Aerial Radar Target Classification using Artificial Neural Networks

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Keywords: Aerial Radar Target Classification, Radar Cross Section (RCS), Time-Series Classification, Fully-Connected Neural Networks, Empirical Mode Decomposition (EMD).

Abstract: In this paper, we propose a new algorithm for classification of aerial radar targets by using Radar Cross Section (RCS) time-series corresponding to target detections of a given track. RCS values are obtained directly from SNR values, according to the radar equation. The classification is based on analysing the behaviour of the RCS time-series, which is the unique “fingerprint” of an aerial radar target. The classification process proposed in this paper is based on training a fully-connected neural network on features extracted from the RCS time-series and its corresponding Intrinsic Mode Functions (IMFs). The training is based on a database containing RCS signatures of various aerial targets. The algorithm has been tested on a large and diverse set of simulative flight trajectories, and its performance has been compared with that of several different methods. We have found that the proposed neural network-based classifier performed better on our database.

1 INTRODUCTION

Conventional uses of radar systems include detection of targets through transmission of radio waves and re-scattering of echoes from targets (Skolnik, 1962). Radar systems, however, do not provide information regarding the specific type of target which is detected.

In the past few decades, there has been an effort to approach the problem of radar target recognition (Herman & Moulin, 2002) – (Notkin \textit{et al}. 2019). Most of the works presented so far utilized Radar Cross Section (RCS) time-series corresponding to target detections for classification. RCS values are not obtained directly by the radar. In fact, the radar yields signal-to-noise ratio (SNR) values, which can be transformed into RCS values by using the radar equation. The RCS signature of aerial targets depends on various factors, such as the target’s unique geometry, size, orientation, and reflectiveness, as well as on the transmission frequency. RCS values can therefore provide useful information regarding target characteristics.

RCS measurements of aerial targets are strongly dependent on the aspect angles (azimuth and elevation), relative to the radar. These angles determine where the radar beam hits the target. Since different points on the target reflect the radar beam differently, RCS values are characterized by large variances, and even a slight change in one of the aspect angles can cause large fluctuations. Nevertheless, development of an aerial target recognition capability is of great interest. There have been several proposals to classify targets based on various methods (Herman & Moulin, 2002), (Molchanov \textit{et al}. 2012), (Tian \textit{et al}. 2015), (Notkin \textit{et al}. 2019).

The RCS time-series corresponding to an aerial target track contains abundant information, which can be used to characterise target types. However, RCS time-series is non-stationary, which makes it difficult to analyse. This calls for a comprehensive signal processing analysis.

Empirical Mode Decomposition (EMD) is an effective nonlinear signal processing technique for adaptively representing non-stationary signals as a sum of zero-mean components, known as Intrinsic Mode Functions (IMFs) (Huang \textit{et al}. 1998). Since its introduction, it has been used in various applications (Colominas \textit{et al}. 2014).

In this paper, we present a new method for classifying aerial radar targets based on fully-connected neural networks. Our algorithm utilizes a database of RCS signatures of various types of aerial targets, at a given resolution of aspect angles. Given an observed flight track, and the corresponding RCS
time-series, we extract RCS signals corresponding to the track, for all available targets in the database. RCS signals are then decomposed into IMFs using EMD. Features are then extracted from this set of RCS and corresponding IMF signals. Finally, a fully-connected neural network is trained with these features to identify the observed target.

We compare the neural network-based classifier with the K-Nearest Neighbour (KNN) classifier and three classifiers that are based on time-series similarity measures. In these types of classifiers, a target can be identified by measuring the similarity between the measured RCS signal, and RCS signals of available targets in the database, corresponding to the same flight track.

The paper is organized as follows: Section 2 describes the data preparation, and feature extraction stages. Section 3 describes the proposed neural network. Section 4 presents the results. Conclusions are provided in section 5.

2 THE METHOD FOR PREPARING RCS DATA FOR THE CLASSIFIER

In this section, we present our method for preparing the training and test data for the neural-network based classifier.

In this work, we simulated a database that contains RCS signatures for 8 different targets at two aspect angles relative to the radar: azimuth $\in [0, 360^\circ]$, and elevation $\in [-90^\circ, 90^\circ]$ at a given resolution. The targets are indicated by the letters A, B, C1, C2, C3, C4, D and E. Targets C1-4 are four different configurations of the same aircraft model, which lead to mild changes in RCS signature.

In addition to the simulated database, we simulated a radar tracker, and target trajectories. The tracker provided us with the position and velocity of the target, as well as the aspect angles (azimuth and elevation), relative to the radar. Knowing these aspect angles enabled us to extract the corresponding RCS values by interpolating the database.

In each simulation of a target trajectory, we obtained a time-series of RCS values. The RCS time-series corresponding to the observed flight track is given by $x \in \mathbb{R}^N$, where $N$ is the number of consecutive RCS measurements for a given trajectory.

Since aspect angles obtained by the radar are not accurate, we generated RCS sequences for each pair of possible aspect angles. This is done for all targets in the database. The set of possible RCS time-sequences for each of the targets form a “dynamic bank”. The dynamic bank is denoted by $B \in \mathbb{R}^{N \times M \times K}$. $N$ is the number of RCS measurements for a given trajectory. Since aspect angle estimation has inherent error, we generate $M$ possible RCS sequences for each target corresponding to a resolution of $M$ possible aspect angles. $K$ is the number of targets in the database.

The RCS time-series of a target-track is generally composed of low-frequency and high-frequency components. The assumption is that the low frequencies correspond to the observation angle and measurement errors, while the higher frequencies are related to the target’s geometry and aspect angles relative to the radar (Tian et al., 2015). Therefore, the rapidly varying components in the RCS time-series can characterize the targets well.

The RCS time-series is decomposed into frequency components by using a signal processing technique known as Empirical Mode Decomposition (EMD). EMD decomposes a non-stationary signal into stationary Intrinsic Mode Functions (IMFs) (Huang et al., 1998; Rilling et al., 2003). The IMFs are ordered according to their frequency components from high to low, as shown in figure 1. By using the temporal RCS data in the dynamic bank $B$, and the RCS time-series of the observed track $x$, we implement EMD to decompose the RCS data into IMFs.

At this stage, we extract ten features from the RCS time-sequences in $B$, and ten features from their corresponding IMFs. These features are later used as training data for the neural network. The features are chosen to characterize the statistical and spectral
nature of the time sequences well, while at the same time enabling separation of targets. Classifying targets based on noisy radar data using these features can suppress the effect the noise, in comparison with classification based on the raw RCS data.

The first and second features, minimum and maximum values, are used as a measure of the range of values that the time-series can take. The next four features; the mean, variance, skewness and kurtosis of the time-series are the 1st-4th standardized moments, where the sample mean is the average of the time-series values, variance indicates the spread of data from the mean, skewness is a measure of the asymmetry of the data around the mean, and kurtosis is a measure of how outlier-prone the distribution of values is. The next feature is the energy of the signal, which is the squared $L^2$ norm. The last two features are Hjorth mobility and complexity (Hjorth, 1970). Mobility represents the mean frequency, or the portion of standard deviation of the power spectrum. Hjorth complexity represents the change in frequency of a signal.

The RCS and IMF features for each time-series in the dynamic bank are concatenated into the tensor:

$$\mathbf{X}(\omega) \in \mathbb{R}^{N_r \times M \times K},$$

where $N_r$ is number of elements in each feature vector, and $M \times K$ is the number of training examples. $M$ is the number of possible aspect angles, and $K$ is the number of targets in the database. Each component in the feature vector is standardized using the z-score normalization. The feature-tensor $\mathbf{X}(\omega)$ has a corresponding label tensor: $\mathbf{Y}(\omega) \in \mathbb{R}^{N_t \times M \times K}$. We denote $Y_{k,i}$ as the $(k,i)$ element in the matrix, where $k = 0,1,\ldots,K-1$, and $i = 0,1,\ldots,MK-1$. $Y_{k,i} = 1$ if training example $i$ belongs to class $k$, and 0 otherwise. The same feature extraction process is applied to the signal $\mathbf{x}$, corresponding to the observed target, with $\mathbf{x}(\text{test}) \in \mathbb{R}^{N_t}$ the corresponding feature vector, which will be used to test the network.

### 3 THE PROPOSED NEURAL NETWORK CLASSIFIER

In this section, we will describe the proposed neural network-based classifier, and how it uses the features to classify the aerial targets. Artificial neural networks are mathematical models for solving complex problems, originally inspired by the way in which the brain processes information (Theodoridis & Koutroumbas, 2003). The network is composed of several layers of neurons, where the first layer is the input layer, and the last layer is the network decision, or solution to the problem. Neurons are nodes in the network that take in a weighted sum of values and produce a single output value, which is then processed by more neurons in the next layer.

In order to identify the observed target as one of the targets in the database, we use a 2-layer fully-connected neural network. The network has one hidden layer, and a softmax output layer that normalizes the outputs into probabilities for each target. The neurons in the hidden layer are defined by a hyperbolic tangent activation function, which take in a weighted sum of the values from the input layer, and map the results to $[-1,1]$. We have found that the network performs best when using one hidden layer, with 20 neurons. Using fewer neurons led to poor results, by being a too general solution, and using more neurons, or more hidden layers, caused overfitting the data.

In figure 2, the neural network architecture is presented. The input layer has $N_r$ neurons, corresponding to the number of features in each feature-vector. The hidden layer’s neurons are denoted by: $a_1, a_2, \ldots, a_{20}$. The output layer has $K$ neurons, denoted by $z_1, z_2, \ldots, z_K$, which are normalized in the softmax layer to obtain the final outputs.

![Figure 2: The proposed neural network architecture.](image)

The neural network is trained on the feature vectors in $\mathbf{X}(\text{train})$ and the corresponding labels in $\mathbf{Y}(\text{train})$, as denoted in section 2. Training a neural network consists of two stages, feedforward, and backpropagation. Feedforward is the stage at which outputs at each layer are fed towards the final output layer. During backpropagation, we minimize a cross-entropy loss function defining the error between the desired values in $\mathbf{Y}(\text{train})$, and the network outputs at the final layer. During the training process, the weights are adjusted accordingly to give a better
solution with each iteration. The weights and bias values in each layer are optimized through scaled-conjugate backpropagation (Møller, 1993).

The data was randomly split into training and validation sets with a ratio of 80% - 20% correspondingly. The training set was used to compute the gradients, and update weights through backpropagation. The validation set was used to monitor the learning process. Both the training and validation set errors are monitored during the training process. At first, validation error decreases with the training error, but after being presented with enough data, the network starts to overfit to the training set, the validation error begins to increase. We stop updating the weights when the validation error is at a minimum. In this way we make sure that the network can generalize when presented with new examples.

Once the network is fully trained, we test the network with $\mathbf{x}^{(test)}$, the feature vector corresponding to the RCS time-series of the observed target. The network calculates probabilities for each target at the output layer. Classification is defined as correct when maximal probability corresponds to the correct target. A pipeline figure for our algorithm is presented in figure 3.

### Figure 3: Dataflow and algorithm pipeline.

<table>
<thead>
<tr>
<th>Radar Data</th>
<th>RCS Estimation</th>
</tr>
</thead>
<tbody>
<tr>
<td>(Target Position, Target Velocity, SNR)</td>
<td>Generation of a dynamic bank of possible RCS time-sequences for targets in the database</td>
</tr>
<tr>
<td></td>
<td>Empirical Mode Decomposition of RCS time-series into Intrinsic Mode Functions</td>
</tr>
<tr>
<td></td>
<td>Feature Extraction</td>
</tr>
<tr>
<td></td>
<td>Neural Network Training and Classification</td>
</tr>
<tr>
<td></td>
<td>Predicted Target Type</td>
</tr>
</tbody>
</table>

### 4 SIMULATION AND RESULTS

In this work, we simulated 640 target trajectories, 80 trajectories for each of the eight target types. The classification accuracy of the neural network was examined under various levels of noise. Additive white Gaussian noise of up to $\pm 0.5^\circ$ was added to the aspect angles of the target relative to the radar.

We defined a classification to be either be correct, incorrect, or unknown. In order to reduce the false-alarm rate, targets are defined to be ‘unknown’ when there isn’t a good match in the database, or due to a lack of data for a proper classification procedure. In other words, it is better to define a target as ‘unknown” than to classify it as an incorrect target. For example, for a short flight track with few RCS measurements, the features described in section 2 provide little value, and therefore we classify the target as unknown.

Table 1 presents the confusion matrix for the 640 trajectories under $0.5^\circ$ of aspect angle noise. For this amount of noise, we achieved an accuracy of 80.1%. The accuracies of the network under various levels of noise is presented in Table 2.

#### Table 1: Confusion matrix for the neural network-based classifier. Results are shown for trajectories with additive white Gaussian noise of $\pm 0.5^\circ$.

<table>
<thead>
<tr>
<th>Actual Target</th>
<th>A</th>
<th>B</th>
<th>C</th>
<th>D</th>
<th>E</th>
<th>Unknown</th>
</tr>
</thead>
<tbody>
<tr>
<td>A</td>
<td>56</td>
<td>0</td>
<td>1</td>
<td>0</td>
<td>2</td>
<td></td>
</tr>
<tr>
<td>B</td>
<td>1</td>
<td>58</td>
<td>15</td>
<td>2</td>
<td>0</td>
<td></td>
</tr>
<tr>
<td>C</td>
<td>16</td>
<td>18</td>
<td>270</td>
<td>11</td>
<td>6</td>
<td></td>
</tr>
<tr>
<td>D</td>
<td>2</td>
<td>0</td>
<td>8</td>
<td>63</td>
<td>0</td>
<td></td>
</tr>
<tr>
<td>E</td>
<td>0</td>
<td>0</td>
<td>1</td>
<td>0</td>
<td>66</td>
<td></td>
</tr>
<tr>
<td>Unknown</td>
<td>5</td>
<td>4</td>
<td>25</td>
<td>4</td>
<td>6</td>
<td></td>
</tr>
</tbody>
</table>

#### Table 2: Final neural network classification results for the simulated trajectories.

<table>
<thead>
<tr>
<th>Aspect Angle Noise</th>
<th>Accuracy</th>
</tr>
</thead>
<tbody>
<tr>
<td>No Noise</td>
<td>93.3%</td>
</tr>
<tr>
<td>$\pm 0.1^\circ$</td>
<td>87.5%</td>
</tr>
<tr>
<td>$\pm 0.3^\circ$</td>
<td>82.7%</td>
</tr>
<tr>
<td>$\pm 0.5^\circ$</td>
<td>80.1%</td>
</tr>
</tbody>
</table>

We compared the results of the neural network-based classifier with 5 other classifiers. The first classifier is the K-Nearest Neighbours (KNN) classifier (Covert & Hart, 1967). We implemented KNN with the Mahalanobis distance metric, which weights the distance by the inverse covariance of each
feature. We choose the target corresponding to the minimum Mahalanobis distance as the correct target, i.e. the first nearest neighbour.

The next three methods that we implemented take a different approach, and rather than using features, utilize time-series \textit{similarity measures} between the raw RCS signals in the dynamic bank and the RCS signal of the observed target. The chosen target is the target in the dynamic bank, with the most “similar” RCS time-series. The first method used for time-series similarity is the matched filter (Turin, 1960), which correlates between signals by maximizing SNR. The other two methods are Dynamic Time Warping (Sakoe & Chiba, 1978), and Minimum Jump-Cost (Serrà & Arcos, 2012), which work by optimally aligning and stretching the time-series for the best temporal match.

In figure 4, we compare the performance of the proposed neural-network classifier with the other methods. The performance of our proposed neural network is better than the other methods. Furthermore, the machine learning methods (neural network and KNN) performed better under large noise than the time-series similarity methods.

5 CONCLUSIONS

In this paper, we proposed a neural-network based classifier for aerial radar targets. The classification is based on features extracted from the RCS time-series of an observed flight track and from its corresponding IMFs. Comparison of the results have shown that our classifier is better than other methods for the same data. We conclude that the use of machine learning can be effective for the task of aerial radar target classification.

ACKNOWLEDGEMENTS

We would like to thank Ariel Rubanenko, Merav Shomroni, Gregory Lukovsky, Nimrod Teneh, David Feldman, and Or Livne for their useful discussion.

REFERENCES


