Improvement of Pairwise Comparison by using Response Time

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Abstract: Pairwise comparison has been widely employed as an easy method for subjective evaluation of several candidates to develop new products or to improve service. In this paper, a method using response time was proposed to improve the accuracy of pairwise comparison. Firstly, a pairwise comparison experiment was conducted to investigate the relationship between response time and difficulty of judgement. Then, a method to improve the accuracy of calculated scales of the objects was proposed where the answer of the pairwise comparison was modified by using the response time and correction function. In this study, three correction functions were compared to find the difference of the accuracy improvement, and two of them showed significant improvement.

1 INTRODUCTION

These days, they have tried to improve products and services based on “how people feel” (e.g., senses, emotions, preference or comfort). This method in affective evaluation is called “Kansei evaluation”, Kansei evaluation has made it possible to find the needs hidden in human senses in many industries.

There are various methods of Kansei evaluation. Among them, pairwise comparison is widely used in various fields. In pairwise comparison, two out of several objects to be evaluated are presented and the evaluator judges better one by comparing the pair. All the combination of two objects are presented like this and the preferable scale values of each object are calculated based on the judgments. Pairwise comparison has the advantage that the evaluator’s burden is light since only two objects are compared at a time and a relative evaluation is required rather than an absolute evaluation. Moreover, it is possible to quantify not only the order of each object but also the scale value. Nakae et al. used pairwise comparison to evaluate patients’ pain (Nakae et al., 2018). Francis et al. used it to assess performance of judges from court data (Francis et al., 2001).

There are some methods for pairwise comparison. Thurstone’s pairwise comparison method, which judges by giving scores of the two, are the typical examples. Thurstone’s pairwise comparison method is easy for the evaluator because it requires an either-or decision, such as “prefer the left / prefer the right”. On the other hand, Scheffe’s pairwise comparison method requires multiple scores, which has the advantage in its high accuracy and the disadvantage that the judgment is complicated and the burden on the evaluator is heavier. Furthermore, in reality, there are many cases when the evaluator is difficult to make complicated judgments such as infants or when it is only possible to collect binary data such as winning and losing in sports (Usami, 2009).

For the above reasons, it is desirable to use the Thurstone’s paired comparison method in consideration of versatility. In the Thurstone’s pairwise comparison method, however, the obtained scale value always contains an error (Tabata et al., 1995).

In this study, the authors focus on the response time to improve Thurstone’s pairwise comparison. Since Thurstone’s pairwise comparison method requires an either-or decision, the evaluator has to choose one of the two options. In case that there is an obvious difference between the two, the evaluators answer with confidence and the obtained answer is highly reliable. When the difference is not obvious, however, “hesitation” occurs in the evaluators,
and they answer without confidence, so the reliability
of the answer result may be low. Thus, assuming that
the reliability of the answer is high when the response
time is short while it is low when the response time
is long, if the relationship between the difficulty of
the comparison task and the response time is clarified
and the answer that takes the “hesitation” into account
can be obtained, it would be able to get high accurate
results regardless of the simplicity of the comparison
task.

2 CONVENTIONAL METHOD

2.1 Thurstone’s Paired Comparison
Method

Thurstone’s paired comparison method (Thurstone, 1927) is a method in which answers are made by two
alternatives. Now, a pair \((j, k)\) \((j, k = 1, 2, \cdots , n)\) is created from \(n\) stimuli. When let the evaluator choose
either \(j\) or \(k\) from the pair \((j, k)\), let \(p_{jk}\) be the probability that \(j\) is chosen and \(x_{jk}\) be the lower percentage
point of \(p_{jk}\). For each pair \((j, k)\), suppose that \(N\) independent comparisons were made. The scale values
\(S_D(j)\) are expressed as

\[
p_{jk} = \frac{1}{\sqrt{2\pi}} \int_{x_{jk}} \exp(-\frac{x^2}{2})dx
\]

\[
\sum_j \{x_{jk} - S_D(k) + S_D(j)\} = 0
\]

Therefore,

\[
S_D(k) = \frac{1}{n} \sum^n_{j=1} x_{jk}
\]  

2.2 Gulliksen’s Method

As can be seen from Eq.(1), when \(p_{jk}\) is 0 or 1, \(x_{jk}\) becomes \(\pm \infty\) or \(-\infty\) respectively, and missing values
appear in the matrix \(X\) which has \(x_{jk}\) as an element.
When a calculation method for such incomplete data,
there is the Gulliksen’s method (Gulliksen, 1956).

When \(X\) is an incomplete matrix, Eq.(2) is expressed as

\[
\sum^n_{j} \{x_{jk} - S_D(k) + S_D(j)\} = 0
\]

\(n_k\) is the number of \(x_{jk}\) which exists in \(k\) columns of \(X\). Therefore, Eq.(4) gives the following: Eq.(5).

\[
Z = MS
\]

Where,

\[
Z = \begin{pmatrix}
\sum^n_{j} x_{j1} \\
\vdots \\
\sum^n_{j} x_{jn}
\end{pmatrix}
\]

\[
S = \begin{pmatrix}
S_D(1) \\
S_D(2) \\
\vdots \\
S_D(n)
\end{pmatrix}
\]

\(M\) is a \(n \times n\) symmetric matrix which has \(n_k\) in its
main diagonal line, \(-1\) when \(x_{jk}\) exists and 0 when
the value misses. The origin of the scale \(S_D\), for example, is defined as \(S_D(1) = 0\).

\[
S_1 = M^{-1} Z_1
\]

\(S_1\) and \(Z_1\) are given by deleting the first element from
\(S\) and \(Z\), and \(M_{11}\) is given by deleting the first row
and the first column from \(M\). By solving Eq.(8), the
value of \(S_D(k)(k \geq 2)\) with \(S_D(1)\) as the origin can be
found.

3 PROPOSED METHOD

3.1 Outline

In the proposed method, the accuracy of the Thur-
stone’s pairwise comparison method, the closeness
between the obtained scale value and true value of the
evaluated object, will be improved by reflecting the
“hesitation” information obtained from the response
time.

A function that corrects the answer of the either-or
decision from the response time (hereinafter referred
to as “correction function”) is considered. In pairwise
comparison, when a stimulus pair \((j, k)\) is given and
stimulus \(j\) is selected, \(p_{jk} = 1\), \(p_{kj} = 0\). For example,
when using the answer result \(p\) and the response
time \(t\), the correction function \(f\) corrects the answer
as below.

\[
(p_{jk}, p_{kj}) = (1, 0) \rightarrow (0.6, 0.4)
\]

3.2 Correction Function

In this study, three correction functions are proposed
to generate an optimal model. First, the conditions
that the correction function should satisfy are listed below.

In the Thurstone’s pairwise comparison method, the evaluator has to select either one of the two presented options, giving

\[ p_{jk} + p_{kj} = 1 \]  \hspace{1cm} (10)
\[ p \in \{0, 1\} \]  \hspace{1cm} (11)

Assuming that the correction function \( f(p, t) \) is a function where inputs the answer result \( p \) and the response time \( t \), and the output is a modified probability.

\[ f(p_{jk}, t) + f(p_{kj}, t) = 1 \]  \hspace{1cm} (12)
\[ 0 \leq f(p, t) \leq 1 \]  \hspace{1cm} (13)

Assume that the superiority of the answer result is not reversed.

\[ f(0, t) \leq f(1, t) \]  \hspace{1cm} (14)

Assume that the answer result \( p \) converges to 0.5 when the answer time increases.

\[ \frac{\partial f(1, t)}{\partial t} \leq 0 \]  \hspace{1cm} (15)
\[ \frac{\partial f(0, t)}{\partial t} \geq 0 \]  \hspace{1cm} (16)
\[ \lim_{t \to \infty} f(p, t) = 0.5 \]  \hspace{1cm} (17)

The following “Correction function 1” and “Correction function 2” are created as candidates that satisfy from Eq. (10) to Eq. (16) and may improve the accuracy of the pairwise comparison.

### 3.2.1 Correction Function 1

The following correction function 1: \( f_1(p, t) \) is defined. The outline of correction function 1 is shown in Fig.1. \( x_0 \) and \( x_1 \) are the parameters of the function.

\[ f_1(p, t) = g_1(t) \cdot (p - 0.5) + 0.5 \]  \hspace{1cm} (19)

\[ g_1(t) = \frac{1}{1 + e^{x_0 \cdot (t - x_1)}} \]  \hspace{1cm} (20)

From Eq. (15)

\[ x_0 > 0 \]  \hspace{1cm} (21)

### 3.2.2 Correction Function 2

The following correction function 2: \( f_2(p, t) \) is defined. The outline of correction function 2 is shown in Fig.2. \( x_0 \) and \( x_1 \) are the parameters of the function.

\[ f_2(p, t) = \frac{1}{1 + e^{-x_2(t)(p-0.5)}} \]  \hspace{1cm} (22)
\[ g_2(t) = e^{-x_0 \cdot (t-x_1)} \]  \hspace{1cm} (23)

From Eq. (15)

\[ x_0 > 0 \]  \hspace{1cm} (24)

### 3.2.3 Correction Function 3

In the physiological field, linear regression is often applied as a method with high generalization performance (Picard et al., 2001; Kunimasa et al., 2017). Thus, the following correction function 3: \( f_3(p, t) \) is defined. The outline of correction function 3 is shown in Fig.3.

\[ f_3(p, t) = g_3(t) \cdot (p - 0.5) + 0.5 \]  \hspace{1cm} (25)

\[ g_3(t) = \begin{cases} \frac{1}{1 + \frac{1}{x_0 + x_1}} & (t < -\frac{1}{x_0} + x_1) \\ x_0 \cdot (t - x_1) + 0.5 & \left(-\frac{1}{x_0} + x_1 \leq t < \frac{1}{x_0} + x_1 \right) \\ 0 & (t \geq \frac{1}{x_0} + x_1) \end{cases} \]  \hspace{1cm} (26)

From Eq. (15)

\[ x_0 > 0 \]  \hspace{1cm} (27)

By applying the correction function to the obtained answer result matrix \( p = (p_{jk}) \) and the response time matrix \( t = (t_{jk}) \), the modified result matrix \( f = (f(p_{jk}, t_{jk})) \) is created. Then, the scale value of each stimulus is calculated using the Gurriksen method described in Section 2.2.

### 3.3 Accuracy Evaluation Method

To evaluate the proposed method, the scale value of each stimulus is compared with the actual physical
quantity of the stimulus. The stimulus to be used for the accuracy evaluation should be, therefore, quantitatively measured such as brightness, sound volume and length of object. When the calculated scale value of each stimulus and the physical quantity of each stimulus are in a linear relationship, the coefficient of determination could be used to evaluate the accuracy of the scale values. That is, simple regression analysis is performed using the physical quantity (e.g. temperature, length, weight) of each stimulus as the explanatory variable and the scale value as the objective variable, and the coefficient of determination $R^2$ is calculated from the simple regression equation. The closer the coefficient of determination $R^2$ is to 1, the more accurate is the scale value.

### 3.4 Accuracy Improvement Method in Pairwise Comparison

The outline of the accuracy improvement method in this study is shown in Fig.4. First, from the modified result matrix $f = (f(p_{jk}, t_{jk}))$ obtained by applying to the correction function, the scale values is calculated by the method of Gurriksen described in Section 2.2. Then, using $x_0$ and $x_1$ of the correction function described in Section 3.2 as variables, the correction function can be optimized to maximize the coefficient of determination $R^2$ by adjusting the parameters such as $x_0$ and $x_1$. If the same stimulus pair is compared multiple times, the average value of $f(p_{jk}, t_{jk})$ is used for scaling.

The differential evolution method which is a global optimization method of evolutionary algorithm (Storn and Price, 1997) is adopted for optimization of the correction functions. By optimizing $x_0$ and $x_1$ where the coefficient of determination $R^2$ is maximized, a correction function can be determined that improves the accuracy of the scale.

### 4 EVALUATION EXPERIMENT

In this study, the relationship between the difficulty of the comparison and the response time was firstly confirmed, then the accuracy improvement of the proposed method was evaluated.

#### 4.1 Participants

Twenty-eight male students participated in the experiments. All participants had normal or corrected-to-normal vision confirmed by taking a questionnaire. Their average age was 21.4 (SD = 2.0).

#### 4.2 Task

The outline of the task used in this experiment is shown in Fig.5, and the actual graphical interface of the task is shown in Fig.6. In this experiment, a pairwise comparison task was created in which two lines were displayed side by side as the stimuli and the participants were asked to answer the longer one.

The reason to adopt the pairwise comparison task which asks the length of the line is as follows; first, the smaller the difference between the actual lengths of the two presented lines, the higher is the task difficulty, and it is possible to quantitatively estimate the task’s difficulty, that is, the tendency to hesitation. Another reason is that line length is hardly affected by the experimental environment. For example, in comparison of color, the degree of difficulty can be quantitatively evaluated from the distance in color map, but how to feel the stimulus is greatly influenced by such as the brightness of the display and the illumination of the experimental room.

In this experiment, six lengths of vertical lines (200px, 202px, 204px, 206px, 208px, 210px) were used as comparison stimuli. The actual lengths on the display were 50.0 mm, 50.5 mm, 51.0 mm, 51.5 mm,
52.0 mm, and 52.5 mm, respectively. The distance between the participant and the display was 0.80 m, and the calculated viewing angles were about 3.58°, 3.62°, 3.65°, 3.69°, 3.72° and 3.76°, respectively. The widths of the line were all 3 px.

Figure 5: Outline of the task.

Figure 6: The actual graphical interface of the task (comparison task).

Two of the vertical lines as comparison stimuli were displayed side by side, and 36 pairs, including pairs of the same length were presented. A series of tasks comparing all the 36 pairs was called one set. A gaze point was displayed at the center every time the pair was switched to make the participant’s gaze in the center of the display. The response was input by clicking on the button displayed under the line which the participant felt longer. The time from the presentation of the pair to the response was measured. If there was no response within 4.0 seconds, the presentation of the pair was automatically terminated and the gaze point was displayed.

4.3 Experiment Environment

The participants were asked to use a computer mouse to conduct the pair comparison task displayed on the screen. The screen size of the display (I-O DATA, LCD-MF243EBR) was 23.6 inches, and the resolution was 1920 × 1080. The illuminance on the desk was 330 lx.

4.4 Experimental Procedure

The experiment was conducted in the period of January 4th to 19th, 2019. All the participants performed a practice of the comparison test for about one minute before the experiment. After that, 12 sets of the tasks described in Section 4.2 were done. A 3 minute break was provided between each set.

4.5 Results

In this experiment, the participants who did not answer within the time limit more than 36 times among the 12 sets / 432 trials, or who selected one of the left and right sides more than 360 times out of 432 trials were considered not to be seriously engaged in the experiment, and were excluded from the analysis below as invalid data. In addition, comparisons that was not answered within 4.0 seconds were regarded as invalid data and were excluded from the analysis.

The average response time of all the participants for each stimulus pair is shown in Fig.7. The vertical axis indicates the line length in pixel displayed on the left side, while the horizontal axis indicates that on the right side. The lighter the color in the cell, the longer is the response time. The response time was standardized for each set to reduce the variation in response time for each experiment participant and each set.

As a result, it was confirmed that the average response time for the all participants tends to increase as the difference in the length decreases.

Next, the results of each participant are described. Here too, the response time was standardized for each set in order to reduce the variation in the response time. As an example of the results, the average response time of all sets of participant number 10 is shown in Fig.8. It was confirmed that the response time tends to increase as the difference in the length decreases. On the other hand, as the response answer time of all sets of participant number 24 shown in
5 EVALUATION OF THE PROPOSED METHOD

In this chapter, the accuracy improvement effect of the proposed method described in Chapter 3 is evaluated using the answer results and response time measured in the experiment.

5.1 Evaluation Method for the Proposed Method

First, the answer result and the response time of learning data were applied to each correction function, and the correction function was optimized to maximize the coefficient of determination $R^2$ for each participant. The optimized correction function was created by the method described in Chapter 3. After that, the accuracy improvement effect of the proposed method was evaluated using test data.

Cross validation was used to evaluate the performance of the optimized correction function. The cross validation is a method of evaluating the accuracy of a model by applying one of the measurement data divided into $K$ as test data and the rest as training data.

In this study, 12 sets performed by each participant were divided into four and the optimized correction function was created from the training data of the 9 sets. After that, the remaining 3 sets were applied to the optimized correction function, and the accuracy was evaluated by calculating the coefficient of determination $R^2$. Finally, the coefficient of determination $R^2$ of each of the four divisions was calculated, and the average value was taken as the estimated accuracy of the participant.

The data of participant number 5 and 18 were treated as invalid data for the reason described in Section 4.4. In addition, for 3 participants in the participant number 7, 9, and 14, there were too many missing values in the answer results in some test data that $M_{11}$ in equation (8) has become a singular matrix with no inverse matrix. Therefore, the scale value could not be calculated and was excluded from analysis.

Python’s open source machine learning library “scikit-learn” (sci, 2019) was used to calculate the coefficient of determination, and the “differential evolution” function in Python’s open source numerical calculation library “SciPy” (Sci, 2018) was used to optimize the correction function.

5.2 Evaluation Results of the Proposed Method

With regard to the correction function 1, the average of the estimated accuracy of all the participants before the function was applied was 0.849, and that after the function was applied was 0.907. As a result of paired t-test before and after applying correction function 1, there was a significant difference at 1% level ($p = 0.00184 < 0.01$).

With regard to the correction function 2, the average of the estimated accuracy of all the participants before the function was applied was 0.849, and that after the function was applied was 0.914. As a result of paired t-test before and after applying correction function 2, there was a significant difference at 0.1% level ($p = 0.000740 < 0.001$).

With regard to the correction function 3, the average of the estimated accuracy of all the participants before the function was applied was 0.849, and that after the function was applied was 0.883. As a result of paired t-test before and after applying correction function 3, there was no significant difference ($p = 0.0526$).

5.3 Discussion

First, participant number 24 is considered whose estimated accuracy has decreased for all correction func-
tions. As shown in Fig.9, the accuracy decreased because the response time did not tend to increase as the difference in the length decreased. It was not consistent with the assumption when creating the correction function that “when the evaluator’s response time is short, confidence in the answer is high, and when the evaluator’s response time is long, confidence in the answer is low”. On the other hand, as shown in Fig.8, the accuracy in participant number 10 increased because the response time tended to increase as the difference in the length decreased.

Then, the result of participant number 26 is discussed. Table 1 to 3 shows the values of the parameters in each test data, the scale value after applying the correction function, the coefficient of determination $R^2$ before applying the correction function, and the coefficient of determination $R^2$ after applying the correction function. No significant difference was found in the coefficient of determination $R^2$ between the correction functions for iteration number 1 to 3 after applying the correction function. This is because $x_0$, the gradient of the correction function, takes a value close to 0 in all correction functions. At this time, from Eq. (17) to Eq. (25), each correction function does not reflect the response time data, and the coefficient of determination $R^2$ after applying the correction function takes a value close to the coefficient of determination $R^2$ before applying the correction function. For iteration number 4, the coefficient of determination $R^2$ decreased after applying the correction function. This is because $x_0$ was large and $x_1$ was small in correction function 1 and correction function 3. Since the correction function is close to 0.5 for the answer with a long response time, it loses high-precision data before applying the correction function.

Finally, the result of participant number 22 is discussed as shown in Table 4 to 6. No significant difference was found between the correction functions for iteration number 1, 3, and 4. For iteration number 2, however, the coefficient of determination $R^2$ decreased only in correction function 3. At iteration number 2, the coefficient of determination before applying the correction function was low, and the error due to the answer itself was large. In the correction function 1 and 2, however, the value of $x_1$ is extremely small, and from Eq. (17) to Eq.(22), the correction function is always close to 0.5 regardless of the response time and response result, so the original low coefficient of determination improved. On the other hand, since the value of $x_1$ is relatively large in correction function 3, it is strongly influenced by the low original coefficient of determination.

### 6 CONCLUSIONS

In this study, response time was applied to pairwise comparison to improve the accuracy of it.

First, the response time was measured by an experiment through a pairwise comparison task, and the relationship between the difficulty of the comparison and the response time was investigated. In this experiment, a pairwise comparison task was created in which two lines were displayed side by side and the participants were asked to answer the longer one. As the result, when averaged across the participants, the response time tended to increase as the difference in length decreased. In addition, when the participants were examined individually, the same tendency was also observed in some participants.

Next three types of “correction function” were created to improve the accuracy of the pairwise com-

### Table 1: Results (correction function 1, participant number 26).

<table>
<thead>
<tr>
<th>iteration number</th>
<th>$x_0$</th>
<th>$x_1$</th>
<th>$R^2$ (before)</th>
<th>$R^2$ (after)</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>0.294</td>
<td>1.463</td>
<td>0.963</td>
<td>0.941</td>
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<tr>
<td>2</td>
<td>0.000</td>
<td>-2.076</td>
<td>0.862</td>
<td>0.943</td>
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<tr>
<td>3</td>
<td>0.000</td>
<td>-2.997</td>
<td>0.953</td>
<td>0.967</td>
</tr>
<tr>
<td>4</td>
<td>2.725</td>
<td>-1.471</td>
<td>0.921</td>
<td>0.768</td>
</tr>
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</table>

### Table 2: Results (correction function 2, participant number 26).

<table>
<thead>
<tr>
<th>iteration number</th>
<th>$x_0$</th>
<th>$x_1$</th>
<th>$R^2$ (before)</th>
<th>$R^2$ (after)</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>0.185</td>
<td>3.000</td>
<td>0.963</td>
<td>0.935</td>
</tr>
<tr>
<td>2</td>
<td>0.000</td>
<td>-1.524</td>
<td>0.862</td>
<td>0.942</td>
</tr>
<tr>
<td>3</td>
<td>0.000</td>
<td>2.620</td>
<td>0.953</td>
<td>0.967</td>
</tr>
<tr>
<td>4</td>
<td>0.000</td>
<td>-0.672</td>
<td>0.921</td>
<td>0.993</td>
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</table>

### Table 3: Results (correction function 3, participant number 26).

<table>
<thead>
<tr>
<th>iteration number</th>
<th>$x_0$</th>
<th>$x_1$</th>
<th>$R^2$ (before)</th>
<th>$R^2$ (after)</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>0.073</td>
<td>1.000</td>
<td>0.963</td>
<td>0.939</td>
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<td>0.862</td>
<td>0.943</td>
</tr>
<tr>
<td>3</td>
<td>0.000</td>
<td>0.572</td>
<td>0.953</td>
<td>0.967</td>
</tr>
<tr>
<td>4</td>
<td>4.590</td>
<td>-0.869</td>
<td>0.921</td>
<td>0.618</td>
</tr>
</tbody>
</table>

### Table 4: Results (correction function 1, participant number 22).

<table>
<thead>
<tr>
<th>iteration number</th>
<th>$x_0$</th>
<th>$x_1$</th>
<th>$R^2$ (before)</th>
<th>$R^2$ (after)</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>3.000</td>
<td>0.261</td>
<td>0.962</td>
<td>0.927</td>
</tr>
<tr>
<td>2</td>
<td>0.393</td>
<td>-3.000</td>
<td>0.659</td>
<td>0.913</td>
</tr>
<tr>
<td>3</td>
<td>0.562</td>
<td>-3.000</td>
<td>0.450</td>
<td>0.960</td>
</tr>
<tr>
<td>4</td>
<td>3.000</td>
<td>-0.230</td>
<td>0.940</td>
<td>0.950</td>
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Table 5: Results (correction function 2, participant number 22).

<table>
<thead>
<tr>
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<th>$x_1$</th>
<th>$R^2$ (before)</th>
<th>$R^2$ (after)</th>
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</thead>
<tbody>
<tr>
<td>1</td>
<td>0.421</td>
<td>-3.000</td>
<td>0.962</td>
<td>0.952</td>
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<td>2</td>
<td>0.264</td>
<td>-3.000</td>
<td>0.659</td>
<td>0.911</td>
</tr>
<tr>
<td>3</td>
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<td>-3.000</td>
<td>0.450</td>
<td>0.960</td>
</tr>
<tr>
<td>4</td>
<td>0.450</td>
<td>-3.000</td>
<td>0.940</td>
<td>0.973</td>
</tr>
</tbody>
</table>

Table 6: Results (correction function 3, participant number 22).

<table>
<thead>
<tr>
<th>iteration number</th>
<th>$x_0$</th>
<th>$x_1$</th>
<th>$R^2$ (before)</th>
<th>$R^2$ (after)</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>5.000</td>
<td>-0.296</td>
<td>0.962</td>
<td>0.953</td>
</tr>
<tr>
<td>2</td>
<td>5.000</td>
<td>0.432</td>
<td>0.659</td>
<td>0.468</td>
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<tr>
<td>3</td>
<td>4.985</td>
<td>0.309</td>
<td>0.450</td>
<td>0.934</td>
</tr>
<tr>
<td>4</td>
<td>4.987</td>
<td>-0.354</td>
<td>0.940</td>
<td>0.970</td>
</tr>
</tbody>
</table>

Comparison method. They modified the answered results from the response time based on the above idea. As the result, the accuracy improved significantly in two correction functions.

In this study, a pairwise comparison task asking the length of the line was used. However, only one type of pairwise comparison task was investigated, and it could not be asserted that the accuracy of the pairwise comparison method always improved from the result of this study. It is necessary to make more pair comparison tasks with more modalities and to conduct experiments and investigations to put the proposed method into practical use. In addition, although three types of correction functions were proposed in this study, it is necessary to find more appropriate correction functions.

REFERENCES


