Hybrid 6D Object Pose Estimation from the RGB Image

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Abstract: In this research, we focus on the 6D pose estimation of known objects from the RGB image. In contrast to state of the art methods, which are based on the end-to-end neural network training, we proposed a hybrid approach. We use separate deep neural networks to: detect the object on the image, estimate the center of the object, and estimate the translation and “in-place” rotation of the object. Then, we use geometrical relations on the image and the camera model to recover the full 6D object pose. As a result, we avoid the direct estimation of the object orientation defined in SO3 using a neural network. We propose the 4D-NET neural network to estimate translation and “in-place” rotation of the object. Finally, we show results on the images generated from the Pascal VOC and ShapeNet datasets.

1 INTRODUCTION

Collaborative robotic arms are designed to share workspace with humans or even physically interact with operators. This is possible mainly due to control algorithms which make the robot compliant when robot unexpectedly touches an obstacle. Also, simple safety sensors stop or slow down the robot when the human operator get too close to the dangerous area.

These types of robot become very popular in manufacturing to perform repetitive tasks. In our research, we are interested in the autonomy of such robots. A collaborative arm, which is mounted on the mobile platform, can move freely in the factory and perform production tasks or help humans in daily activity. To this end, the mobile robot should be equipped with the perception system which allows detecting and estimating the pose of the objects and then perform manipulation tasks (Fig. 1).

In this paper, we consider the problem of visual objects detection and pose estimation. Most of the state of the art methods are based on the visual or depth features (Hinterstoisser et al., 2012; Hodan et al., 2015), which are used to detect and find the 6D pose (position and orientation) of the object. Recently, great progress was made in this field. Kehl et al. (Kehl et al., 2017) showed that the Deep Convolutional Neural Network can be applied to detect objects on the RGB images and simultaneously estimate the pose of the object. On the other hand, the traditional methods based on online optimization have proven to be very efficient. (Bibby and Reid, 2016; Tjaden et al., 2016; Prisacariu and Reid, 2012). Bibby et al. propose the object tracking method which minimizes the error defined directly on the RGB image. The silhouette generated from the object model is compared with the intensity of pixels on the current image. The pose of the object model is modified using the gradient-based method. The algorithm is designed for object tracking. It means that the algorithm requires a very accurate initial guess and can’t be used for object detection.

In this research, we propose a new hybrid method for 6D object pose estimation (3D translation and rotation). In contrast to end-to-end solutions, we propose a method which utilizes deep neural network
pose estimator and a geometrical model of the camera.

1.1 Related Work

Many traditional approaches to 6D objects pose estimation are based on visual RGB or depth features. Then, the features are compared with the reference models to produce an object category and pose estimation. In (Hinterstoisser et al., 2012), which is an extension of the LINEMOD method (Hinterstoisser et al., 2011), the color gradient features located on the object silhouette and surface normal features inside the object silhouette are selected to describe discretized object pose. The detector is trained using texture-less 3D CAD models of the objects. In (Ulrich et al., 2012) RGB edges are used for objects detection and pose estimation. The pose estimation is boosted by the hierarchical view model of the object (Ulrich et al., 2012). Hodan et al. propose a sliding window detector based on surface normals, image gradients, depth, and color (Hodan et al., 2015). The pose of the object is estimated using a black-box optimization technique (Particle Swarm Optimization) which minimizes the objective function defined using the current depth image and the synthetic image generated from the CAD model of the object.

To detect an object in the image a Random Forest classifier can be used (Brachmann et al., 2016). The obtained distribution of object classes is used to obtain preliminary pose estimates for the object instances. Then, the initial poses are refined using object coordinate distributions projected on the RGB image. Similar Latent-Class Hough Forests allow learning the pose estimator using RGB-D LINEMOD features (Tejani et al., 2016).

Another method for pose estimation is Iterative Closest Point algorithm (Segal et al., 2009). In contrast to previously mentioned methods, the ICP relies on depth data (point clouds). In practice the point cloud obtained from popular Kinect-like sensors are noisy. We avoid using depth data and rely mainly on the RGB images for pose estimation because the error of the single depth measurement can be larger than 5 cm on our depth sensor (Kinect v2) (Khoshelham, 2011). We also avoid methods similar to ICP because they are very sensitive to initial guess about the object pose. The initial pose of the object should be close to the real pose of the object because the ICP is prone to local minima.

Another group of object detection methods is based on Deep Convolutional Neural Networks. Kehl et al. (Kehl et al., 2017) proposed the extension to the Single Shot Detector (SSD) (Liu et al., 2016), to detect the position of the objects on the image and produces 6D pose hypotheses of the objects. The network is trained using synthetic images generated from the MS COCO dataset images as a background and 3D CAD models of the objects. The 6D pose hypotheses of each object are later refined using RGB-D images.

Also, Xiang et al. use a Convolutional Neural Network to estimate the 6D pose of the objects from the RGB image (Xiang et al., 2018). In this case, the estimation of translation and rotation of the object is decoupled. To estimate the translation of the object the neural network estimates the center of the object. Then, the translation of the object is computed from the camera model. The orientation of the object is estimated by the neural network working on the Region of Interests (bounding boxes) detected on the input image. In the method proposed by Thanh-Toan Do et al., the neural network estimates the distance to the camera only (Do et al., 2018). The remaining components of the translation vector are estimated from the bounding box. The rotation of the object is estimated using Lie algebra representation.

Estimation of the orientation of the object is the most challenging part of the 6D pose estimation. In (Sundermeyer et al., 2018) the orientation of the object is defined implicitly by samples in latent space. Utilizing the depth data improves the results (Wang et al., 2019) but also template matching-based method has been proven to be efficient in this case (Konishi et al., 2018).

To deal with the 6D pose estimation we decouple the solution into two sub-problems. First, we use the neural network to find the pose of the object with respect to the camera frame assuming that the camera axis goes through the center of the object. Then, we analytically correct the estimated pose of the object using camera model. Moreover, we have used degenerated representations for describing 6D pose in order to simplify specific tasks.

2 4D-2D POSE ESTIMATION

Given an RGB input image, the task of pose estimation pipeline is to estimate the rigid transform between coordinate systems $O$ and $C$ belonging to the object and the camera, respectively. We state that the full representation of the rigid transform can be retrieved through an ensemble of specific tasks with reduced dimensionality. The first constraint reducing the dimensionality to four parameters is the relation between the z-axis of $C$ coordinate system and the origin position of $O$ coordinate system. If we as-
sume that the z-axis belonging to C intersects the origin of O coordinate system then it is possible to create a rigid transform using only four parameters: XYZ translation and in-place rotation angle \( \theta \). The XYZ translation determines the location of camera as well as the direction of its z-axis. The x and y axes of the camera rigid transform depend on the in-place rotation angle. It can be perceived as a tilt movement of camera. In-place rotation angle determines the measure of camera rotation around its z-axis.

The neural network estimates transformation between the camera \( \mathcal{C}' \) and the object frame O. Because we assume that the z-axis of the \( \mathcal{C}' \) frame goes through the center of the object frame \( O \) the neural network has to estimate only four parameters. The natural choice is the representation with three Euler angles and distance to the object \( z \). In this case, \( x \) and \( y \) is always zero. However, the Euler angles are not the best choice to represent the orientation of the object because of singularities and nonlinearity. Another possibility is to represent the pose of the object by the axis-angle representation and distance to the object. However, we chose the representation which contains three parameters defined in the Euclidean space (translation from the object frame \( O \) to the camera frame \( \mathcal{C}' \) and the in-place rotation angle \( \theta \). As it was stated before the translation represents the position of the camera on a spherical surface around the object and the \( \theta \) angle represents the rotation around z-axis of the camera.

The method of calculating the \( \mathbf{X} \) vector leads to a singularity when the first two components of \( \mathbf{Z} \) vector equal zero. In practical implementation it is very unlikely for a neural network to output such values of its rarity in single-precision floating-point number format. However, we assign a constant value to \( \mathbf{X} \) in order to ensure that the computation will not fail.

Further calculation of the goal representation of \( \mathbf{C} \) rigid transform can be carried out when the relevant camera parameters are known. Let \( w, h \) be the width and height of images produced by the camera. Additionally the camera parameters are defined by \( f_x \) and \( f_y \) which denote camera field of view for width and height, respectively. If we know the actual position \( \mathbf{l}_{xy} \) of the object’s centre on the image \( I \), then the correction \( \mathbf{T} \) that should be applied is represented by:

\[
\Phi_x = \frac{I_x}{w} \cdot f_x \\
\Phi_y = \frac{I_y}{h} \cdot f_y \\
\mathbf{T} = \begin{bmatrix}
\cos(\Phi_x) & \sin(\Phi_x) & 0 & 0 \\
0 & 1 & 0 & 0 \\
-\sin(\Phi_y) & 0 & \cos(\Phi_y) & 0 \\
0 & 0 & 0 & 1
\end{bmatrix}
\]

2.1 Methodology

Let \( \mathbf{C} \) denote a rigid transform between the object and the camera coordinate system given by \( O \) and \( \mathcal{C} \), which are shown in Fig. 2. Apart from that let \( \mathcal{C}' \) denote a rigid transform whose z-axis intersects the origin of the \( O \) coordinate system. The homogeneous matrix representation of \( \mathcal{C}' \) is derived from translation vector \( \mathbf{C}'_T \) and in-place rotation angle \( \theta \). In order to determine the matrix representation of \( \mathcal{C}' \) we assume that the x-axis of camera coordinate system is parallel to the \( O_{xy} \) plane if \( \theta \) equals zero. Given these assumptions we determine \( \mathcal{C}' \) as follows:

\[
\mathbf{z} = \frac{\mathbf{C}'_T}{||\mathbf{C}'_T||}, \quad (1)
\]

\[
\mathbf{x} = \frac{[\mathbf{z}_2, \mathbf{z}_1, \theta]^T}{\sqrt{\mathbf{z}_1^2 + \mathbf{z}_2^2}}, \quad (2)
\]

\[
\mathbf{y} = \mathbf{z} \times \mathbf{x}, \quad (3)
\]

\[
\mathbf{C}' = \begin{bmatrix}
\mathbf{x} & \mathbf{y} & \mathbf{z} & \mathbf{C}'_T
\end{bmatrix} \cdot \begin{bmatrix}
\cos(\theta) & -\sin(\theta) & 0 & 0 \\
\sin(\theta) & \cos(\theta) & 0 & 0 \\
0 & 0 & 1 & 0 \\
0 & 0 & 0 & 1
\end{bmatrix}. \quad (4)
\]

2.2 Architecture

The whole pipeline for 6D pose estimation presented in Fig. 3 consists of three modules: object extractor (Mask R-CNN (He et al., 2017)), camera coarse
2.3 Object Extractor

The first network in the pipeline is the object extractor. The object extractor is fed by RGB data and outputs the mask and bounding box information about all the detected objects. We use the Mask R-CNN architecture which provides the 2D mask, class information and bounding boxes of objects (He et al., 2017). After successful detection all the objects are cut out from the image according to their bounding boxes. The input shape of 4D-NET and 2D-NET is constant and square which involves reshaping bounding boxes in order to match the dimensions.

2.4 4D-NET Architecture

The architecture of the 4D-NET is presented in Fig. 4. The base of the network is built in a fully convolutional manner. The input of the network has a shape of $64 \times 64 \times 3$. We use strides of 1 and kernel of shape $3 \times 3$ across the whole network. We apply weights regularization according to the L2 rule with a scale coefficient set to 0.01. At the beginning of the training weights are initialized with the usage of Xavier initializer. The reasons behind a convolutional-based architecture are its proven capabilities of separating relevant image data and overall generalization properties. The output of the last convolutional layer is flattened and fed then to another two fully connected layers with 512 and 4 units. The latter layer provides a prediction of relative translation from the camera to the object as $\hat{T}$ coordinates and in-place rotation angle $\theta$. In order to avoid overfitting the convolutional layers are trained with batch normalization technique and the fully connected layers apply dropout omitting half of the connections. The ReLU activation function is used across the entire network.

2.5 4D-NET Loss Function

Since the goal of estimating XYZ translation and in-place rotation angle is to determine the $C'$ rigid transform we have decided not to treat each parameter separately but rather couple them all together. Imprecise XYZ prediction results in an increasing angle error between target and predicted rigid transforms when we compare them in angle-axis representation. With that in mind, we have introduced a loss function which penalizes the network for any trial to compensate the distance error at the expense of rotation. Moreover, the order of magnitude of translation error may vary significantly within the dataset. This kind of data instability is alleviated by varying normalizing
Figure 4: The architecture of 4D-NET. The network takes as input a three-channel color image and converts it into four-element vector through consecutive convolutional and two dense layers. The resultant vector consist of relative camera to object XYZ translation and in-place rotation angle.

Figure 5: The architecture of 2D-NET. The input of 2D-NET is a three-channel color image, same as in 4D-NET, and it outputs a two-element vector, which describes the center of the object projected on the image plane. The image coordinates are normalized during training and the network outputs values within a range of 0 to 1.

term which is directly dependent on the translation label.

Let $T, \hat{T}, R, \hat{R}$ denote the target and predicted translation vectors and the rigid transforms’ rotation matrices. The function $G(R, \hat{R})$ defines the angle difference between target and predicted rotation matrices in angle-axis representation:

$$G(R, \hat{R}) = \arccos \frac{\text{Tr}(R \cdot \hat{R}) - 1}{2}.$$  \hfill (6)

The overall loss function is a sum of resultant distance and rotation errors. The $\lambda$ coefficient has been added in order to weigh the practically incomparable distance and rotation measures:

$$\ell(T, \hat{T}, R, \hat{R}) = \frac{||T - \hat{T}||_2}{||T||_2} + \lambda \cdot G(R, \hat{R}).$$  \hfill (7)

2.6 2D-NET Architecture

The architecture of the 4D-NET is presented in Fig. 5. The architecture of the network consists of 6 convolutional, 3 pooling and 2 fully connected layers. The network uses strides of 1 and kernels of shape 3x3 for convolutional layers. The convolutional layers increase the overall filters count after every max-pooling layer. As in the 4D-NET the batch normalization, dropout and L2 regularization have been applied. The network outputs two parameters which stand for the $I_{xy}$ location (the center of the object on the image plane). Fairly minimalist setup suits well the problem and the network extracts relevant features and does not need much computational power for training.

2.7 2D-NET Loss Function

For training 2D-NET the Euclidean distance loss has been employed. We did not notice any major improvement when changing the loss function to Manhattan distance as both approaches tend to be easily minimized during learning process.

2.8 Dataset

We have prepared a synthetic dataset for validation of our method. The dataset consist of objects of six classes (car, faucet, chair, phone, screen, pistol) and the models were derived from the ShapeNet dataset (Chang et al., 2015). The selected objects from the dataset are presented in Fig. 6. The objects are characterized by different shape, size and visual features. In a real-world setting it would be an extremely arduous effort to create an annotated dataset, which fully covers all objects’ representation in the space of all possible Euler rotations with varying distance. The currently available non-synthetic datasets such as YCB Video (Xiang et al., 2018) and LineMOD (Hinterstoisser et al., 2011) provide very detailed images and
annotations of object of different classes but the objects are not sampled uniformly and some camera angles are omitted due to the manual camera operation.

Figure 6: Representations of objects from our dataset (from the top row: car, chair, faucet, phone, pistol, screen).

The easiness of creating synthetic sceneries with predefined conditions suits best the scenario of training neural networks for big data consumption. We have therefore rendered multitude of samples for every aforementioned object.

The dataset consists of 256 × 256 px RGB images and binary masks. The camera points from which the objects have been rendered were laid out uniformly on a surface of unit sphere. These points have been also multiplied by random distance factor in order to achieve representations of varying magnitude and perspective. The in-place rotation angle ranged from -60 up to 60 degrees with a step of 3 degrees.

Each object has been rendered with random background images which have been derived from the Pascal VOC dataset.

2.9 Training the Networks

We trained every module of pose estimation pipeline independently. The Mask R-CNN network was already pretrained on the COCO dataset, containing 80 classes. As a next step we fine-tuned the pretrained network on a smaller dataset of objects.

Training both 4D-NET and 2D-NET was common when it comes to data preparation stage. It is worth to mention that the visual centre of bounding box does not necessarily match the geometrical center of object. Moreover, the input data has to be cropped to the dimensions of 64 × 64 px. The rectangular bounding box must be properly transformed to a square shape with respect to the center position. The Mask R-CNN does not extract instances perfectly in all cases. For that reason we shift and scale the bounding boxes, so that the final crops are not matched perfectly. Bounding boxes randomization increases robustness to imprecisely detected mask through Mask R-CNN.

The 4D-NET was trained with the batch size of 2 and learning rate=0.001. The network was being trained 12 hours on Nvidia Titan XP before reaching satisfactory results. The 2D-NET was trained with the batch size of 5 and with the same learning rate as the previous network. It turned out that the centre detection is not challenging and the network provides close to zero error after one hour of training.

3 RESULTS

3.1 Center Estimation

We have tested the performance of the network for middle point detection on the test data from our dataset. The samples provided by the dataset contain images with binary masks and middle point coordinates of the objects. Therefore we used this information to create excerpts using bounding boxes of randomized origin positions and dimensions. The idea bounding box randomization resembles the case of inexact instance segmentation of the object extractor. This approach allowed us to test the robustness of the network while having only limited data.

The used error metrics for center point estimation was the Euclidean distance between for both normalized and absolute 2D image coordinates. We use image excerpt coordinates in order to compare the accuracy of middle point detection. At the very end the excerpts are resized to match the dimensions of the input layer of neural network.

The testing procedure using randomized bounding boxes always ensures that the object is present in an image. However, some part the object may be invisible. We have observed that the network performs very well given a valid object excerpt. Images presented in Fig. 7 reflect sample predictions produced by the network.

The pixel distance error is represented by following equation:

\[ e_{\text{distance}} = \sqrt{(\hat{x} - x)^2 + (\hat{y} - y)^2}. \]  

The results of the center estimation for each object from the dataset are presented in Tab. 1. The average inference error was within 1.72 px for all of the objects in our dataset. We did not noticed any significant
outliers during the testing phase. The resultant error exerts only a slight influence on the ultimately estimated pose. The final error derived from the network for center detection depends linearly on the initial resolution of an image except due to the scale factor.

Table 1: Results of the object’s center estimation.

<table>
<thead>
<tr>
<th></th>
<th>car</th>
<th>chair</th>
<th>faucet</th>
<th>screen</th>
<th>phone</th>
<th>pistol</th>
<th>average</th>
</tr>
</thead>
<tbody>
<tr>
<td>$e_{\text{distance}}$ [px]</td>
<td>1.89</td>
<td>1.77</td>
<td>1.07</td>
<td>1.75</td>
<td>1.64</td>
<td>2.17</td>
<td>1.72</td>
</tr>
<tr>
<td>$e_{\text{distance_std}}$ [px]</td>
<td>1.53</td>
<td>1.45</td>
<td>1.06</td>
<td>1.60</td>
<td>1.55</td>
<td>2.10</td>
<td>1.55</td>
</tr>
</tbody>
</table>

Figure 7: Example results of the object center estimation.

3.2 Pose Estimation

In the case of pose estimation we have tested the whole pipeline consisting of three neural networks to evaluate the inference error. The resultant inference error is influenced only to a small degree by the center detection network. Therefore the final pose prediction may be impaired estimated when the 4D-NET network does not perform well. The input data for testing procedure were the object representations detected by Mask-RCNN network. We only evaluated the error metrics for valid detections.

We considered the Euclidean distance error, the distance between rotation in angle-axis representation and IoU as the metrics applied for testing the validity of the method. In order to disregard the distance disparity among the rendered objects of different size we normalize the absolute distance error separately for each label. The results on the pose estimation are summarized in Tab. 2.

We have established that is possible to retrieve 6D pose based within a tolerable margin using only color data. The average distance error adds up to 9 cm which is an acceptable result since we use only cropped and resized color data. The relative distance can therefore be determined according to the minor changes of object representation caused by camera projection. The rotation error lies within a range from 9 to 12 degrees. We noticed that the in-place angle step used for dataset creation has a major impact on the rotation error. The more in-place angles are used for every single camera position, the better rotation estimation becomes. During the inference stage we have observed outliers to occur rarely for both distance and rotation parts. The effectiveness of center point estimation allowed to achieve representation with a high IoU factor as the binary masks overlap each other to a very large extent in most of the cases.

The normalized distance and rotation errors are defined by equation (9). We express the rotation difference between two rotation matrices in degrees:

$$ e_{\text{distance}} = \frac{||T - \hat{T}||_2}{||T||_2} \cdot 100\% $$

$$ e_{\text{rotation}} = \frac{\arccos \left( \frac{\text{Tr}(R \cdot \hat{R}) - 1}{2} \right) \cdot 180}{\pi} $$

Table 2: Pose estimation results.

<table>
<thead>
<tr>
<th></th>
<th>car</th>
<th>chair</th>
<th>faucet</th>
<th>screen</th>
<th>phone</th>
<th>pistol</th>
<th>average</th>
</tr>
</thead>
<tbody>
<tr>
<td>$e_{\text{distance}}$ [%]</td>
<td>5.43</td>
<td>6.19</td>
<td>5.87</td>
<td>6.59</td>
<td>7.12</td>
<td>5.57</td>
<td>6.12</td>
</tr>
<tr>
<td>$e_{\text{distance_std}}$ [%]</td>
<td>5.12</td>
<td>5.79</td>
<td>6.27</td>
<td>7.04</td>
<td>7.53</td>
<td>5.23</td>
<td>6.16</td>
</tr>
<tr>
<td>$e_{\text{rotation}}$ [deg]</td>
<td>2.83</td>
<td>3.19</td>
<td>3.03</td>
<td>3.76</td>
<td>4.22</td>
<td>3.58</td>
<td>3.43</td>
</tr>
<tr>
<td>$e_{\text{rotation_std}}$ [deg]</td>
<td>3.21</td>
<td>3.68</td>
<td>3.46</td>
<td>4.15</td>
<td>4.59</td>
<td>4.01</td>
<td>3.85</td>
</tr>
<tr>
<td>accIoU [%]</td>
<td>97.2</td>
<td>95.6</td>
<td>96.4</td>
<td>96.1</td>
<td>95.8</td>
<td>96.1</td>
<td>96.4</td>
</tr>
</tbody>
</table>

Figure 8: Example estimated 6D poses compared to the ground truth data.

Figure 9: Invalid pose predictions. The overlaying projections does not match silhouettes of the presented objects.

We also visualize the pose error on the image plane by projecting the estimated object pose on the RGB image. The example results are presented in Fig. 8.
In some cases the output of the 4D-NET did not match the ground truth accurately, as it is shown in the Fig. 9. We have noticed that the biggest error was caused by rotation disparity. In most of the cases this was affected by improper in-place angle prediction, while the translation influenced the rotational difference to a relatively small extent. We have established that such situations make up 8% of all cases during testing phase.

3.3 Runtime

The biggest overhead in the computation pipeline is imposed by the Mask R-CNN network. The inference time for both 4D-NET and 2D-NET are negligible and they jointly provide a result in 7 milliseconds on Nvidia Titan XP. Therefore we can report the runability at approximately 13-15 frames per second. The complexity of computation is not influenced significantly for multi-object pose estimation since the proposed network architectures are quite lightweight.

4 CONCLUSIONS AND FUTURE WORK

In this paper, we show that the 6D pose estimation can be split into two smaller sub-problems. First, the neural network (4D-NET) estimates the camera translation and in-place rotation with respect to the object. At this stage, we assume that the camera axis goes through the center of the object. Second, the full 3D pose of the camera with respect to the object is computed using the mathematical model of the camera. The two-stage solution to the object pose estimation allows simplifying the problem in comparison to end-to-end solutions (Kehl et al., 2017). As a result, the neural network used for the pose estimation (4D-NET) can be more compact and computationally efficient.

To detect the object on the RGB image we use the Mask R-CNN method (He et al., 2017). The center of the detected bounding box does not correspond with the projection of the object’s center on the image plane. Thus, we designed the neural network which estimates the center of the object on the image plane (2D-NET). Finally, we show results on the publicly available dataset. The obtained average translation error is smaller than 7% and the obtained rotation error is smaller than 5 degrees. It means that we can precisely and efficiently (up to 15 frames per second) estimate the pose of known objects in the 3D space using RGB image only.

In the future, we are going to verify the method in real-world robotics applications. We are going to use the proposed method to detect and grasp the objects by the mobile manipulating robot. We also plan to investigate the accuracy of the proposed method in real-world scenarios and work on the precision of the pose estimation.

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