Neuroevolution with CMA-ES for Real-time Gain Tuning of a Car-like Robot Controller

Ashley Hill¹, Eric Lucet¹ and Roland Lenain²

¹CEA, LIST, Interactive Robotics Laboratory, Gif-sur-Yvette, F-91191, France
²Université Clermont Auvergne, Irstea, UR TSCF, Centre de Clermont-Ferrand, P-63178 Aubière, France

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Abstract: This paper proposes a method for dynamically varying the gains of a mobile robot controller that takes into account, not only errors to the reference trajectory but also the uncertainty in the localisation. To do this, the covariance matrix of a state observer is used to indicate the precision of the perception. CMA-ES, an evolutionary algorithm is used to train a neural network that is capable of adapting the robot’s behaviour in real-time. Using a car-like vehicle model in simulation. Promising results show significant trajectory following performances improvements thanks to control gains fluctuations by using this new method. Simulations demonstrate the capability of the system to control the robot in complex environments, in which classical static controllers could not guarantee a stable behaviour.

1 INTRODUCTION

Mobile robots are used to accomplish different missions, their sensors being used to correctly and efficiently understand the robot’s environment. Those sensors have varying degrees of certainty in their measurement depending on the environment and their properties. This limits the efficiency of robots using static controllers, as the tuning of their parameters takes into consideration the nominal behaviour of the robot, which has a negative effect on the robot’s efficiency when operating in sub-nominal states. The purpose of tuning these controllers is also to guarantee a higher level of margins, which has a negative effect on robot performance during nominal states. This compromise reduces the overall performance of the robot. In control theory, noise robustness is an essential quality (Ghorbel et al., 1991); it is therefore relevant to use the noise information directly to adjust control parameters in real-time.

In the field of mobile robotics, finding an optimal control policy is a challenging task. Especially in complex environments where sensor precision varies considerably and as so the level of noise in the system. The aim of this paper is to integrate the noise into the control policy in order to adjust the robot’s behaviour to its complex environment. Different types of controllers can be proposed (Jalali and Ghafarian, 2009; Jiang et al., 2008; Doicin et al., 2016). However, tuning controller gains relies on many parameters (Daful, 2018). As a solution to the tuning problem, Neural networks have been used, with promising results (Guo et al., 2009; Shu et al., 2015; Carlucho et al., 2017); however such methods use small neural networks that are not capable of complex inference, and are using the error or state vector as the basis for the gradient which can cause instability if noisy.

In this paper, a new strategy for on-line gains adaptation is propose and summarised in Figure 1. CMA-ES (Hansen, 2016) is the optimisation algorithm for the parameters of the neural network. The neural network block takes parameters and environmental information as inputs, and outputs the gains of the controller. The controller uses the gains defined by the neural network in order to effectively follow
the requested trajectory. The robot’s dynamics simulate the behaviour of the robot. The noise mimics real world conditions, and so an extended Kalman filter (EKF) is used to observe the state of the robot. It provides the estimated state \( \hat{x} \) and the corresponding covariance matrix \( P \).

In the following, the paper is structured into three main sections before conclusions. The second section presents all the localisation, modelling, and control algorithms applied to the robot. The third section is dedicated to the presentation of gains adaptation. Finally, results are detailed and discussed along with perspectives.

2 LOCALISATION PROCESS AND CONTROL

2.1 Modelling

The focus of this study is to adapt the control policy of a car-like mobile robot to the precision of the perception, the lateral error, the angular error, and the current curvature of the trajectory; using a neuroevolution algorithm. In order to train the system and test it, a model of the robot was used to simulate its behaviour. The model is fairly representative of the task and had been used in previous works (Jaulin, 2015). The robot is described by the following kinematic model:

\[
\begin{align*}
\dot{X} &= \begin{pmatrix}
x \\
y \\
\theta 
\end{pmatrix} =
\begin{pmatrix}
v \cos(\theta) + \alpha_x \\
v \sin(\theta) + \alpha_y \\
v \tan(\alpha_\psi + \alpha_\theta) / L + \alpha_\psi 
\end{pmatrix} + \begin{pmatrix}
\alpha_x \\
\alpha_y \\
\alpha_\psi 
\end{pmatrix}
\end{align*}
\]

The state variables are: \( x, y \) the coordinates of the robot in the world frame, \( \theta \) its heading, \( L \) its wheelbase, and \( v \) its rear velocity. \( u_1 \) and \( u_2 \) are the acceleration and steering inputs respectively. \( \alpha_i \) is the white Gaussian noise of the \( i \) state variable.

In Figure 2, \( u_2 \) is the steering angle of the robot (Ackermann angle) and constitutes the control input, \( \epsilon_\psi \) is the distance from the robot to the path, \( \epsilon_\theta \) is the robot heading, \( (D) \) is the trajectory, \( \kappa \) is the curvature of the trajectory, \( L \) is the wheelbase of the robot. The angular deviation \( \epsilon_\theta \) is representative of the difference between the robot heading and the orientation of the trajectory.

2.2 Control Law

The robot has to complete a task, which is in our case following a trajectory. To accomplish this, the following controller is used:

\[
u_2 = \arctan \left( \frac{L \cos^3 \epsilon_\theta}{\alpha} \left( k_0 \epsilon_\theta + \frac{\kappa}{\cos^2(\epsilon_\theta)} \right) \right) \tag{2}\]

with \( \epsilon_\theta = \tan \epsilon_\theta - \frac{k_1 \epsilon_\psi}{\alpha} \) is the relative orientation error of the robot to reach its trajectory (i.e. ensuring the convergence of \( \epsilon_\theta \) to 0). This control detailed in (Lenain et al., 2017) guarantees the stabilisation of the robot to its reference trajectory, providing a relevant choice for the gains \( k_0 \) and \( k_1 \). Theoretically, a relevant choice for these gains may be:

\[
k_1 = \frac{\sqrt{kp}}{2L} \quad \text{and} \quad k_0 = 2 \sqrt{k_p}
\]

it implies \( k_0 \times k_1 = \frac{k_p}{L} \) and guarantees that the constraint \( k_0 > k_1 \) is respected, we then get our final controller with \( k_p \) the controller gain. As a result, the control law (2) has only one parameter \( k_p \), defining the theoretical distance of convergence of the robot to the trajectory (as it has been proven in (Lenain et al., 2017)). As a result, the higher the gain is, the more reactive the robot is. However the sensor noise as well as delays in the low level may lead to instability. The choice of this gain has to then be made with respect to localisation properties.

2.3 Robot Localisation

In order to feed the control law (2) with lateral and angular error, the state vector defined by (1) has to be known. For estimating the state of the robot, an EKF is proposed. It assists in determining the linear speed, the \( x, y \) position, and the heading. It is widely used due to its simplicity and robustness.

In the proposed system, \( P \) is the covariance matrices of the estimation and it is used to determine the level of precision of the perception. A novelty of this paper is that both the estimate and the corresponding
covariance matrix are integrated in the tuning of the Controller. The observed variables are used to control the robot along a path. Even though the controller is easy to implement, the tuning of its parameters is not a simple task and is a large research area (Ho et al., 1996; Tyreus and Luyben, 1992; Hang et al., 2002).

3 CONTROL GAINS ADAPTATION

The nature of the environment forces the mobile robot’s perception to vary in precision. These changes in precision will be given by the changes in the covariance matrix of the EKF. Therefore, the controller gains must adjust periodically. In order to adapt the controller’s parameters to the level of precision in the perception, but also to the properties of the trajectory, a neural network is used. The network will tune the controller in real-time, based on the tracking errors, the path curvature and the covariance matrix of the EKF.

3.1 The Neural Network Model

![Graphical representation of the used neural network](image)

Figure 3: Graphical representation of the used neural network. With 7 neurons in the input layer, 3 hidden layers of 40, 100, and 10 neurons respectively, and 1 neuron for the output layer, all the layers except the output layer go through a hyperbolic tangent function as the activation function.

Neural networks (NN) are highly connected systems which are used to model complex non-linear functions. In neural networks the inputs are transformed through matrix multiplications and non-linear activation functions, in order to obtain a universal function estimator through the tuning of the weights (Hornik et al., 1990). The used neural network (see Figure 3) has as input the vector of concatenated values for: the lateral error $\varepsilon_l$, the angular error $\varepsilon_\theta$, the curvature of the trajectory $\kappa$, and the diagonal of the EKF covariance matrix $P$. As output, this neural network returns a vector corresponding to each controller gain respectively. The training of the neural network is the proposed neuroevolution algorithm, which means that an evolution strategy will be used to optimise the neural network. Evolution strategies are stochastic optimisation algorithms (Beyer and Schwefel, 2002). The great advantage of this family of algorithms is that they do not need to calculate any gradient when optimising a neural network. This allows to reduce computation when training and it is robust to noisy return signals (e.g. reward, objective function, etc ...), unlike reinforcement learning for example (Salimans et al., 2017). All evolutionary algorithms go through the same steps: mutation, evaluation, selection, reproduction and repeat until a termination criterion is met. There exists multiple algorithms in the family of evolution strategies, a few of them were considered, especially genetic algorithms. However, the CMA-ES (Hansen, 2016) optimisation algorithm has shown its superiority in highly modal, non-convex, noisy functions (Hansen et al., 2010); such as the highly non-convex search spaces of neural networks with a noisy objective function (Salimans et al., 2017; Risi and Togelius, 2014; Such et al., 2017).

3.2 CMA-ES Neuroevolution

To adjust the behaviour of the robot, a neural network was chosen to adjust the parameters of the controller. This neural network’s architecture was chosen based on previous work and experimentation, in order to be able to infer a complex enough non linear outputs from the given inputs. Neural network parameters, such as weights and biases, are optimised by the CMA-ES method during the offline training phase. The CMA-ES optimisation algorithm starts by generating an initial population of parameters for the neural network, by drawing samples from the following distribution:

$$x_{k+1}^g \sim m^g + \sigma^g \mathcal{N}(0, C^g) \text{ for } k = 1, \ldots, \lambda$$  \hspace{1cm} (3)

with $m^g$ the mean vector of the current generation, $\sigma^g$ the step size vector of the generation, $C^g$ the covariance matrix of the generation which differs from the covariance matrix of the Kalman filter, and $\lambda$ the size of the population. CMA-ES uses the covariance matrix to chose the optimal direction of the search and the step size over every parameter to know the optimal length of the step to take between consecutive generations. Here both phases are presented. The first one is the training phase where the neural network is optimised to learn the behaviour which robot is intended to have. After this, the neural network and the controller are deployed into the robot to work online.
During the online training phase, a simulation of the robot’s kinematics is used to simulate its behaviour, and a controller is used to follow the requested path. The robot’s state is measured by adding noise to the simulated state, and an EKF is then used to observe the state of the robot. Once the online training is completed and the objective function is calculated, the CMA-ES method then optimises the neural network parameters based on the objective function.

The CMA-ES generates a population of neural networks based on the architecture. Each neural network is used by the simulation to generate controller gains for each timestep using the current errors, curvature, and EKF covariance matrix. These parameters are then used to control the robot. For each neural network, a series of simulated trajectories are used in order to calculate the objective function of the neural network using the robot over many examples to avoid overfitting; this objective function is the criterion for comparing the performance of each neural network. CMA-ES puts the neural networks found in order, based on their score. A set of the best performing individuals are then used to produce the next generation and the cycle continues until a stopping criterion is met. By the end of the training, the resulting neural network is the one with the lowest score. For a neural network to have the best score, it must adapt the behaviour of the robot so as to decrease the error by considering the real state and not the observed one. For this to happen, the neural network has to choose high gains on the controller to force the robot to follow the reference, especially when cornering or correcting any lateral errors. However, when the level of noise is high, it must lower the mean values of the gains to not have an oscillatory behaviour which compromises both the mechanical structure of the robot and the comfort of the passengers in the case of occupied vehicles.

For the deployment phase, the trained neural network and the controller are deployed into the robot. The neural network does not consume too much resource as it is only used for inference of the controller gains and not for training.

3.3 The Objective Function

The objective function is an essential part of evolution strategies, it is what the algorithm tries to minimise in order to find the best local optimum for the search space. To minimise the objective function, CMA-ES tweaks the parameters of the neural network in order to have the lowest possible value; this tweaking of the parameters is what is called learning, because the model is in fact a system that has the capacity to learn certain behaviours, and is adapting to reach said behaviours. Since the objective function determines the behaviour of the neural networks, we have tested the following objective functions formulated as:

$$ob_1 = \sum_{\tau=0}^{T} |e_l(\tau)| + |e_0(\tau) L| \quad (4)$$

$$ob_2 = \sum_{\tau=0}^{T} |e_l(\tau)| + |e_0(\tau) L| + |u_2(\tau) L| \quad (5)$$

$$ob_3 = \sum_{\tau=0}^{T} |e_l(\tau)| + |e_0(\tau) L| + k_{steer} |u_2(\tau) L| \quad (6)$$

with $e_l$ the lateral error, $e_\theta$ the angular error, $u_2$ the steering input, $L$ the wheelbase of the robot, $k_{steer}$ the weight of the steering input in the objective function, and $T$ the total timesteps of the simulation. The absolute value of the errors and steering input are used as we are measuring the accumulated amplitude of these values. Since the objective functions take into account both the lateral and the angular errors, using the accumulation of them at the end of the simulations guarantees a coherent objective function that will perform a similar trade-off as the controller, meaning it won’t degrade the overall performance in order to optimise one of the errors.

4 RESULTS AND DISCUSSIONS

Here are presented the results of the developed system. Since evolution strategies are comparable to reinforcement learning methods (Salimans et al., 2017), we will compare this method to reinforcement learning methods using the negative amplitude of lateral and angular errors as its rewards, and a constant gain method trained using CMA-ES on the same objective function as the proposed method, similarly to existing methods (Wakasa et al., 2010; Sivananitaiperumal and Baskar, 2014; Marova, 2016). Tests are focused on the trained system and not on the training phase. This section is divided into two main parts. In the first part, the experimental environment is presented. Then, the limitations of using a constant gain method are shown qualitatively. Then, the qualitative results from the training phase are presented. Finally, the system performance is compared to results in same conditions with a fix gain controller and with a reinforcement learning algorithm. And in the second part, the results are discussed in a general context and improvements are suggested.
4.1 Results

4.1.1 Simulated Environment

The training setup for all the methods were on a simulated robotic environment, with a cinematic model, without wheel slipping, and without control latency, written in Python and C, where the robot must follow a series of trajectories, with noisy position measurements distributed randomly in zones along the trajectories to simulated GPS-like perturbations, and with a randomly placed change lane along the trajectories to simulated abrupt changes in the setpoints. This allows rather realistic types of noises that a robot can encounter that will cause instability and higher overall errors to occur. The trajectories are: a line, a sine wave, a parabola, a Bezier spline in an sigmoid shape called spline1, and a Bezier spline in a u-turn shape called spline2. With the perturbations and trajectories, this setup helps prevent CMA-ES or reinforcement learning methods from falling into bad local optimaums and overfitting, due to the high randomness of the perturbations and the variations in the trajectories.

4.1.2 Limitations of the Constant Gain Model

An ideal gain model must allow the controller associated to the gains, to simultaneously minimise the errors and not be too reactive to noise present in said error. In our case study this means finding the gains that are able to follow a line as closely as possible, whilst avoiding undesirable reactions to noise that can induce unstable behaviours.

Looking at figure 4, we can see the compromise a constant gain model must achieve. In the first plot with a small gain, we can see the robot having trouble following the line when the corners occur; however it is quite steady and stable in the noisy region of the trajectory. In the third plot with the very high gain, we see the complete opposite of this, the robot becomes completely unstable in the perturbed region; however it was very close to the curve in the high accuracy region. And in the second plot with a gain that is midway of the first and third plot, we can see some difficulties following the lines in the stable region, and some instability and oscillation in the noisy region.

One can then see the limitations of a constant gain model that must reach a paradoxical compromise between contradicting gains. In this case, the clear solution is an adaptive model, such as the proposed contribution.

4.1.3 Qualitative Results

In order to help visualise the gain adaptation to the perturbations, the trajectory in figure 5 is used in the following results:

Figure 4: The x,y view of the simulation using the spline1 trajectory and a constant gain model. Midway through the trajectory noise is applied to the position measurements. Above: The first plot with a low gain of 0.1. Middle: The second plot with a high gain of 3.0. Below: The third plot with a very high gain of 7.0.

Figure 5: The x,y view of the simulation using the sine trajectory. Midway through the trajectory noise is applied to the position measurements, and then a change lane occurs just before the last corner.

After training, (see Figure 6), the real vehicle handles the EKF covariance matrix’s errors, the curvature of the trajectory, and even the lateral error due to a change lane.

It can be seen that, as expected, a higher gain is computed when cornering, when an unexpected perturbation occurs, and when the position accuracy is high. In contrast, the gain is reduced when the position accuracy is too low, in order to avoid a possibly unstable behaviour.

Furthermore, when using objective functions $ob_2$ and $ob_3$, the neural network is able to lower significantly the oscillatory behaviour of the steering, as shown in Figure 7.
Additional experiments such as ablation over the given inputs to the neural network were done. The EKF covariance matrix seems to be an invaluable information for predicting a useful gain, as when trained without it causes a much lower gain overall, as it cannot know the regions where instability occurs (see Figure 8). Also the curvature is helping to obtain a lower objective function overall when the trajectory is not curved, allowing for smoother control.

Some tools were developed in order to understand the training process in further details. On the history of the trained network displayed in Figure 9, we can see that the CMA-ES method first optimises the gain using the covariance of the Kalman filter, then using the lateral error, and then using the curvature. This order makes sense, as it is from the most to the least impactful to the objective function through the gain, and as such, it should be optimised in this order.

4.1.4 Quantitative Results

In order to help verify quantitatively the relevance of our results, we used the Welch t-test (Welch, 1947) over the distribution of the values of the objective functions, with the null hypothesis being that our method produces the same results as the constant gain.

![Figure 6: Above: the gain outputed by the neural network in the solid line, and the chosen constant gain value in the dashed line. Below: the curvature of the trajectory over time.](image)

![Figure 7: Steering input $u_2$ over time by using the proposed method. Above: when trained with the objective function $ob_2$. Below: when trained with the objective function $ob_1$.](image)

![Figure 8: The gain outputed by the neural network in the solid line, and the optimal constant gain value in the dashed line. Above: when trained without using the EKF covariance matrix as input. Below: when trained without using the curvature of the trajectory as input.](image)

![Figure 9: Gain values over the training generations. The gain outputed by the neural network in the solid line, and the optimal constant gain value in the dashed line.](image)
method. The resulting test returns p-values, that are the probability of obtaining these results if the null hypothesis is true; as such, if the p-value is lower than 1.00e-2 we can consider the null hypothesis being rejected, and show the significance of our results.

We used two methods to compare our results quantitatively. The first is to see the improvement relative to a static gain controller using the objective function with a Welch t-test over multiple trajectories and seeds. The second is to see the improvement relative to a gain tuned by reinforcement learning methods using the objective function with over multiple trajectories and seeds. These two methods should allow us to see how the suggested method improves the quality of the control over the traditional constant gain method and over reinforcement learning based methods.

Table 1: Welch test p-values between fixed gain and the suggested method, for every trajectory over the objective functions. With k_{steer} = 0.5.

<table>
<thead>
<tr>
<th>Trajectory</th>
<th>ob₁</th>
<th>ob₂</th>
<th>ob₃</th>
</tr>
</thead>
<tbody>
<tr>
<td>line</td>
<td>3.22e-2</td>
<td>1.80e-8</td>
<td>7.01e-5</td>
</tr>
<tr>
<td>sine</td>
<td>1.61e-4</td>
<td>4.07e-9</td>
<td>6.06e-7</td>
</tr>
<tr>
<td>parabola</td>
<td>6.53e-12</td>
<td>4.20e-21</td>
<td>1.49e-17</td>
</tr>
<tr>
<td>spline₁</td>
<td>2.09e-28</td>
<td>3.63e-21</td>
<td>5.08e-19</td>
</tr>
<tr>
<td>spline₂</td>
<td>3.48e-1</td>
<td>8.42e-16</td>
<td>1.49e-9</td>
</tr>
</tbody>
</table>

We can see from the table 2 that across all the objective functions and the trajectories, that the proposed method obtained between 3% to 20% improvement with an average of 10% improvement over the constant gain method. Furthermore, with the table 1 we can see that the p-values associated with these improvements, are for the most part significant, except for the line and spline2 trajectories, which are both hard to improve upon as the first is a very easy trajectory for the constant gain, and the second is quite hard for the robot model to follow with its given design. Nevertheless, the other results are quite significant and do indeed show the benefit of this method when compared to the constant gain method.

As discussed earlier, CMA-ES based neuroevolution can obtain similar if not better performance when compared to reinforcement learning (RL) based methods. The trade-off is that neuroevolution is more stable to noise, but requires more time to train than reinforcement learning. Here four commonly used models where tested on the training environment: Soft actor critic (labeled SAC) (Haarnoja et al., 2018), Proximal policy optimization (labeled PPO) (Schulman et al., 2017), Deep deterministic policy gradient (labeled DDPG) (Lillicrap et al., 2015), and Advantage actor critic (labeled A2C) (Mnih et al., 2016); using the RL library stable-baselines (Hill et al., 2018).

We can see from the table 3 that none of the reinforcement learning models where capable of reaching even the baseline constant gain model; with most of the models between 19% and 3670% with an average of 588% of degradation in performance when compared to the constant gain model. Considering the scale of the amplitude and variance of the performance loss, no t-test was performed on this dataset.

4.2 Discussion

Neuroevolution is used to tune controller gains in real-time after a training phase. As mentioned before, the CMA-ES optimises a neural network, then the said neural network tunes the controller gains. The proposed controller was used due to its simplicity and ease of use. The objective was to develop an adaptable system that works with different types of controllers whose parameters must be tuned.

As demonstrated in the results section, the proposed method outperforms the traditional constant gain method by a significant amount; as it is capable of adapting the robot behaviour to the environment using the information present in the control loop. It is able to achieve such performance by minimising the wanted objective function through the CMA-ES training.

We also showed that modern reinforcement learning methods are not capable of learning a beneficial behaviour in the same environment. This is probably due to the fact that the reward signal depends on the information in the control loop, such as lateral and angular errors; as in our experiments, they become very noisy due to the position noise. This noise on the reward signal prevents the critic of actor critic models from correctly converging, causing erratic learning. This flaw does not occurs when using CMA-ES, as it is inherently resilient to noisy objective functions (Hansen, 2016; Salimans et al., 2017).

It is important to note that the selection of the objective function is very important to the quality of the gain tuning, as the optimisation can compromise the performance of other features. For example during experimentation, the objective function ob₂ had higher lateral error when compared to ob₁, however this is a trade off as ob₂ is more stable with respect to the steering.

The training time for the method was about 5 hours wall time using 8 CPU cores, and can be scaled extremely well with more CPUs thanks to the CMA-ES method (Salimans et al., 2017). This training is only feasible in simulation however, as the 5 hours of training time is the equivalent of 1 simulated year. To
address the simulation issue, transfer learning could be used to bridge the difference between simulated and real world robotics. For example using domain randomisation (OpenAI et al., 2018; Tan et al., 2018), or by learning the gap between the simulation and the real world (Golemo et al., 2018).

Further care should be taken should this method be used in the real world, as even though the p-values and objective functions values are favourable, the method can have unexpected behaviour because it is not currently possible to prove the stability of method due to neural networks being black boxes and CMA-ES not having a proof of convergence; this can be mitigated with a supervisor that can replace the method with a constant gain in unseen states, or by clipping gain between certain bounds.

5 CONCLUSIONS

This paper presents a method of neuroevolution, which is used to train a neural network to then tune a controller in real time in order to adapt a robot’s behaviour to a varying level of precision in the perception. The proposed method has been shown to improve the overall performance in the context of mobile robotics when compared with constant gain models or reinforcement learning methods. Furthermore, the proposed method can be used with varying controllers in many different applications, such as navigation in urban landscapes, agricultural application, or even drones. Many possible variants exist of this method that could be put in application, such as variants of the CMA-ES algorithm could be used, or even the possible variants of the objective function for different tasks. In this paper, first simulation tests have been achieved to prove the theoretical validity of the proposed approach, accounting for sensors noises and low level settling times. Further experimentation with existing adaptive control algorithms, and experimentation with real world robots are required for future works, especially with respect to grip conditions.

REFERENCES


