easily and locally but still offers more resilience or efficiency at performing certain tasks. When these benefits are rewarded accordingly, even purely self-interested Multi-Agent reinforcement learning systems will thus learn to form swarms for each individual’s benefit. In this work we show, however, that under certain conditions swarms also pose Nash equilibria when interpreting the agents’ given task as multi-player game. We show that these conditions can be achieved by altering the area size (while allowing individual action choices) in a setting known from literature. We conclude that aside from offering valuable benefits to rational agents, swarms may also form due to pressuring deviants from swarming behavior into joining the swarm as is typical for Nash equilibria in social dilemmas.

1 INTRODUCTION

Flocking behavior can be observed in many species in nature. For example fish or birds coordinate their actions in order to form a swarm. This yields benefits like: hydrodynamic efficiency, higher mating chances, enhanced foraging success, enhanced predator detection, decreased probability of being caught and overall reduced individual effort. In order to profit from such benefits, swarming has also been transferred to technical systems featuring multiple robots or drones (Brambilla et al., 2013; Christensen et al., 2015). Swarms can be especially useful when they allow to use smaller, simpler and effectively cheaper robots and use the swarm to still allow for complex behavior and error resilience (against communication failures, bugs or external influences). However, since swarms rely on the emergent behavior of a group of individual agents, swarm behavior is often hard to pre-program or even just predict (Pinciroli and Beltrame, 2016).

In this paper, we consider the issue of swarms consisting of self-adaptive, learning agents and raise the question under which conditions these agents tend to form swarms purely out of self-interest. Here, multiple agents coming together within a swarm in the first place is not given or programmed but on its own already an emergent behavior. Özgüler and Yildiz (Özgüler and Yıldız, 2013) introduced a theoretical model to examine how swarms form. They modeled foraging swarm behavior as a non-cooperative N-player game and have shown that the resulting swarms pose a Nash equilibrium.

Hahn et al. (Hahn et al., 2019) have considered a continuous predator-prey scenario where a swarm of agents (resembling fishes) aims to survive for as long as possible in the presence of an enemy agent (resembling a shark, e.g.). Under certain conditions, swarms in such Multi-Agent system can emerge solely by training (using reinforcement learning, e.g.) each agent on the purely self-interested goal of securing its own survival. It has been observed that the agents learn to form clusters because the predator can be distracted by multiple agents in its vicinity, which increases the survival chance of any individual. In their work only the prey agents are actively trained while the present predator follows a predefined static heuristic strategy. The prey agents are self-interested and maximize solely their own reward (i.e., surviving as long as possible). The group of agents is trained by iteratively training only one of the prey agents and copying its learned policy to all other homogeneous agents.

The work of (Hahn et al., 2019) focuses mainly on the examination of the resulting swarms and their comparison to existing related swarm approaches.
(Reynolds, 1987; Morihiro et al., 2008). But they also investigate origin and characteristics of the social behavior between prey agents and hint that the swarm behavior of multiple self-interested agents trained using Multi-Agent reinforcement learning is linked to Nash Equilibria.

We build on this foundation to further investigate Nash equilibria in Multi-Agent swarms resulting from Multi-Agent reinforcement learning. We adopt the scenario of (Hahn et al., 2019) for our research and further examine the conditions under which forming a swarm pays off for each individual agent or under which running individually is the superior strategy. We show that the partial observable scenario can be expanded and the learned policies can adapt without any re-training. We relax the imposed criteria on agent homogeneity, i.e., we allow each agent to choose for itself if it wants to join a swarm or roam on its own. We observe that this decision poses a social dilemma as swarms only offer a benefit at a certain size. However, we also show that some swarm configurations form Nash equilibria under certain conditions, which means that even when swarming might not be the strictly superior strategy in a certain situation, deviating from an already instituted is still worse for a single agent.

2 FOUNDATIONS

2.1 Reinforcement Learning

Reinforcement Learning (RL) is a machine learning paradigm which models an autonomous agent that has to find a decision strategy in order to solve a task. The problem is typically formulated as Markov Decision Process (MDP) (Howard, 1961; Puterman, 2014) which is defined by a tuple \( M = (S, \mathcal{A}, P, R) \), where \( S \) is a set of states, \( \mathcal{A} \) is the set of actions, \( P(s_{t+1} | s_t, a_t) \) is the transition probability function and \( R(s_t, a_t) \) is the scalar reward function. We assume that \( s_t, s_{t+1} \in S, a_t \in \mathcal{A}, r_t = R(s_t, a_t) \), where \( s_{t+1} \) is reached after executing \( a_t \) in \( s_t \) at time step \( t \). \( \Pi \) is the policy space.

The goal is to find a policy \( \pi : S \rightarrow \mathcal{A} \) with \( \pi \in \Pi \), which maximizes the expected (discounted) return \( G_t \) at state \( s_t \) for a horizon \( h \):

\[
G_t = \sum_{k=0}^{h-1} \gamma^k \cdot R(s_{t+k}, a_{t+k})
\]

where \( \gamma \in [0, 1] \) is the discount factor.

A policy \( \pi \) can be evaluated with a value function \( Q^\pi(s_t, a_t) = \mathbb{E}_\pi [G_t | s_t, a_t] \), which is defined by the expected return when executing \( a_t \) at state \( s_t \) and following \( \pi \) afterwards (Bellman, 1957; Howard, 1961). \( \pi \) is optimal if \( Q^\pi(s_t, a_t) \geq Q^{\pi'}(s_t, a_t) \) for all \( s_t \in S \), \( a_t \in \mathcal{A} \), and all policies \( \pi' \in \Pi \). The optimal value function, which is the value function for any optimal policy \( \pi^* \), is denoted as \( Q^* \) and defined by (Bellman, 1957):

\[
Q^*(s_t, a_t) = r_t + \gamma \sum_{s' \in S} P(s' | s_t, a_t) \cdot \max_{a' \in \mathcal{A}} \{Q^*(s', a')\}
\]

When \( Q^* \) is known, then \( \pi^* \) is defined by \( \pi^*(s_t) = \arg\max_{a \in \mathcal{A}} \{Q^*(s_t, a)\} \).

Q-Learning is a popular RL algorithm to approximate \( Q^* \) from experience samples (Watkins, 1989). In the past few years, Q-Learning variants based on deep learning, called Deep Q-Networks (DQN), have been applied to high dimensional domains like video games and Multi-Agent systems (Mnih et al., 2015; Hausknecht and Stone, 2015; Leibo et al., 2017).

2.2 Game Theory and Multi-Agent Reinforcement Learning

Multi-Agent Reinforcement Learning (MARL) problems can be formulated as stochastic game \( M = (S, \mathcal{A}, P, R, \mathcal{Z}, O, n) \), where \( S, \mathcal{A} \) are \( P \) equivalently defined as in MDPs. \( n \) is the number of agents, \( \mathcal{A} = \mathcal{A}_1 \times \ldots \times \mathcal{A}_n \) the set of joint actions, \( \mathcal{Z} \) is the set of local observations, and \( O(s_t, i) \) is the observation function for agent \( i \) with \( 1 \leq i \leq n \). \( R = R_1 \times \ldots \times R_n \) is the joint reward function, with \( R_i(s_t, a_{t,i}) \) being the individual reward of agent \( i \).

In MARL, each agent \( i \) has to find a local policy \( \pi_i \), which is optimal w.r.t. the policies of the other agents. If the other agents change their behavior then agent \( i \) also need to adapt, since its previous policy might have become suboptimal. The simplest approach to MARL is to use single-agent RL algorithms like Q-Learning and scale them up to multiple agents (Tan, 1993; Leibo et al., 2017). In homogeneous settings, the policies can be shared by effectively learning only one local policy \( \pi_i \), and replicate the learned policy to all agents. This can accelerate the learning process as experience can be shared during training (Tan, 1993; Foerster et al., 2016). While many other approaches to MARL in games exist which incorporate global information into the training process (Foerster et al., 2016; Lowe et al., 2017; Foerster et al., 2018; Rashid et al., 2018), we focus on the simple case of applying single-agent RL to games with policy sharing.
2.3 Swarm Intelligence

One of the most common approaches for generating artificial flocking behavior is the so-called “Boids” approach proposed by (Reynolds, 1987). Reynolds proposed three basic steering rules which only require local knowledge of an individual about other individuals within its view radius. The rules are:

- **Alignment**: Steer towards the average heading direction of nearby individuals
- **Cohesion**: Steer towards the average position (center of mass) of visible individuals
- **Separation**: Steer in order to keep a minimum distance to nearby individuals (to avoid collisions and crowding)

If each individual follows these rules, naturally appearing swarm formations can be observed. Implementing the rules can be done by expressing them as forces that act upon an individual. They can be extended in order to repel from an enemy or obstacles respectively be attracted by food, for example.

Hahn et al. (Hahn et al., 2019) introduced SELFish, a Multi-Agent system in which multiple homogeneous agents (independently from each other) try to survive as long as possible while a predator is chasing them. The predator might get distracted by multiple preys in its vicinity. Hahn et al. showed that agents trained using Multi-Agent reinforcement learning realize to exploit this property by forming a swarm in order to increase their survival chances. This swarming behavior is extensively examined and compared to other swarming/flocking algorithms (for example the “Boids” approach). Furthermore (Hahn et al., 2019) measured the survival time of the agents and compared it to other policies, among others a hand crafted policy called TurnAway. By following the TurnAway strategy, agents turn in the opposite direction the predator and flee without considering other agents or obstacles. Hahn et al. ended their paper with a hypothesis of Nash equilibria in Multi-Agent swarms. This hypothesis will be picked up and extended in this work.

Özgüler and Yıldız (Özgüler and Yıldız, 2013) also investigated Nash equilibria in Multi-Agent swarms. To do so, they modeled the foraging process of multiple agents as a non-cooperative N-player game. They assumed that each agent wants to minimize its individual total effort in a time interval by controlling its velocity. By establishing a nonlinear differential equation in terms of positions of the agents and solving this equation they show that the game has a Nash equilibrium.

2.4 Nash Equilibria

Game theory considers strategic interactions within a group of individuals. In doing so, the actions of each individual affect the outcome and the individuals are aware of this fact. In addition, the participating individuals are considered rational. This means, that they have clearly defined goals within the possible outcomes of the interactions and that they implement the best available strategy to pursue their goals. Usually, the rules of the game and rationality are well known.

Basically, two different forms of representation exist: the normal form is used when the players choose one strategy without knowing the others’ choices. The extensive form is used when some players know what other players have done while playing. In many settings, no communication between the players is possible or desired, which is why in the following only the normal form game (also: strategic form game) is described. A normal form game \( G = (N, \{A_i\}_{i \in N}, \{u_i\}_{i \in N}) \) consists of a set of players \( N \), a set of actions with \( A_i \) for each player \( i \) and a payoff function \( u_i : A \rightarrow R \) for each player \( i \). The action profile \( a = (a_1, ..., a_n) \) is a collection of actions, one for each player, also called strategy profile. \( a_i \) is a strategy profile without the action of player \( i \). All possible collections of actions are also called space of action profiles \( A = (a_1, ..., a_n) : a_i \in A_i, i = 1, ..., n \).

A Nash Equilibrium (NE) is a strategy profile so that each strategy is a best response to all other strategies. A best response is the reaction to an action that maximizes the payoff.

Expressed in formal terms, a result \( a^* = (a_1^*, ..., a_n^*) \) is a Nash Equilibrium, if for every player \( i \) the following holds: \( u_i(a_i^*, a_j^*) \geq u_i(a_i, a_j^*) \quad \forall a_i \in A_i \).

The most interesting feature about NEs is that they are self-assertive: no player has an incentive to deviate unilaterally.

Regarding the swarm environment in this paper, the self interested agents correspond to the non-cooperative players of a normal form game. SELFish\(_DQN\) and TurnAway, which will be explained in the Section 3 match to the possible set of actions, a player, respectively agent, can choose from. The reward of a agent, which correlates to the survival time of an individual corresponds to the payoff of a certain strategy profile. With defining such a swarm environment as a normal form game it is possible to find NEs with a common Nash solver. In this work the popular Gambit Solver was used (McKelvey et al., 2016).
2.5 Social Dilemmas in Multi-Agent Systems

In many Multi-Agent Systems, agents need to cooperate in order to maximize their own utilities. In (de Cote et al., 2006), the authors analyze Multi-Agent social dilemmas in which RL algorithms are confronted with Nash Equilibria forming a rational optimal solution on the short term but not being optimal in repeated interaction. They propose heuristic principles to improve cooperation and overcome such one-shot Nash Equilibrium strategies. However, their experiments are limited to a prisoner’s dilemma scenario with three agents and four actions. More recently, (Leibo et al., 2017) demonstrated that the learned behavior of agents in Multi-Agent systems changes as a function of environmental factors. They experimentally show how conflicts can emerge from competition over shared resources and how the sequential nature of real world social dilemmas affects cooperation. While their environments’ complexity is comparable to this paper’s, their experiments are limited to two agents. Nevertheless, the Nash Equilibria suspected in (Hahn et al., 2019) and further examined in this paper shares many characteristics with the sequential social dilemmas introduced in (Leibo et al., 2017). The swarming behavior learned is a strategy spanning over multiple actions and is experimentally shown to not be the optimal strategy for the collective of agents. But as swarming behavior clearly requires some form of coordination, the analysis of whether or not swarming may be considered a defect in the sense of (Leibo et al., 2017) is left open for further analysis.

3 EXPERIMENTAL SETUP

3.1 SELFish Environment

We use the same environment as (Hahn et al., 2019) and extend their experiments. The agents can roam freely in a two-dimensional area (see Figure 1). The area wraps around at the edges, meaning an agent that leaves it on the right side will immediately re-enter it from the left (same with top and bottom). Aside with the trained agents the environment is inhabited by a predator which pursues a predefined static policy. The predator can sense prey agents within a certain radius and chooses one randomly as target (and keeps this target for a certain time). This means that the predator might be distracted by multiple agents in its proximity, which implies that it might be beneficial for an agent to be close to others, thus modeling one of the established benefits of joining a swarm. Both the prey agents and the predator are embodied as circles with a certain radius and a variable orientation (see Figure 1). A prey agent is considered caught when it collides with the predator. It is then immediately respawned in the area. The predator and the prey usually move at the same speed to encourage situations in which a prey agent can escape from the predator when it gets distracted. However, because of the torus property of the area, this would allow a prey agent to simply turn in the opposite direction of the predator and move away without the possibility of the predator ever catching up. That is why the predator increases its speed every 80 steps over a duration of 20 steps.

The objective that is learned by the prey agents is to survive as long as possible. This is reinforced with a reward of +1 for each step survived and -1000 for colliding with the predator. As soon as the learning agent collides with the predator, the episode ends and its knowledge is copied to all other agents.

As all agents move at a constant speed, the only decision an agent has to make every step, is the degree the agent wants to turn before it is moved a certain unit in that direction. For DQN the action space comprises of five discrete degree values \{-90°, -45°, 0°, +45°, +90°\}.

3.2 State Encoding

The state of the environment is only partially observable for an agent. This facilitates the scalability of the approach and represents autonomous agents or biological individuals in reality as it is unlikely that an individual can sense the whole state of any physical environment/world. It is also in accordance with other related swarming algorithms like (Reynolds, 1987) where an agent only considers a local neighborhood
of other agents and adjusts its direction according to rules of cohesion, alignment and separation.

In SELFish (Hahn et al., 2019), every agent can at most observe \( n \) other entities (i.e., other prey agents or the predator) in its vicinity. As observation, every agent \( a \) receives for all other agents \( e_i, i \in [1,n] \), within its observation the distance between \( a \) and \( e_i \), the angle \( a \) would have to turn in order to face in the direction of \( e_i \) and the absolute orientation of \( e_i \) in space. The angle an agent has to turn in order to face another observed entity is pre-calculated in degrees in the range of \((-180^\circ, 180^\circ]\). The absolute orientation of an entity in space is measured in degrees in the range of \([0^\circ, 360^\circ)\). \( 0^\circ \) corresponds to facing eastwards, measuring the angle counter-clockwise.

Every agent receives the previously explained measurements as observation for the predator, itself and for a certain number of \( n \) neighboring agents, in which the \( n \) neighbors are ordered by their distance. The measurements are flattened into a vector before they are handed to the agents. Furthermore the distance is divided by the area width and the direction and orientation are normalized to the interval \([0, 1]\).

### 3.3 Training

Training is performed using the Keras-RL (Plappert, 2016) implementation of DQN. As DQN is intended for single agent use, the training of the multiple homogeneous agents is executed as proposed by (Egorov, 2016): Only one agent is actually trained and its policy is copied to the others after the end of an episode. An episode ends if the learning agent is caught by the predator or after 10,000 steps were executed.

During the training the edge lengths of the area always are 40 by 40 pixels. However, the agents as well as the predator can take every real valued position in \([0,40] \times [0,40]\). The agents and the predator have the size of a circle with radius 1, meaning a collision (catch) occurs at a distance below 2. Please note that no other collisions are considered (between agents and other agents or agents and walls). Also there are no obstacles in the area. During training there are 10 agents in the environment.

In order to assess the quality of a training run, the cumulative reward of the learning agent is measured. According to the reward structure this essentially corresponds with the number of time steps the learning agent survived.

Reproduced from (Hahn et al., 2019), the results of training showed swarming behavior of the agents in order to increase their survival chances, although only 10 agents were present during training.

### 4 SCALING OF PARTIALLY OBSERVABLE SCENARIOS

Because of the partial observability and the normalization of the observation the learned policy of the case with 10 agents can also be used in scenarios with other parameters in regard to the number of agents present or the size of the available area. This interrelationship will be further investigated in the following section.

Figure 2 shows the average episode length, which essentially corresponds to the average survival time of a certain agent (i.e., the learning agent). An episode ends if the learning agent is caught by the predator or 10,000 steps were made. As the learning agent receives a +1 for every step and −1000 for being caught, it is encouraged to survive as long as possible to maximize its accumulated reward. For the static strategy of turning 180° away from the predator without minding other agents (i.e., TurnAway) this means that a certain agent is caught in order for an episode to end.\(^1\). In Figure 2 the number of agents is varied while the size of the area remains the same (40 × 40 pixels). Please note that although the number of agents is varied, the policy of SELFish\(_{DQN}\), which was learned with 10 agents in the environment, stays the same. One can see that the performance of the policy, despite the fact that the environment settings are modified, does not collapse. The increase of the average episode length for higher number of agents comes from the circumstance that, with more agents in the environment, the probability decreases that any particular agent is caught. The measurements for TurnAway are given for comparison. Nevertheless, Figure 2 shows that TurnAway performs better w.r.t. the

\(^1\)For a short video showing an example of the policies SELFish\(_{DQN}\) and TurnAway please refer to https://youtu.be/nYKamj9qIFM

![Figure 2: Average episode length (survival time) of the learning agent in accordance with (Hahn et al., 2019). The policy SELFish\(_{DQN}\) was trained with 10 agents on 40 × 40 pixels and it then used for larger numbers of agents.](image-url)
average episode length or the survival time of a particular agent, respectively. This raises the question, why this policy was not found by reinforcement learning, which will be further examined in the following section.

5 NASH EQUILIBRIA IN SWARMS

As previously mentioned, 10 homogeneous agents were trained on a 40×40 pixel area, while only one agent was actually trained using reinforcement learning and its policy was copied to all other agents after each episode. An episode ended if the learning agent was caught by the predator (i.e., collided with it) or 10,000 steps were executed. The reward was structured in such a way that the learning agent was encouraged to stay alive as possible. The predator has the property that it might get distracted by multiple prey agents in its proximity. That is why the agents learned to form swarms in order to increase their survival chances. Another strategy in which the agent always turned in the opposite direction of the predator and fled without minding other agents was implemented for comparison (TurnAway). Figure 2 showed that the policy learned with 10 agents on a 40×40 pixel area can be used in settings with more agents without breaking. But furthermore it showed that the static policy of turning away performs better than the learned policy in terms of survival time.

To further investigate this phenomenon we carry out an experiment in which agents pursuing both policies (learned and static) are present. The results are shown in Figure 3. Figure 3 shows a setup where in an area of 40×40 pixels 10 agents are present. These agents either use the learned SELFishDQN policy (trained with 10 homogeneous agents on 40×40 pixel) or the static TurnAway policy. The agents following SELFishDQN tend to form swarms as they learned that this might increase their survival chances (given the property of a distractible predator) while TurnAway-agent do not care about others (except for the predator). The abscissa illustrate the mixing proportion of the agents with their particular type. For example, the entry (6,4) on the abscissa means that there are 6 agents executing TurnAway and 4 agents executing SELFishDQN in the setting. On the ordinate the survival time (in steps) of individuals following either SELFishDQN or TurnAway is indicated (averaged over individuals inside each policy type). The experiment was carried out over 10 runs (with different seeds), each with 10 episodes which lasted 100,000 steps (with no other stopping criteria). This resulted in thousand of caught agents in both policy groups whose survival time was then averaged. Caught agents respawned at the most dense spot of the swarm (determined with Kernel Density Estimation (Phillips et al., 2006; Hahn et al., 2019)). This was done because moving away from the swarm respectively ignoring the action of other agents was of particular interest for this experiment and the swarm behavior should not be disturbed by respawning agents.

The experiment reveals multiple interesting insights:

1. The performance of SELFishDQN w.r.t. the survival time in the setting it was actually trained on is better than TurnAway. This means that the usage of a policy obtained in a partially observable model in a setting with other parameters is possible but might not result in consistent performance with the trained setting (cf. Figure 2).

2. Flocking behavior resulting from reinforcement learning in this setting (multiple homogeneous agents evading/distracting a predator) is a Nash equilibrium (green line at (0,10) in Figure 3). This means that if there are 10 agents performing SELFishDQN with a tendency to swarming/grouping (and zero performing TurnAway), then no agent has an incentive to deviate from this policy of “swarming” while all others keep their strategy. We can see that moving out of the swarm and ignoring the others (like TurnAway) leads the agent onto the free space, where it is an easy prey for the predator. We also confirmed this intuition by calculating the Nash equilibria with the Gambit software tools for game theory (McKelvey et al., 2016). This was done by considering the average survival time of an agent pursuing a certain strategy as payoff in a normal-form game. This means, for example, that if 9 agents perform SELFishDQN, the payoff of ev-

![Figure 3: Performance of SELFishDQN (trained with 10 agents on 40×40 pixel) versus TurnAway on a 40×40 pixel area. Nash equilibria marked with a green line.](image-url)
Every agent following this strategy is 561 while the one agent performing TurnAway has a payoff of 415. Gambit also revealed a less obvious Nash equilibrium at (7, 3). At this point an agent performing TurnAway (payoff 619) has no incentive to switch its strategy to SELFishDQN (payoff 614 of SELFishDQN at point (6, 4)). In addition, an agent performing SELFishDQN (payoff 610) has no incentive to switch to TurnAway (payoff 574 at (8, 2)) while the other agents keep their strategy (see Table 1).

3. Policies in Multi-Agent scenarios produced with DQN and the method proposed by (Egorov, 2016) can only take the outer points (0, 10) and (10, 0) as all agents perform the same policy. In the example of an area size of 40 × 40 pixels, (0, 10) is surely better while a ratio of (6, 4) is the best mixture of both strategies (although) still not the best performance achievable in this setting.

To further substantiate our results, we repeat this experiment in area sizes of 80 × 80 and 20 × 20 pixels. The results can be seen in Figure 4 and 5. They show that the results vary for different area sizes, like pure

Table 1: Survival time/payoff of 10 agents with different policies in an area of 40 × 40 pixels.

<table>
<thead>
<tr>
<th>Number of agents</th>
<th>Survival time</th>
</tr>
</thead>
<tbody>
<tr>
<td>Turn Away</td>
<td>SELFishDQN</td>
</tr>
<tr>
<td>Turn Away</td>
<td>SELFishDQN</td>
</tr>
<tr>
<td>0</td>
<td>nan</td>
</tr>
<tr>
<td>1</td>
<td>9</td>
</tr>
<tr>
<td>2</td>
<td>8</td>
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<tr>
<td>3</td>
<td>7</td>
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<td>4</td>
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<td>3</td>
</tr>
<tr>
<td>8</td>
<td>2</td>
</tr>
<tr>
<td>9</td>
<td>1</td>
</tr>
<tr>
<td>10</td>
<td>0</td>
</tr>
</tbody>
</table>

TurnAway clearly outperforming pure SELFishDQN in the 80 × 80 pixel case and different Nash equilibria like (4, 6) in the 20 × 20 pixel case.

6 CONCLUSION

In this paper we further examine the experimental setup of (Hahn et al., 2019). Hahn et al. trained multiple homogeneous agents to evade a predator for as long as possible. The predator in that setting follows a static pre-defined policy and can be distracted by multiple possible preys in its vicinity. This modelled one of the benefits of forming a swarm and the agents learned to exploit this circumstance accordingly.

Expanding this setup, we showed that policies obtained through reinforcement learning in partially observable scenarios can be used in other settings without a collapse of the performance, although consistent performance (compared to the setting the policy was actually trained on) cannot be guaranteed. Furthermore we showed that the swarm resulting from Multi-Agent reinforcement learning in a predator/prey scenario has a Nash equilibrium, i.e., that there are scenarios were specific swarm configurations are stable (assuming rational agents) but still suboptimal. We analyzed this effect in dependance of the area size. We concluded swarming or not swarming can be formulated as a social dilemma in some settings.

This sheds some light on the reasons why swarms emerge. The introduction started by listing benefits observed from biological swarms. The presented research, however, might list another reason for the formation of swarms: social pressure. The existence of a swarm of substantial size may actively impede
the survival of non-swarming individuals, thus urging them to join the swarm even when it is suboptimal to all individuals’ survival. Note that this affects rational agents, i.e., swarm participants that act locally optimal at every single one of their decisions.

Interestingly, the phenomenon of pressure arising from lack of communication and control structures has been observed in natural evolution as well (Dawkins, 1976). Thus, swarms can (under certain conditions) also be interpreted as self-perpetuating, which means that they should be handled with additional care when employing them in practical applications. Self-perpetuating swarms might introduce additional targets for emergent behavior that affect the system designer’s intended purpose. It is up to future research to examine the interplay between using such emergent behavior and controlling it to employ useful swarm applications.

REFERENCES


